PROJECT 3 - Zebo Xiong | A04907051

QUICK SORT and ALGORITHM ANALYSIS

Using Quick Sort algorithms implement a Program in any language you desire

(C++ or java or Python) to sort an array of real numbers of size N.

Do both part A, B, and C.



1. Input at least 4 or more sets of sorted data with at least N real numbers in each. For example, N= 10, 25, 35, and 45

```
1 import java.util.Random;
3 * public class TestRandom {
4
5 +
      public static void main(String[] args) {
7
           int[] all = {10, 25, 35, 45, 60, 70, 85, 95};
8
9 +
           for(int a : all) {
10
               System.out.print("N = " + a + " - ");
11
               for (int i = 0; i < a; i++) System.out.print(getR(5, 70) + " ");
13
14
               System.out.println("");
15
16
           }
17
18
19 - private static int getR(int min, int max) {
20
21
           Random r = new Random();
22
           return r.nextInt((max - min) + 1) + min;
23
24
25 }
```

2. Plot a graph to compare the Worst Case Complexity of the quick sort algorithm and actual count putting counters in strategic points of your programs. (Time counter not allowed.)

Input data must be good for Worst Case Quick Sort.

N = 10 - 67 28 5 40 42 13 49 19 66 15 Sorted - 5 13 15 19 28 40 42 49 66 67

Worst Case: N^2 = 100 Average Case: N^LogN = 30

Actual Count: = 54

N = 25 - 50 56 57 64 70 15 16 34 6 32 60 68 65 68 36 30 7 40 39 18 29 34 8 38 33 Sorted - 6 7 8 15 16 18 29 30 32 33 34 34 36 38 39 40 50 56 57 60 64 65 68 68 70

Worst Case: N^2 = 625 Average Case: N^LogN = 100

Actual Count : = 324

N = 35 - 8 42 24 7 52 54 49 17 53 18 54 64 38 29 63 48 32 55 38 21 31 47 63 13 37 49 47 29 59 31 44 40 17 43 61 Sorted - 7 8 13 17 17 18 21 24 29 29 31 31 32 37 38 38 40 42 43 44 47 47 48 49 49 52 53 54 54 55 59 61 63 63 64

Worst Case: N^2 = 1225 Average Case: N^LogN = 175

Actual Count : = 629

N = 45 - 14 24 31 33 33 8 64 10 53 47 68 48 59 64 22 9 33 41 49 60 56 46 11 14 56 11 70 24 47 48 64 36 13 29 26 35 30 18

44 62 61 43 44 51 27

Sorted - 8 9 10 11 11 13 14 14 18 22 24 24 26 27 29 30 31 33 33 35 36 41 43 44 44 46 47 47 48 48 49 51 53 56 56 59 60

61 62 64 64 64 68 70 Worst Case: N^2 = 2025 Average Case: N^LogN = 225

Actual Count : = 1034

N = 60 - 26 57 62 6 61 57 53 37 43 66 9 14 11 22 40 24 62 50 44 30 55 38 67 57 35 16 70 13 36 14 50 54 30 9 56 55 35 42 5 51 31 54 15 45 58 18 61 69 11 7 58 19 60 19 50 32 19 16 54 10

Sorted - 5 6 7 9 9 10 11 11 13 14 14 15 16 16 18 19 19 19 22 24 26 30 30 31 32 35 35 36 37 38 40 42 43 44 45 50 50 50 51

53 54 54 54 55 55 56 57 57 57 58 58 60 61 61 62 62 66 67 69 70

Worst Case: N^2 = 3600 Average Case: N^LogN = 300

Actual Count : = 1829

N = 70 - 63 40 27 66 36 21 25 22 34 13 37 56 65 30 30 40 10 24 17 35 41 62 55 55 13 10 32 60 24 39 11 69 47 24 29 34 22 42 31 13 27 12 66 67 69 9 59 33 49 62 14 12 41 33 18 32 12 34 54 48 14 16 21 63 18 29 43 50 29 56

