xlapes02

December 16, 2023

1 Import Packages

```
[125]: from pathlib import Path
    import numpy as np
    import matplotlib.pyplot as plt
    import scipy.stats as stats
    import pandas as pd
    from scipy import stats
    import statsmodels.api as sm
    import statsmodels.formula.api as smf
    import statsmodels.stats.api as sms
    from statsmodels.stats.outliers_influence import variance_inflation_factor
    import seaborn as sns
    from sklearn.preprocessing import PolynomialFeatures
    from statsmodels.stats.outliers_influence import OLSInfluence
```

2 Setup basic configuration + define helper functions

```
[126]: def write_to_file(file_name, content):
    with open(file_name, 'w') as f:
        f.write(content)

# Create directory for output files
Path('tmp/out').mkdir(parents=True, exist_ok=True)

# Set dark theme
plt.style.use('dark_background')

# Set grid thickness
plt.rcParams['grid.linewidth'] = 0.3
```

3 Load Data

```
[127]: excel_file = pd.ExcelFile("Projekt-2_Data.xlsx")
       df_uloha_1: pd.DataFrame = excel_file.parse(excel_file.sheet_names[0])
       df_uloha_2 = excel_file.parse(excel_file.sheet_names[1])
       data = {
           '1': df_uloha_1,
           '1_a': df_uloha_1['uloha_1 a)'],
           '1_b_prior': df_uloha_1['uloha_1 b)_prior'],
           '1 g': df uloha 1['skupina'],
           '1_b_observation': df_uloha_1['uloha_1 b)_pozorování'],
           '2': df_uloha_2,
           '2 os': df uloha 2['OSType'],
           '2_as': df_uloha_2['ActiveUsers'],
           '2 ip': df uloha 2['InteractingPct'],
           '2_sp': df_uloha_2['ScrollingPct'],
           '2_p': df_uloha_2['Ping [ms]'],
       }
       # data
```

```
/Users/zlapik/.pyenv/versions/3.10.13/lib/python3.10/xml/etree/ElementTree.py:16
47: ResourceWarning: unclosed file <_io.BufferedReader
name='Projekt-2_Data.xlsx'>
attrib = {}
ResourceWarning: Enable tracemalloc to get the object allocation traceback
```

4 ULOHA 1 - Bayesovske odhady

4.1 ULOHA 1.a - Konjugované apriorní a aposteriorní rozdělení, prediktivní rozdělení [2 body]

4.1.1 Clean data

- Remove outliers
- Remove nan values
- Remove +-inf values
- Remove values with Z-score > 3
- Remove values with Z-score < -3

```
[128]: df_uloha_1 = data['1_a']

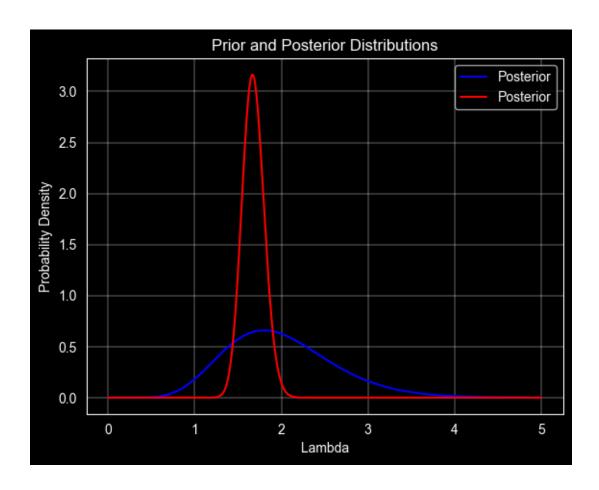
# Extract observed data
observed_data = df_uloha_1.values

# Remove nan or +-inf values
observed_data = observed_data[~np.isnan(observed_data)]

# Calculate Z-scores
```

