

# Paper 060010907: Machine Learning

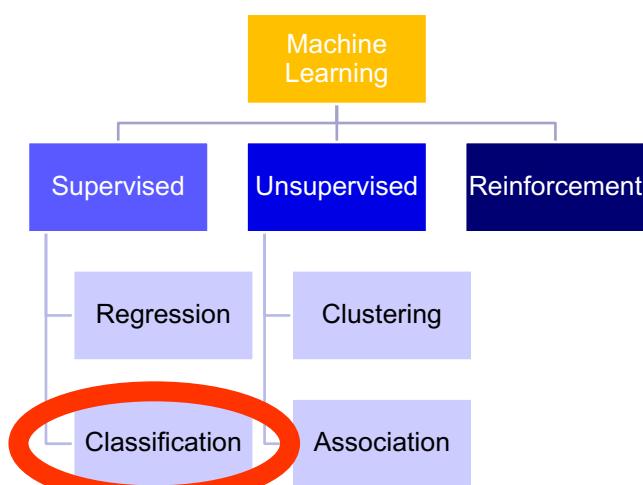
## Unit-3 Classification

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## Types of Machine Learning



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## Supervised Learning



- **Supervised learning** is the machine learning task of learning a function that maps an input to an output based on example input-output pairs.
- It infers a function from labeled training data consisting of a set of training examples.

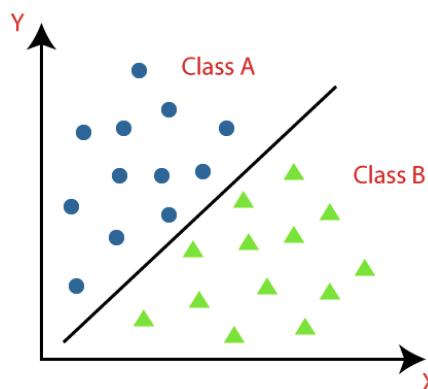
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## Types of Supervised Learning



- Classification



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# Types of Supervised Learning



- Classification

- Output variable in classification is categorical or discrete
- Classification algorithms attempt to estimate the mapping function ( $f$ ) from the input variables ( $x$ ) to discrete or categorical output variables ( $y$ ).
- Helps in solving questions like "Is this email spam?" or "Is this customer going to purchase the product or not?"

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# Types of Supervised Learning



- Classification algorithms

- Logistic Regression
- K-Nearest Neighbors (K-NN)
- Support Vector Machine (SVM)
- Naive Bayes

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# Types of Classification



## Classification

Binary Classification

Multi-Class Classification

Multi-Label Classification

Imbalanced Classification

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# Classification



## ● Binary Classification

○ Classifying the elements of a given dataset into two groups

○ i.e.

- spam or not
- attack or normal traffic
- rain or not

○ Typically, binary classification involve one class as the normal and another class as the abnormal.

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# Classification



## ● Multi-Class Classification

- Classifying the elements of a given dataset into more than two groups
- i.e
  - Face detection
  - Mango type classification
  - Optical character recognition

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# Classification



## ● Multi-Class Classification

- Algorithms that are designed for binary classification can be adapted for use for multi-class problems.
  - One-vs-Rest
  - One-vs-One

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# Classification



## ● Multi-Class Classification

### ○ One-vs-Rest

- Split the multi-class dataset into multiple binary classification problems
- Each classification sub-problem is one class versus rest all classes

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# Classification



## ● Multi-Class Classification

### ○ One-vs-Rest

- i.e. For four classes “Triangle”, “Rectangle”, “Pentagon”, “Hexagon”, we require four models
  - Model 1 – “Triangle” vs [“Rectangle”, “Pentagon”, “Hexagon”]
  - Model 2 – “Rectangle” vs [“Triangle”, “Pentagon”, “Hexagon”]
  - Model 3 – “Pentagon” vs [“Triangle”, “Rectangle”, “Hexagon”]
  - Model 4 – “Hexagon” vs [“Triangle”, “Rectangle”, “Pentagon”]
- Largest score is used to predict the class

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# Classification



## ● Multi-Class Classification

### ○ One-vs-One

- Split the multi-class dataset into multiple binary classification problems
- One dataset for each class versus every other classes

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# Classification



## ● Multi-Class Classification

### ○ One-vs-One

- i.e. For four classes “Triangle”, “Rectangle”, “Pentagon”, “Hexagon”, we require six models
  - Model 1 – “Triangle” vs “Rectangle”
  - Model 2 – “Triangle” vs “Pentagon”
  - Model 3 – “Triangle” vs “Hexagon”
  - Model 4 – “Rectangle” vs “Pentagon”
  - Model 5 – “Rectangle” vs “Hexagon”
  - Model 6 – “Pentagon” vs “Hexagon”
- Largest score is used to predict the class

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## Classification



- Multi-Label Classification

- have two or more classes and
- one or more classes may be predicted for each record
- i.e. identify presence of “human”, “car”, “building” in the photo

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## Classification



- Imbalanced Classification

- number of examples in each class is unequally distributed
- Typically like binary classification, but majority of examples in the training dataset belong to the normal class and a minority of examples belong to the abnormal class
- i.e. fraud detection, outlier detection
- requires under-sampling the majority class or over-sampling the minority class

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## Classification

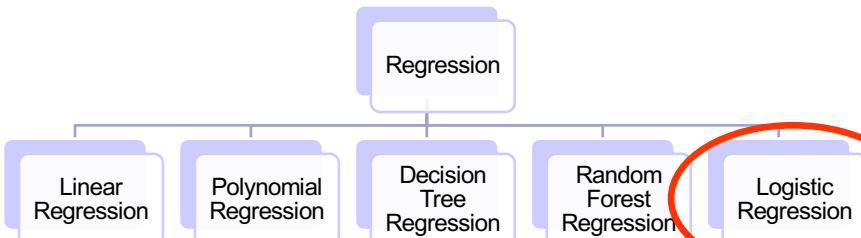
- Logistic Regression
- K-Nearest Neighbors (K-NN)
- Support Vector Machine (SVM)
- Naïve Bayes

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## Types of Regression



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## Logistic Regression



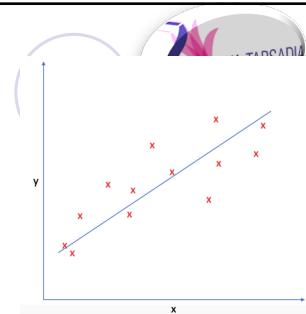
- Supervised machine learning
- Outcome will be categorical or discrete dependent variable
- Instead of giving the exact value as 0 and 1, it gives the probabilistic values which lie between 0 and 1.

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## Logistic Regression



- Simple Linear Regression

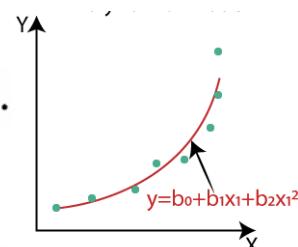
$$y = b_0 + b_1 x_1$$

- Multiple Linear Regression

$$y = b_0 + b_1 x_1 + b_2 x_2 + \dots$$

- Polynomial Regression

$$y = b_0 + b_1 x_1 + b_2 x_1^2 + \dots + b_n x_1^n$$



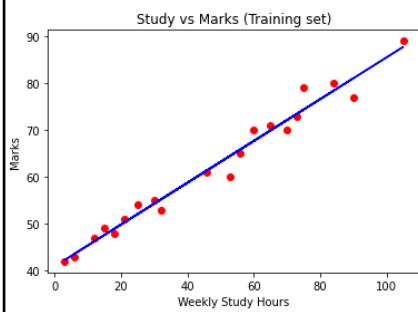
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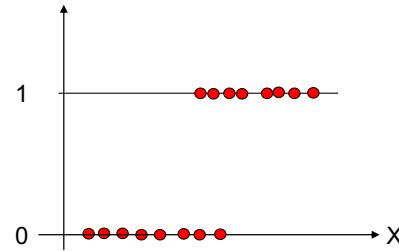
# Logistic Regression

## Linear Regression



## Logistics Regression

Purchase or not (Yes/No)



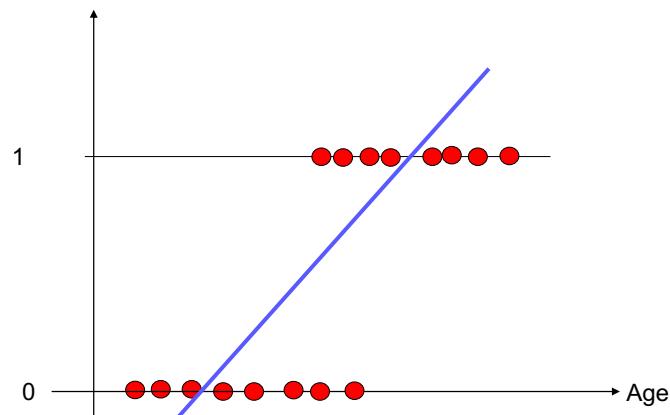
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# Logistic Regression

Purchase or not (Yes/No)



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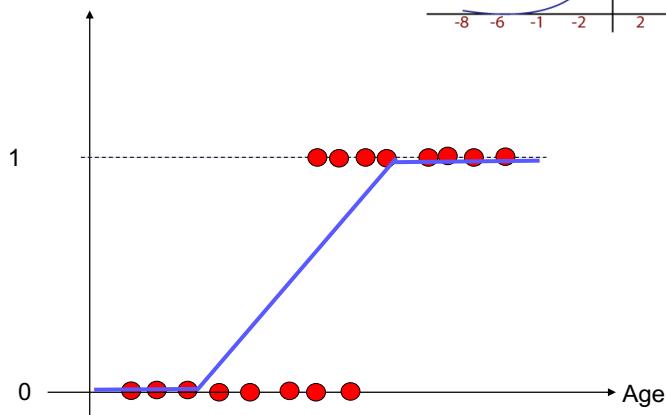
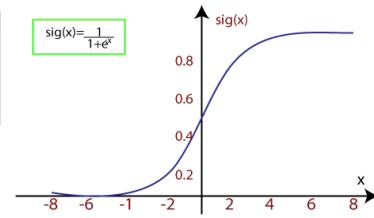
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# Logistic Regression