Sorted - 9 10 10 11 12 12 12 13 13 13 14 14 16 17 18 18 21 21 22 22 24 24 24 25 27 27 29 29 29 30 30 31 32 32 33 33 34 34 34 35 36 37 39 40 40 41 41 42 43 47 48 49 50 54 55 55 56 56 59 60 62 62 63 63 65 66 66 67 69 69

Worst Case: N^2 = 4900 Average Case: N^LogN = 420

Actual Count : = 2484

N = 85 - 41 13 61 8 22 11 55 60 66 42 44 65 12 7 58 10 10 46 22 38 54 54 65 64 6 69 69 50 37 54 31 48 64 52 54 68 57 11 60 62 18 48 27 18 50 59 70 8 9 22 22 49 35 50 44 6 28 8 32 46 40 21 51 64 58 48 44 44 10 20 20 51 44 70 22 40 61 37 62 25 15 58 67 14 30

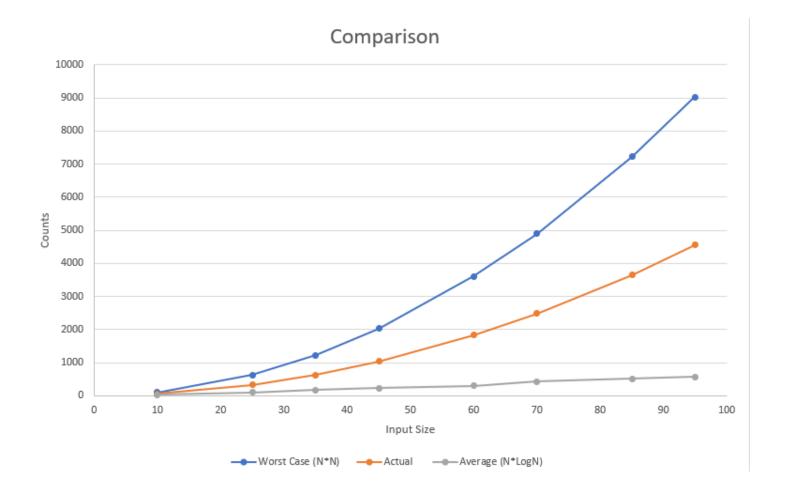
Sorted - 6 6 7 8 8 8 9 10 10 10 11 11 12 13 14 15 18 18 20 20 21 22 22 22 22 22 25 27 28 30 31 32 35 37 37 38 40 40 41 42 44 44 44 44 46 46 48 48 48 49 50 50 50 51 51 52 54 54 54 54 55 57 58 58 58 59 60 60 61 61 62 62 64 64 64 65 65 66 67 68 69 69 70 70

Worst Case: N^2 = 7225 Average Case: N^LogN = 510 Actual Count : = 3654

N = 95 - 53 8 42 51 9 63 20 26 40 17 20 46 30 53 36 20 52 45 9 17 22 6 17 33 13 31 27 30 45 30 22 52 50 44 31 66 32 42 39 33 16 50 65 66 44 14 14 54 51 46 63 35 70 34 66 45 31 27 49 5 25 29 6 23 19 20 48 15 66 44 68 49 21 59 35 69 50 7 58 48 13 44 55 43 47 59 56 11 17 51 14 6 67 20 32

Sorted - 5 6 6 6 7 8 9 9 11 13 13 14 14 14 15 16 17 17 17 17 19 20 20 20 20 20 21 22 22 23 25 26 27 27 29 30 30 30 31 31 31 32 32 33 33 34 35 35 36 39 40 42 42 43 44 44 44 45 45 45 45 46 46 47 48 48 49 49 50 50 50 51 51 51 52 52 53 53 54 55 56 58 59 59 63 63 65 66 66 66 67 68 69 70

Worst Case: N^2 = 9025 Average Case: N^LogN = 570 Actual Count : = 4559



3. Display the beginning sorted data input and ending sorted data output for each array of N elements.

4. Display a table of N, Actual count and T(N)= Theta (n**2).

Input	Worst Case (N*N)	Average (N*LogN)	Actual
10	100	30	54
25	625	100	324
35	1225	175	629
45	2025	225	1034
60	3600	300	1829
70	4900	420	2484
85	7225	510	3654
95	9025	570	4559

Β.