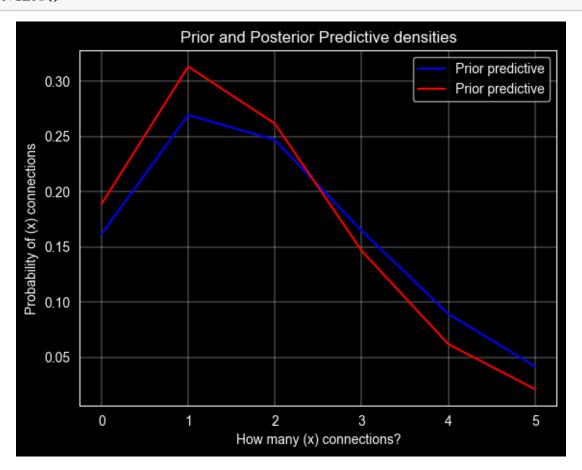
```
z_scores = stats.zscore(observed_data, nan_policy='raise')
       # Define a threshold for outliers (e.g., 3 standard deviations)
       threshold = 3
       # Filter out rows with Z-scores beyond the threshold
       filtered_data = observed_data[(np.abs(z_scores) < threshold)]</pre>
       filtered_data
[128]: array([2., 2., 1., 3., 0., 1., 1., 3., 2., 2., 3., 1., 5., 3., 1., 1., 2.,
              1., 1., 1., 2., 3., 2., 0., 3., 1., 2., 1., 5., 1., 0., 0., 2., 1.,
              1., 0., 0., 1., 3., 1., 0., 1., 2., 0., 1., 3., 0., 1., 1., 4., 1.,
              2., 1., 1., 2., 4., 2., 2., 3., 4., 4., 4., 0., 2., 0., 0., 3., 5.,
              1., 2., 1., 0., 1., 1., 4., 1., 1., 3., 0., 1., 2., 2., 2., 3., 1.,
              2., 2., 2., 1., 2., 2., 1., 0., 1., 1., 3., 0., 3., 1., 1.])
      4.2 ULOHA 1.a.1 - Do jednoho obrázku vykreslíte apriorní a aposteriorní hus-
           totou parametru Poissonova rozdělení \lambda.
[129]: alpha_prior = 10 # connection count
       beta_prior = 5 # time within the connection count (alpha prior) was observed
       lambda_expert = alpha_prior / beta_prior # expert's estimate of the connection_
        \hookrightarrow count
[130]: alpha_posterior = alpha_prior + np.sum(filtered_data)
       beta_posterior = beta_prior + len(filtered_data)
[131]: x_prior = np.linspace(0, np.max(filtered_data), 1000)
       y_prior = stats.gamma.pdf(x_prior, alpha_prior, scale=1 / beta_prior)
[132]: x_posterior = np.linspace(0, np.max(filtered_data), 1000)
       y_posterior = stats.gamma.pdf(x_posterior, alpha_posterior, scale=1 /__
        ⇔beta_posterior)
[133]: plt.plot(x_prior, y_prior, label='Posterior', color='blue')
       plt.plot(x posterior, y_posterior, label='Posterior', color='red')
       plt.title('Prior and Posterior Distributions')
       plt.xlabel('Lambda')
       plt.ylabel('Probability Density')
       plt.legend()
```

plt.show()



4.3 ULOHA 1.a.2 - Do jednoho obrázku vykreslíte apriorní a aposteriorní prediktivní hustotou pozorovaní x za jeden časový interval.

```
plt.legend()
plt.show()
```



```
[137]: # Task 3: Construct 95% confidence intervals for from prior and posterior_

distributions

prior_ci = stats.gamma.interval(0.95, alpha_prior, scale=1 / beta_prior)

posterior_ci = stats.gamma.interval(0.95, alpha_posterior, scale=1 /_

beta_posterior)

print(f"Prior 95% CI: {prior_ci[0]:.5f}, {prior_ci[1]:.5f}")

print(f"Posterior 95% CI: {posterior_ci[0]:.5f}, {posterior_ci[1]:.5f}")

Prior 95% CI: 0.95908, 3.41696

Posterior 95% CI: 1.43769, 1.93272
```

```
[138]: # Task 4: Select two posterior point estimates for and compare them
    posterior_mean = alpha_posterior / beta_posterior
    posterior_mode = (alpha_posterior - 1) / beta_posterior
    print(f"Aposteriori mean: {posterior_mean:.5f}")
    print(f"Aposteriori mode: {posterior_mode:.5f}")
```