Purchase or not (Yes/No)

$$\text{sig}(x) = \frac{1}{1+e^{-x}}$$



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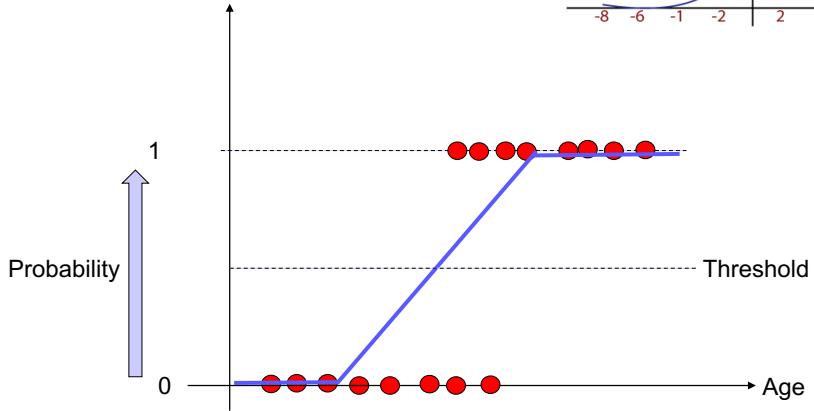
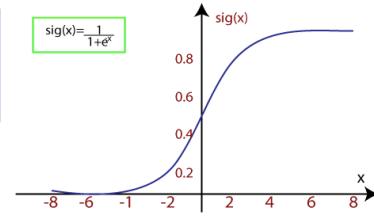
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# Logistic Regression

Purchase or not (Yes/No)

$$\text{sig}(x) = \frac{1}{1+e^{-x}}$$



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# Logistic Regression



- Assumptions for Logistic Regression
  - The dependent variable must be categorical
  - No multicollinearity among independent variables

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# Logistic Regression



## Logistic Regression

Binomial

Multinomial

Ordinal

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## Logistic Regression



- Binomial

- Dependent variable must have two classes only
- i.e.
  - yes or no
  - pass or fail
  - spam or normal
  - purchase or no

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## Logistic Regression



- Multinomial

- Dependent variable must have 3 or more **unordered** classes
- i.e.
  - red, green, blue
  - Information Technology, Computer Science, Forensic Science

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# Logistic Regression



- Ordinal

- Dependent variable must have 3 or more **ordered** classes
- i.e.
  - poor, average, good, very good
  - low, medium, high

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## Logistic Regression – Python

Independent Variables

	A	B	C	D	E
1	User ID	Gender	Age	EstimatedSalary	Purchased
2	15624510	Male	19	19000	0
3	15810944	Male	35	20000	0
4	15668575	Female	26	43000	0
5	15603246	Female	27	57000	0
6	15804002	Male	19	76000	0
7	15728773	Male	27	58000	0
8	15598044	Female	27	84000	0
9	15694829	Female	32	150000	1
10	15600575	Male	25	33000	0
11	15727311	Female	35	65000	0
12	15570769	Female	26	80000	0
13	15606274	Female	26	52000	0
14	15746139	Male	20	86000	0
15	15704987	Male	32	18000	0
16	15628972	Male	18	82000	0
17	15697686	Male	29	80000	0
18	15733883	Male	47	25000	1
19	15617482	Male	45	26000	1
20	15704583	Male	46	28000	1

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# Logistic Regression – Python



## ● Importing Libraries

```
9  # Logistic Regression
10
11 # Importing the libraries
12 import numpy as np
13 import matplotlib.pyplot as plt
14 import pandas as pd
```

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# Logistic Regression – Python



## ● Importing Dataset

```
16 # Importing the dataset
17 dataset = pd.read_csv('Social_Network_Ads.csv')
18 X = dataset.iloc[:, [2, 3]].values
19 y = dataset.iloc[:, -1].values
```

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# Logistic Regression – Python

## • Importing Dataset

Index	User ID	Gender	Age	EstimatedSala	Purchased
0	15624510	Male	19	19000	0
1	15810944	Male	35	20000	0
2	15668575	Female	26	43000	0
3	15603246	Female	27	57000	0
4	15804002	Male	19	76000	0
5	15728773	Male	27	58000	0
6	15598044	Female	27	84000	0
7	15694829	Female	32	150000	1
8	15600575	Male	25	33000	0
9	15727311	Female	35	65000	0
10	15570769	Female	26	80000	0
11	15606274	Female	26	52000	0
12	15746139	Male	20	86000	0

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# Logistic Regression – Python

## • Create two vectors X and y

X - NumPy object array	
0	19
1	35
2	26
3	27
4	19
5	27
6	27
7	32
8	25
	19000
	20000
	43000
	57000
	76000
	58000
	84000
	150000
	33000

y - NumPy object array	
0	0
1	0
2	0
3	0
4	0
5	0
6	0
7	1
8	0

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## Logistic Regression – Python



- Splitting the dataset into the Training set and Test set

```
21 # Splitting the dataset into the Training set and Test set
22 from sklearn.model_selection import train_test_split
23 X_train, X_test, y_train, y_test = train_test_split(
24     X, y, test_size = 0.25, random_state = 0)
```

- Total 400 records: 300 for training, 100 for testing

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## Logistic Regression – Python



- Feature Scaling

```
26 # Feature Scaling
27 from sklearn.preprocessing import StandardScaler
28 sc = StandardScaler()
29 X_train = sc.fit_transform(X_train)
30 X_test = sc.transform(X_test)
```

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# Logistic Regression – Python

## Feature Scaling

X_train - NumPy object array		
	0	1
0	44	39000
1	32	120000
2	38	50000
3	32	135000
4	52	21000
5	53	104000
6	39	42000
7	38	61000
8	36	50000

X_test - NumPy object array		
	0	1
0	30	87000
1	38	50000
2	35	75000
3	30	79000
4	35	50000
5	27	20000
6	31	15000
7	36	144000
8	18	68000

X_train - NumPy object array		
	0	1
0	0.581649	-0.886707
1	-0.606738	1.46174
2	-0.01254...	-0.567782
3	-0.606738	1.89663
4	1.37391	-1.40858
5	1.47294	0.997847
6	0.0864882	-0.799728
7	-0.01254...	-0.248858
8	-0.210609	-0.567782

X_test - NumPy object array		
	0	1
0	-0.804802	0.504964
1	-0.01254...	-0.567782
2	-0.309641	0.157046
3	-0.804802	0.273019
4	-0.309641	-0.567782
5	-1.1019	-1.43758
6	-0.70577	-1.58254
7	-0.210609	2.15757
8	-1.99319	-0.04590...

37

# Logistic Regression – Python

- Training the Logistic Regression model on the Training set

```
32 # Training the Logistic Regression model on the Training set
33 from sklearn.linear_model import LogisticRegression
34 classifier = LogisticRegression(random_state = 0)
35 classifier.fit(X_train, y_train)
```

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## Logistic Regression – Python

- Predicting the Test set results

```
37 # Predicting the Test set results  
38 y_pred = classifier.predict(X_test)
```

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## Logistic Regression – Python

- Predicting the Test set results

The image shows two adjacent Jupyter Notebook cells. Both cells have a header 'y\_test - NumPy object array' and a footer 'y\_pred - NumPy object array'. The left cell displays a 19x2 matrix where all rows except row 7 and row 18 have the first column as 0 and the second column as 0. Row 7 has the first column as 0 and the second column as 1. Row 18 has the first column as 0 and the second column as 1. The right cell displays a similar 19x2 matrix, also with most rows having 0s in both columns, but with row 7 and row 18 having 1s in the second column.

	0
0	0
1	0
2	0
3	0
4	0
5	0
6	0
7	1
8	0
9	0
10	0
11	0
12	0
13	0
14	0
15	0
16	0
17	0
18	1

	0
0	0
1	0
2	0
3	0
4	0
5	0
6	0
7	1
8	0
9	1
10	0
11	0
12	0
13	0
14	0
15	0
16	0
17	0
18	1

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# Logistic Regression – Python



- Making the Confusion Matrix

```
40  # Making the Confusion Matrix
41  from sklearn.metrics import confusion_matrix
42  cm = confusion_matrix(y_test, y_pred)
43  print(cm)
```

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# Logistic Regression – Python



- Making the Confusion Matrix

A screenshot of a Jupyter Notebook cell. The title bar says "cm - NumPy object array". The cell contains a 2x2 NumPy array:

	0	1
0	65	3
1	8	24

		Predicted class	
		<i>P</i>	<i>N</i>
Actual Class	<i>P</i>	True Positives (TP)	False Negatives (FN)
	<i>N</i>	False Positives (FP)	True Negatives (TN)

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# Logistic Regression – Python



## ● Plotting training set results

```
45 # Visualising the Training set results
46 from matplotlib.colors import ListedColormap
47 X_set, y_set = X_train, y_train
48 X1, X2 = np.meshgrid(np.arange(start = X_set[:, 0].min() - 1,
49                      stop = X_set[:, 0].max() + 1, step = 0.01),
50                      np.arange(start = X_set[:, 1].min() - 1,
51                      stop = X_set[:, 1].max() + 1, step = 0.01))
52 plt.contourf(X1, X2, classifier.predict(
53             np.array([X1.ravel(), X2.ravel()]).T).reshape(X1.shape),
54             alpha = 0.75, cmap = ListedColormap(['orange', 'yellow']))
55 plt.xlim(X1.min(), X1.max())
56 plt.ylim(X2.min(), X2.max())
57 for i, j in enumerate(np.unique(y_set)):
58     plt.scatter(X_set[y_set == j, 0], X_set[y_set == j, 1],
59                 c = ListedColormap(['red', 'green'])(i), label = j)
60 plt.title('Logistic Regression (Training set)')
61 plt.xlabel('Age')
62 plt.ylabel('Estimated Salary')
63 plt.legend()
64 plt.show()
```

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# Logistic Regression – Python



