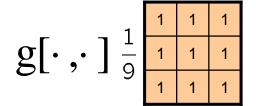
Convolution

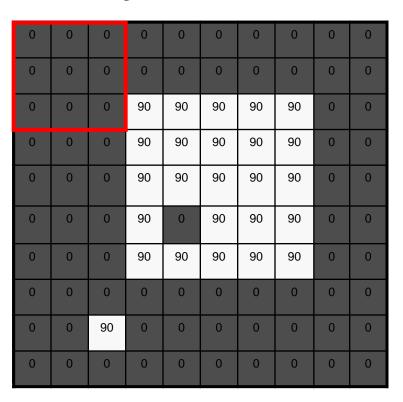
Based on slides by J. Xiao

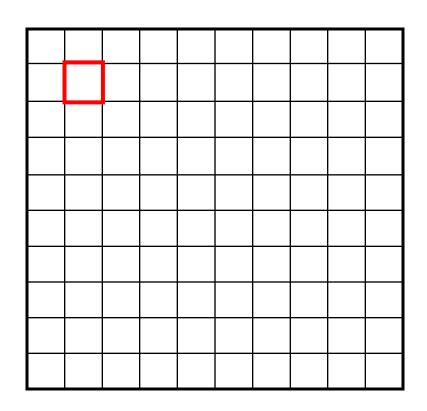
Example: box filter

$$g[\cdot\,,\cdot\,]$$

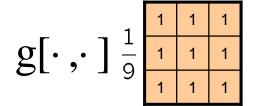
$$\frac{1}{9}\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

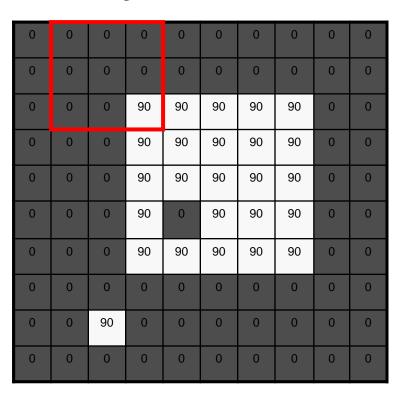


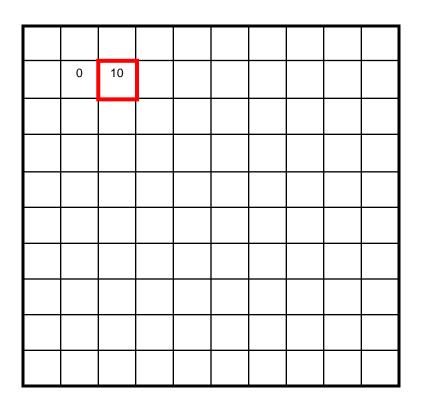




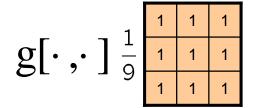
$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

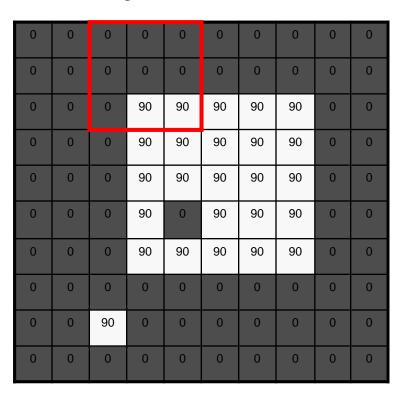


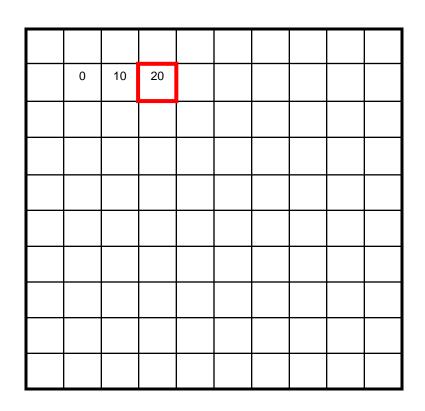




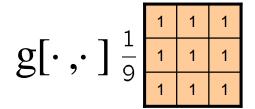
$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$



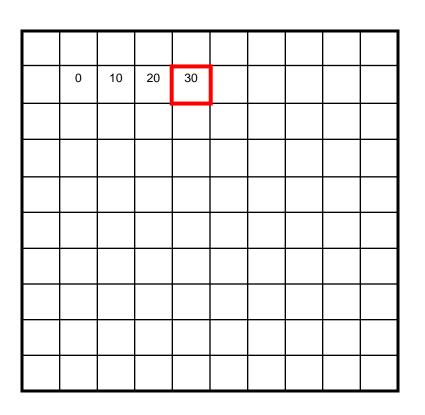




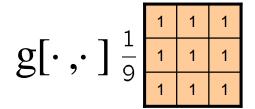
$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