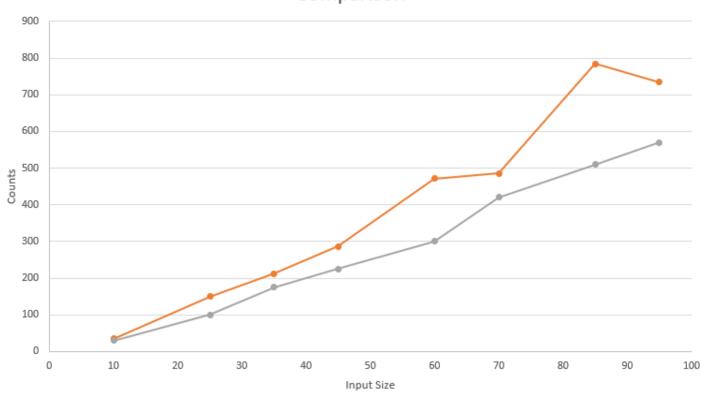
5. Input at least 4 or more sets of data with at least N real numbers in each set by using random generator for partition. For example, N= 10, 25, 35, and 45.

```
He = 10 - 90 48 34 22 47 5 19 45 15 32 Sorted - 5 15 19 22 12 34 45 47 48 50 Morat Case: N°2 - 100 Morat Case:
```

6. Plot a graph to compare the Complexity of the quick sort algorithm and actual count putting counters in strategic points of your programs.

Input data must be good for general Quick Sort randomized algorithm.





---- Average (N*LogN)

Actual

7. Display the beginning data input and ending sorted data output for each array of N elements.

N = 10 - 50 48 34 22 47 5 19 45 15 32 Sorted - 5 15 19 22 32 34 45 47 48 50

Worst Case: N^2 = 100 Average Case: N^LogN = 30

Actual Count : = 35

N = 25 - 5 34 32 24 58 68 18 6 37 65 14 58 30 24 51 47 32 24 27 6 37 42 34 60 59 Sorted - 5 6 6 14 18 24 24 27 30 32 32 34 34 37 37 42 47 51 58 58 59 60 65 68

Worst Case: N^2 = 625 Average Case: N^LogN = 100

Actual Count : = 149

N = 35 - 64 11 21 26 16 54 42 9 37 5 64 33 17 27 42 21 25 30 55 25 8 16 39 38 48 69 25 7 7 53 46 29 33 47 12 Sorted - 5 7 7 8 9 11 12 16 16 17 21 21 25 25 25 26 27 29 30 33 33 37 38 39 42 42 46 47 48 53 54 55 64 64 69

Worst Case: N^2 = 1225 Average Case: N^LogN = 175

Actual Count : = 212

 $N = 45 - 66\ 30\ 56\ 43\ 23\ 26\ 7\ 68\ 6\ 44\ 38\ 50\ 12\ 68\ 17\ 15\ 14\ 26\ 30\ 41\ 40\ 39\ 50\ 64\ 6\ 17\ 48\ 13\ 24\ 18\ 70\ 59\ 5\ 38\ 62\ 23\ 20\ 5\ 63$

36 68 31 70 68 12

Sorted - 5 5 6 6 7 12 12 13 14 15 17 17 18 20 23 23 24 26 26 30 30 31 36 38 38 39 40 41 43 44 48 50 50 56 59 62 63 64 66

68 68 68 68 70 70 Worst Case: N^2 = 2025 Average Case: N^LogN = 225

Actual Count : = 286

N = 60 - 11 59 38 45 30 10 26 36 17 67 6 15 21 54 56 37 34 60 50 22 41 47 11 46 29 7 42 68 62 17 67 50 6 44 5 43 7 54 32 36 11 70 36 30 11 28 47 27 52 63 36 39 25 41 35 6 62 17 46 18

Sorted - 5 6 6 6 7 7 10 11 11 11 11 15 17 17 17 18 21 22 25 26 27 28 29 30 30 32 34 35 36 36 36 36 37 38 39 41 41 42 43 44