Aposteriori mean: 1.67619

Aposteriori mode: 1.66667

Prior estimate: 2.00000 Posterior estimate: 1.67619

4.4 ULOHA 1.b - Aproximace diskrétním rozdělením [2 body]

```
[140]: mu = 3
sigma = np.sqrt(1)
a = 1
```

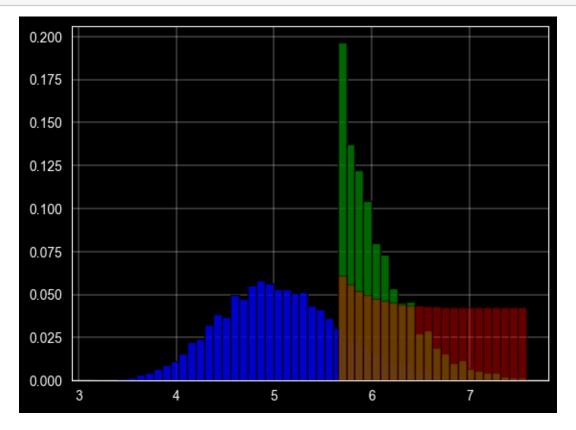
4.4.1 Load data

4.4.2 Uloha 1.b.1: Plot prior, posterior, and likelihood functions

```
[143]: bin_centers = (bin_edges[:-1] + bin_edges[1:]) / 2
       def likelyhood_func(observed_data, b):
           Calculate likelyhood function
           :param observed_data:
           :param b:
           :return:
           a_truncnorm = (a - mu) / sigma
           b truncnorm = (b - mu) / sigma
           pdf = stats.truncnorm.pdf(observed_data, a=a_truncnorm, b=b_truncnorm,_u
        →loc=mu, scale=sigma)
           return pdf
       # Calculate likelyhood function for each bin
       likelihood = [likelyhood func(observed data, b center) for b center in__
       ⇔bin_centers]
       # Calculate product of all likelyhoods
       likelihood = np.prod(likelihood, axis=1)
       # Normalize likelyhood
       likelihood_normalized = likelihood / np.sum(likelihood)
       # Plot likelyhood
       # plt.bar(x=bins, height=likelihood_normalized, width=bin_width,__
        ⇔edgecolor='black', color='red', label='Likelyhood', alpha=0.7)
       # plt.show()
[144]: # Calculate posterior
       posterior_probs = likelihood * bin_height
       posterior_probs_normalized = posterior_probs / np.sum(posterior_probs)
       # plt.bar(bin_centers, posterior_probs_normalized, width=bin_width,_
       ⇔edgecolor='black', color='green', label='Aposteriórne rozdelenie', alpha=0.7)
       # plt.show()
[145]: # Plot all together: prior, likelyhood, posterior
       plt.bar(x=bins, height=bin_height, width=bin_width, color='blue', alpha=0.8,
        ⇔edgecolor='black')
       plt.bar(bin_centers, posterior_probs_normalized, width=bin_width,_u
        ⇔edgecolor='black', color='green',
               label='Aposteriórne rozdelenie', alpha=0.8)
       plt.bar(bin_centers, likelihood_normalized, width=bin_width, edgecolor='black',u

¬color='red', label='Vierohodnost',
               alpha=0.4)
```





4.4.3 Uloha 1.b.2. Z aposteriorní hustoty určete 95% interval spolehlivosti (konfidenční interval) pro parametr .

95% Confidence Interval for Parameter b: 5.69371, 7.00891

4.4.4 Uloha 1.b.3. Vyberte dva bodové odhady parametru a spočítejte je.

```
[147]: # Calculate point estimates
mean = np.sum(bin_centers * posterior_probs_normalized)
median = bin_centers[np.argmax(posterior_probs_normalized)]
print(f'First point estimate: {mean:.5f}')
print(f'Second point estimate: {median:.5f}') # Is this value OK?
```

