

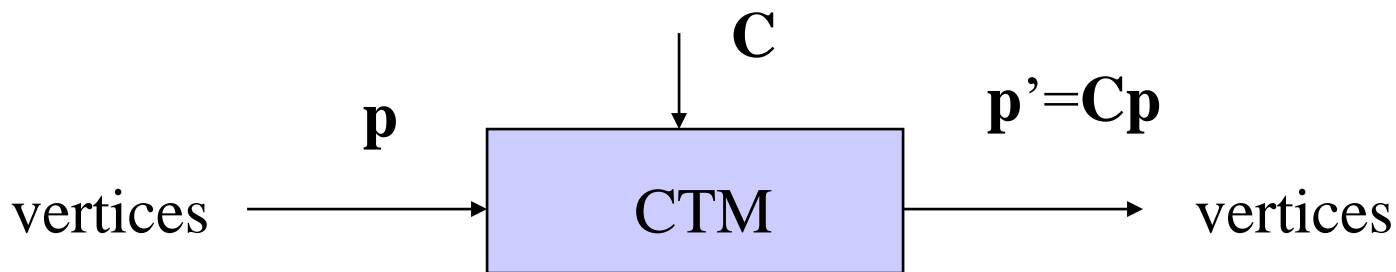


OpenGL Matrices

- In OpenGL matrices are part of the state
- Multiple types
 - Model-View (`GL_MODELVIEW`)
 - Projection (`GL_PROJECTION`)
 - Texture (`GL_TEXTURE`) (ignore for now)
 - Color (`GL_COLOR`) (ignore for now)
- Single set of functions for manipulation
- Select which to manipulated by
 - `glMatrixMode(GL_MODELVIEW);`
 - `glMatrixMode(GL_PROJECTION);`

Current Transformation Matrix (CTM)

- Conceptually there is a 4 x 4 homogeneous coordinate matrix, the *current transformation matrix* (CTM) that is part of the state and is applied to all vertices that pass down the pipeline
- The CTM is defined in the user program and loaded into a transformation unit





CTM operations

- The CTM can be altered either by loading a new CTM or by postmultiplication

Load an identity matrix: $\mathbf{C} \leftarrow \mathbf{I}$

Load an arbitrary matrix: $\mathbf{C} \leftarrow \mathbf{M}$

Load a translation matrix: $\mathbf{C} \leftarrow \mathbf{T}$

Load a rotation matrix: $\mathbf{C} \leftarrow \mathbf{R}$

Load a scaling matrix: $\mathbf{C} \leftarrow \mathbf{S}$

Postmultiply by an arbitrary matrix: $\mathbf{C} \leftarrow \mathbf{C}\mathbf{M}$

Postmultiply by a translation matrix: $\mathbf{C} \leftarrow \mathbf{C}\mathbf{T}$

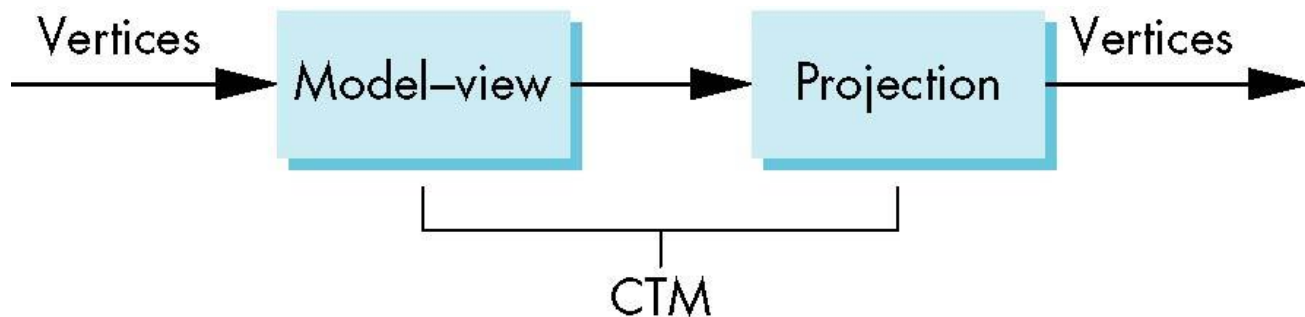
Postmultiply by a rotation matrix: $\mathbf{C} \leftarrow \mathbf{C}\mathbf{R}$

Postmultiply by a scaling matrix: $\mathbf{C} \leftarrow \mathbf{C}\mathbf{S}$



CTM in OpenGL

- OpenGL has a model-view and a projection matrix in the pipeline which are concatenated together to form the CTM
- Can manipulate each by first setting the correct matrix mode





Rotation, Translation, Scaling

Load an identity matrix:

```
glLoadIdentity()
```

Multiply on right:

```
glRotatef(theta, vx, vy, vz)
```

theta in degrees, (**vx**, **vy**, **vz**) define axis of rotation

```
glTranslatef(dx, dy, dz)
```

```
glScalef( sx, sy, sz)
```

Each has a float (f) and double (d) format (**glScaled**)



Example

- Rotation about z axis by 30 degrees with a fixed point of (1.0, 2.0, 3.0)

```
glMatrixMode(GL_MODELVIEW) ;  
glLoadIdentity() ;  
glTranslatef(1.0, 2.0, 3.0) ;  
glRotatef(30.0, 0.0, 0.0, 1.0) ;  
glTranslatef(-1.0, -2.0, -3.0) ;
```

- Remember that last matrix specified in the program is the first applied



Matrix Stacks

- In many situations we want to save transformation matrices for use later
 - Traversing hierarchical data structures (Chapter 10)
 - Avoiding state changes when executing display lists
- OpenGL maintains stacks for each type of matrix
 - Access present type (as set by `glMatrixMode`) by
 - `glPushMatrix()`
 - `glPopMatrix()`



Reading Back Matrices

- Can also access matrices (and other parts of the state) by *query* functions

```
glGetIntegerv  
glGetFloatv  
glGetBooleanv  
glGetDoublev  
glIsEnabled
```

- For matrices, we use as

```
double m[16];  
glGetFloatv(GL_MODELVIEW, m);
```