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Animations



Double Buffering

- Instead of one color buffer, we use two
 - **Front Buffer**: one that is displayed but not written to
 - **Back Buffer**: one that is written to but not displayed
- Program then requests a double buffer in main.c
 - `glutInitDisplayMode(GL_RGB | GL_DOUBLE)`
 - At the end of the display callback buffers are swapped

```
void mydisplay()  
{  
    glClear(GL_COLOR_BUFFER_BIT|...)  
    .  
    /* draw graphics here */  
    .  
    glutSwapBuffers()  
}
```



Using Double Buffering for Animation

For animation we can generate a sequence of progressing scenes:

1. Place scene i in the current front buffer
2. Prepare scene $i+1$ in the current back buffer
3. Swap and go to (1)

Examples of animation are located in the QT4 demos folder



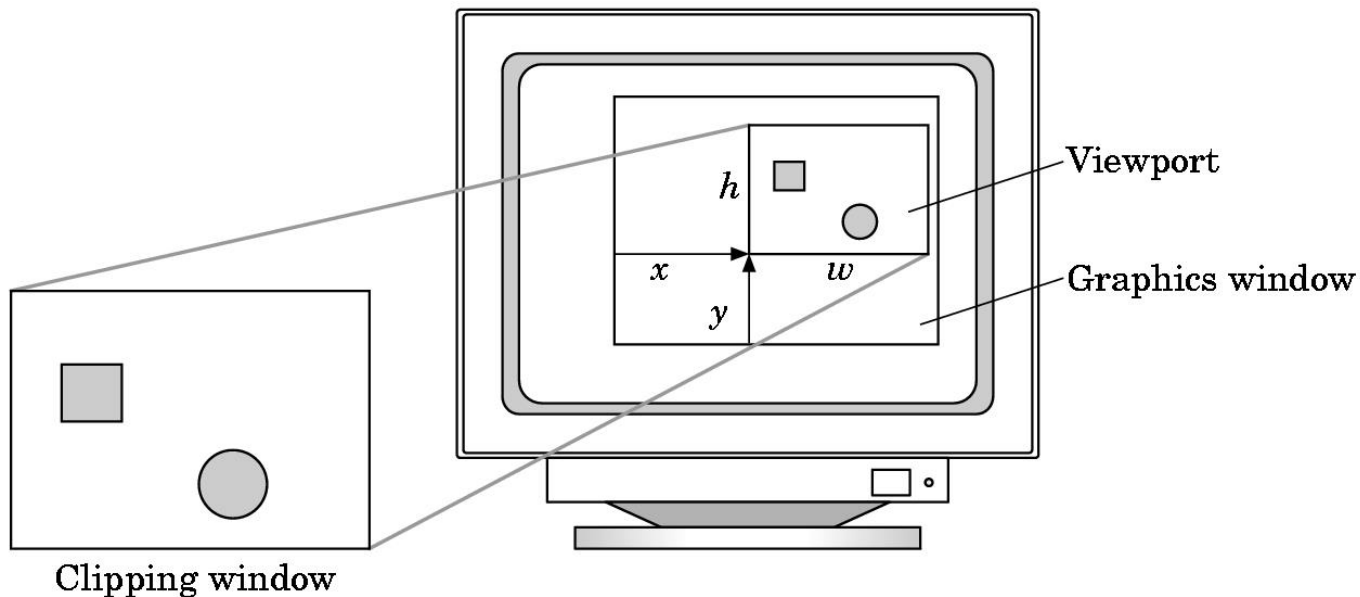
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Camera / View Volume Specifications



Viewports

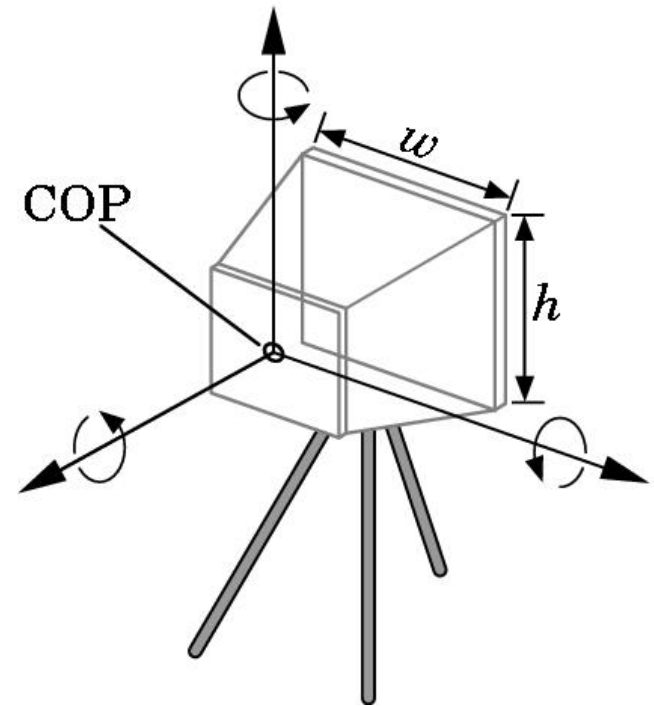
- Do not have use the entire window for the image: **`glViewport(x, y, w, h)`**
- Values in pixels (screen coordinates)





Camera Specification

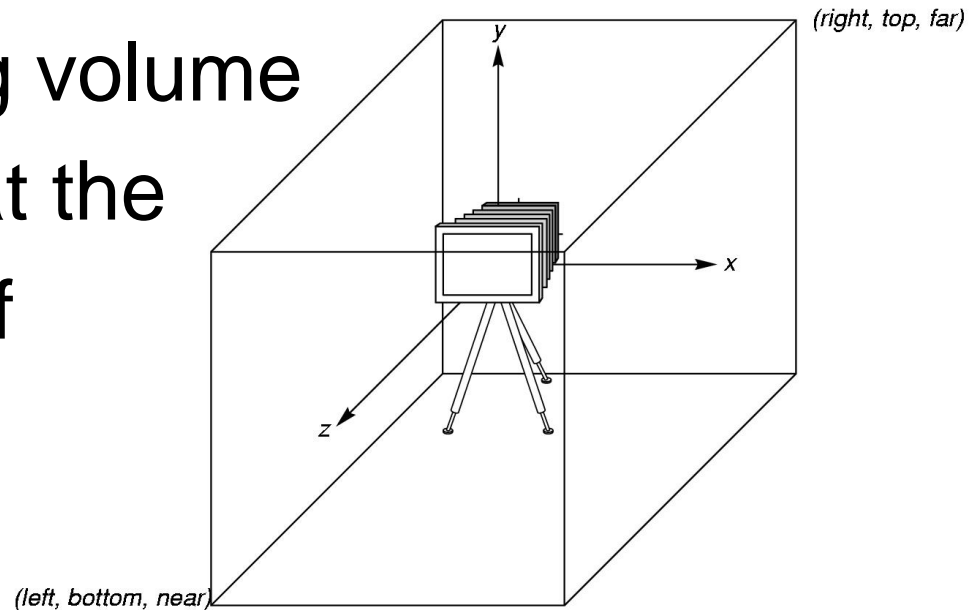
- Six degrees of freedom
 - Position of center of lens
 - Orientation
- Lens
- Film size
- Orientation of film plane





OpenGL Camera

- OpenGL places a camera at the origin in object space pointing in the negative z direction
- The default viewing volume is a box centered at the origin with a side of length 2

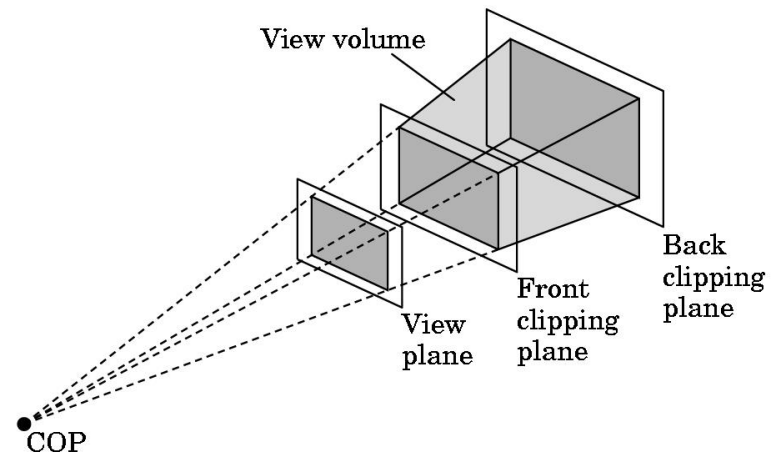
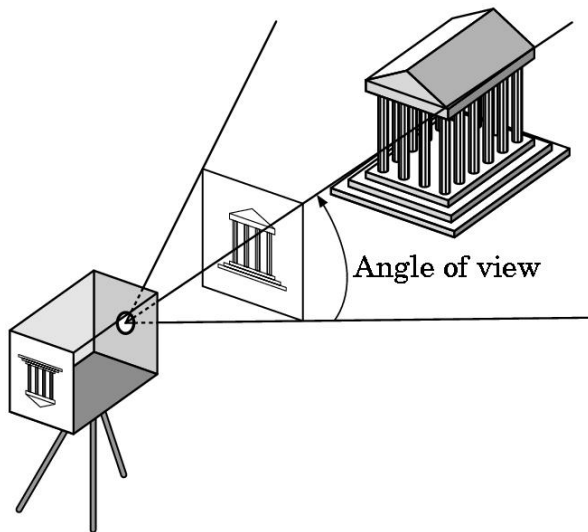




Clipping

Just as a real camera cannot “see” the whole world, the virtual camera can only see part of the world or object space

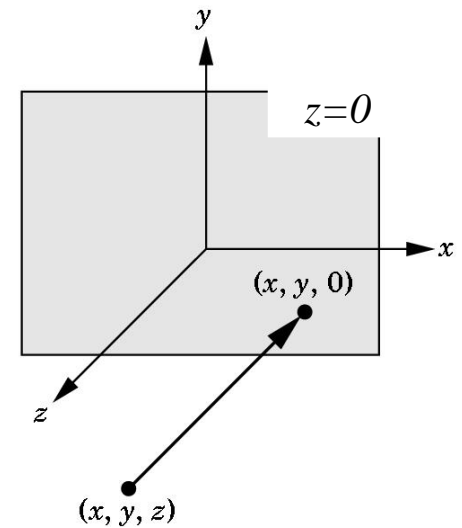
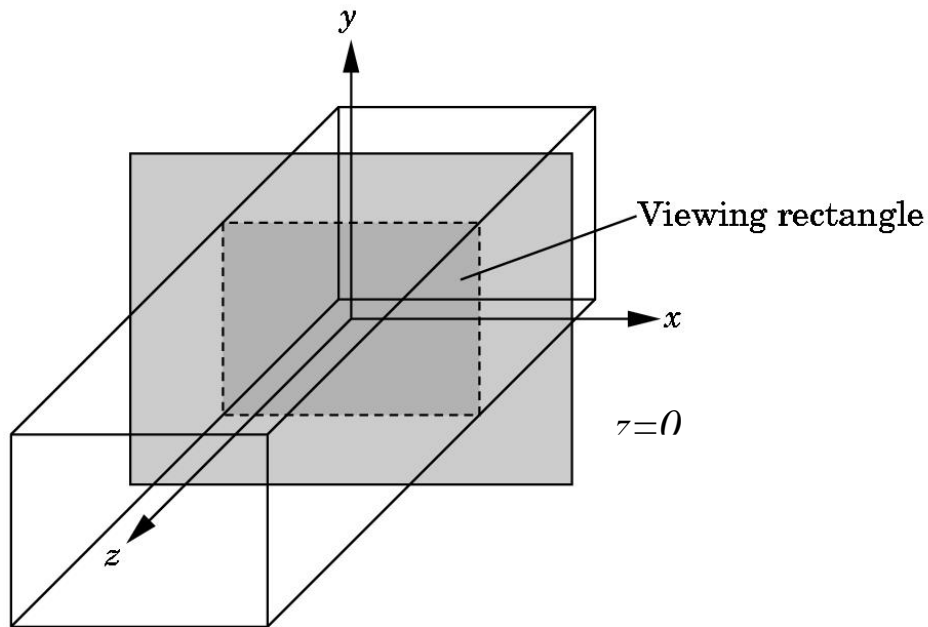
- Objects that are not within this volume are said to be *clipped* out of the scene