45 46 46 47 47 50 50 52 54 54 56 59 60 62 62 63 67 67 68 70

Worst Case: N^2 = 3600 Average Case: N^LogN = 300

Actual Count : = 471

N = 70 - 34 32 13 13 24 29 23 28 65 31 36 30 43 69 26 12 28 48 25 61 8 69 6 66 42 37 13 19 12 54 27 43 14 13 26 62 16 70 51 24 25 35 30 28 8 43 6 58 37 36 51 69 43 30 38 63 52 46 38 46 7 65 27 70 48 55 28 65 25 34

Sorted - 6 6 7 8 8 12 12 13 13 13 13 14 16 19 23 24 24 25 25 25 26 26 27 27 28 28 28 28 29 30 30 30 31 32 34 34 35 36 36 37 37 38 38 42 43 43 43 44 46 48 48 51 51 52 54 55 58 61 62 63 65 65 66 69 69 69 70 70

Worst Case: N^2 = 4900 Average Case: N^LogN = 420

Actual Count : = 486

N = 85 - 64 10 61 41 60 48 33 11 39 55 14 48 16 43 31 47 59 34 50 46 5 45 37 44 36 65 9 55 57 58 57 13 56 59 15 57 43 62 14 53 51 6 32 29 56 68 5 12 70 45 67 53 24 10 42 13 35 25 28 56 6 68 49 46 49 49 23 24 30 52 50 15 33 41 9 55 64 8 17 31

Sorted - 5 5 6 6 6 8 9 9 10 10 10 11 12 13 13 14 14 15 15 16 17 23 24 24 25 28 29 30 31 31 32 33 33 34 35 36 37 39 41 41 42 43 43 44 45 45 46 46 47 48 48 49 49 49 50 50 51 52 53 53 55 55 55 56 56 56 57 57 57 58 59 59 59 60 61 62 64 64 65

67 68 68 70 70 Worst Case: N^2 = 7225

Average Case: N^LogN = 510

Actual Count : = 784

N = 95 - 40 19 22 35 26 45 55 42 26 48 66 63 14 19 10 55 39 13 31 38 8 31 35 14 5 69 49 45 49 37 22 24 30 13 53 11 24 10 44 48 43 9 18 48 16 28 36 26 63 63 39 43 9 11 11 31 25 44 19 57 32 57 31 61 11 6 7 45 56 10 5 7 9 26 15 15 31 19 46 44 12 34 23 41 32 19 49 17 64 24 66 44 52

53 55 55 56 57 57 61 63 63 63 64 66 66 69

Worst Case: N^2 = 9025 Average Case: N^LogN = 570 Actual Count : = 734

8. Display a table of N, Actual count and T(N)= Theta (n lg n).

Input	Average (N*LogN)	Actual
10	30	30
25	100	149
35	175	212
45	225	286
60	300	471
70	420	486
85	510	784
95	570	734

C.

9. Use the original version (1962) of Quick Sort by C A R Hoare which is listed in page 185, problem 7.1 of

Cormen's book and do part B again

```
HOARE-PARTITION (A, p, r)
1 \quad x = A[p]
2 i = p-1
 j = r + 1
   while TRUE
5
        repeat
6
            j = j - 1
7
        until A[j] \leq x
8
        repeat
9
            i = i + 1
10
        until A[i] \ge x
11
        if i < j
12
            exchange A[i] with A[j]
13
        else return j
```

```
180
          /** Hoare-Partition **/
181 -
          private static int partition(int[] A, int p, int r){
182
183
              int x = A[p];
184
              int i = p - 1;
185
186
              int j = r + 1;
187
188
              while(true){
189 +
190
191 -
192
                  \} while (A[j] > x);
193
194
195 +
                  do {
196
                        i++;
197
                  } while ( A[i] < x);</pre>
198
199 -
                  if(i<j){
200
201
                       int tmp = A[i];
202
                       A[i] = A[j];
203
                       A[j] = tmp;
204
205
                   } else return j;
206
207
208
209
210
          }
```