First point estimate: 6.05277 Second point estimate: 5.69371

5 ULOHA 2 - ÚLOHA 2 - Regrese - 8. bodů

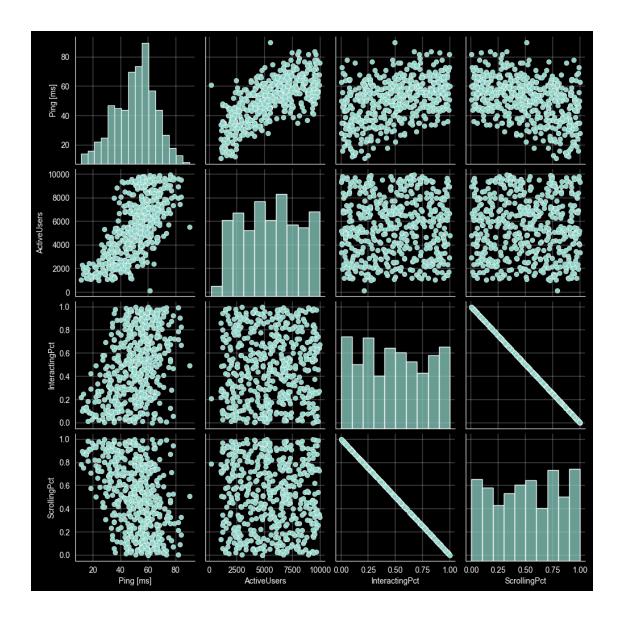
- 5.1 ULOHA 2.1. [4. body] Pomocí zpětné eliminace určete vhodný regresní model. Za výchozí "plný" model považujte plný kvadratický model (všechny interakce druhého řádu a všechny druhé mocniny, které dávají smysl).
- 5.2 Learn more about data

```
[148]: # Load data
df_uloha_2 = data['2']

# Print data info to learn more about data
print(df_uloha_2.head())
print(df_uloha_2.describe())
```

	0S	Туре	Active	Jsers	Interactin	ngPct	Scrolli	ngPct	Ping	[ms]
	0	iOS		4113	0.	8283	0	. 1717		47
	1	iOS		7549	0.	3461	0	. 6539		46
	2 Win	dows		8855	0.	2178	0	.7822		55
	3 And	roid		8870	0.	0794	0	.9206		56
	4 M	acOS		9559	0.	7282	0	. 2718		76
		Acti	veUsers	Inte	eractingPct	Scro	llingPct	Pin	g [ms]	
	count	502	.000000		502.000000	50	2.000000	502.	000000)
1	mean	5485	.830677		0.488613		0.511387	50.	545817	•
	std	2548	.935679		0.296000		0.296000	14.	797937	•
1	min	153	.000000		0.000500		0.001400	11.	000000)
	25%	3357	.500000		0.229300		0.257525	40.	000000)
	50%	5456	.000000		0.482950		0.517050	52.	000000)
	75%	7461	.500000		0.742475		0.770700	60.	000000)
]	max	9953	.000000		0.998600		0.999500	90.	000000)

5.2.1 Visualize data using matrix plot



Based on the previos correlation matrix, we can see that there is a high correlation between InteractingPct and ScrollingPct. Therefore we can remove one of them.

I choose to remove $\mathbf{ScrollingPct}$

```
[150]: # Remove correlated parameters
X = pd.DataFrame({
        'ActiveUsers': df_uloha_2.loc[:, 'ActiveUsers'],
        'InteractingPct': df_uloha_2.loc[:, 'InteractingPct'],
        'ScrollingPct': df_uloha_2.loc[:, 'ScrollingPct'],
})

# Standardize
```

```
¬X['ActiveUsers'].std()
      X['InteractingPct'] = (X['InteractingPct'] - X['InteractingPct'].mean()) / __
        # OS types Instead True/False values, we can use 1/0
      X['Windows'] = df_uloha_2['OSType'].apply(lambda x: 1 if x == 'Windows' else 0)
      X['iOS'] = df_uloha_2['OSType'].apply(lambda x: 1 if x == 'iOS' else 0)
      X['MacOS'] = df_uloha_2['OSType'].apply(lambda x: 1 if x == 'MacOS' else 0)
      X['Android'] = df_uloha_2['OSType'].apply(lambda x: 1 if x == 'Android' else 0)
      correlation_matrix = np.corrcoef(X.values.T)
      corr params = np.abs(correlation matrix) > 0.7
       # Print all correlated parameters that are not on the main diagonal and those u
       ⇔only above main diagonal
      print("Correlated parameters:")
      for i in range(corr_params.shape[0]):
          for j in range(corr_params.shape[1]):
               if i != j and i < j and corr_params[i, j]:</pre>
                   print(f"{X.columns[i]} - {X.columns[j]}")
                  print(f"Removing {X.columns[j]}")
                   X = X.drop(X.columns[j], axis=1)
      X.head()
      Correlated parameters:
      InteractingPct - ScrollingPct
      Removing ScrollingPct
[150]:
         ActiveUsers InteractingPct Windows
                                               iOS MacOS Android
           -0.538590
                            1.147592
                                            0
                                                 1
                                                         0
      1
            0.809424
                            -0.481464
                                            0
                                                 1
                                                         0
                                                                  0
      2
                                                 0
                                                         0
                                                                  0
            1.321795
                            -0.914910
                                            1
      3
             1.327679
                                            0
                                                 0
                                                         0
                            -1.382478
                                                                  1
            1.597988
                            0.809416
                                            0
                                                 0
                                                         1
                                                                  0
[151]: # Polynomial degree
      degree = 2
      # Use PolynomialFeatures
      poly = PolynomialFeatures(degree=degree, include_bias=True)
      poly_features = poly.fit_transform(X)
       # Create a new dataframe with the polynomial features and original column names
      poly_X = pd.DataFrame(poly_features, columns=poly.get_feature_names_out(X.
        ⇔columns))
       # Rename 1 to const
      poly_X.rename(columns={'1': 'const'}, inplace=True)
```