Orthographic Viewing

In the default orthographic view, points are projected forward along the z axis onto the plane $z=0$

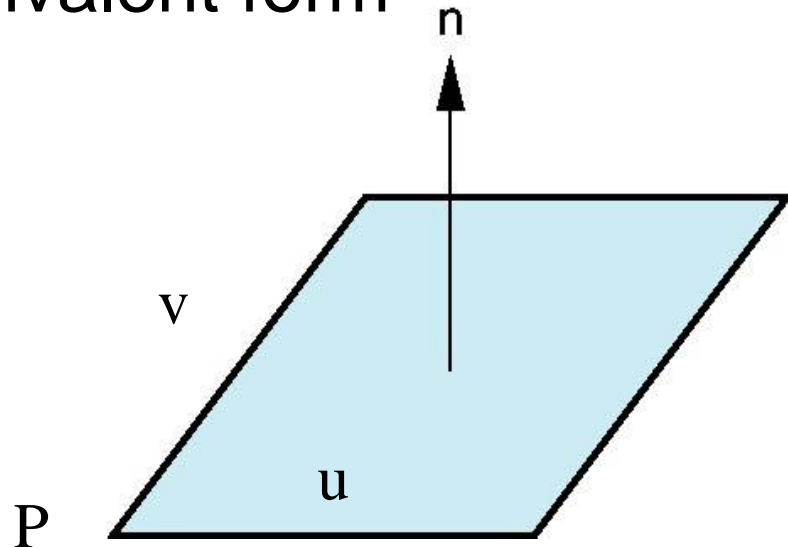




Normals

- Every plane has a vector n normal (perpendicular, orthogonal) to it
- From point-two vector form $P(\alpha, \beta) = R + \alpha u + \beta v$, we know we can use the cross product to find $n = u \times v$ and the equivalent form

$$(P(\alpha) - P) \cdot n = 0$$

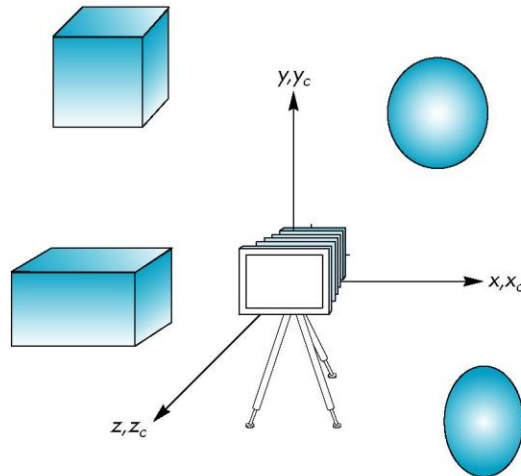




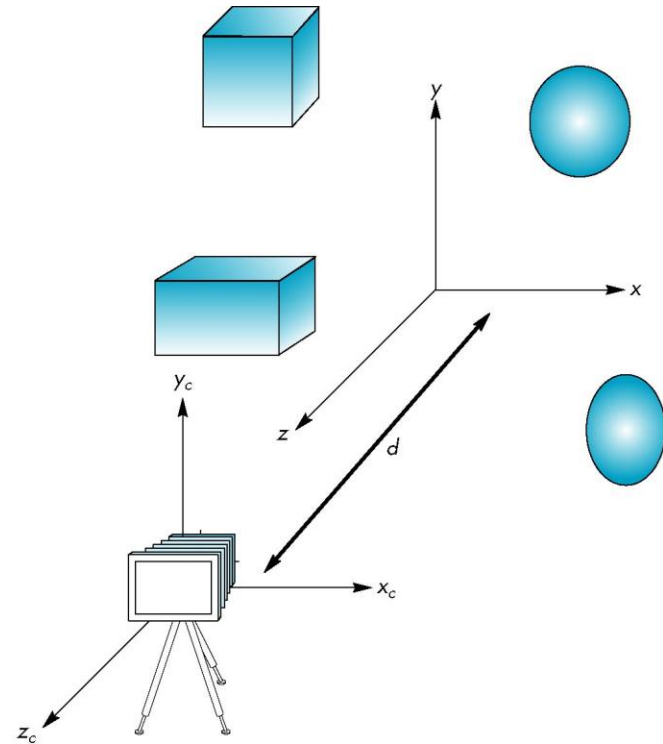
Moving the Camera

If objects are on both sides of $z=0$, we must move camera frame

$$\mathbf{M} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & -d \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



(a)

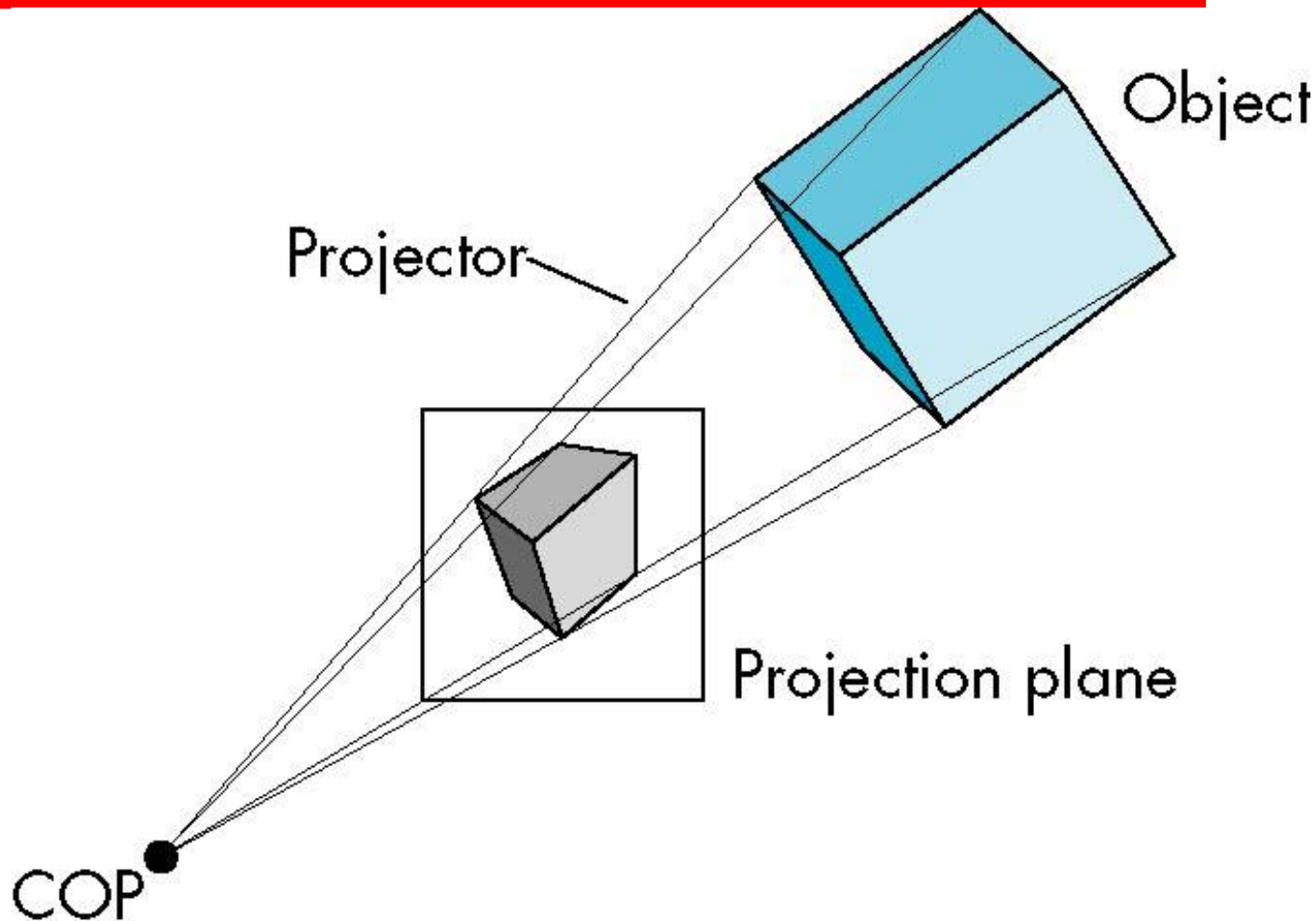


(b)



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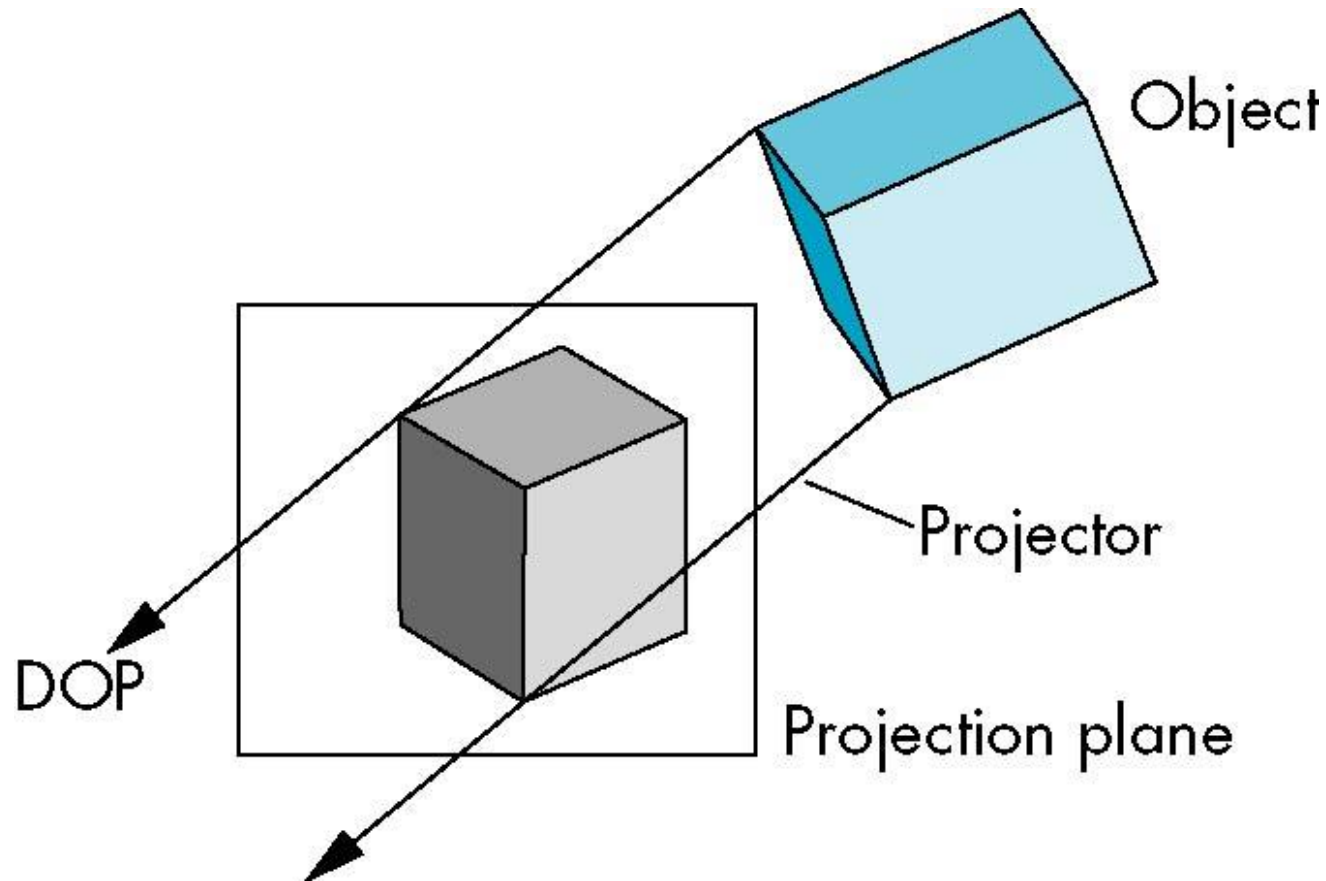
Perspective Projection





