

Prob 2

2)

a)

$$\text{Fr}[0] = 32.50 \quad \text{Fi}[0] = 0$$

$$\text{Fr}[1] = -9.58 \quad \text{Fi}[1] = -3.61$$

$$\text{Fr}[2] = 8.75 \quad \text{Fi}[2] = 0.72$$

$$\text{Fr}[3] = -20.83 \quad \text{Fi}[3] = 0$$

$$\text{Fr}[4] = 8.75 \quad \text{Fi}[4] = -0.72$$

$$\text{Fr}[5] = -9.58 \quad \text{Fi}[5] = 3.61$$

$$|\text{Fr}[0]| = (\text{Fr}[0]^2 + \text{Fi}[0]^2)^{1/2} = 32.5$$

$$|\text{Fr}[1]| = (\text{Fr}[1]^2 + \text{Fi}[1]^2)^{1/2} = 10.24$$

$$|\text{Fr}[2]| = (\text{Fr}[2]^2 + \text{Fi}[2]^2)^{1/2} = 8.78$$

$$|\text{Fr}[3]| = (\text{Fr}[3]^2 + \text{Fi}[3]^2)^{1/2} = 20.83$$

$$|\text{Fr}[4]| = (\text{Fr}[4]^2 + \text{Fi}[4]^2)^{1/2} = 8.78$$

$$|\text{Fr}[5]| = (\text{Fr}[5]^2 + \text{Fi}[5]^2)^{1/2} = 10.24$$

$$\text{Phase0} = \tan^{-1}(\text{Fi}[0]/\text{Fr}[0]) = 0$$

$$\text{Phase1} = \tan^{-1}(\text{Fi}[1]/\text{Fr}[1]) = -2.78$$

$$\text{Phase2} = \tan^{-1}(\text{Fi}[2]/\text{Fr}[2]) = 0.08$$

$$\text{Phase3} = \tan^{-1}(\text{Fi}[3]/\text{Fr}[3]) = 3.14$$

$$\text{Phase4} = \tan^{-1}(\text{Fi}[4]/\text{Fr}[4]) = .0.08$$

$$\text{Phase5} = \tan^{-1}(\text{Fi}[5]/\text{Fr}[5]) = 2.78$$

b)

$$\begin{aligned}
f_0 &= (32.5 + 0i) \cdot e^{(i2\pi \cdot 0 \cdot 0/6)} + (-9.58 - 3.61i) \cdot e^{(i2\pi \cdot 0 \cdot 1/6)} + (8.75 + 0.72i) \cdot e^{(i2\pi \cdot 0 \cdot 2/6)} + \\
&(-20.83 + 0i) \cdot e^{(i2\pi \cdot 0 \cdot 3/6)} + (8.75 - 0.72i) \cdot e^{(i2\pi \cdot 0 \cdot 4/6)} + (-9.58 + 3.61i) \cdot e^{(i2\pi \cdot 0 \cdot 5/6)} \\
&= 32.5 - 9.58 + 8.75 - 20.83 + 8.75 - 9.58 \\
&= \mathbf{9.99}
\end{aligned}$$

$$\begin{aligned}
f_1 &= (32.5 + 0i) \cdot e^{(i2\pi \cdot 1 \cdot 0/6)} + (-9.58 - 3.61i) \cdot e^{(i2\pi \cdot 1 \cdot 1/6)} + (8.75 + 0.72i) \cdot e^{(i2\pi \cdot 1 \cdot 2/6)} + \\
&(-20.83 + 0i) \cdot e^{(i2\pi \cdot 1 \cdot 3/6)} + (8.75 - 0.72i) \cdot e^{(i2\pi \cdot 1 \cdot 4/6)} + (-9.58 + 3.61i) \cdot e^{(i2\pi \cdot 1 \cdot 5/6)} \\
&= 32.5 - 9.58 \cos(\pi/3) + 3.61 \sin(\pi/3) - i(9.58 \sin(\pi/3) + 3.61 \cos(\pi/3)) + \\
&8.75 \cos(\pi \cdot 2/3) - 0.72 \sin(\pi \cdot 2/3) + i(8.75 \sin(\pi \cdot 2/3) + 0.72 \cos(\pi \cdot 2/3)) - \\
&20.83 \cos(\pi) - i20.83 \sin(\pi) + \\
&8.75 \cos(\pi \cdot 4/3) + 0.72 \sin(\pi \cdot 4/3) + i(8.75 \sin(\pi \cdot 4/3) - 0.72 \cos(\pi \cdot 4/3)) - \\
&9.58 \cos(\pi \cdot 5/3) - 3.61 \sin(\pi \cdot 5/3) - i(9.58 \sin(\pi \cdot 5/3) - 3.61 \cos(\pi \cdot 5/3)) \\
&= \mathbf{40.00}
\end{aligned}$$