N = 10 - 39 6 23 52 15 56 49 64 65 24 Sorted - 15 6 23 24 39 49 52 56 64 65

--> Worst Case: N^2 = 100 --> Average Case: N^LogN = 30

--> Actual Count : = 82

N = 25 - 47 19 28 47 59 59 19 43 34 11 11 40 32 46 26 11 31 65 49 5 57 44 56 28 32 Sorted - 5 11 11 11 19 19 26 28 28 31 32 32 34 40 43 44 46 47 47 49 56 57 59 59 65

--> Worst Case: N^2 = 625 --> Average Case: N^LogN = 100

--> Actual Count : = 316

N = 35 - 63 69 69 67 5 16 9 44 25 34 59 8 6 9 64 14 43 65 67 67 69 9 31 52 23 33 63 26 47 11 52 14 51 11 22 Sorted - 5 8 9 6 9 9 11 11 14 14 16 22 23 25 26 33 31 34 43 44 47 51 52 52 63 59 63 64 65 67 67 67 69 69 69

--> Worst Case: N^2 = 1225 --> Average Case: N^LogN = 175

--> Actual Count : = 551

N = 45 - 61 68 37 31 6 12 51 43 44 33 50 10 38 63 69 46 64 68 19 48 29 15 37 5 65 66 42 19 31 51 49 7 68 59 21 10 55 10 37 10 27 15 28 62 52

Sorted - 5 6 7 10 10 10 10 12 15 19 15 19 21 27 28 31 31 29 33 37 37 37 38 42 43 44 48 49 46 50 51 51 52 55 59 61 63 62 64 65 66 68 68 69

--> Worst Case: N^2 = 2025 --> Average Case: N^LogN = 225

--> Actual Count : = 802

N = 60 - 46 20 22 28 46 43 55 5 6 5 11 38 47 9 61 37 62 37 47 64 19 25 70 33 22 54 66 39 35 60 30 28 63 44 16 20 16 55 64 37 64 29 18 33 18 61 68 36 10 60 64 16 64 27 20 65 39 14 61 38

Sorted - 5 5 6 9 10 11 16 14 16 16 18 18 19 20 20 22 20 22 25 27 28 29 28 30 33 33 35 36 37 37 37 38 38 39 39 43 44 46 46 47 47 55 54 55 60 60 61 61 62 61 63 64 64 64 64 65 66 68 70

--> Worst Case: N^2 = 3600 --> Average Case: N^LogN = 300

--> Actual Count : = 1410

 $N = 70 - 30\ 60\ 69\ 60\ 7\ 41\ 37\ 60\ 66\ 21\ 57\ 7\ 64\ 43\ 24\ 64\ 64\ 14\ 15\ 61\ 62\ 37\ 68\ 59\ 61\ 53\ 49\ 34\ 48\ 19\ 47\ 40\ 10\ 37\ 24\ 33\ 58\ 46$ 29\ 19\ 14\ 17\ 60\ 42\ 68\ 34\ 15\ 37\ 49\ 37\ 9\ 59\ 53\ 54\ 46\ 65\ 55\ 9\ 49\ 52\ 16\ 18\ 66\ 48\ 43\ 53\ 21\ 16

Sorted - 7 9 7 10 14 9 14 15 15 16 16 17 19 18 19 21 21 24 24 29 30 33 34 34 37 37 37 37 37 40 42 43 41 43 44 46 46 48 47 48 49 49 52 53 53 55 54 57 58 59 59 60 60 60 61 61 62 64 64 64 65 66 66 68 68 68 69

--> Worst Case: N^2 = 4900 --> Average Case: N^LogN = 420 --> Actual Count : = 1792

N = 85 - 21 9 31 48 14 10 6 58 37 62 21 56 9 33 54 11 59 29 11 37 47 61 8 12 62 58 35 50 44 7 20 55 52 60 21 6 20 18 22 11 65 20 57 61 31 7 36 64 18 58 27 7 68 52 54 59 41 46 70 43 36 44 11 69 17 58 21 29 22 61 11 63 22 41 10 28 26 22 46 55 31 15 70 21 55