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Parallel Projection

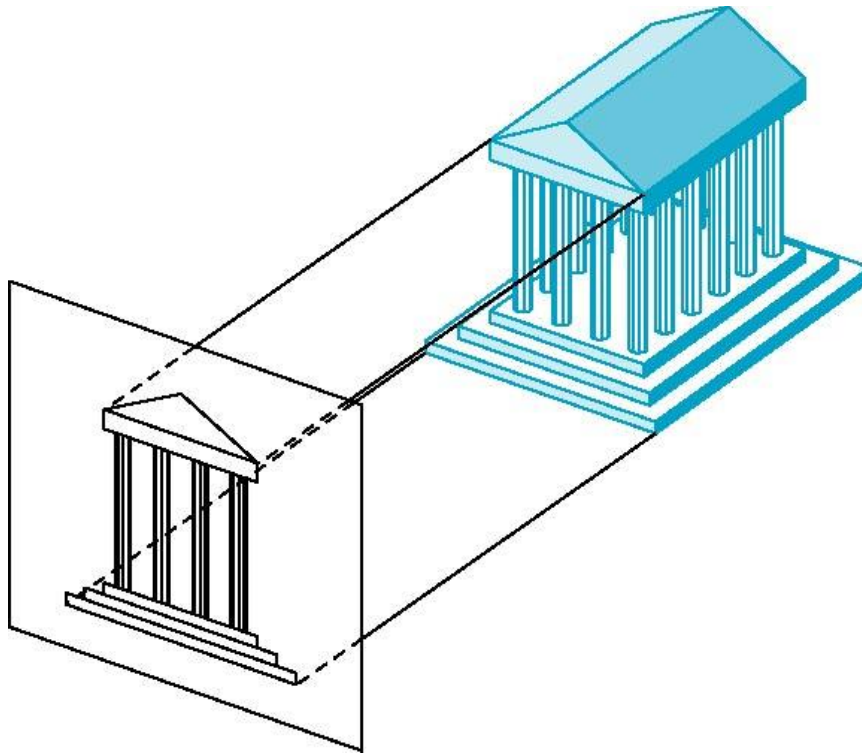




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Orthographic Projection

Projectors are orthogonal to projection surface

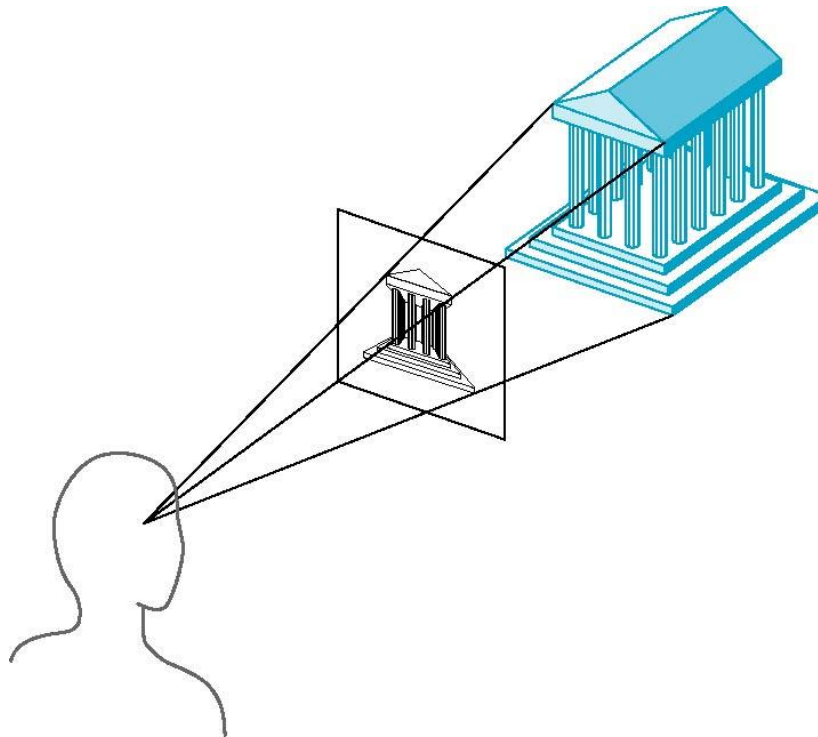




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Perspective Projection

Projectors converge at center of projection





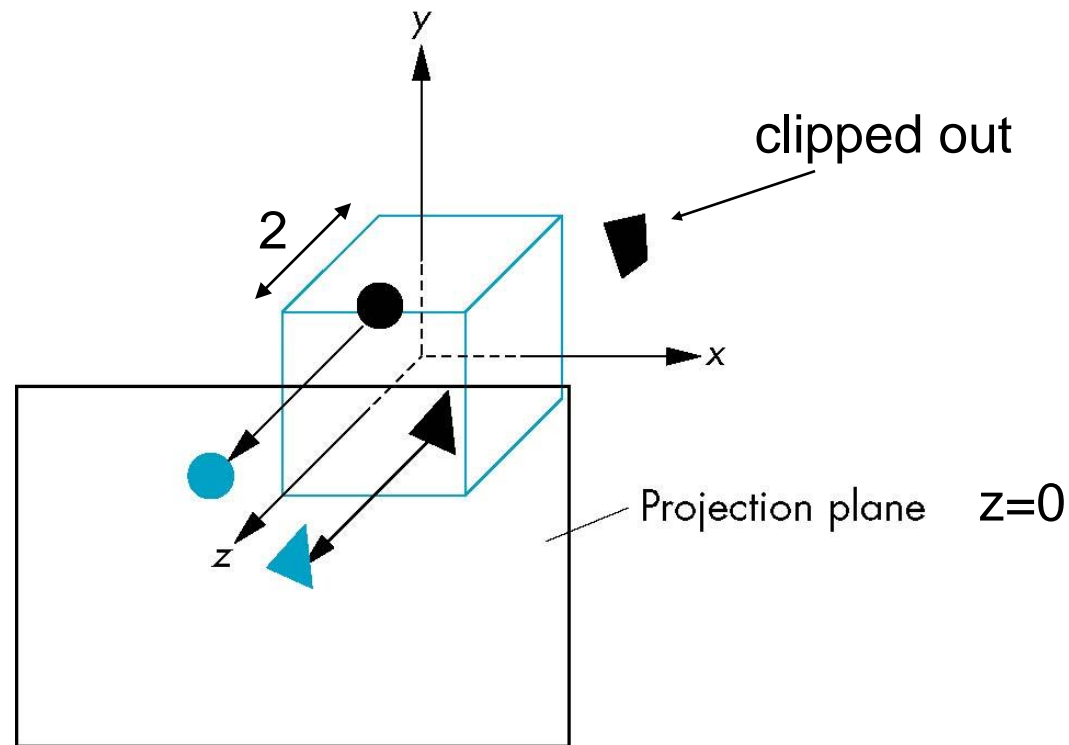
The OpenGL Camera

- In OpenGL, initially the object and camera frames are the same
 - Default model-view matrix is an identity
- The camera is located at origin and points in the negative z direction
- OpenGL also specifies a default view volume that is a cube with sides of length 2 centered at the origin
 - Default projection matrix is an identity



Default Projection

Default projection is orthogonal





Moving the Camera Frame

- If we want to visualize object with both positive and negative z values we can either
 - Move the camera in the positive z direction
 - Translate the camera frame
 - Move the objects in the negative z direction
 - Translate the world frame
- Both of these views are equivalent and are determined by the model-view matrix
 - Want a translation (`glTranslatef(0.0, 0.0, -d);`)
 - $d > 0$

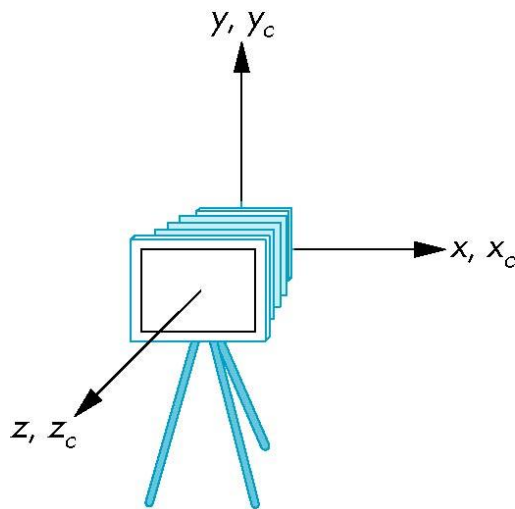


Moving Camera back from Origin

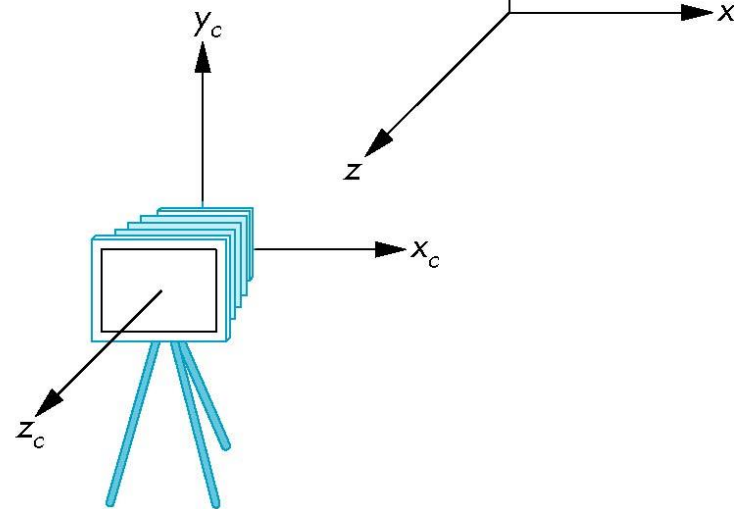
frames after translation by $-d$

$$d > 0$$

default frames



(a)

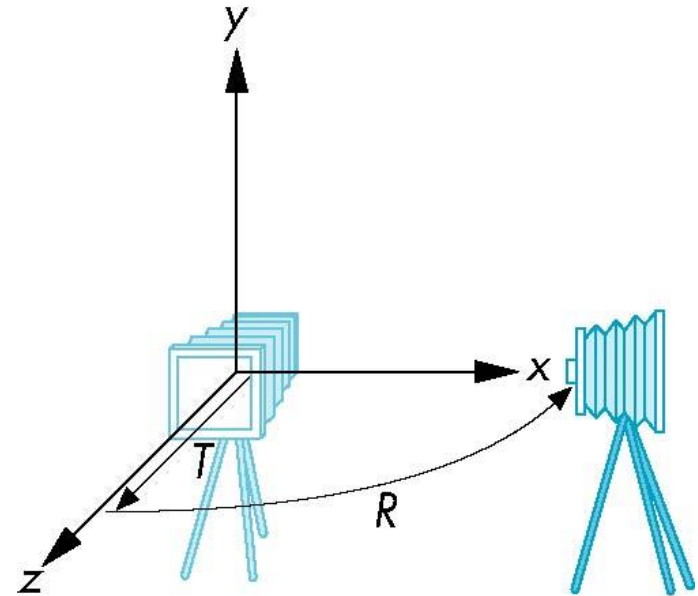


(b)