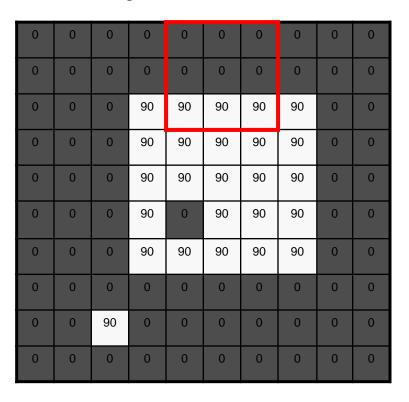


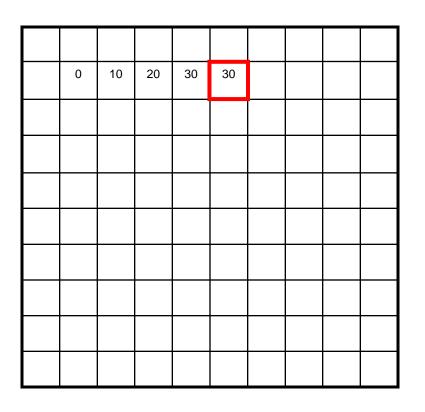
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0



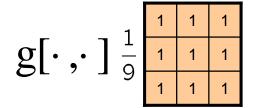
$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$



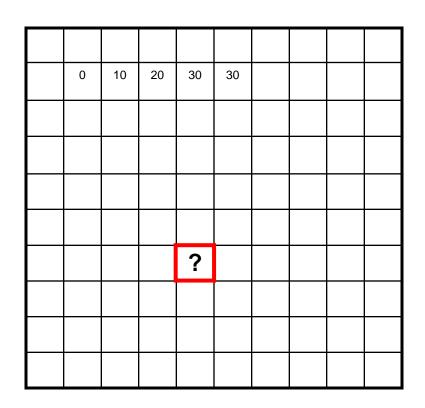




$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$



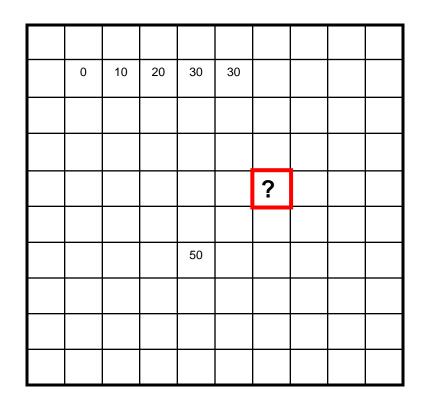
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0



$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

$$g[\cdot,\cdot]^{\frac{1}{9}}$$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0



$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

$$g[\cdot,\cdot]_{\frac{1}{9}}$$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

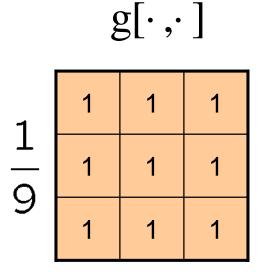
0	10	20	30	30	30	20	10	
0	20	40	60	60	60	40	20	
0	30	60	90	90	90	60	30	
0	30	50	80	80	90	60	30	
0	30	50	80	80	90	60	30	
0	20	30	50	50	60	40	20	
10	20	30	30	30	30	20	10	
10	10	10	0	0	0	0	0	

$$h[m,n] = \sum_{l=1}^{n} g[k,l] f[m+k,n+l]$$

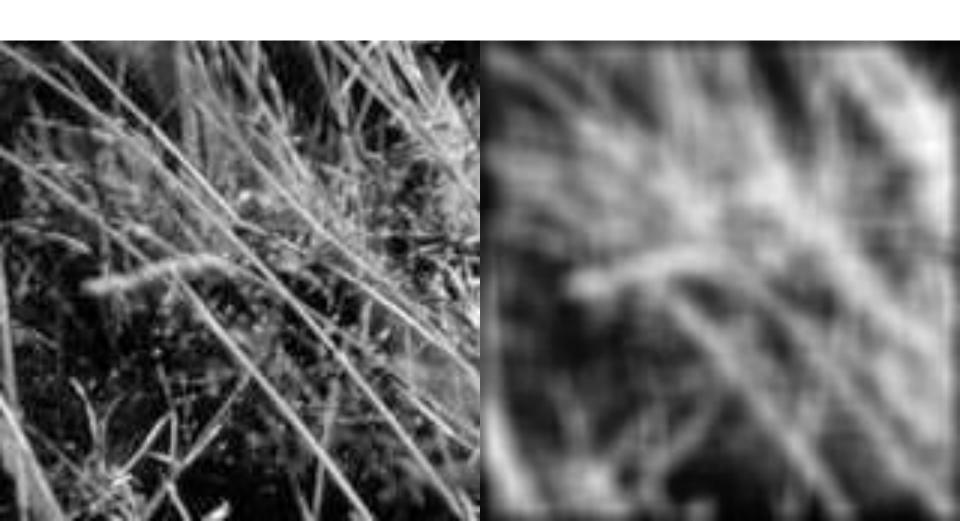
Box Filter

What does it do?

