Table 1. Complete component list for World4 model in four parts. (a) Variables. (b) Flows. (c) Stocks. (d) Equations. Variables in bold italics were fit to data. Best value is one solution of many. Range shows values that can be fit to data with less than a specific residual depending on range of years fit. Fit years is the range used for fitting in *hyperfit*. (a)

Var.	Best value	Range	Fit years	Physical meaning
а	0.426	0.35 to 0.48	1970-2010	Ecosystem fragility. Relates cc_E vs $ecosphere$. A higher/lower a means that ecosystem services are fragile/robust with respect to $ecosphere$, respectively
b	1.0 people/gha	0.7 to 1.7	1000-1970	Base level carrying capacity for ecosphere.
\boldsymbol{c}	5.5 people/gha	4.5 to 7.0	1000-1970	Base level carrying capacity for <i>humansphere</i> .
d	-110	-150 to -90	n/a	Rule of diminishing returns. Relates <i>knowledge</i> to <i>CC</i> . A more negative value for <i>d</i> means <i>knowledge</i> raises <i>CC</i> more.
E_{θ}	7.05E+09 gha	4.3e9 to 8.1e9	1970-2010	Initial biocapacity of the ecosphere.
H_{θ}	1.5e8 gha	1.2e8 to 1.6e8	1-1970	Domesticated land in 0CE. Initial value of humansphere.
I_{θ}	0.05 y ⁻¹	0.05 to 0.25	n/a	Base mortality. Multiplied by <i>humansphere</i> to get <i>rewilding</i> . Must be higher than maximum value of <i>knowledge</i> . Past population is insensitive to this variable but it affects future population.
K_{θ}	7.25e-11 y-1	2.0e-11 to 2.0e-9	1000-1970	Technology in Year 0. Initial value of knowledge in 0CE.
p	n/a	0 to 1.0	n/a	Enforcement level of conservation policy. Higher p means stronger enforcement of policy.
py	n/a	0 to inf.	n/a	Policy phase-in time of conservation policy. Linear phase-in for enforcement of conservation policy w.
sy	n/a	1960 to inf.	n/a	Starting date of phase-in of conservation policy. When $p_E < w$, domestication is multiplied by $g = g(((y-sy)/py)p+(1-(y-sy)/py)(1-exp(-10(w-p_E))) + exp(-10(w-p_E))$, where y is the current year. Used only in the phase-in period sy through $sy+py$.
и	-8.6	-inf. to -6.5	1970-2010	Aggressiveness of growth.
ν	-11.46	-inf. to -9.0	1970-2010	Aggressiveness of technological development.
w	n/a	0 to 0.5	n/a	Fraction of <i>ecosphere</i> to save using conservation policy. When $p_E < w$, <i>domestication</i> is multiplied by $p(1-\exp(-10(w-p_E))) + \exp(-10(w-p_E))$
×	9.6E-03 y ⁻¹	6.5e-3 to 1.0e-2	1000-1970	Learning rate. Rate of the intrinsic growth of knowledge.
τ	852 y	700 to 1525	1-1970	Doubling time of humansphere in Year 0.

(b)

Flow	Source	Sink	Formula	Physical meaning
rewilding	humansphere	ecosphere	ignorance • humansphere	Deaths expressed as change in ecological footprint.
domestication	ecosphere	humansphere	g • humansphere	Births expressed as change in ecological footprint.
learning	ignorance	knowledge	≈ • knowledge	Intrinsic technology growth.
obsolescence	knowledge	ignorance	r • knowledge	Loss of technology.

(c)						
Stock	Initial value	Physical meaning				
humansphere $H_{ heta}$		Amount of total biocapacity appropriated for human use in Year 0, in gha.				
ecosphere E_{θ}		Amount of total biocapacity not appropriated for human use in Year 0, in gha.				
knowledge	K_{θ}	Mortality eradicated by technology, in per year rate units y-1.				
ignorance	I_{0}	Base mortality rate. Eradicated by technology. In per year rate units, y-1.				

(d)					
Equation	Formula	Physical meaning			
cc_E	$b p_E^{(0.5/(1+pE-2a))}$	Carrying capacity contributed by the ecosphere.			
cc_H	$c(1 - exp(d \cdot knowledge)) cc_E$	Carrying capacity contributed by the humansphere .			
p_E	e $cosphere$ / $m{E_{ heta}}$	The wild fraction of the environment.			
g	$(I_0 + ln(2)/\tau)(1 - exp(\mathbf{u} p_E))$	ecosphere-dependent net intrinsic growth rate of humansphere			
r	$exp(\mathbf{v} p_E)$	ecosphere-dependent depletion rate of knowledge			
CC	$cc_E + cc_H$	Global carrying capacity in humans per gha.			
population	CC • humansphere	Carrying capacity determines population number.			