## ● Plotting training set results



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# Logistic Regression – Python

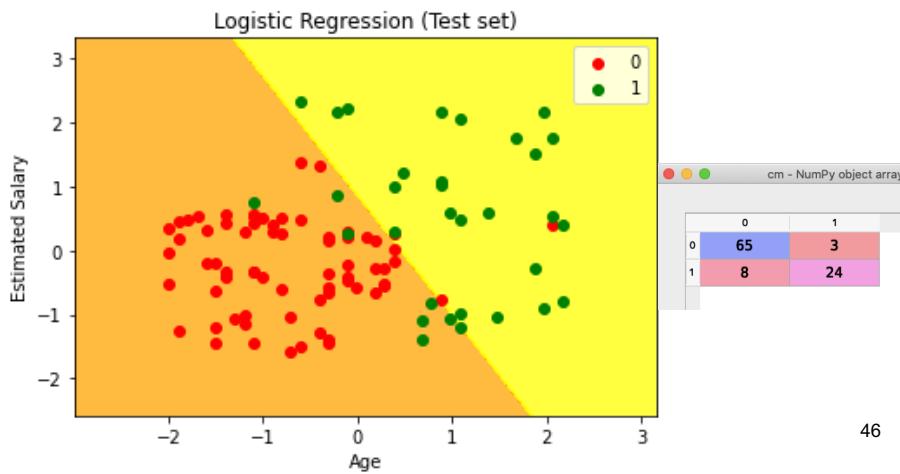
## ● Plotting testing set results

```
66 # Visualising the Test set results
67 from matplotlib.colors import ListedColormap
68 X_set, y_set = X_test, y_test
69 X1, X2 = np.meshgrid(np.arange(start = X_set[:, 0].min() - 1,
70                         stop = X_set[:, 0].max() + 1, step = 0.01),
71                      np.arange(start = X_set[:, 1].min() - 1,
72                         stop = X_set[:, 1].max() + 1, step = 0.01))
73 plt.contourf(X1, X2, classifier.predict(
74             np.array([X1.ravel(), X2.ravel()]).T).reshape(X1.shape),
75             alpha = 0.75, cmap = ListedColormap(('orange', 'yellow')))
76 plt.xlim(X1.min(), X1.max())
77 plt.ylim(X2.min(), X2.max())
78 for i, j in enumerate(np.unique(y_set)):
79     plt.scatter(X_set[y_set == j, 0], X_set[y_set == j, 1],
80                 c = ListedColormap(('red', 'green'))(i), label = j)
81 plt.title('Logistic Regression (Test set)')
82 plt.xlabel('Age')
83 plt.ylabel('Estimated Salary')
84 plt.legend()
85 plt.show()
```

45

# Logistic Regression – Python

## ● Plotting testing set results



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## K-Nearest Neighbors (K-NN)



- Supervised machine learning algorithm
- Used for classification

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## K-Nearest Neighbors (K-NN)



- K-NN is a non-parametric algorithm (it does not make any assumption on underlying data).

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## K-Nearest Neighbors (K-NN)



- K-NN stores information of all training cases and classifies new cases based on similarity.
- For a new data point, K-NN searches through the entire training set for the K most similar training data and select the most common outcome.

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## K-Nearest Neighbors (K-NN)



- It is also called a **lazy learner** algorithm because it does not learn from the training set immediately instead it stores the dataset and at the time of classification, it performs an action on the dataset.

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## K-Nearest Neighbors (K-NN)

- Example

LecturesAttended	StudyHours	Result
32	30	pass
32	10	pass
10	15	fail
20	25	pass
5	32	fail
20	10	fail

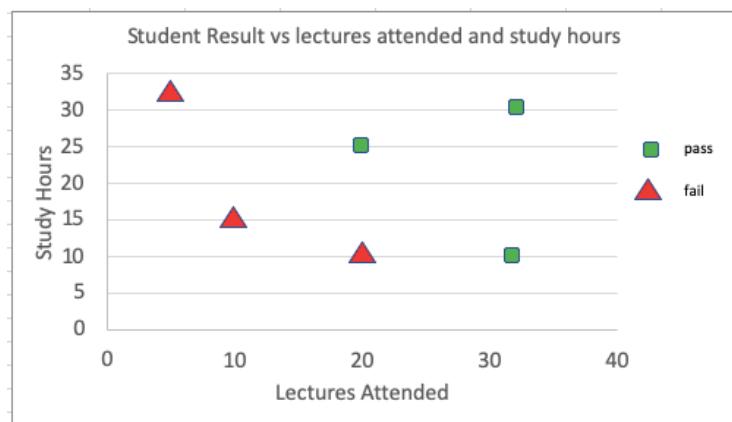
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## K-Nearest Neighbors (K-NN)

- Example



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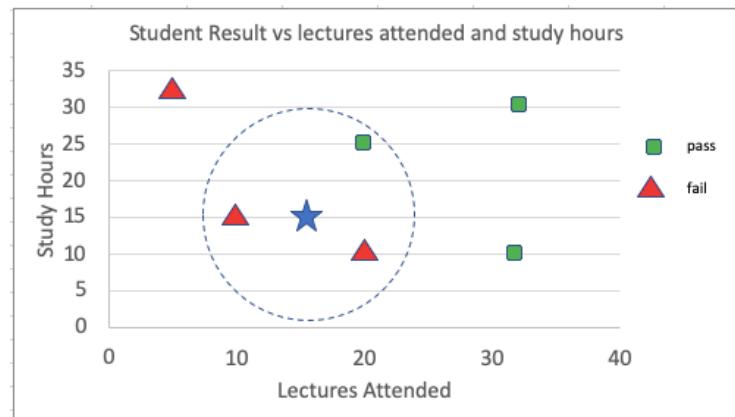
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## K-Nearest Neighbors (K-NN)

### Example

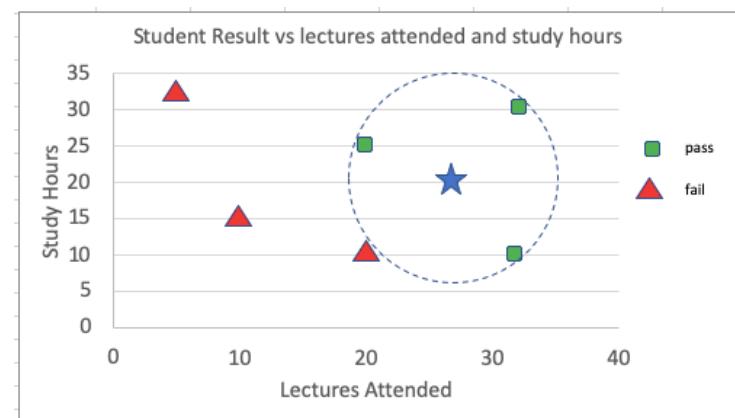


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## K-Nearest Neighbors (K-NN)

### Example



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## K-Nearest Neighbors (K-NN)



- Step-1:
  - Initialize parameter K = number of nearest neighbors
- Step-2:
  - Calculate the distance between the new/test datapoint and all training records

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## K-Nearest Neighbors (K-NN)



- Step-3:
  - Find the K training points with smallest distances
- Step-4:
  - Among these K neighbors, count the number of the data points in each category

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## K-Nearest Neighbors (K-NN)



- Step-5:

- Assign the new data points to that category for which the number of the neighbor is maximum.

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## K-Nearest Neighbors (K-NN)



- Calculate result for LecturesAttended=15 and StudyHours=15

LecturesAttended	StudyHours	Result
32	30	pass
32	10	pass
10	15	fail
20	25	pass
5	32	fail
20	10	fail

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## K-Nearest Neighbors (K-NN)



- Step-1:

- Initialize parameter K = number of nearest neighbors

- Suppose K = 3

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## K-Nearest Neighbors (K-NN)



- Step-2:

- Calculate the squared distance between the new/test datapoint and all training records

D2	A	B	C	D
1	LecturesAttended	StudyHours	Result	Squared distance to New Point (15, 15)
2	32	30	pass	514
3	32	10	pass	314
4	10	15	fail	25
5	20	25	pass	125
6	5	32	fail	389
7	20	10	fail	50

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## K-Nearest Neighbors (K-NN)



- Step-3:

- Find the K training points with smallest distances

LecturesAttended	StudyHours	Result	Squared distance to New Point (15, 15)
32	30	pass	514
32	10	pass	314
10	15	fail	25
20	25	pass	125
5	32	fail	389
20	10	fail	50

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## K-Nearest Neighbors (K-NN)



- Step-4:

- Among these K neighbors, count the number of the data points in each category
  - Number of datapoints in “fail” category =2
  - Number of datapoints in “pass” category =1

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## K-Nearest Neighbors (K-NN)



- Step-5:
  - Assign the new data point to that category for which the number of the neighbor is maximum.
  - No. of datapoints in “fail” category > No. of datapoints in “pass” category so prediction for new datapoint is “**fail**”

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## K-Nearest Neighbors (K-NN)



- How to calculate distance??

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## K-Nearest Neighbors (K-NN)

- How to calculate distance??

- For continuous variables,

Distance functions

Euclidean  $\sqrt{\sum_{i=1}^k (x_i - y_i)^2}$

Manhattan  $\sum_{i=1}^k |x_i - y_i|$

Minkowski  $\left( \sum_{i=1}^k (|x_i - y_i|)^q \right)^{1/q}$

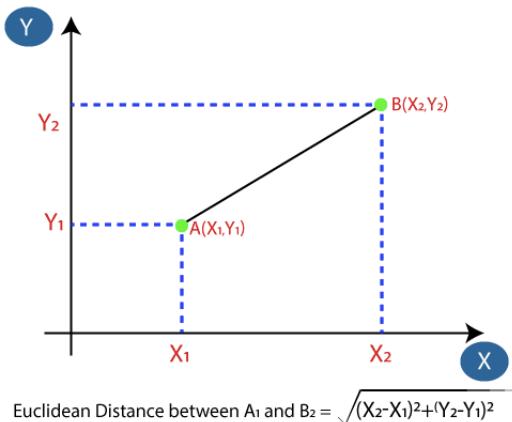
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## K-Nearest Neighbors (K-NN)

- How to calculate distance??

