

1 Introduction

2 Solver

This section details all the pieces of the solver. The scheme is designed to solve the full 2-D Navier-Stokes equations using a finite volume method using local time-stepping. The equations to be solved are

$$\begin{aligned}\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x_i} \rho u_i &= 0, \\ \frac{\partial \rho u_i}{\partial t} + \frac{\partial}{\partial x_j} (\rho u_i u_j + P \delta_{ij} - \tau_{ij}) &= 0, \\ \frac{\partial \rho E}{\partial t} + \frac{\partial}{\partial x_i} (\rho u_i H + Q_i - \tau_{ij} u_j) &= 0,\end{aligned}\tag{1}$$

where τ_{ij} is the viscous stress tensor, $\rho E = \frac{P}{\gamma-1} + \frac{1}{2}\rho(u^2 + v^2)$ is the internal energy, and $\rho H = \rho E + P$ is the internal enthalpy.

2.1 Euler Fluxes

2.2 Viscous Fluxes

2.3 Time Stepping

2.4 Boundary Conditions

3 Test Case: Oblique Shock

Convergence and contour plots

4 Flat Plate Boundary Layer

Convergence and contour plots

5 Transonic Symmetric Airfoil

Convergence and contour plots

6 Conclusion