 $X['ActiveUsers'] = (X['ActiveUsers'] - X['ActiveUsers'].mean()) /_{\sqcup}$

```
# poly_X
```

```
[152]: def get_column_to_remove(model):
           Firstly get all quadratic columns ending with ^2, then remove interaction_
        \hookrightarrow terms and after all linear terms
           :param model:
           :return:
           pvalues = model.pvalues
           # Find all columns with p-value > 0.05 and nan
           pvalues = pvalues[(pvalues > 0.05) | (pvalues.isna())]
           pvalues = pvalues.drop('const') if 'const' in pvalues else pvalues
           # Check if there is any quadratic term
           quadratic terms = [i for i in pvalues.index if i.endswith('^2')]
           # Check if there is any interaction term
           interaction_terms = [i for i in pvalues.index if ' ' in i]
           # Check if there is any linear term
           linear_terms = [i for i in pvalues.index if i not in quadratic_terms and iu
        →not in interaction_terms]
           # Find nan values
           nan_values = [i for i in pvalues.index if
                         i not in quadratic_terms and i not in interaction_terms and iu
        →not in linear_terms]
           if len(quadratic_terms) > 0:
               return quadratic_terms[0]
           elif len(interaction_terms) > 0:
               return interaction_terms[0]
           elif len(linear_terms) > 0:
               return linear_terms[0]
           elif len(nan_values) > 0:
               return nan_values[0]
           else:
               return None
```

```
[153]: # Train
y = df_uloha_2['Ping [ms]']
model = sm.OLS(endog=y, exog=poly_X).fit()

# Remove from poly_X the values that has p-value >= 0.05
while remove_col := get_column_to_remove(model):
```

```
print(f"Removing {remove_col}")
   poly_X = poly_X.drop(remove_col, axis=1) # remove column from X
   model = sm.OLS(endog=y, exog=poly_X).fit() # fit model again
# Print summary
print(model.summary())
write_to_file('tmp/out/model_summary_pvalue.txt', model.summary().as_text())
Removing InteractingPct^2
Removing ActiveUsers Windows
Removing ActiveUsers iOS
Removing InteractingPct Android
Removing InteractingPct Windows
Removing InteractingPct iOS
Removing InteractingPct MacOS
Removing Windows iOS
Removing Windows MacOS
Removing Windows Android
Removing iOS MacOS
Removing iOS Android
Removing MacOS Android
                        OLS Regression Results
______
Dep. Variable:
                        Ping [ms]
                                  R-squared:
                                                               0.843
Model:
                             OLS Adj. R-squared:
                                                               0.840
                   Least Squares F-statistic:
Method:
                                                               293.7
                Sat, 16 Dec 2023 Prob (F-statistic):
                                                        1.62e-191
Date:
Time:
                         22:24:53 Log-Likelihood:
                                                             -1599.6
No. Observations:
                             502 AIC:
                                                               3219.
Df Residuals:
                             492
                                 BIC:
                                                               3261.
                               9
Df Model:
Covariance Type:
                       nonrobust
_____
                            coef std err t
                                                       P>|t|
[0.025 0.975]
                          35.2506 0.258 136.475
                                                       0.000
const
34.743 35.758
ActiveUsers
                          7.7862 0.367
                                             21.210
                                                        0.000
7.065
          8.507
InteractingPct
                          5.0493 0.266
                                              18.977
                                                        0.000
4.527
       5.572
Windows
                          9.8027
                                    0.233
                                              42.041
                                                        0.000
9.345
       10.261
iOS
                          5.0093 0.246
                                              20.331
                                                        0.000
4.525
        5.493
```