- For continuous variables,



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## K-Nearest Neighbors (K-NN)

- How to calculate distance??

- For categorical variables,

Hamming Distance

$$D_H = \sum_{i=1}^k |x_i - y_i|$$

$$x = y \Rightarrow D = 0$$

$$x \neq y \Rightarrow D = 1$$

X	Y	Distance
Male	Male	0
Male	Female	1

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## K-Nearest Neighbors (K-NN)

- How to calculate distance??

- When independent variables in training data are measured in different units, standardize variables before calculating distance.

$$X_s = \frac{X - \text{mean}}{\text{s. d.}}$$

$$X_s = \frac{X - \text{mean}}{\text{max} - \text{min}}$$

$$X_s = \frac{X - \text{min}}{\text{max} - \text{min}}$$

Standardization

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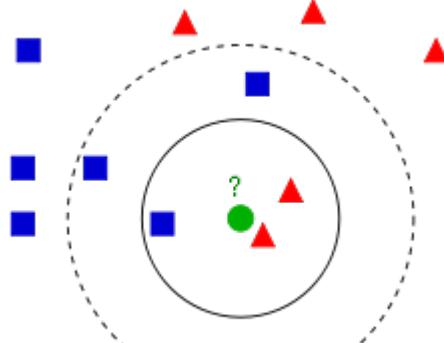
68

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## K-Nearest Neighbors (K-NN)

- How to select value of parameter K??



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## K-Nearest Neighbors (K-NN)

- How to select value of parameter K??
- Low k-value is sensitive to outliers and a higher K-value is more resilient to outliers as it considers more voters to decide prediction.

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## K-Nearest Neighbors (K-NN)



- How to select value of parameter K??
- Solution:
  - Use validation data for deciding value of parameter K.

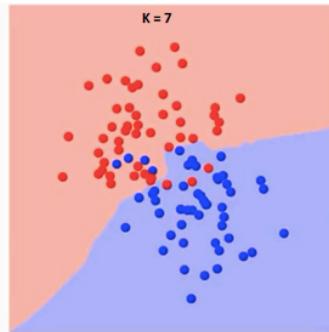
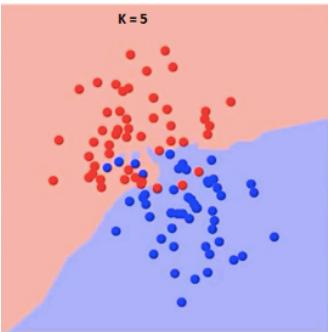
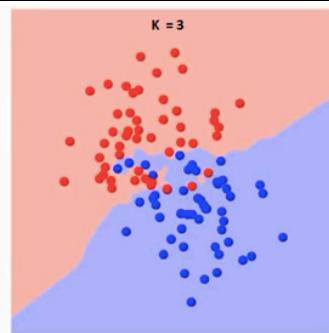
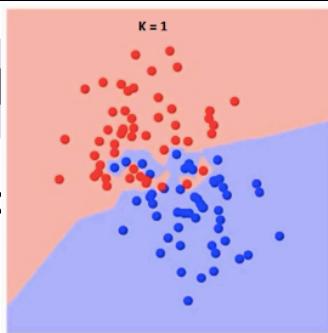
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K-N

● Hc



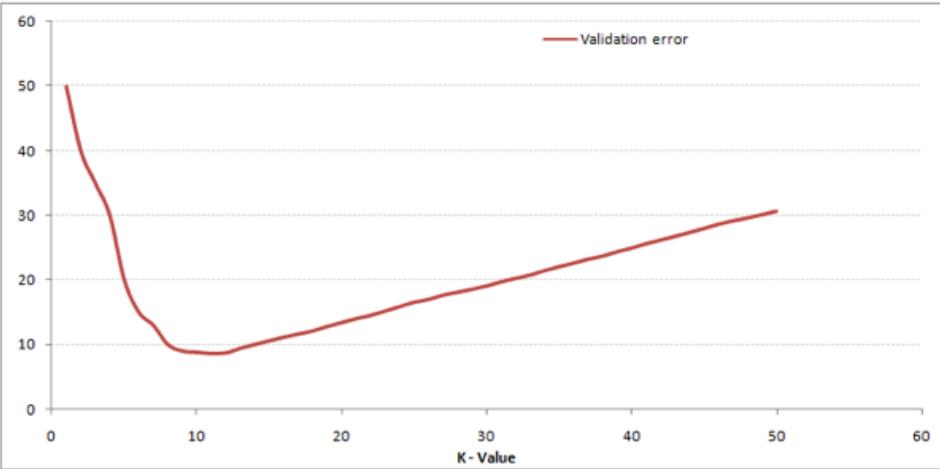
72

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## K-Nearest Neighbors (K-NN)

- How to select value of parameter K??



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## K-Nearest Neighbors (K-NN)

- How to select value of parameter K??

- Very small K results in high validation error
- Very high K also results in high validation error
- Select K where validation error is minimum

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## K-Nearest Neighbors – Python

	A	B	C	D	E	
1	User ID	Gender	Age	EstimatedSalary	Purchased	Dependent Variable
2	15624510	Male	19	19000	0	
3	15810944	Male	35	20000	0	
4	15668575	Female	26	43000	0	
5	15603246	Female	27	57000	0	
6	15804002	Male	19	76000	0	
7	15728773	Male	27	58000	0	
8	15598044	Female	27	84000	0	
9	15694829	Female	32	150000	1	
10	15600575	Male	25	33000	0	
11	15727311	Female	35	65000	0	
12	15570769	Female	26	80000	0	
13	15606274	Female	26	52000	0	
14	15746139	Male	20	86000	0	
15	15704987	Male	32	18000	0	
16	15628972	Male	18	82000	0	
17	15697686	Male	29	80000	0	
18	15733883	Male	47	25000	1	
19	15617482	Male	45	26000	1	
20	15704583	Male	46	28000	1	

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## K-Nearest Neighbors – Python

### • Importing the Libraries

```
9 # K-Nearest Neighbors (K-NN)
10
11 # Importing the libraries
12 import numpy as np
13 import matplotlib.pyplot as plt
14 import pandas as pd
```

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## K-Nearest Neighbors – Python

- Importing the Dataset

```
16 # Importing the dataset
17 dataset = pd.read_csv('Social_Network_Ads.csv')
18 X = dataset.iloc[:, [2, 3]].values
19 y = dataset.iloc[:, -1].values
```

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## K-Nearest Neighbors – Python

- Splitting the dataset into the Training set and Test set

```
21 # Splitting the dataset into the Training set and Test set
22 from sklearn.model_selection import train_test_split
23 X_train, X_test, y_train, y_test = train_test_split(
24     X, y, test_size = 0.25, random_state = 0)
```

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# K-Nearest Neighbors – Python



## • Feature Scaling

```
26 # Feature Scaling
27 from sklearn.preprocessing import StandardScaler
28 sc = StandardScaler()
29 X_train = sc.fit_transform(X_train)
30 X_test = sc.transform(X_test)
```

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# K-Nearest Neighbors – Python

## Feature Scaling

The image shows four Jupyter Notebook cells arranged in a 2x2 grid. The top-left cell displays the original data for X\_train, which includes columns for index (0-8), sepal length (44-36), and sepal width (39000-50000). The top-right cell shows the scaled data for X\_train, where values range from -0.210609 to 0.581649. The bottom-left cell shows the original data for X\_test, with values ranging from 18 to 36. The bottom-right cell shows the scaled data for X\_test, with values ranging from -1.99319 to 0.504964.

	0	1
0	44	39000
1	32	120000
2	38	50000
3	32	135000
4	52	21000
5	53	104000
6	39	42000
7	38	61000
8	36	50000

	0	1
0	0.581649	-0.886707
1	-0.606738	1.46174
2	-0.01254...	-0.567782
3	-0.606738	1.89663
4	1.37391	-1.40858
5	1.47294	0.997847
6	0.0864882	-0.799728
7	-0.01254...	-0.248858
8	-0.210609	-0.567782

	0	1
0	30	87000
1	38	50000
2	35	75000
3	30	79000
4	35	50000
5	27	20000
6	31	15000
7	36	144000
8	18	68000

	0	1
0	-0.804802	0.504964
1	-0.01254...	-0.567782
2	-0.309641	0.157046
3	-0.804802	0.273019
4	-0.309641	-0.567782
5	-1.1019	-1.43758
6	-0.70577	-1.58254
7	-0.210609	2.15757
8	-1.99319	-0.04590...

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## K-Nearest Neighbors – Python



- Training the K-NN model on the Training set

```
32 # Training the K-NN model on the Training set
33 from sklearn.neighbors import KNeighborsClassifier
34 classifier = KNeighborsClassifier(
35     n_neighbors = 5, metric = 'minkowski', p = 2)
36 classifier.fit(X_train, y_train)
```

### KNeighborsClassifier

**Definition :** KNeighborsClassifier(\*, self, n\_neighbors=5, weights='uniform', algorithm='auto', leaf\_size=30, p=2, metric='minkowski', metric\_params=None, n\_jobs=None, radius=None)

Classifier implementing the k-nearest neighbors vote.

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## K-Nearest Neighbors – Python



- Predicting the Test set results

```
38 # Predicting the Test set results
39 y_pred = classifier.predict(X_test)
```

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## K-Nearest Neighbors – Python

- Making the Confusion Matrix

```
41 # Making the Confusion Matrix
42 from sklearn.metrics import confusion_matrix
43 cm = confusion_matrix(y_test, y_pred)
44 print(cm)
```

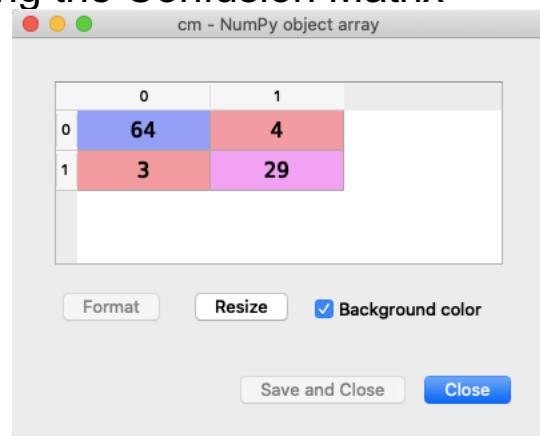
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## K-Nearest Neighbors – Python

- Making the Confusion Matrix



A screenshot of a dialog box titled "cm - NumPy object array". The dialog displays a 2x2 confusion matrix:

	0	1
0	64	4
1	3	29

The dialog includes buttons for "Format", "Resize", "Background color" (with a checked checkbox), "Save and Close", and "Close".