Moving the Camera

- We can move the camera to any desired position by a sequence of rotations and translations
- Example: side view
 - Rotate the camera
 - Move it away from origin
 - Model-view matrix $C = TR$





OpenGL code

- Remember that last transformation specified is first to be applied

```
glMatrixMode(GL_MODELVIEW)
glLoadIdentity();
glTranslatef(0.0, 0.0, -d);
glRotatef(90.0, 0.0, 1.0, 0.0);
```



The LookAt Function

- The GLU library contains the function `gluLookAt` to form the required modelview matrix through a simple interface
- Note the need for setting an up direction
- Still need to initialize
 - Can concatenate with modeling transformations
- Example: isometric view of cube aligned with axes

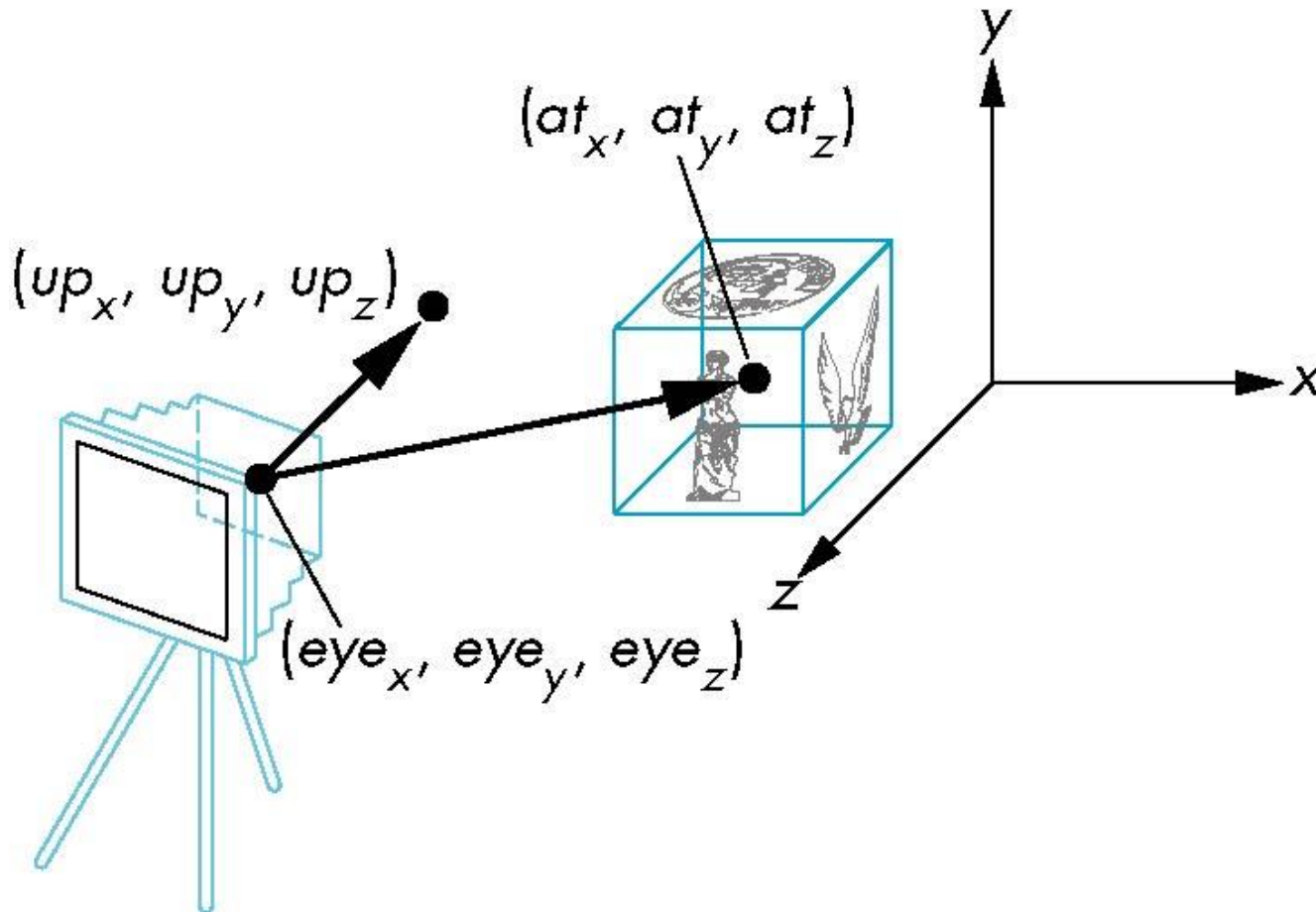
```
glMatrixMode(GL_MODELVIEW) :  
glLoadIdentity() ;  
gluLookAt(1.0, 1.0, 1.0, 0.0, 0.0, 0.0, 0., 1.0, 0.0) ;
```