- Replaces each pixel with an average of its neighborhood
- Achieve smoothing effect (remove sharp features)



Smoothing with box filter





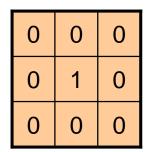
\sim	•	•	1
()	111	0.11	nal
$\mathbf{\mathcal{O}}$	\mathbf{L}	211	ıaı
	•	$\overline{}$	

0	0	0
0	1	0
0	0	0





Original





Filtered (no change)



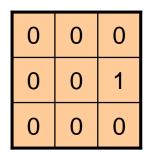
Ori	igin	al
	_	

0	0	0
0	0	1
0	0	0





Original





Shifted left By 1 pixel

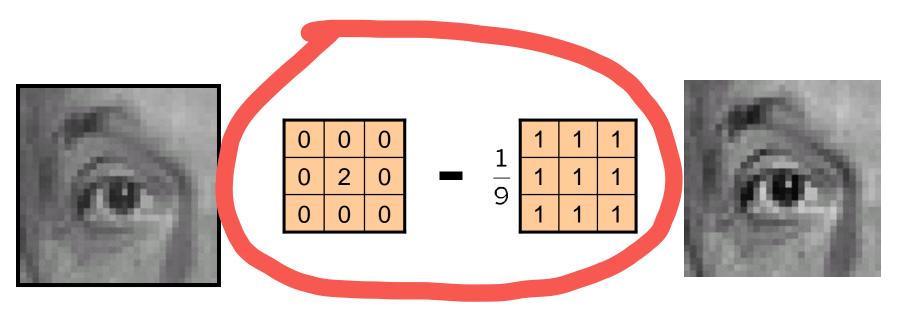


Original

0	0	0	1	1	1	1
0	2	0	<u> </u>	1	1	1
0	0	0	9	1	1	1

(Note that filter sums to 1)

Source: D. Lowe

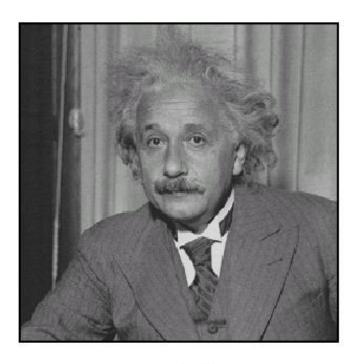


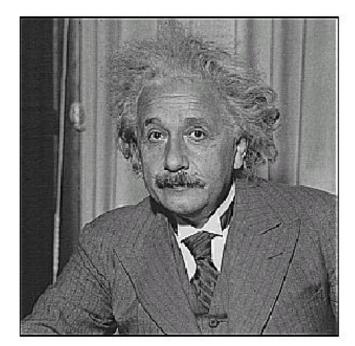
Original

Sharpening filter

- Accentuates differences with local average

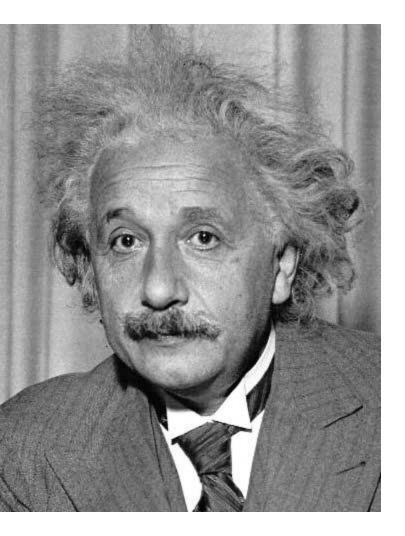
Sharpening





before after

Other filters



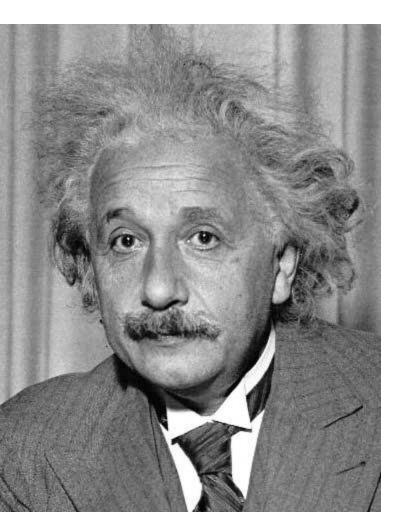
1	0	-1
2	0	-2
1	0	-1

Sobel



Vertical Edge (absolute value)

Other filters



1	2	1
0	0	0
-1	-2	-1

Sobel



Horizontal Edge (absolute value)