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## K-Nearest Neighbors – Python

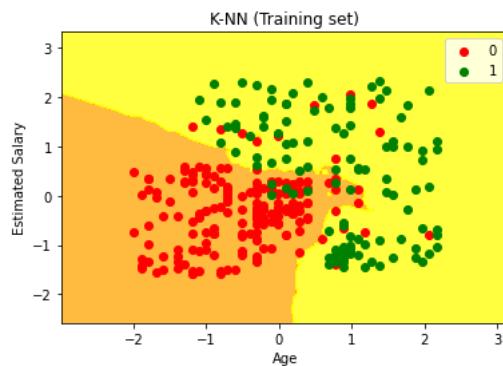
### ● Visualising the Training set results

```
46 # Visualising the Training set results
47 from matplotlib.colors import ListedColormap
48 X_set, y_set = X_train, y_train
49 X1, X2 = np.meshgrid(np.arange(start = X_set[:, 0].min() - 1,
50                           stop = X_set[:, 0].max() + 1, step = 0.01),
51                           np.arange(start = X_set[:, 1].min() - 1,
52                           stop = X_set[:, 1].max() + 1, step = 0.01))
53 plt.contourf(X1, X2, classifier.predict(
54     np.array([X1.ravel(), X2.ravel()]).T).reshape(X1.shape),
55     alpha = 0.75, cmap = ListedColormap(('orange', 'yellow')))
56 plt.xlim(X1.min(), X1.max())
57 plt.ylim(X2.min(), X2.max())
58 for i, j in enumerate(np.unique(y_set)):
59     plt.scatter(X_set[y_set == j, 0], X_set[y_set == j, 1],
60                 c = ListedColormap(('red', 'green'))(i), label = j)
61 plt.title('K-NN (Training set)')
62 plt.xlabel('Age')
63 plt.ylabel('Estimated Salary')
64 plt.legend()
65 plt.show()
```

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## K-Nearest Neighbors – Python

### ● Visualising the Training set results



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# K-Nearest Neighbors – Python

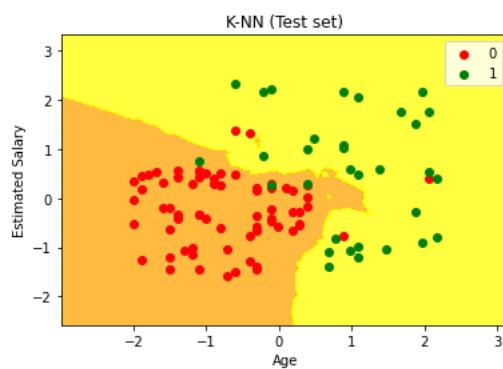
## • Visualising the Testing set results

```
67 # Visualising the Test set results
68 from matplotlib.colors import ListedColormap
69 X_set, y_set = X_test, y_test
70 X1, X2 = np.meshgrid(np.arange(start = X_set[:, 0].min() - 1,
71                             stop = X_set[:, 0].max() + 1, step = 0.01),
72                      np.arange(start = X_set[:, 1].min() - 1,
73                             stop = X_set[:, 1].max() + 1, step = 0.01))
74 plt.contourf(X1, X2, classifier.predict(
75     np.array([X1.ravel(), X2.ravel()]).T.reshape(X1.shape),
76     alpha = 0.75, cmap = ListedColormap(('orange', 'yellow')))
77 plt.xlim(X1.min(), X1.max())
78 plt.ylim(X2.min(), X2.max())
79 for i, j in enumerate(np.unique(y_set)):
80     plt.scatter(X_set[y_set == j, 0], X_set[y_set == j, 1],
81                 c = ListedColormap(('red', 'green'))(i), label = j)
82 plt.title('K-NN (Test set)')
83 plt.xlabel('Age')
84 plt.ylabel('Estimated Salary')
85 plt.legend()
86 plt.show()
```

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# K-Nearest Neighbors – Python

## • Visualising the Testing set results



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## Support Vector Machine (SVM)

- Supervised Learning algorithm
- Used for Classification

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## Support Vector Machine (SVM)

- It is a linear binary classifier.
- The SVM algorithm was invented by Vladimir N. Vapnik and Alexey Ya. Chervonenkis in 1963.

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## Support Vector Machine (SVM)

- How to classify??

- A data point is viewed as a p-dimensional vector (a list of p numbers), and we want to know whether we can separate such points with a  $(p - 1)$ -dimensional hyperplane.

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## Support Vector Machine (SVM)

- Many hyperplanes are possible which might classify the data.
- Select the best hyperplane which represents the largest margin between the two classes.

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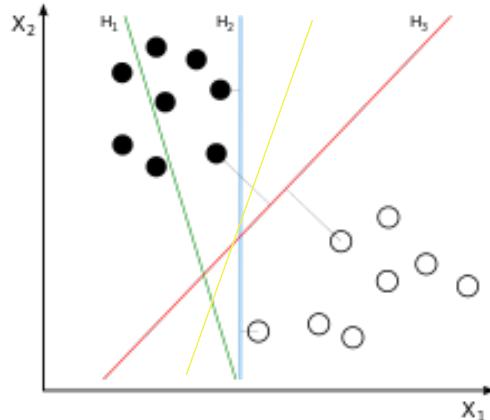
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## Support Vector Machine (SVM)

- Select H1 or H2 or H3 hyperplane??



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## Support Vector Machine (SVM)

- Answer:

- Choose the hyperplane so that the distance from it to the nearest data point on each side is maximized.

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## Support Vector Machine (SVM)



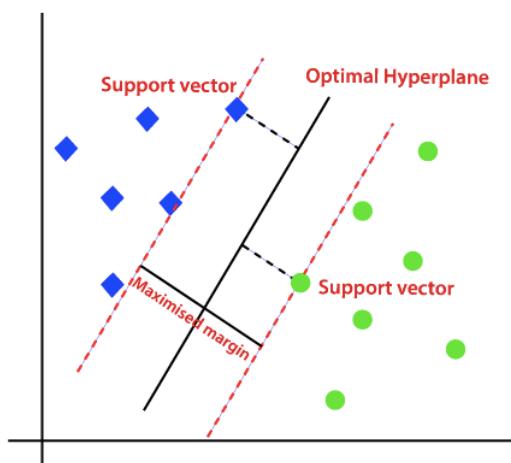
- SVM chooses the extreme points/vectors that help in creating the hyperplane.
- These extreme cases are called support vectors.

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## Support Vector Machine (SVM)



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## Support Vector Machine (SVM)



- The dimensions of the hyperplane depend on the features present in the dataset
  - If there are 2 features, then hyperplane will be a straight line
  - If there are 3 features, then hyperplane will be a 2-dimension plane
  - If there more than 3 features, then it will be a hyperplane

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## Support Vector Machine (SVM)



- Hyperplane
  - Decision plane which divides set of data points in to two different classes
- Margin
  - gap between two lines on the closet data points of different classes
- Support Vectors
  - Data points/vectors closest to the optimal hyperplane

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## Support Vector Machine – Python

	A	B	C	D	E	
1	User ID	Gender	Age	EstimatedSalary	Purchased	Dependent Variable
2	15624510	Male	19	19000	0	
3	15810944	Male	35	20000	0	
4	15668575	Female	26	43000	0	
5	15603246	Female	27	57000	0	
6	15804002	Male	19	76000	0	
7	15728773	Male	27	58000	0	
8	15598044	Female	27	84000	0	
9	15694829	Female	32	150000	1	
10	15600575	Male	25	33000	0	
11	15727311	Female	35	65000	0	
12	15570769	Female	26	80000	0	
13	15606274	Female	26	52000	0	
14	15746139	Male	20	86000	0	
15	15704987	Male	32	18000	0	
16	15628972	Male	18	82000	0	
17	15697686	Male	29	80000	0	
18	15733883	Male	47	25000	1	
19	15617482	Male	45	26000	1	
20	15704583	Male	46	28000	1	99

99

## Support Vector Machine – Python

### • Importing the libraries

```
9 # Support Vector Machine (SVM)
10
11 # Importing the libraries
12 import numpy as np
13 import matplotlib.pyplot as plt
14 import pandas as pd
```

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## Support Vector Machine – Python

- Importing the dataset

```
16 # Importing the dataset
17 dataset = pd.read_csv('Social_Network_Ads.csv')
18 X = dataset.iloc[:, [2, 3]].values
19 y = dataset.iloc[:, -1].values
```

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## Support Vector Machine – Python

- Importing the dataset

Index	User ID	Gender	Age	EstimatedSalary	Purchased
0	15624510	Male	19	19000	0
1	15810944	Male	35	20000	0
2	15668575	Female	26	43000	0
3	15603246	Female	27	57000	0
4	15804002	Male	19	76000	0
5	15728773	Male	27	58000	0
6	15598044	Female	27	84000	0
7	15694829	Female	32	150000	1
8	15600575	Male	25	33000	0
9	15727311	Female	35	65000	0
10	15570769	Female	26	80000	0
11	15606274	Female	26	52000	0
12	15746139	Male	20	86000	0

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## Support Vector Machine – Python

- Create two vectors X and y

The image shows two side-by-side data visualization windows. The left window is titled "X - NumPy object array" and displays a 9x2 grid of numerical values. The right window is titled "y - NumPy object array" and displays a 9x1 grid of numerical values. Both windows have "Format", "Resize", and "Background color" buttons at the bottom.