$$\begin{aligned}
f_2 &= (32.5 + 0i) \cdot e^{(i2\pi \cdot 2 \cdot 0/6)} + (-9.58 - 3.61i) \cdot e^{(i2\pi \cdot 2 \cdot 1/6)} + (8.75 + 0.72i) \cdot e^{(i2\pi \cdot 2 \cdot 2/6)} + \\
&(-20.83 + 0i) \cdot e^{(i2\pi \cdot 2 \cdot 3/6)} + (8.75 - 0.72i) \cdot e^{(i2\pi \cdot 2 \cdot 4/6)} + (-9.58 + 3.61i) \cdot e^{(i2\pi \cdot 2 \cdot 5/6)} \\
&= 32.5 - 9.58 \cos(\pi \cdot 2/3) + 3.61 \sin(\pi \cdot 2/3) - i(9.58 \sin(\pi \cdot 2/3) + 3.61 \cos(\pi \cdot 2/3)) + \\
&8.75 \cos(\pi \cdot 4/3) - 0.72 \sin(\pi \cdot 4/3) + i(8.75 \sin(\pi \cdot 4/3) + 0.72 \cos(\pi \cdot 4/3)) - \\
&20.83 \cos(2\pi) - i20.83 \sin(2\pi) + \\
&8.75 \cos(\pi \cdot 8/3) + 0.72 \sin(\pi \cdot 8/3) + i(8.75 \sin(\pi \cdot 8/3) - 0.72 \cos(\pi \cdot 8/3)) - \\
&9.58 \cos(\pi \cdot 10/3) - 3.61 \sin(\pi \cdot 10/3) - i(9.58 \sin(\pi \cdot 10/3) - 3.61 \cos(\pi \cdot 10/3)) \\
&= \mathbf{20}
\end{aligned}$$

$$\begin{aligned}
f_3 &= (32.5 + 0i)e^{(i2\pi \cdot 3 \cdot 0/6)} + (-9.58 - 3.61i)e^{(i2\pi \cdot 3 \cdot 1/6)} + (8.75 + 0.72i)e^{(i2\pi \cdot 3 \cdot 2/6)} + \\
&(-20.83 + 0i)e^{(i2\pi \cdot 3 \cdot 3/6)} + (8.75 - 0.72i)e^{(i2\pi \cdot 3 \cdot 4/6)} + (-9.58 + 3.61i)e^{(i2\pi \cdot 3 \cdot 5/6)} \\
&= 32.5 - 9.58\cos(\pi) + 3.61\sin(\pi) - i(9.58\sin(\pi) + 3.61\cos(\pi)) + \\
&8.75\cos(\pi^2) - 0.72\sin(\pi^2) + i(8.75\sin(\pi^2) + 0.72\cos(\pi^2)) - \\
&20.83\cos(3\pi) - i20.83\sin(3\pi) + \\
&8.75\cos(\pi^4) + 0.72\sin(\pi^4) + i(8.75\sin(\pi^4) - 0.72\cos(\pi^4)) - \\
&9.58\cos(\pi^5) - 3.61\sin(\pi^5) - i(9.58\sin(\pi^5) - 3.61\cos(\pi^5)) \\
&= \mathbf{90.00}
\end{aligned}$$

$$\begin{aligned}
f_4 &= (32.5 + 0i)e^{(i2\pi \cdot 4 \cdot 0/6)} + (-9.58 - 3.61i)e^{(i2\pi \cdot 4 \cdot 1/6)} + (8.75 + 0.72i)e^{(i2\pi \cdot 4 \cdot 2/6)} + \\
&(-20.83 + 0i)e^{(i2\pi \cdot 4 \cdot 3/6)} + (8.75 - 0.72i)e^{(i2\pi \cdot 4 \cdot 4/6)} + (-9.58 + 3.61i)e^{(i2\pi \cdot 4 \cdot 5/6)} \\
&= 32.5 - 9.58\cos(\pi^4/3) + 3.61\sin(\pi^4/3) - i(9.58\sin(\pi^4/3) + 3.61\cos(\pi^4/3)) + \\
&8.75\cos(\pi^8/3) - 0.72\sin(\pi^8/3) + i(8.75\sin(\pi^8/3) + 0.72\cos(\pi^8/3)) - \\
&20.83\cos(4\pi) - i20.83\sin(4\pi) + \\
&8.75\cos(\pi^{16}/3) + 0.72\sin(\pi^{16}/3) + i(8.75\sin(\pi^{16}/3) - 0.72\cos(\pi^{16}/3)) - \\
&9.58\cos(\pi^{20}/3) - 3.61\sin(\pi^{20}/3) - i(9.58\sin(\pi^{20}/3) - 3.61\cos(\pi^{20}/3)) \\
&= \mathbf{5}
\end{aligned}$$

$$\begin{aligned}
f_5 &= (32.5 + 0i)e^{(i2\pi \cdot 5 \cdot 0/6)} + (-9.58 - 3.61i)e^{(i2\pi \cdot 5 \cdot 1/6)} + (8.75 + 0.72i)e^{(i2\pi \cdot 5 \cdot 2/6)} + \\
&(-20.83 + 0i)e^{(i2\pi \cdot 5 \cdot 3/6)} + (8.75 - 0.72i)e^{(i2\pi \cdot 5 \cdot 4/6)} + (-9.58 + 3.61i)e^{(i2\pi \cdot 5 \cdot 5/6)} \\
&= 32.5 - 9.58\cos(\pi^5/3) + 3.61\sin(\pi^5/3) - i(9.58\sin(\pi^5/3) + 3.61\cos(\pi^5/3)) +
\end{aligned}$$

$$\begin{aligned}
& 8.75 \cos(\pi \cdot 10/3) - 0.72 \sin(\pi \cdot 10/3) + i(8.75 \sin(\pi \cdot 10/3) + 0.72 \cos(\pi \cdot 10/3)) - \\
& 20.83 \cos(5\pi) - i 20.83 \sin(5\pi) + \\
& 8.75 \cos(\pi \cdot 20/3) + 0.72 \sin(\pi \cdot 20/3) + i(8.75 \sin(\pi \cdot 20/3) - 0.72 \cos(\pi \cdot 20/3)) - \\
& 9.58 \cos(\pi \cdot 25/3) - 3.61 \sin(\pi \cdot 25/3) - i(9.58 \sin(\pi \cdot 25/3) - 3.61 \cos(\pi \cdot 25/3)) \\
& = \mathbf{29.99}
\end{aligned}$$