MacOS		12.5724	0.229	54.900	0.000
12.122	13.022				
Android		7.8661	0.249	31.600	0.000
7.377	8.355				
ActiveUsers	^2	-2.6838	0.285	-9.432	0.000
-3.243	-2.125				
	${\tt InteractingPct}$	-2.3187	0.269	-8.621	0.000
-2.847	-1.790				
ActiveUsers		5.8465	0.633	9.232	0.000
4.602	7.091				
ActiveUsers		2.2256	0.690	3.225	0.001
0.870	3.582				
Windows^2		9.8027	0.233	42.041	0.000
	10.261				
iOS^2		5.0093	0.246	20.331	0.000
4.525	5.493	40 5504		54 000	0.000
MacOS^2	40.000	12.5724	0.229	54.900	0.000
12.122	13.022	T 0004	0.040	04 000	0.000
Android^2	0.055	7.8661	0.249	31.600	0.000
7.377	8.355				
Omnibus:		228.381			1.925
Prob(Omnibu	s):	0.000			3196.157
Skew:	~, -	1.598	-	- (02).	0.00
Kurtosis:		14.941			6.71e+16
	==========		*		

Notes:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The smallest eigenvalue is 3.27e-31. This might indicate that there are strong multicollinearity problems or that the design matrix is singular.

```
[154]: def get_column_to_remove_vif(df):
    """
    Firstly get all quadratic columns ending with "2, then remove interaction_
    terms and after all linear terms
    :param model:
    :return:
    """
    # Calculate vif
    vif = pd.Series([variance_inflation_factor(df.values, i) for i in range(df.shape[1])], index=df.columns)

# Remove all values above 5 (infinite included), const can not be removed
    vif = vif[vif > 5]
```

```
# Don't remove const
  vif = vif.drop('const') if 'const' in vif else vif
  # Check if there is any quadratic term
  quadratic_terms = [i for i in vif.index if i.endswith('^2')]
  # Check if there is any interaction term
  interaction_terms = [i for i in vif.index if ' ' in i]
  # Check if there is any linear term
  linear terms = [i for i in vif.index if i not in quadratic terms and i not | |
→in interaction_terms]
  # Find nan values
  nan values = [i for i in vif.index if
                 i not in quadratic_terms and i not in interaction_terms and i _{\sqcup}
→not in linear_terms]
  if len(quadratic_terms) > 0:
      return quadratic_terms[0]
  elif len(interaction_terms) > 0:
      return interaction_terms[0]
  elif len(linear_terms) > 0:
      return linear_terms[0]
  elif len(nan_values) > 0:
      return nan_values[0]
  else:
      return None
```


Removing Windows^2 Removing iOS^2 Removing MacOS^2 Removing Android^2 Removing Windows

OLS Regression Results

Dep. Variable:	Ping [ms]	R-squared:	0.843			
Model:	OLS	Adj. R-squared:	0.840			
Method:	Least Squares	F-statistic:	293.7			
Date:	Sat, 16 Dec 2023	Prob (F-statistic):	1.62e-191			
Time:	22:24:53	Log-Likelihood:	-1599.6			
No. Observations:	502	AIC:	3219.			
Df Residuals:	492	BIC:	3261.			

Df Model: 9
Covariance Type: nonrobust

_____ coef std err t P>|t| [0.025 0.975] 54.8560 0.591 92.857 0.000 const 53.695 56.017 0.367 ActiveUsers 7.7862 21.210 0.000 7.065 8.507 5.0493 0.266 18.977 0.000 InteractingPct 4.527 5.572 iOS -9.5869 0.749 -12.804 0.000 -11.058 -8.116 MacOS 5.5393 0.720 7.696 0.000 4.125 6.954 Android -3.8732 0.761 -5.088 0.000 -5.369-2.3770.285 ActiveUsers^2 -2.6838 -9.432 0.000 -3.243-2.125ActiveUsers InteractingPct -2.31870.269 -8.621 0.000 -2.847-1.790ActiveUsers MacOS 5.8465 0.633 9.232 0.000 4.602 7.091 ActiveUsers Android 2.2256 0.690 3.225 0.001 0.870 3.582

```
      Omnibus:
      228.381
      Durbin-Watson:
      1.925

      Prob(Omnibus):
      0.000
      Jarque-Bera (JB):
      3196.157

      Skew:
      1.598
      Prob(JB):
      0.00

      Kurtosis:
      14.941
      Cond. No.
      7.07
```