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gluLookAt

`glLookAt(eyex, eyey, eyez, atx, aty, atz, upx, upy, upz)`

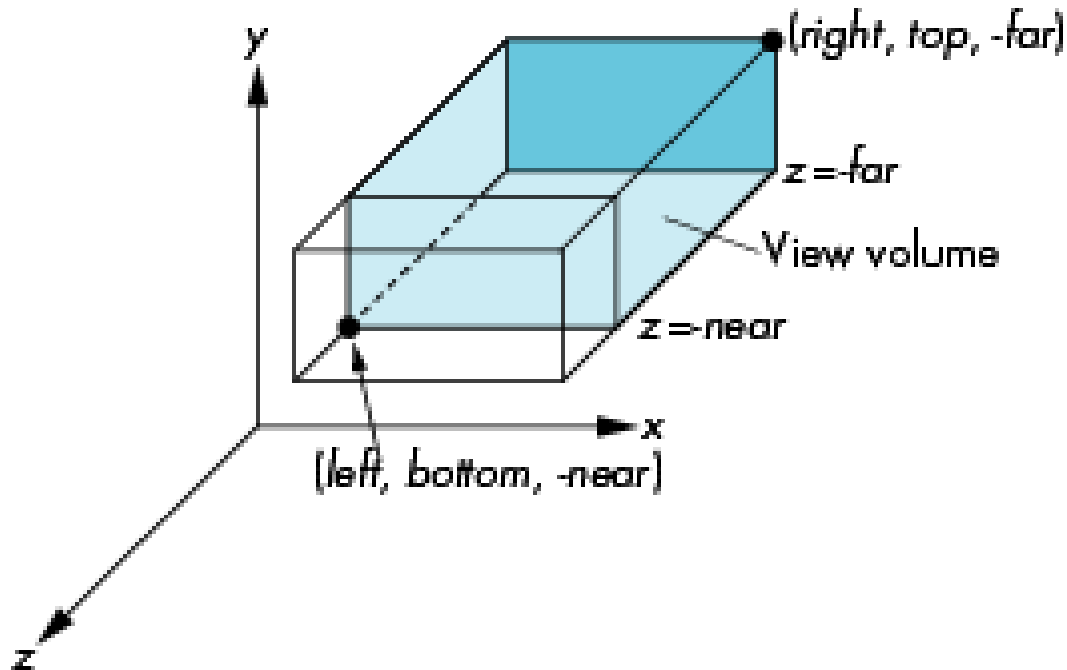




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OpenGL Orthogonal Viewing

`glOrtho(left, right, bottom, top, near, far)`



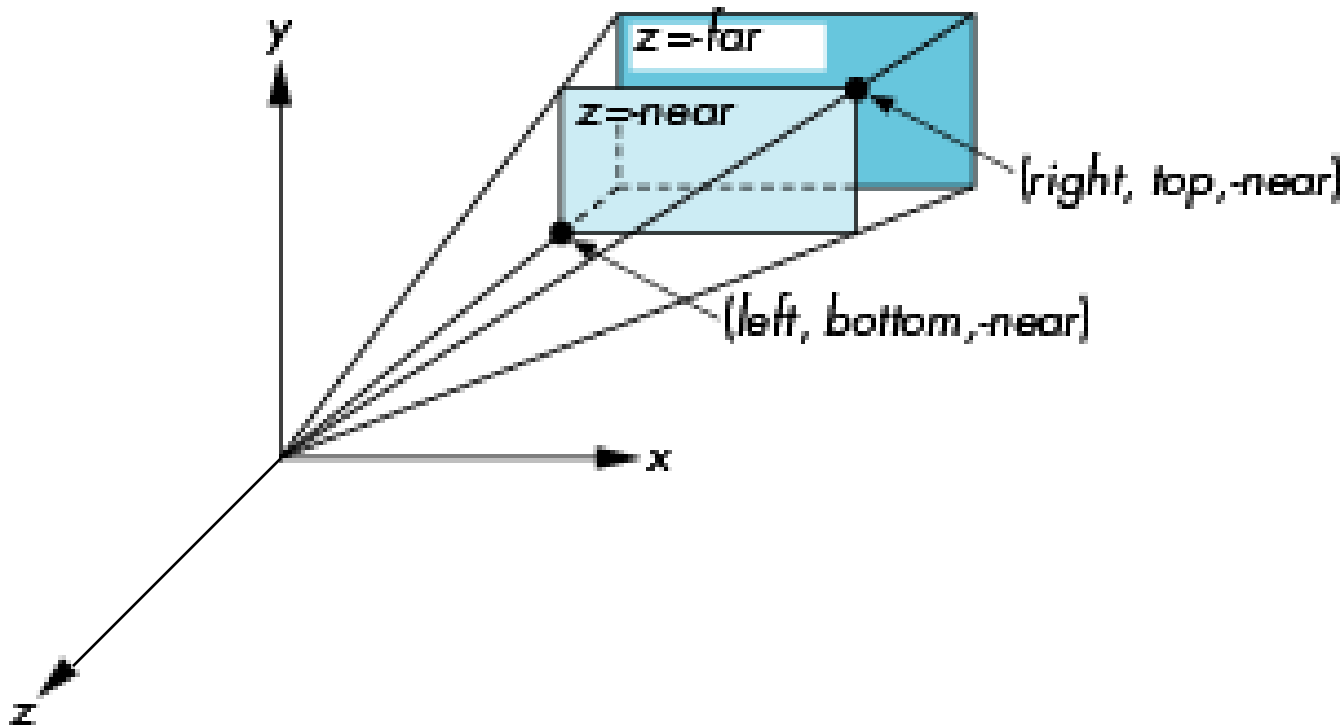
`near` and `far` measured from camera



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OpenGL Perspective

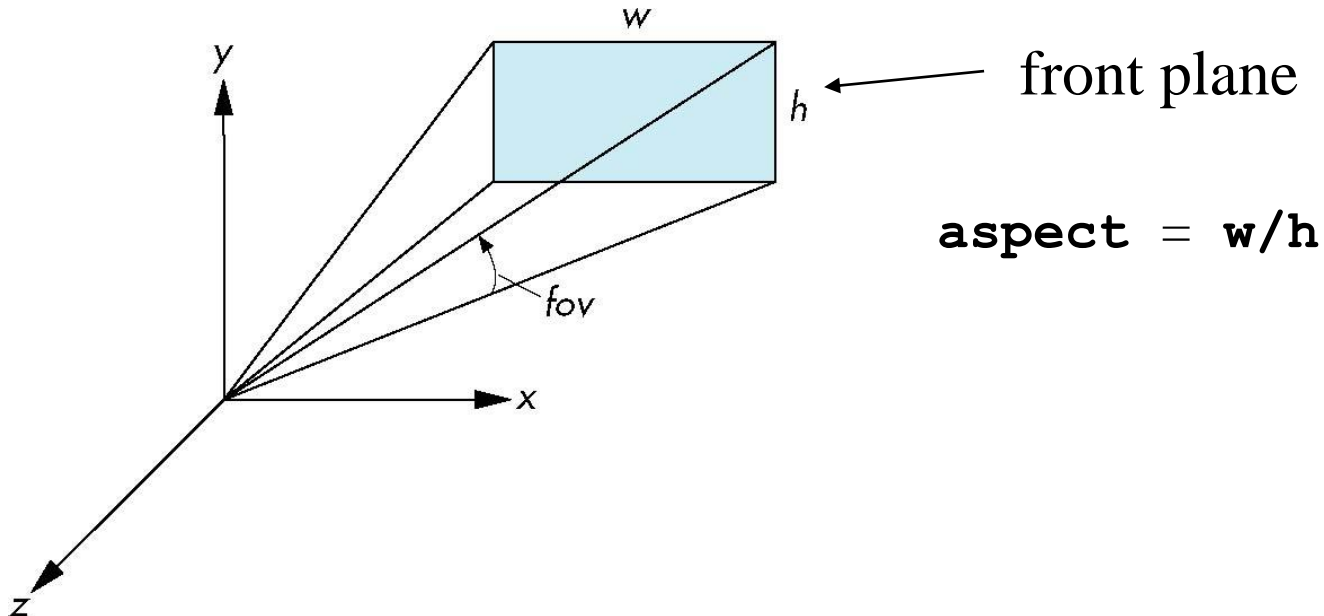
`glFrustum(left, right, bottom, top, near, far)`





Using Field of View

- With `glFrustum` it is often difficult to get the desired view
- `gluPerspective(fovy, aspect, near, far)` often provides a better interface





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Shading



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Shading I

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Objectives

- Learn to shade objects so their images appear three-dimensional
- Introduce the types of light-material interactions
- Build a simple reflection model---the Phong model--- that can be used with real time graphics hardware



Color and State

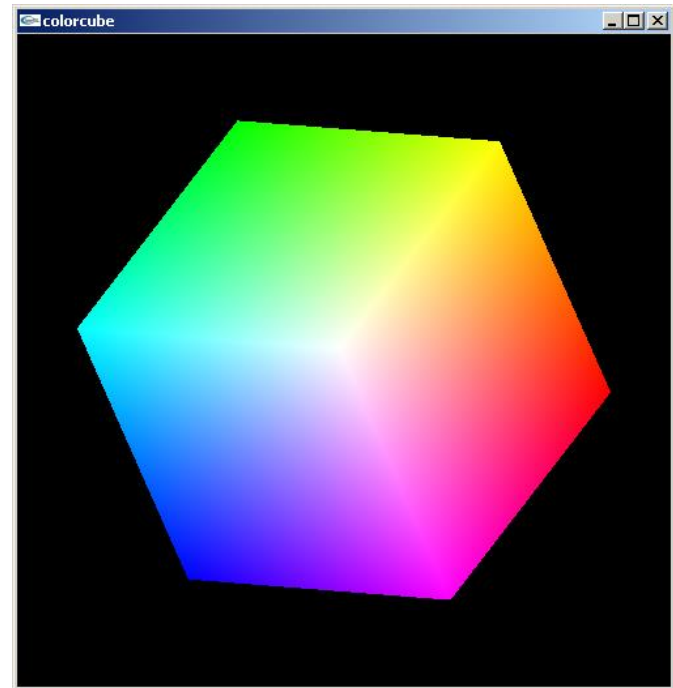
- The color as set by `glColor` becomes part of the state and will be used until changed
 - Colors and other attributes are not part of the object but are assigned when the object is rendered
- We can create conceptual *vertex colors* by code such as

```
glColor  
glVertex  
glColor  
glVertex
```



Smooth Color

- Default is *smooth* shading
 - OpenGL interpolates vertex colors across visible polygons
- Alternative is *flat shading*
 - Color of first vertex determines fill color
- **glShadeModel**
(GL_SMOOTH)
or GL_FLAT





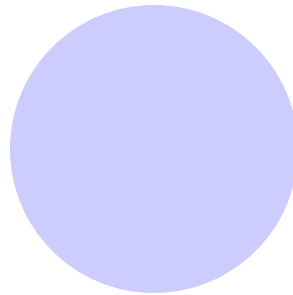
Lights and Materials

- Types of lights
 - Point sources vs distributed sources
 - Spot lights
 - Near and far sources
 - Color properties
- Material properties
 - Absorption: color properties
 - Scattering
 - Diffuse
 - Specular

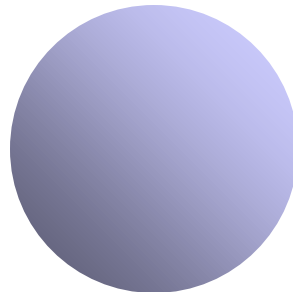


Why we need shading

- Suppose we build a model of a sphere using many polygons and color it with `glColor`. We get something like



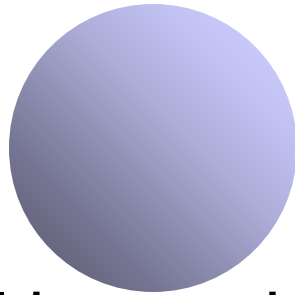
- But we want





Shading

- Why does the image of a real sphere look like

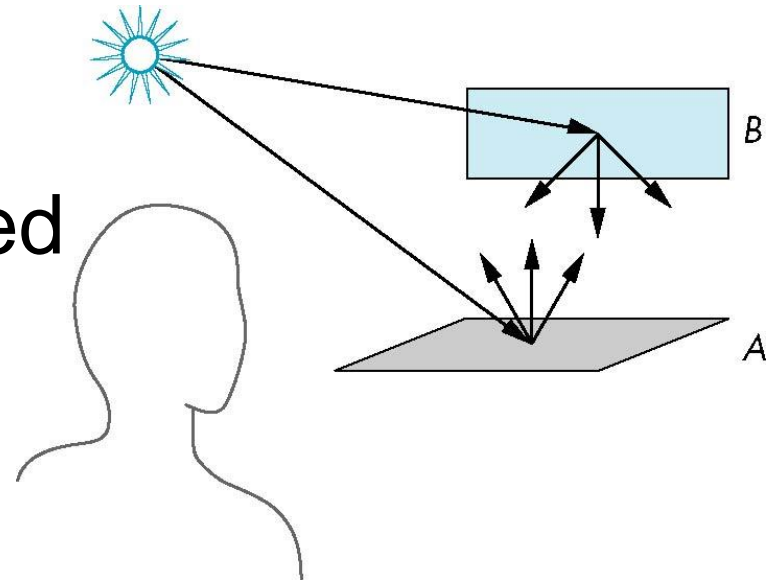


- Light-material interactions cause each point to have a different color or shade
- Need to consider
 - Light sources
 - Material properties
 - Location of viewer
 - Surface orientation



Scattering

- Light strikes A
 - Some scattered
 - Some absorbed
- Some of scattered light strikes B
 - Some scattered
 - Some absorbed
- Some of this scattered light strikes A and so on





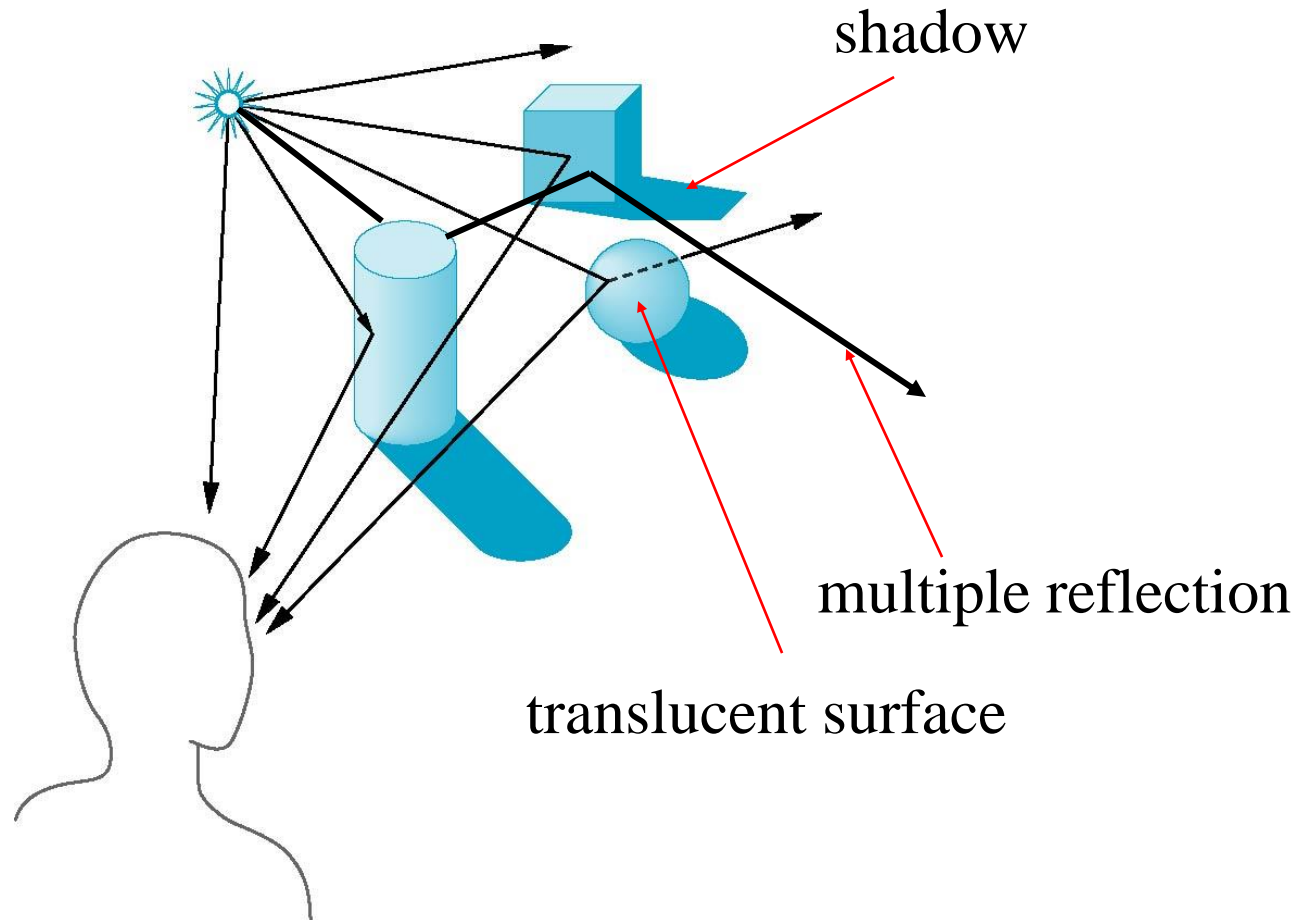
Rendering Equation

- The infinite scattering and absorption of light can be described by the *rendering equation*
 - Cannot be solved in general
 - Ray tracing is a special case for perfectly reflecting surfaces
- Rendering equation is global and includes
 - Shadows
 - Multiple scattering from object to object