	0	1
0	19	19000
1	35	20000
2	26	43000
3	27	57000
4	19	76000
5	27	58000
6	27	84000
7	32	150000
8	25	33000

	0
0	0
1	0
2	0
3	0
4	0
5	0
6	0
7	1
8	0

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## Support Vector Machine – Python

- Splitting the dataset into the Training set and Test set

```
21 # Splitting the dataset into the Training set and Test set
22 from sklearn.model_selection import train_test_split
23 X_train, X_test, y_train, y_test = train_test_split(
24     X, y, test_size = 0.25, random_state = 0)
```

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# Support Vector Machine – Python



## • Feature Scaling

```
26 # Feature Scaling
27 from sklearn.preprocessing import StandardScaler
28 sc = StandardScaler()
29 X_train = sc.fit_transform(X_train)
30 X_test = sc.transform(X_test)
```

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# Support Vector Machine – Python

## Feature Scaling

The figure consists of four screenshots of Jupyter Notebook cells, arranged in a 2x2 grid. The top-left cell shows the original training data (X\_train) as a NumPy array:

	0	1
0	44	39000
1	32	120000
2	38	50000
3	32	135000
4	52	21000
5	53	104000
6	39	42000
7	38	61000
8	36	50000

The other three cells show the scaled training data (X\_train), scaled test data (X\_test), and unscaled test data (X\_test). The scaled data shows values between -1 and 1.

	0	1
0	0.581649	-0.886707
1	-0.606738	1.46174
2	-0.01254...	-0.567782
3	-0.606738	1.89663
4	1.37391	-1.40858
5	1.47294	0.997847
6	0.0864882	-0.799728
7	-0.01254...	-0.248858
8	-0.210609	-0.567782

	0	1
0	30	87000
1	38	50000
2	35	75000
3	30	79000
4	35	50000
5	27	20000
6	31	15000
7	36	144000
8	18	68000

	0	1
0	-0.804802	0.504964
1	-0.01254...	-0.567782
2	-0.309641	0.157046
3	-0.804802	0.273019
4	-0.309641	-0.567782
5	-1.1019	-1.43758
6	-0.70577	-1.58254
7	-0.210609	2.15757
8	-1.99319	-0.04590...

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## Support Vector Machine – Python



- Training the SVM model on the Training set

```
32 # Training the SVM model on the Training set
33 from sklearn.svm import SVC
34 classifier = SVC(kernel = 'linear', random_state = 0)
35 classifier.fit(X_train, y_train)
```

SVC

```
Definition : SVC(*, self, C=1.0, kernel='rbf', degree=3,
gamma='scale', coef0=0.0, shrinking=True,
probability=False, tol=1e-3, cache_size=200,
class_weight=None, verbose=False, max_iter=-1,
decision_function_shape='ovr', break_ties=False,
random_state=None)
```

C-Support Vector Classification.

The implementation is based on libsvm. The fit time scales at least quadratically with the number of samples and may be impractical beyond tens of thousands of samples. For large datasets consider using `sklearn.svm.LinearSVC` or `sklearn.linear_model.SGDClassifier` instead, possibly after a `sklearn.kernel_approximation.Nystroem` transformer.

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The multiclass support is handled according to a one-vs-one scheme.

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## Support Vector Machine – Python



- Predicting the Test set results

```
37 # Predicting the Test set results
38 y_pred = classifier.predict(X_test)
```

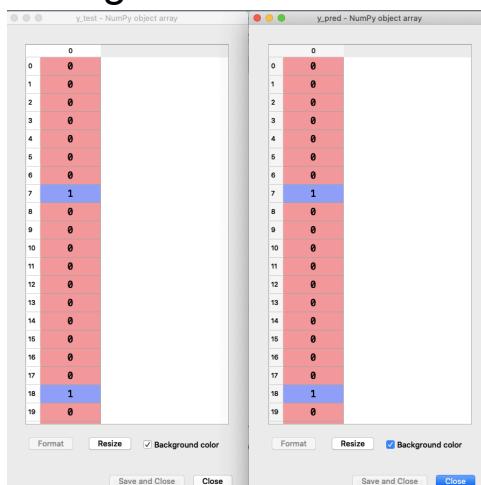
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## Support Vector Machine – Python

- Predicting the Test set results



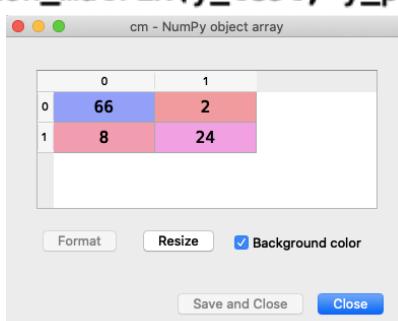
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## Support Vector Machine – Python

- Calculate the Confusion Metrix

```
40 # Making the Confusion Matrix
41 from sklearn.metrics import confusion_matrix
42 cm = confusion_matrix(y_test, y_pred)
43 print(cm)
```



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# Support Vector Machine – Python

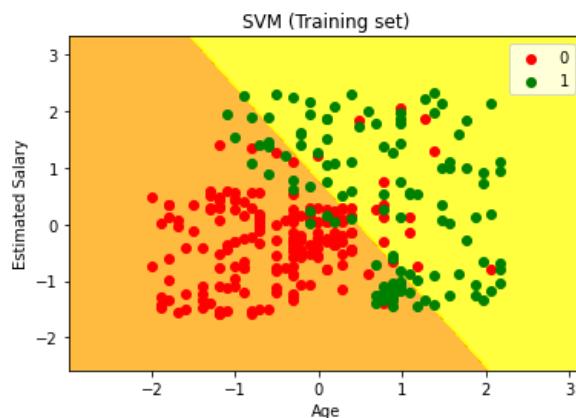
## • Visualising the Training set results

```
45 # Visualising the Training set results
46 from matplotlib.colors import ListedColormap
47 X_set, y_set = X_train, y_train
48 X1, X2 = np.meshgrid(np.arange(start = X_set[:, 0].min() - 1,
49                      stop = X_set[:, 0].max() + 1, step = 0.01),
50                      np.arange(start = X_set[:, 1].min() - 1,
51                      stop = X_set[:, 1].max() + 1, step = 0.01))
52 plt.contourf(X1, X2, classifier.predict(
53     np.array([X1.ravel(), X2.ravel()]).T).reshape(X1.shape),
54     alpha = 0.75, cmap = ListedColormap(('red', 'green')))
55 plt.xlim(X1.min(), X1.max())
56 plt.ylim(X2.min(), X2.max())
57 for i, j in enumerate(np.unique(y_set)):
58     plt.scatter(X_set[y_set == j, 0], X_set[y_set == j, 1],
59                 c = ListedColormap(('red', 'green'))(i), label = j)
60 plt.title('SVM (Training set)')
61 plt.xlabel('Age')
62 plt.ylabel('Estimated Salary')
63 plt.legend()
64 plt.show()
```

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# Support Vector Machine – Python

## • Visualising the Training set results



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# Support Vector Machine – Python

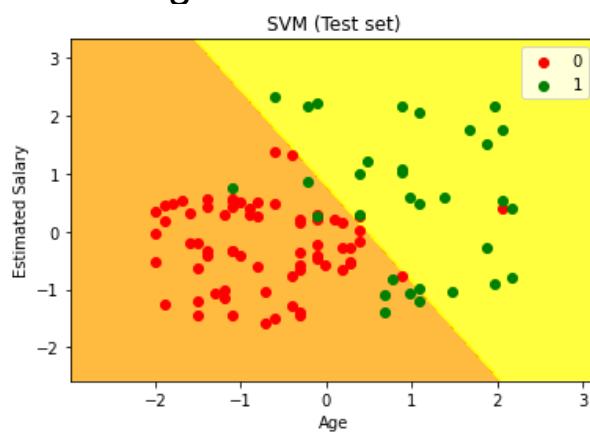
## • Visualising the Test set results

```
66 # Visualising the Test set results
67 from matplotlib.colors import ListedColormap
68 X_set, y_set = X_test, y_test
69 X1, X2 = np.meshgrid(np.arange(start = X_set[:, 0].min() - 1,
70                         stop = X_set[:, 0].max() + 1, step = 0.01),
71                         np.arange(start = X_set[:, 1].min() - 1,
72                         stop = X_set[:, 1].max() + 1, step = 0.01))
73 plt.contourf(X1, X2, classifier.predict(
74     np.array([X1.ravel(), X2.ravel()]).T).reshape(X1.shape),
75     alpha = 0.75, cmap = ListedColormap(('red', 'green')))
76 plt.xlim(X1.min(), X1.max())
77 plt.ylim(X2.min(), X2.max())
78 for i, j in enumerate(np.unique(y_set)):
79     plt.scatter(X_set[y_set == j, 0], X_set[y_set == j, 1],
80                 c = ListedColormap(('red', 'green'))(i), label = j)
81 plt.title('SVM (Test set)')
82 plt.xlabel('Age')
83 plt.ylabel('Estimated Salary')
84 plt.legend()
85 plt.show()
```

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# Support Vector Machine – Python

## • Visualising the Test set results



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## Support Vector Machine (SVM)

- In 1992, Bernhard Boser, Isabelle Guyon and Vladimir Vapnik suggested a way to create nonlinear classifiers by applying the kernel trick to maximum-margin hyperplanes.
- The current incarnation (soft margin) was proposed by Corinna Cortes and Vapnik in 1993 and published in 1995.

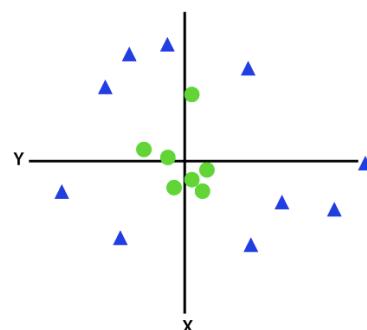
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## Support Vector Machine (SVM)

- For non-linear data, we cannot have a single straight line.



