

Object Mouse Trackball

Obtém o vetor de quaternions:

$$z(x', y') = \begin{cases} \sqrt{r^2 - (x'^2 + y'^2)} & x'^2 + y'^2 \leq \frac{r^2}{2} \\ \frac{r^2/2}{\sqrt{x'^2 + y'^2}} & \text{otherwise} \end{cases}$$

$$V_1 = \frac{(x'_1, y'_1, z(x'_1, y'_1))}{|(x'_1, y'_1, z(x'_1, y'_1))|}$$

$$V_2 = \frac{(x'_2, y'_2, z(x'_2, y'_2))}{|(x'_2, y'_2, z(x'_2, y'_2))|}$$

$$N = V_1 \times V_2$$

$$\theta = \arccos V_1 \cdot V_2$$

$$Q = (\cos \frac{\theta}{2}, \sin \frac{\theta}{2} N)$$

With each incremental mouse movement from (x'_1, y'_1) to (x'_2, y'_2) we apply (accumulate) the rotation Q and then unitize the result to ensure we retain a rotation.

Onde r é o raio da esfera de track

Obtém a matriz de rotação a partir do vetor q

The 3x3 matrix itself is the rotation matrix equivalent to the quaternion rotation;

$$M_R = \begin{pmatrix} 1 - 2y^2 - 2z^2 & 2xy - 2sz & 2xz + 2sy \\ 2xy + 2sz & 1 - 2x^2 - 2z^2 & 2yz - 2sx \\ 2xz - 2sy & 2yz + 2sx & 1 - 2x^2 - 2y^2 \end{pmatrix}$$

$$\text{where } q = s + ix + jy + kz, \quad |q| = 1$$

Or, as 4x4 matrix;

$$M_R = \begin{pmatrix} 1 - 2y^2 - 2z^2 & 2xy - 2sz & 2xz + 2sy & 0 \\ 2xy + 2sz & 1 - 2x^2 - 2z^2 & 2yz - 2sx & 0 \\ 2xz - 2sy & 2yz + 2sx & 1 - 2x^2 - 2y^2 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\text{where } q = s + ix + jy + kz, \quad |q| = 1$$