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Global Effects





Local vs Global Rendering

- Correct shading requires a global calculation involving all objects and light sources
 - Incompatible with pipeline model which shades each polygon independently (local rendering)
- However, in computer graphics, especially real time graphics, we are happy if things “look right”
 - Exist many techniques for approximating global effects



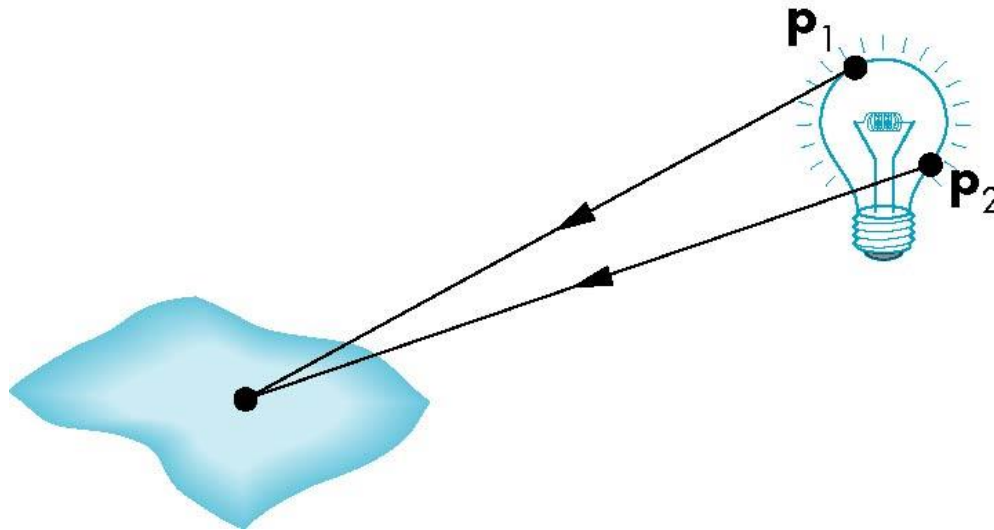
Light-Material Interaction

- Light that strikes an object is partially absorbed and partially scattered (reflected)
- The amount reflected determines the color and brightness of the object
 - A surface appears red under white light because the red component of the light is reflected and the rest is absorbed
- The reflected light is scattered in a manner that depends on the smoothness and orientation of the surface



Light Sources

General light sources are difficult to work with because we must integrate light coming from all points on the source





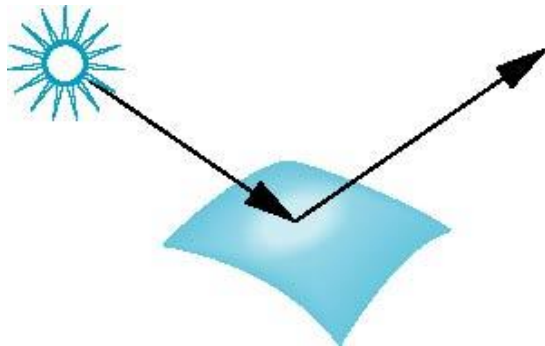
Simple Light Sources

- Point source
 - Model with position and color
 - Distant source = infinite distance away (parallel)
- Spotlight
 - Restrict light from ideal point source
- Ambient light
 - Same amount of light everywhere in scene
 - Can model contribution of many sources and reflecting surfaces

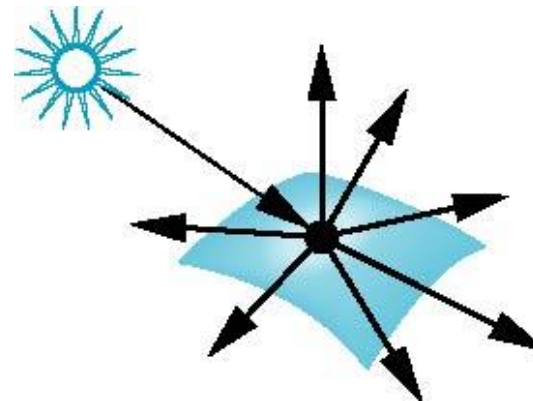


Surface Types

- The smoother a surface, the more reflected light is concentrated in the direction a perfect mirror would reflect the light
- A very rough surface scatters light in all directions



smooth surface

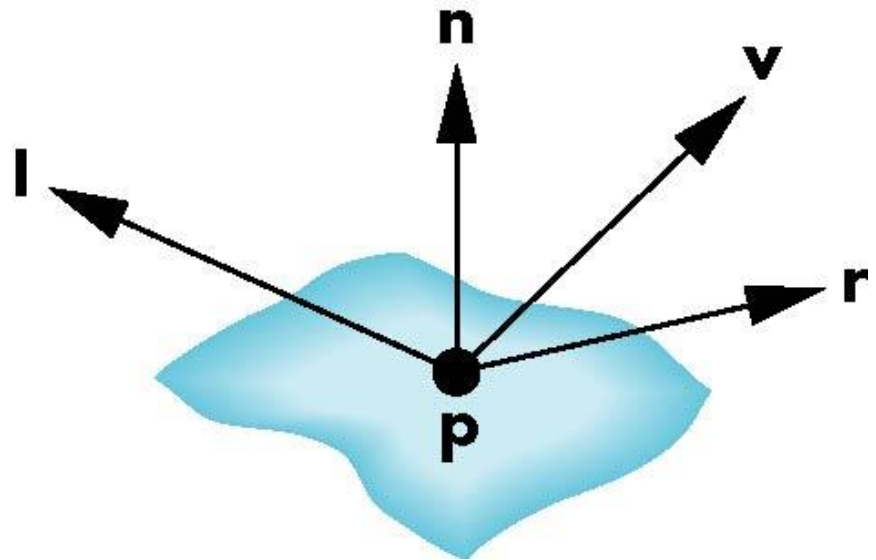


rough surface



Phong Model

- A simple model that can be computed rapidly
- Has three components
 - Diffuse
 - Specular
 - Ambient
- Uses four vectors
 - To source
 - To viewer
 - Normal
 - Perfect reflector

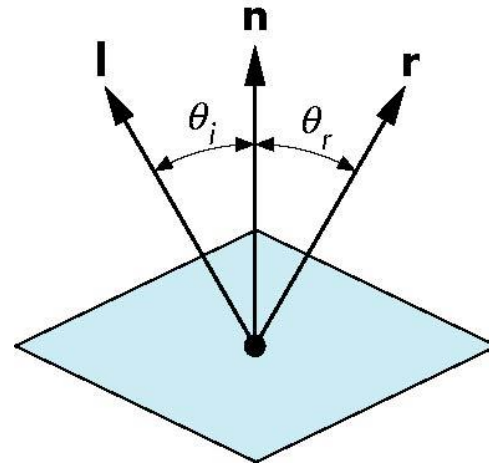




Ideal Reflector

- Normal is determined by local orientation
- Angle of incidence = angle of reflection
- The three vectors must be coplanar

$$\mathbf{r} = 2 (\mathbf{l} \cdot \mathbf{n}) \mathbf{n} - \mathbf{l}$$





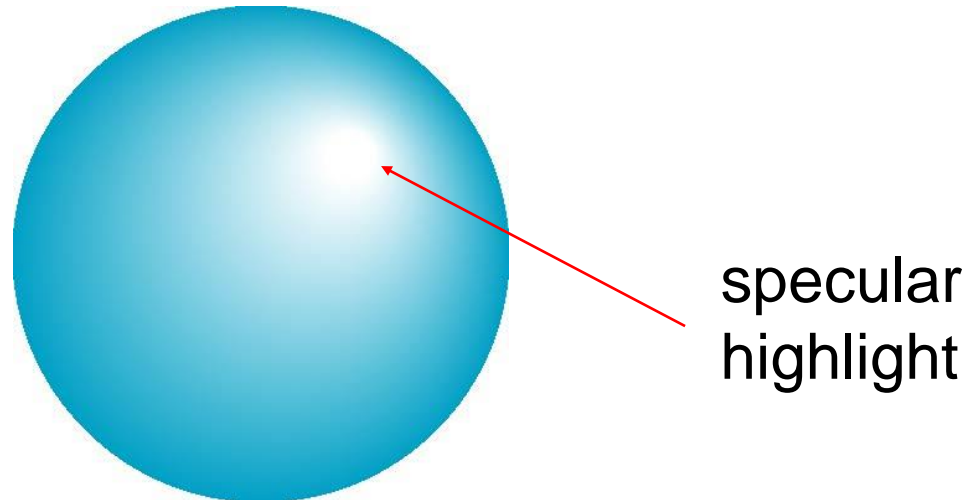
Lambertian Surface

- Perfectly diffuse reflector
- Light scattered equally in all directions
- Amount of light reflected is proportional to the vertical component of incoming light
 - reflected light $\sim \cos \theta_i$
 - $\cos \theta_i = \mathbf{l} \cdot \mathbf{n}$ if vectors normalized
 - There are also three coefficients, k_r , k_b , k_g that show how much of each color component is reflected



Specular Surfaces

- Most surfaces are neither ideal diffusers nor perfectly specular (ideal reflectors)
- Smooth surfaces show specular highlights due to incoming light being reflected in directions concentrated close to the direction of a perfect reflection





Modeling Specular Reflections

- Phong proposed using a term that dropped off as the angle between the viewer and the ideal reflection increased

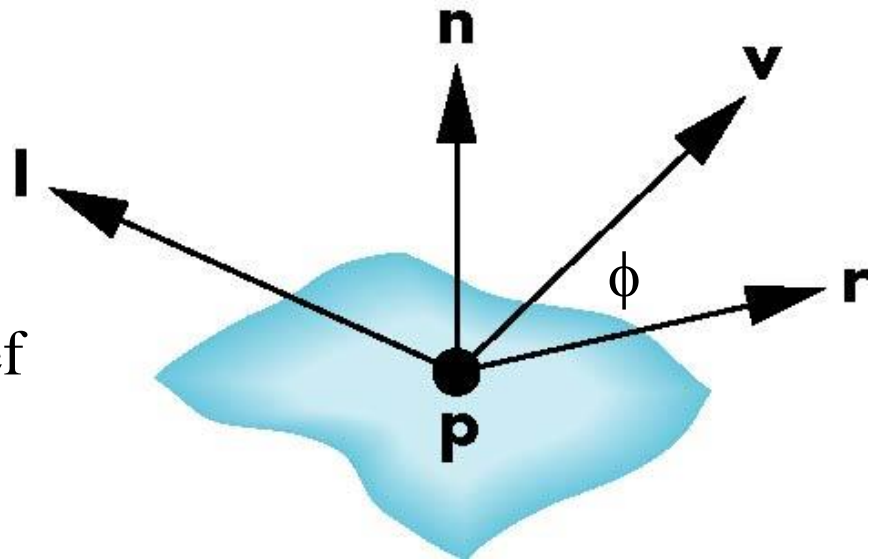
$$I_r \sim k_s I \cos^\alpha \phi$$

reflected intensity

absorption coef

incoming intensity

shininess coef

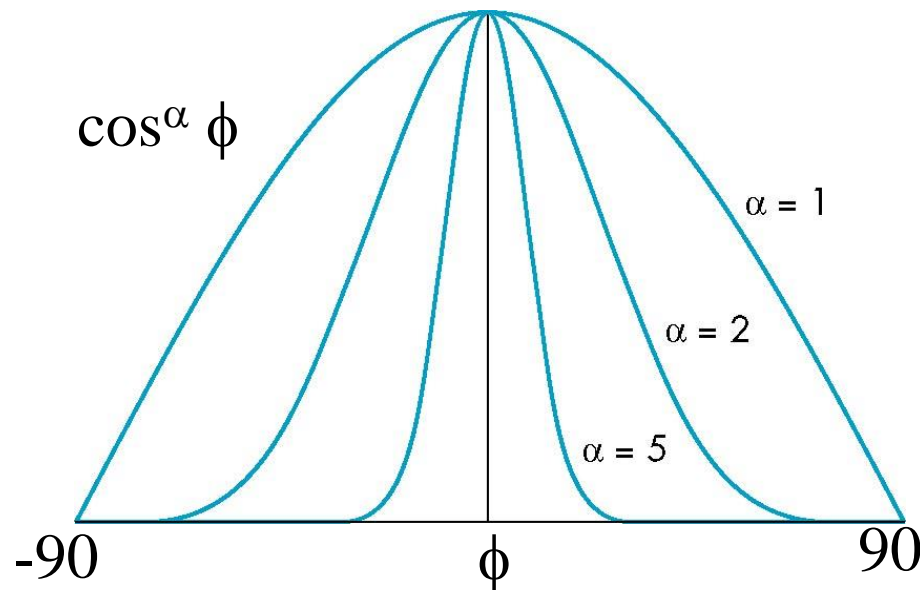




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The Shininess Coefficient

- Values of α between 100 and 200 correspond to metals
- Values between 5 and 10 give surface that look like plastic