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## Support Vector Machine (SVM)



- Solution: add one more dimension.
  - For linear data, we have used two dimensions x and y, so for non-linear data, we will add a third dimension z.
  - $z=x^2 +y^2$

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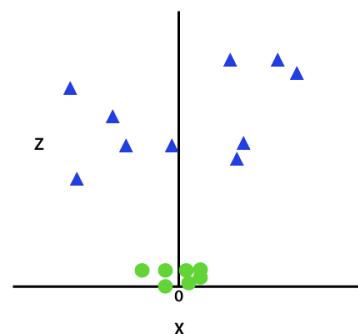
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## Support Vector Machine (SVM)



- Solution: add one more dimension.



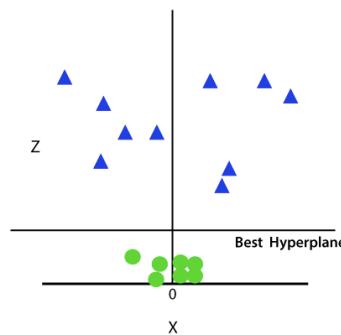
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## Support Vector Machine (SVM)

- Now, divide the data into two classes



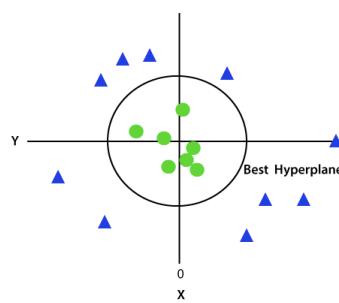
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## Support Vector Machine (SVM)

- In 2-D space it will look like



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## Support Vector Machine (SVM)

- A **Kernel function** transforms the training data so that a non-linear decision surface is transformed to a linear equation in a higher number of dimensions.

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## Support Vector Machine (SVM)

### Non Linear SVMs

Polynomial

Radial Basis Function  
(Gaussians)

Sigmoid

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## Support Vector Machine (SVM)

- Linear Kernel

- It can be used as a dot product between any two observations.
- The formula of linear kernel is –  
$$K(x,xi) = \sum(x * xi)$$

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## Support Vector Machine (SVM)

- Polynomial Kernel

- It is more generalized form of linear kernel and distinguish curved or nonlinear input space.
- Following is the formula for polynomial kernel –  
$$k(X,Xi) = 1 + \sum(X * Xi)^d$$
- Here d is the degree of polynomial, which we need to specify manually in the learning algorithm.

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## Support Vector Machine (SVM)



- Radial Basis Function (RBF) Kernel
  - RBF kernel, mostly used in SVM classification, maps input space in indefinite dimensional space.
  - Following formula explains it mathematically –  
$$K(x,xi)=\exp(-\gamma \sum (x-xi)^2)$$
  - Here, *gamma* ranges from 0 to 1.
  - We need to manually specify it in the learning algorithm.
  - A good default value of *gamma* is 0.1.

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## Support Vector Machine (SVM)



- Sigmoid Kernel
  - Hyperbolic tangent kernel
  - Also known as Neural Network activation function
  - Following formula explains it mathematically –  
$$K(x,xi)=\tanh(\alpha x^T xi - \delta)$$
  - A common value for alpha is  $1/N$ , where N is the data dimension.
  - SVM model using a sigmoid kernel function is equivalent to a two-layer, perceptron neural network.

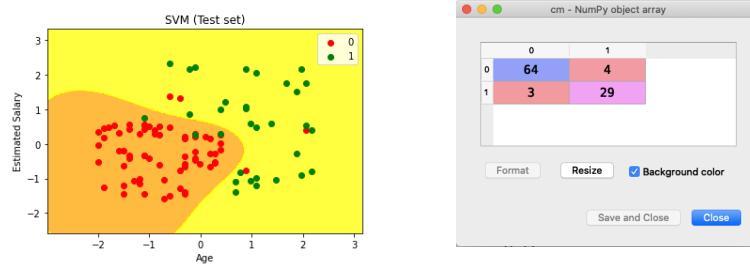
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## Support Vector Machine (SVM)

- classifier = SVC(kernel = 'linear', random\_state = 0)
- classifier = SVC(kernel = 'poly', degree=3, random\_state = 0)
- classifier = SVC(kernel = 'rbf', random\_state = 0)



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## Naïve Bayes

- Supervised machine learning algorithm
- Used for classification

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## Naïve Bayes



- Bayes' theorem

- In probability theory and statistics, Bayes' theorem describes the probability of an event, based on prior knowledge of conditions that might be related to the event.

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## Naïve Bayes



- Bayes' theorem

- For example, if the risk of developing health problems is known to increase with age, Bayes's theorem allows the risk to an individual of a known age to be assessed more accurately than simply assuming that the individual is typical of the population as a whole.

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## Naïve Bays



- Bayes' theorem – mathematical equation

$$\text{P}(B | A) * P(A)$$
$$\text{P}(A | B) = \frac{\text{P}(B | A) * P(A)}{\text{P}(B)}$$

- Where A and B are events and  $\text{P}(B) \neq 0$

- $\text{P}(A | B)$  is conditional probability: the likelihood of event A occurring given that B is true.
- $\text{P}(B | A)$  is also a conditional probability: the likelihood of event B occurring given that A is true.
- $\text{P}(A)$  and  $\text{P}(B)$  are the probabilities of events A and B respectively; they are known as marginal probability.

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## Naïve Bays



- In statistics, Naive Bayes classifiers are a family of simple "probabilistic classifiers" based on applying Bayes' theorem with strong (naïve) independence assumptions between the features.

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## Naïve Bayes



- When to use???

- **Real-time Prediction:** As Naive Bayes is super fast, it can be used for making predictions in real time.
- **Multi-class Prediction:** This algorithm can predict the posterior probability of multiple classes of the target variable.
- **Scalable:** Used for Very large datasets

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## Naïve Bayes – Example1



- <https://machinelearningmastery.com/naive-bayes-tutorial-for-machine-learning/>

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## Naïve Bays – Example1



- Weather, car condition, action example

1	Weather	Car	Class
2	sunny	working	go-out
3	rainy	broken	go-out
4	sunny	working	go-out
5	sunny	working	go-out
6	sunny	working	go-out
7	rainy	broken	stay-home
8	rainy	broken	stay-home
9	sunny	working	stay-home
10	sunny	broken	stay-home
11	rainy	broken	stay-home

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## Naïve Bays – Example1



- Encode categorical data

1	Weather	Car	Class
2	1	1	1
3	0	0	1
4	1	1	1
5	1	1	1
6	1	1	1
7	0	0	0
8	0	0	0
9	1	1	0
10	1	0	0
11	0	0	0

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## Naïve Bays – Example1



- **Calculate the Class Probabilities**

- $P(\text{class}=1) = \text{count}(\text{class}=1) / (\text{count}(\text{class}=0) + \text{count}(\text{class}=1))$
- $P(\text{class}=1) = 5 / (5 + 5)$
- $P(\text{class}=0) = \text{count}(\text{class}=0) / (\text{count}(\text{class}=0) + \text{count}(\text{class}=1))$
- $P(\text{class}=0) = 5 / (5 + 5)$
- 0.5 probability for any given data instance belonging to class 0 or class 1.

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## Naïve Bays – Example1



- **Calculate the Conditional Probabilities**

- The conditional probabilities are the probability of each input value given each class value.

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## Naïve Bayes – Example1



### • Calculate the Conditional Probabilities

#### ○ Weather Input Variable

- $P(\text{weather}=\text{sunny}|\text{class}=\text{go-out}) = \text{count}(\text{weather}=\text{sunny} \text{ and } \text{class}=\text{go-out}) / \text{count}(\text{class}=\text{go-out})$
- $P(\text{weather}=\text{rainy}|\text{class}=\text{go-out}) = \text{count}(\text{weather}=\text{rainy} \text{ and } \text{class}=\text{go-out}) / \text{count}(\text{class}=\text{go-out})$
- $P(\text{weather}=\text{sunny}|\text{class}=\text{stay-home}) = \text{count}(\text{weather}=\text{sunny} \text{ and } \text{class}=\text{stay-home}) / \text{count}(\text{class}=\text{stay-home})$
- $P(\text{weather}=\text{rainy}|\text{class}=\text{stay-home}) = \text{count}(\text{weather}=\text{rainy} \text{ and } \text{class}=\text{stay-home}) / \text{count}(\text{class}=\text{stay-home})$

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## Naïve Bayes – Example1



### • Calculate the Conditional Probabilities

#### ○ Weather Input Variable

- $P(\text{weather}=\text{sunny}|\text{class}=\text{go-out}) = 0.8$
- $P(\text{weather}=\text{rainy}|\text{class}=\text{go-out}) = 0.2$
- $P(\text{weather}=\text{sunny}|\text{class}=\text{stay-home}) = 0.4$
- $P(\text{weather}=\text{rainy}|\text{class}=\text{stay-home}) = 0.6$

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## Naïve Bayes – Example1



### • Calculate the Conditional Probabilities

#### ○ Car Input Variable

- $P(\text{car}=\text{working}|\text{class}=\text{go-out}) = \text{count}(\text{car}=\text{working} \text{ and } \text{class}=\text{go-out}) / \text{count}(\text{class}=\text{go-out})$
- $P(\text{car}=\text{broken}|\text{class}=\text{go-out}) = \text{count}(\text{car}=\text{brokenrainy} \text{ and } \text{class}=\text{go-out}) / \text{count}(\text{class}=\text{go-out})$
- $P(\text{car}=\text{working}|\text{class}=\text{stay-home}) = \text{count}(\text{car}=\text{working} \text{ and } \text{class}=\text{stay-home}) / \text{count}(\text{class}=\text{stay-home})$
- $P(\text{car}=\text{broken}|\text{class}=\text{stay-home}) = \text{count}(\text{car}=\text{brokenrainy} \text{ and } \text{class}=\text{stay-home}) / \text{count}(\text{class}=\text{stay-home})$