Sorted - 6 7 6 7 7 8 9 9 10 10 11 11 11 11 11 12 14 15 17 18 18 20 21 20 21 20 21 21 21 22 22 22 22 22 26 27 28 29 29 31 31 31 33 35 36 36 37 41 37 41 43 44 44 46 46 47 48 50 52 52 54 54 55 55 55 56 57 58 58 59 58 59 60 61 61 61 62 62 63 64 65 68 69 70 70

--> Worst Case: N^2 = 7225 --> Average Case: N^LogN = 510 --> Actual Count : = 2354 N = 95 - 34 6 58 35 11 30 43 43 26 50 15 18 8 20 68 61 59 15 35 58 65 66 27 26 41 64 60 45 12 20 32 53 23 64 66 37 6 38 43 6 61 36 6 25 47 58 57 44 31 28 35 34 39 11 53 13 51 21 9 60 21 5 8 21 52 30 9 54 23 24 40 46 16 42 27 67 36 63 36 12 48 63 15 42 35 64 7 8 17 46 17 29 43 66 68

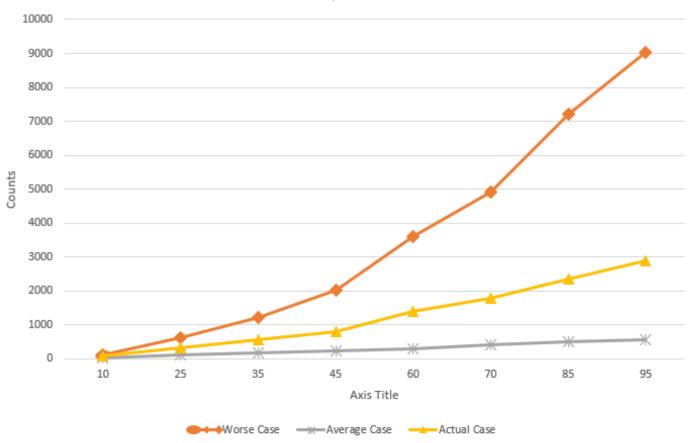
Sorted - 5 6 6 6 6 7 8 8 8 9 11 9 11 12 12 13 15 15 15 16 17 17 18 20 20 21 21 21 23 23 24 25 26 26 27 27 28 29 30 30 31 34 32 34 35 35 36 36 36 37 38 39 40 41 42 42 43 43 43 45 46 44 46 47 48 50 51 53 52 53 54 57 58 58 58 59 60 60 61 61 63 63 64 64 64 66 65 66 66 68 67 68

--> Worst Case: N^2 = 9025 --> Average Case: N^LogN = 570 --> Actual Count : = 2877

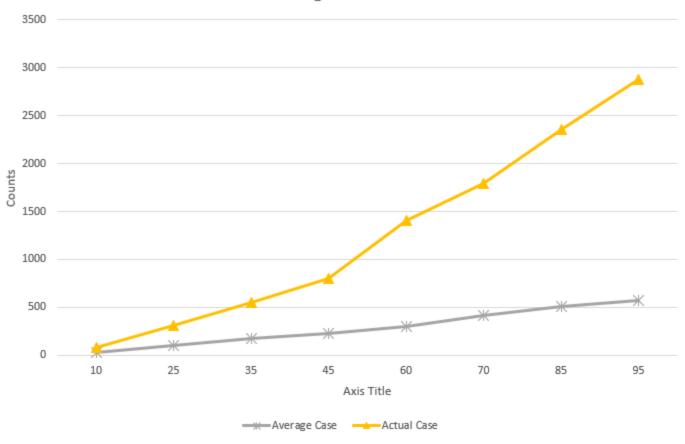
10. The final graph of part C may be combined or separated from Part B.

Input Size	Worse Case	Average Case	Actual Case
10	100	30	82
25	625	100	316
35	1225	175	551
45	2025	225	802
60	3600	300	1410
70	4900	420	1792
85	7225	510	2354
95	9025	570	2877

Comparison



Average VS Actual



11. Professional output with necessary information for readers are required.

Done