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Shading II

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Objectives

- Continue discussion of shading
- Introduce modified Phong model
- Consider computation of required vectors



Ambient Light

- Ambient light is the result of multiple interactions between (large) light sources and the objects in the environment
- Amount and color depend on both the color of the light(s) and the material properties of the object
- Add $k_a I_a$ to diffuse and specular terms

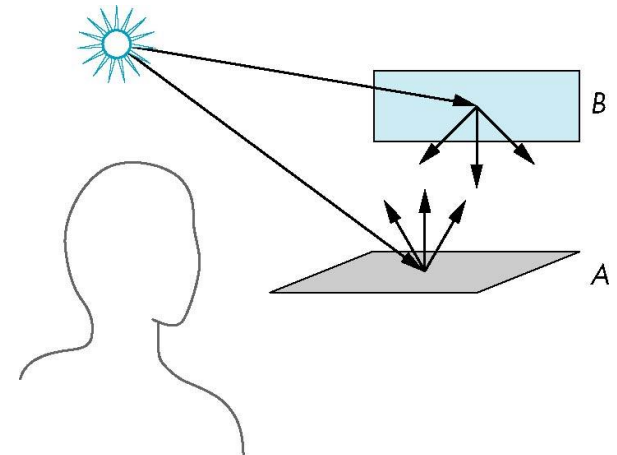
reflection coef

intensity of ambient light



Distance Terms

- The light from a point source that reaches a surface is inversely proportional to the square of the distance between them
- We can add a factor of the form $1/(ad + bd + cd^2)$ to the diffuse and specular terms
- The constant and linear terms soften the effect of the point source





Light Sources

- In the Phong Model, we add the results from each light source
- Each light source has separate diffuse, specular, and ambient terms to allow for maximum flexibility even though this form does not have a physical justification
- Separate red, green and blue components
- Hence, 9 coefficients for each point source
 - $I_{dr}, I_{dg}, I_{db}, I_{sr}, I_{sg}, I_{sb}, I_{ar}, I_{ag}, I_{ab}$



Material Properties

- Material properties match light source properties
 - Nine absorption coefficients
 - k_{dr} , k_{dg} , k_{db} , k_{sr} , k_{sg} , k_{sb} , k_{ar} , k_{ag} , k_{ab}
 - Shininess coefficient α

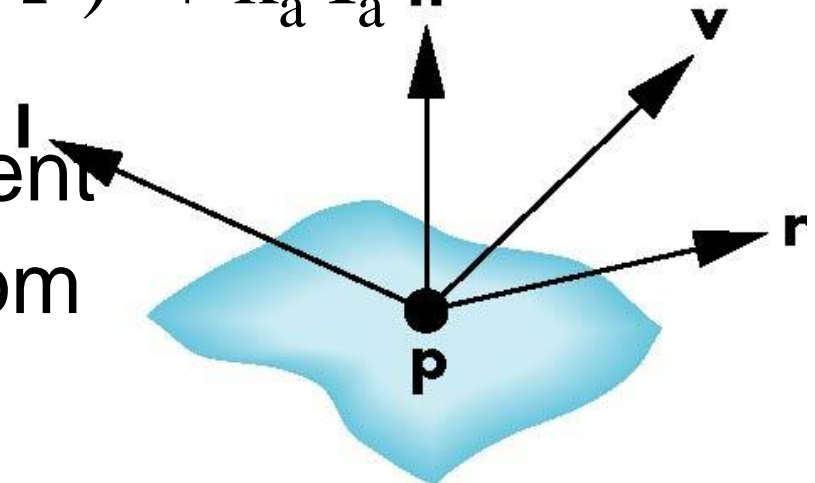


Adding up the Components

For each light source and each color component, the Phong model can be written (without the distance terms) as

$$I = k_d I_d \mathbf{l} \cdot \mathbf{n} + k_s I_s (\mathbf{v} \cdot \mathbf{r})^\alpha + k_a I_a$$

For each color component we add contributions from all sources





Modified Phong Model

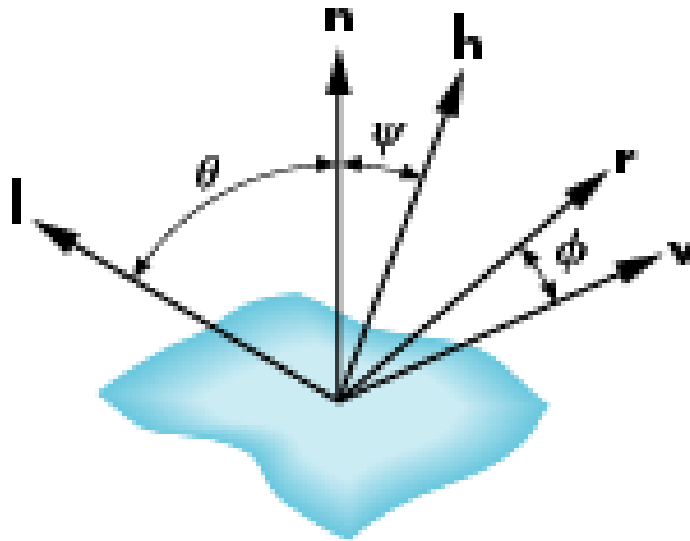
- The specular term in the Phong model is problematic because it requires the calculation of a new reflection vector and view vector for each vertex
- Blinn suggested an approximation using the halfway vector that is more efficient



The Halfway Vector

- ***h*** is normalized vector halfway between ***l*** and ***v***

$$\mathbf{h} = (\mathbf{l} + \mathbf{v}) / |\mathbf{l} + \mathbf{v}|$$





Using the halfway vector

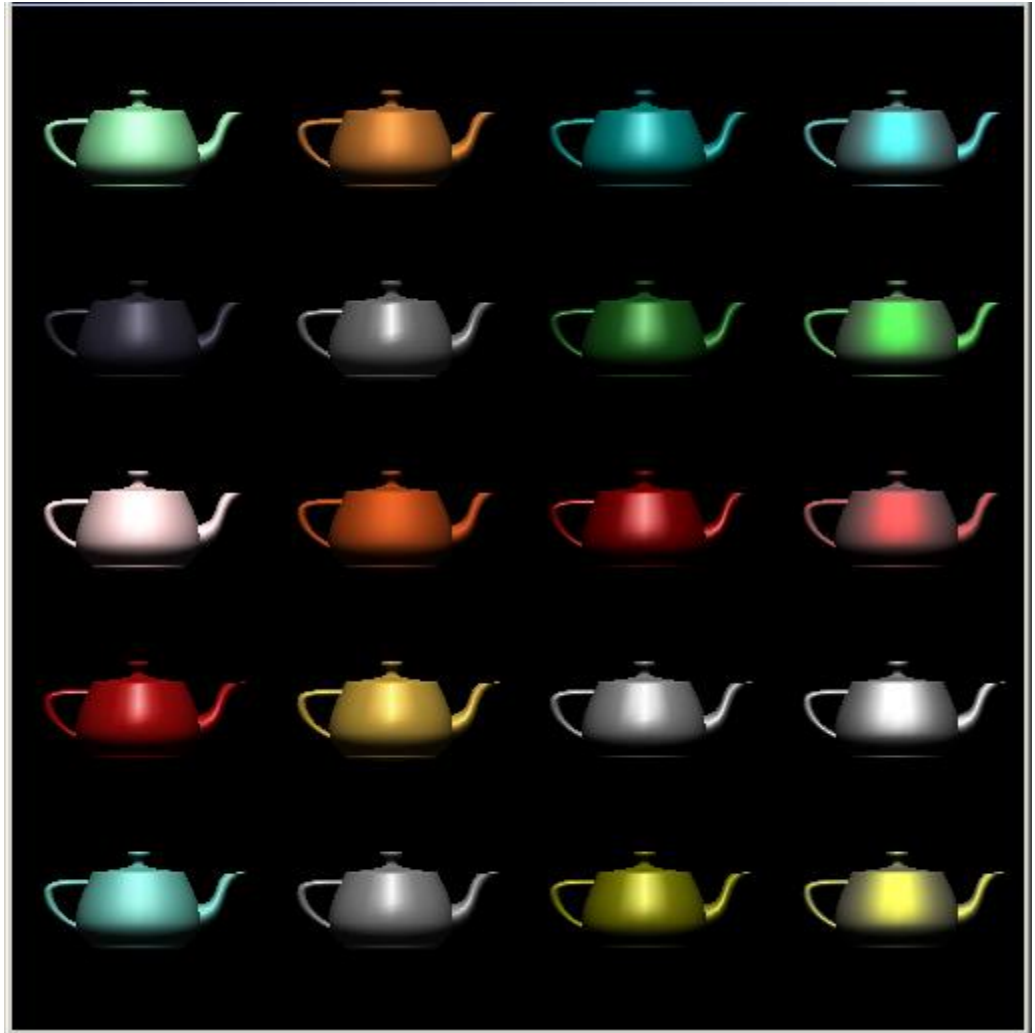
- Replace $(\mathbf{v} \cdot \mathbf{r})^\alpha$ by $(\mathbf{n} \cdot \mathbf{h})^\beta$
- β is chosen to match shininess
- Note that halfway angle is half of angle between \mathbf{r} and \mathbf{v} if vectors are coplanar
- Resulting model is known as the modified Phong or Blinn lighting model
 - Specified in OpenGL standard



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Example

Only differences in these teapots are the parameters in the modified Phong model





Computation of Vectors

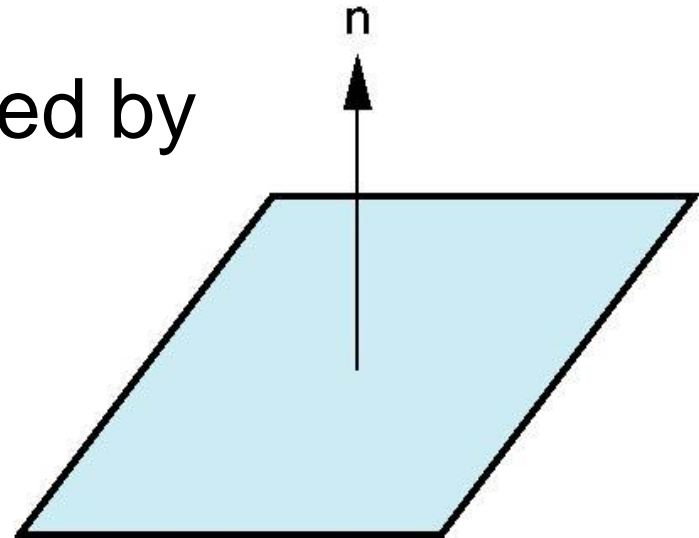
- \mathbf{l} and \mathbf{v} are specified by the application
- Can compute \mathbf{r} from \mathbf{l} and \mathbf{n}
- Problem is determining \mathbf{n}
- For simple surfaces \mathbf{n} can be determined but how we determine \mathbf{n} differs depending on underlying representation of surface
- OpenGL leaves determination of normal to application
 - Exception for GLU quadrics and Bezier surfaces (Chapter 11)