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
[155]: const
                                     5.006291
      ActiveUsers
                                     1.929304
      InteractingPct
                                     1.013519
      iOS
                                     1.446080
      MacOS
                                     1.481309
      Android
                                    1.440922
      ActiveUsers^2
                                    1.013961
      ActiveUsers InteractingPct 1.016595
      ActiveUsers MacOS
                                    1.527704
      ActiveUsers Android
                                    1.416742
      dtype: float64
```

5.2.2 ULOHA 2.1.1 Zapište rovnici Vašeho finálního modelu.

```
[156]: # Print equation
       model_params = model.params.drop('const')
       equation = f"ping = \n{model.params['const']:.5f}\n"
       for k, v in model_params.items():
           equation += f''+ \{v:.5f\} * \{k\}\n''
       print(equation)
      ping =
      54.85603
      + 7.78621 * ActiveUsers
      + 5.04932 * InteractingPct
      + -9.58693 * iOS
      + 5.53933 * MacOS
      + -3.87321 * Android
      + -2.68377 * ActiveUsers^2
      + -2.31866 * ActiveUsers InteractingPct
      + 5.84648 * ActiveUsers MacOS
      + 2.22559 * ActiveUsers Android
```

5.2.3 ULOHA 2.1.2 Diskutujte splnění předpokladů lineární regrese a základní regresní diagnostiky.

TODO

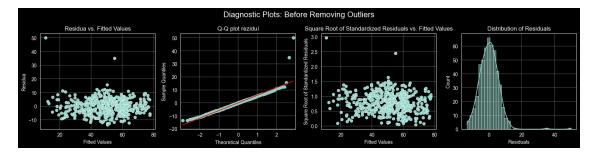
5.2.4 ULOHA 2.1.3 Pokud (až během regresního modelování) identifikujete některé "extrémně odlehlé hodnoty" můžete ty "nejodlehlejší" hodnoty, po alespoň krátkém zdůvodnění, vyřadit.

TODO

```
[157]: | def plot diagnostic subplots(model, title: str = 'Diagnostic Plots'):
           Plot diagnostic subplots
           :param model:
           :param title:
           :return:
           11 11 11
           # Set up subplots
           fig, axes = plt.subplots(1, 4, figsize=(4*4, 4))
           # Set title for whole plots
           fig.suptitle(title, fontsize=16)
           # Residua vs. Fitted Values (diagnostic graph)
           sns.scatterplot(x=model.fittedvalues, y=model.resid, ax=axes[0])
           axes[0].set title("Residua vs. Fitted Values")
           axes[0].set xlabel("Fitted Values")
           axes[0].set_ylabel("Residua")
           # Normality reziduí (Q-Q plot)
           sm.qqplot(model.resid, line='s', ax=axes[1])
           axes[1].set_title("Q-Q plot reziduí")
           # Homoskedasticita (diagnostic graph)
           influence = model.get_influence()
           residuals_studentized = influence.resid_studentized_internal
           fitted values = model.fittedvalues
           sns.scatterplot(x=fitted_values, y=np.sqrt(np.abs(residuals_studentized)),_
        \Rightarrowax=axes[2])
           axes[2].set_title("Square Root of Standardized Residuals vs. Fitted Values")
           axes[2].set_xlabel("Fitted Values")
           axes[2].set_ylabel("Square Root of Standardized Residuals")
           # Distribution of Residuals
           residuals = model.resid
           sns.histplot(residuals, kde=True, ax=axes[3])
           axes[3].set_title('Distribution of Residuals')
           axes[3].set xlabel('Residuals')
           axes[3].set_ylabel('Count')
           # Adjust layout to prevent clipping of titles
           plt.tight_layout()
```

```
# Show the plots
_title = title.lower().replace(' ', '_')
plt.savefig(f"tmp/out/diagnostic_plots_{_title}.png")
plt.show()
```

[158]: plot_diagnostic_subplots(model, title='Diagnostic Plots: Before Removing_
Outliers')