Plane Normals

- Equation of plane: $ax+by+cz+d = 0$
- From Chapter 4 we know that plane is determined by three points p_0, p_2, p_3 or normal \mathbf{n} and p_0
- Normal can be obtained by

$$\mathbf{n} = (p_2 - p_0) \times (p_1 - p_0)$$





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Shading in OpenGL

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Objectives

- Introduce the OpenGL shading functions
- Discuss polygonal shading
 - Flat
 - Smooth
 - Gouraud



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Steps in OpenGL shading

1. Enable shading and select model
2. Specify normals
3. Specify material properties
4. Specify lights



Normals

- In OpenGL the normal vector is part of the state
- Set by `glNormal*` ()
 - `glNormal3f(x, y, z);`
 - `glNormal3fv(p);`
- Usually we want to set the normal to have unit length so cosine calculations are correct
 - Length can be affected by transformations
 - Note that scaling does not preserved length
 - `glEnable(GL_NORMALIZE)` allows for autonormalization at a performance penalty



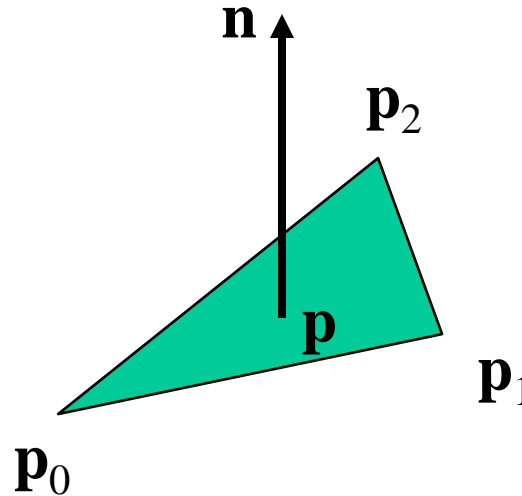
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Normal for Triangle

plane $\mathbf{n} \cdot (\mathbf{p} - \mathbf{p}_0) = 0$

$$\mathbf{n} = (\mathbf{p}_2 - \mathbf{p}_0) \times (\mathbf{p}_1 - \mathbf{p}_0)$$

normalize $\mathbf{n} \leftarrow \mathbf{n} / |\mathbf{n}|$



Note that right-hand rule determines outward face



Enabling Shading

- Shading calculations are enabled by
 - `glEnable(GL_LIGHTING)`
 - Once lighting is enabled, `glColor()` ignored
- Must enable each light source individually
 - `glEnable(GL_LIGHTi)` $i=0,1,\dots$
- Can choose light model parameters
 - `glLightModeli(parameter, GL_TRUE)`
 - `GL_LIGHT_MODEL_LOCAL_VIEWER` do not use simplifying distant viewer assumption in calculation
 - `GL_LIGHT_MODEL_TWO_SIDED` shades both sides of polygons independently



Defining a Point Light Source

- For each light source, we can set an RGBA for the diffuse, specular, and ambient components, and for the position

```
GL float diffuse0[]={1.0, 0.0, 0.0, 1.0};  
GL float ambient0[]={1.0, 0.0, 0.0, 1.0};  
GL float specular0[]={1.0, 0.0, 0.0, 1.0};  
GLfloat light0_pos[]={1.0, 2.0, 3.0, 1.0};
```

```
glEnable(GL_LIGHTING);  
glEnable(GL_LIGHT0);  
glLightv(GL_LIGHT0, GL_POSITION, light0_pos);  
glLightv(GL_LIGHT0, GL_AMBIENT, ambient0);  
glLightv(GL_LIGHT0, GL_DIFFUSE, diffuse0);  
glLightv(GL_LIGHT0, GL_SPECULAR, specular0);
```



Distance and Direction

- The source colors are specified in RGBA
- The position is given in homogeneous coordinates
 - If $w = 1.0$, we are specifying a finite location
 - If $w = 0.0$, we are specifying a parallel source with the given direction vector
- The coefficients in the distance terms are by default $a=1.0$ (constant terms), $b=c=0.0$ (linear and quadratic terms). Change by

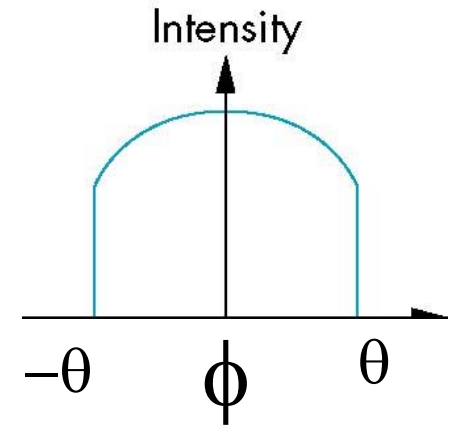
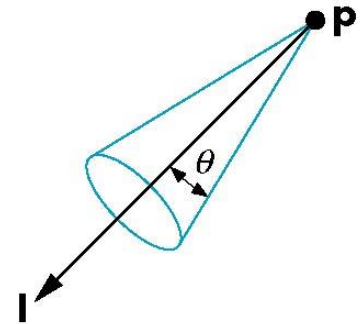
```
a= 0.80;
```

```
glLightf(GL_LIGHT0, GLCONSTANT_ATTENUATION, a);
```



Spotlights

- Use `glLightv` to set
 - Direction `GL_SPOT_DIRECTION`
 - Cutoff `GL_SPOT_CUTOFF`
 - Attenuation `GL_SPOT_EXPONENT`
 - Proportional to $\cos^\alpha \phi$





Global Ambient Light

- Ambient light depends on color of light sources
 - A red light in a white room will cause a red ambient term that disappears when the light is turned off
- OpenGL also allows a global ambient term that is often helpful for testing
 - `glLightModelfv(GL_LIGHT_MODEL_AMBIENT, global_ambient)`



Moving Light Sources

- Light sources are geometric objects whose positions or directions are affected by the model-view matrix
- Depending on where we place the position (direction) setting function, we can
 - Move the light source(s) with the object(s)
 - Fix the object(s) and move the light source(s)
 - Fix the light source(s) and move the object(s)
 - Move the light source(s) and object(s) independently



Material Properties

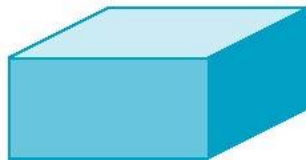
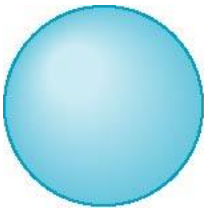
- Material properties are also part of the OpenGL state and match the terms in the modified Phong model
- Set by `glMaterialv()`

```
GLfloat ambient[] = {0.2, 0.2, 0.2, 1.0};  
GLfloat diffuse[] = {1.0, 0.8, 0.0, 1.0};  
GLfloat specular[] = {1.0, 1.0, 1.0, 1.0};  
GLfloat shine = 100.0  
glMaterialf(GL_FRONT, GL_AMBIENT, ambient);  
glMaterialf(GL_FRONT, GL_DIFFUSE, diffuse);  
glMaterialf(GL_FRONT, GL_SPECULAR, specular);  
glMaterialf(GL_FRONT, GL_SHININESS, shine);
```

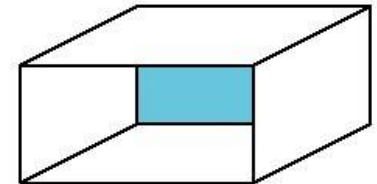
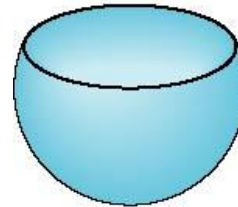


Front and Back Faces

- The default is shade only front faces which works correctly for convex objects
- If we set two sided lighting, OpenGL will shade both sides of a surface
- Each side can have its own properties which are set by using `GL_FRONT`, `GL_BACK`, or `GL_FRONT_AND_BACK` in `glMaterialf`



back faces not visible



back faces visible



Emissive Term

- We can simulate a light source in OpenGL by giving a material an emissive component
- This component is unaffected by any sources or transformations

```
GLfloat emission[] = 0.0, 0.3, 0.3, 1.0);  
glMaterialf(GL_FRONT, GL_EMISSION, emission);
```



Transparency

- Material properties are specified as RGBA values
- The A value can be used to make the surface translucent
- The default is that all surfaces are opaque regardless of A
- Later we will enable blending and use this feature



Polygonal Shading

- Shading calculations are done for each vertex
 - Vertex colors become vertex shades
- By default, vertex shades are interpolated across the polygon
 - `glShadeModel (GL_SMOOTH) ;`
- If we use `glShadeModel (GL_FLAT) ;` the color at the first vertex will determine the shade of the whole polygon



Polygon Normals

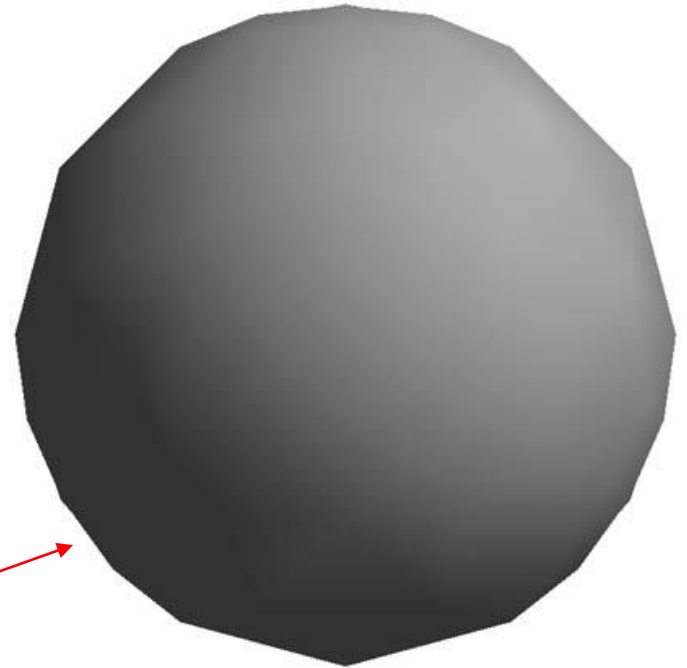
- Polygons have a single normal
 - Shades at the vertices as computed by the Phong model can be almost same
 - Identical for a distant viewer (default) or if there is no specular component
- Consider model of sphere
- Want different normals at each vertex even though this concept is not quite correct mathematically





Smooth Shading

- We can set a new normal at each vertex
- Easy for sphere model
 - If centered at origin $\mathbf{n} = \mathbf{p}$
- Now smooth shading works
- Note *silhouette edge*





Mesh Shading

- The previous example is not general because we knew the normal at each vertex analytically
- For polygonal models, Gouraud proposed we use the average of the normals around a mesh vertex

$$\mathbf{n} = (\mathbf{n}_1 + \mathbf{n}_2 + \mathbf{n}_3 + \mathbf{n}_4) / |\mathbf{n}_1 + \mathbf{n}_2 + \mathbf{n}_3 + \mathbf{n}_4|$$