```
[159]:  # Fit an OLS model
       ols_model = OLSInfluence(model)
[160]: # Standardized residuals
       standardized_residuals = ols_model.resid_studentized_internal
       # Identify outliers based on standardized residuals
       outliers = np.abs(standardized_residuals) > 5
       outliers[outliers == True].index
[160]: Index([255, 476], dtype='int64')
[161]: # Cook's distance
       cooks_distance = ols_model.cooks_distance[0]
       # Identify outliers based on Cook's distance
       cooks_outliers = cooks_distance > 10 / poly_X.shape[0]
       cooks_outliers[cooks_outliers == True].index
[161]: Index([255, 476], dtype='int64')
[162]: merged_outliers = list(set(outliers[outliers == True].index) |
        set(cooks_outliers[cooks_outliers == True].index))
       merged_outliers.sort()
       # Remove outliers, if was not removed before
       if len(poly_X) == len(X):
```

```
poly_X = poly_X.drop(merged_outliers, axis=0)
y = y.drop(merged_outliers, axis=0)
# poly_X
```

[163]: # Retrain model

OLS Regression Results

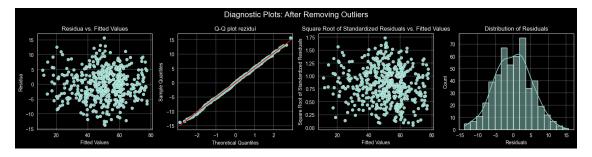
Dep. Varia	ble:		R-squared:		0.877	
Model:			OLS Adj. R-squared:		0.875	
Method:		Least Squares			388.1	
Date:	Sa		Prob (F-statistic):		1.43e-216	
Time:		22:24:55	Log-Likelihood:		-1529.5	
No. Observ		500			3079.	
Df Residua	ls:	490	BIC:		3121.	
Df Model:		9				
Covariance Type:						
			========			
		coef	std err	t	P> t	
[0.025	0.975]					
const		54.9364	0.525	104.738	0.000	
53.906	55.967					
ActiveUser	s	7.7474	0.323	23.970	0.000	
7.112	8.382					
${\tt InteractingPct}$		5.1512	0.234	21.970	0.000	
4.691	5.612					
iOS		-9.3373	0.660	-14.140	0.000	
-10.635	-8.040					
MacOS		5.3424	0.637	8.391	0.000	
	6.593					
Android		-3.6638	0.671	-5.456	0.000	
-4.983	-2.344					
ActiveUser		-2.9856	0.254	-11.764	0.000	
	-2.487					
ActiveUser	s Interacting	gPct -2.5439	0.238	-10.693	0.000	
ActiveUser		6.7342	0.565	11.929	0.000	
5.625	7.843	21.012			,	
ActiveUser		2.2951	0.608	3.777	0.000	
1.101			-	•		

Omnibus: 0.799 Durbin-Watson: 1.981 Prob(Omnibus): 0.671 Jarque-Bera (JB): 0.865 Skew: 0.002 Prob(JB): 0.649 Cond. No. Kurtosis: 2.796 7.06

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

[164]: plot_diagnostic_subplots(model_without_outliers, title='Diagnostic Plots: After_ After_ Outliers')



5.3 ULOHA 2.2. [1. body] - Pomocí Vašeho výsledného modelu identifikujte, pro které nastavení parametrů má odezva nejproblematičtější hodnotu.

```
[165]: # Find max ping value
max_ping = model_without_outliers.predict().argmax()
max_ping
```

[165]: 10

5.4 ULOHA 2.3. [1. bod] - Odhadněte hodnotu odezvy uživatele s Windows, při průměrném nastavení ostatních parametrů a vypočtěte konfidenční interval a predikční interval pro toto nastavení.

```
[166]: # Average values
mean_poly_X = poly_X.mean()

# Predict ping for user with Windows
predicted_ping = model_without_outliers.predict(mean_poly_X)
print(f"Predikovaná odezva uživatele s Windows: {predicted_ping.values[0]:.5f}")

# Calculate confidence interval
```

Predikovaná odezva uživatele s Windows: 50.44600

```
Konfidenční interval:
[[49.98837369 50.90362631]]
Predikční interval:
[[40.20293692 60.68906308]]
```

5.5 ULOHA 2.4. [2. body] - Na základě jakýchkoli vypočtených charakteristik argumentujte, zdali je Váš model "vhodný" pro další použití.