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## Naïve Bayes – Example1



### • Calculate the Conditional Probabilities

#### ○ Car Input Variable

- $P(\text{car}=\text{working}|\text{class}=\text{go-out}) = 0.8$
- $P(\text{car}=\text{broken}|\text{class}=\text{go-out}) = 0.2$
- $P(\text{car}=\text{working}|\text{class}=\text{stay-home}) = 0.2$
- $P(\text{car}=\text{broken}|\text{class}=\text{stay-home}) = 0.8$

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## Naïve Bayes – Example1



### ● Make Predictions with Naive Bayes

- Test record: weather=sunny, car=working

- Calculate for go-out class:

- $\text{go-out} = P(\text{weather}=\text{sunny}|\text{class}=\text{go-out}) * P(\text{car}=\text{working}|\text{class}=\text{go-out}) * P(\text{class}=\text{go-out})$
- $\text{go-out} = 0.8 * 0.8 * 0.5$
- $\text{go-out} = 0.32$

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## Naïve Bayes – Example1



### ● Make Predictions with Naive Bayes

- Test record: weather=sunny, car=working

- Calculate for stay-home class:

- $\text{stay-home} = P(\text{weather}=\text{sunny}|\text{class}=\text{stay-home}) * P(\text{car}=\text{working}|\text{class}=\text{stay-home}) * P(\text{class}=\text{stay-home})$
- $\text{stay-home} = 0.4 * 0.2 * 0.5$
- $\text{stay-home} = 0.04$

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## Naïve Bays – Example1



- **Make Predictions with Naive Bayes**

- Test record: weather=sunny, car=working
- We can see that 0.32 is greater than 0.04, therefore we predict “go-out” for this instance

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## Naïve Bays – Example2



- <https://www.simplilearn.com/tutorials/machine-learning-tutorial/naive-bayes-classifier>
- Game play prediction using weather data

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## Naïve Bays – Example2



Day	Outlook	Humidity	Wind	Play
D1	Sunny	High	Weak	No
D2	Sunny	High	Strong	No
D3	Overcast	High	Weak	Yes
D4	Rain	High	Weak	Yes
D5	Rain	Normal	Weak	Yes
D6	Rain	Normal	Strong	No
D7	Overcast	Normal	Strong	Yes
D8	Sunny	High	Weak	No
D9	Sunny	Normal	Weak	Yes
D10	Rain	Normal	Weak	Yes
D11	Sunny	Normal	Strong	Yes
D12	Overcast	High	Strong	Yes
D13	Overcast	Normal	Weak	Yes
D14	Rain	High	Strong	No

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## Naïve Bays – Example2



- First, we will create a **frequency** table using each attribute of the dataset.

Frequency Table		Play	
		Yes	No
Outlook	Sunny	3	2
	Overcast	4	0
	Rainy	3	2

Frequency Table		Play	
		Yes	No
Humidity	High	3	4
	Normal	6	1

Frequency Table		Play	
		Yes	No
Wind	Strong	6	2
	Weak	3	3

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## Naïve Bayes – Example2



- For each frequency table, we will generate a **likelihood** table.

Likelihood Table		Play		$P(x c) = P(\text{Sunny} \text{Yes}) = 3/10 = 0.3$
		Yes	No	
Outlook	Sunny	3/10	2/4	$P(x) = P(\text{Sunny}) = 5/14 = 0.36$
	Overcast	4/10	0/4	$4/14$
	Rainy	3/10	2/4	$5/14$
		10/14	4/14	$P(c) = P(\text{Yes}) = 10/14 = 0.71$

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## Naïve Bayes – Example2



- Likelihood of ‘Yes’ given ‘Sunny’ is:
  - $P(c|x)$
  - $= P(\text{Yes}|\text{Sunny})$
  - $= P(\text{Sunny}|\text{Yes}) * P(\text{Yes}) / P(\text{Sunny})$
  - $= (0.3 \times 0.71) / 0.36$
  - $= 0.591$

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## Naïve Bayes – Example2



- Similarly Likelihood of 'No' given 'Sunny' is:

$$\textcircled{P(c|x)}$$

$$\textcircled{= P(No|Sunny)}$$

$$\textcircled{= P(Sunny|No) * P(No) / P(Sunny)}$$

$$\textcircled{= (0.4 \times 0.36) / 0.36}$$

$$\textcircled{= 0.40}$$

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## Naïve Bayes – Example2



- Now, in the same way, we need to create the Likelihood Table for other attributes as well.

Likelihood table for Humidity

Likelihood Table		Play		
		Yes	No	
Humidity	High	3/9	4/5	7/14
	Normal	6/9	1/5	7/14
		9/14	5/14	

Likelihood table for Wind

Likelihood Table		Play		
		Yes	No	
Wind	Weak	6/9	2/5	8/14
	Strong	3/9	3/5	6/14
		9/14	5/14	

$$P(\text{Yes}/\text{High}) = 0.33 \times 0.6 / 0.5 = 0.42$$

$$P(\text{Yes}/\text{Weak}) = 0.67 \times 0.64 / 0.57 = 0.75$$

$$P(\text{No}/\text{High}) = 0.8 \times 0.36 / 0.5 = 0.58$$

$$P(\text{No}/\text{Weak}) = 0.4 \times 0.36 / 0.57 = 0.25$$

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## Naïve Bays – Example2



- Test for NEW data point
  - Suppose we have a **Day** with the following values :
    - **Outlook = Rain**
    - **Humidity = High**
    - **Wind = Weak**
    - **Play =?**
  - we have to predict whether “we can play on that day or not”.

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## Naïve Bays – Example2



- **Likelihood of ‘Yes’ on that Day**
  - $= P(\text{Outlook} = \text{Rain}|\text{Yes}) * P(\text{Humidity} = \text{High}|\text{Yes}) * P(\text{Wind} = \text{Weak}|\text{Yes}) * P(\text{Yes})$
  - $= 2/9 * 3/9 * 6/9 * 9/14$
  - $= 0.0199$
- **Likelihood of ‘No’ on that Day**
  - $= P(\text{Outlook} = \text{Rain}|\text{No}) * P(\text{Humidity} = \text{High}|\text{No}) * P(\text{Wind} = \text{Weak}|\text{No}) * P(\text{No})$
  - $= 2/5 * 4/5 * 2/5 * 5/14$
  - $= 0.0166$

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## Naïve Bayes – Example2



- Now we normalize the values, then
  - $P(\text{Yes}) = 0.0199 / (0.0199 + 0.0166) = 0.55$
  - $P(\text{No}) = 0.0166 / (0.0199 + 0.0166) = 0.45$
- Our model predicts that there is a **55%** chance there will be a Game on selected day.

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## Naïve Bayes – Python

Independent Variables

	A	B	C	D	E	
1	User ID	Gender	Age	EstimatedSalary	Purchased	Dependent Variable
2	15624510	Male	19	19000	0	
3	15810944	Male	35	20000	0	
4	15668575	Female	26	43000	0	
5	15603246	Female	27	57000	0	
6	15804002	Male	19	76000	0	
7	15728773	Male	27	58000	0	
8	15598044	Female	27	84000	0	
9	15694829	Female	32	150000	1	
10	15600575	Male	25	33000	0	
11	15727311	Female	35	65000	0	
12	15570769	Female	26	80000	0	
13	15606274	Female	26	52000	0	
14	15746139	Male	20	86000	0	
15	15704987	Male	32	18000	0	
16	15628972	Male	18	82000	0	
17	15697686	Male	29	80000	0	
18	15733883	Male	47	25000	1	
19	15617482	Male	45	26000	1	
20	15704583	Male	46	28000	1	

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## Naïve Bayes – Python



### ● Importing the libraries

```
9 # Naive Bayes
10
11 # Importing the libraries
12 import numpy as np
13 import matplotlib.pyplot as plt
14 import pandas as pd
```

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## Naïve Bayes – Python



### ● Importing the dataset

```
16 # Importing the dataset
17 dataset = pd.read_csv('Social_Network_Ads.csv')
18 X = dataset.iloc[:, [2, 3]].values
19 y = dataset.iloc[:, -1].values
```

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## Naïve Bays – Python

### Importing the dataset

Index	User ID	Gender	Age	EstimatedSala	Purchased
0	15624510	Male	19	19000	0
1	15810944	Male	35	20000	0
2	15668575	Female	26	43000	0
3	15603246	Female	27	57000	0
4	15804002	Male	19	76000	0
5	15728773	Male	27	58000	0
6	15598044	Female	27	84000	0
7	15694829	Female	32	150000	1
8	15600575	Male	25	33000	0
9	15727311	Female	35	65000	0
10	15570769	Female	26	80000	0
11	15606274	Female	26	52000	0
12	15746139	Male	20	86000	0

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## Naïve Bays – Python

### Create two vectors X and y

X - NumPy object array	
0	19
1	19000
2	35
3	20000
4	26
5	43000
6	27
7	57000
8	19
9	76000
10	27
11	58000
12	27
13	84000
14	32
15	150000
16	25
17	33000

y - NumPy object array	
0	0
1	0
2	0
3	0
4	0
5	0
6	0
7	1
8	0

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## Naïve Bayes – Python



- Splitting the dataset into the Training set and Test set

```
21 # Splitting the dataset into the Training set and Test set
22 from sklearn.model_selection import train_test_split
23 X_train, X_test, y_train, y_test = train_test_split(
24     X, y, test_size = 0.25, random_state = 0)
```

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## Naïve Bayes – Python



- Feature Scaling

```
26 # Feature Scaling
27 from sklearn.preprocessing import StandardScaler
28 sc = StandardScaler()
29 X_train = sc.fit_transform(X_train)
30 X_test = sc.transform(X_test)
```

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# Naïve Bayes – Python

## Feature Scaling

The screenshot shows four tables representing training and testing datasets before and after scaling.

**X\_train - NumPy object array:**

	0	1
0	44	39000
1	32	120000
2	38	50000
3	32	135000
4	52	21000
5	53	104000
6	39	42000
7	38	61000
8	36	50000

**X\_train - NumPy object array (scaled):**

	0	1
0	0.581649	-0.886707
1	-0.606738	1.46174
2	-0.01254...	-0.567782
3	-0.606738	1.89663
4	1.37391	-1.40858
5	1.47294	0.997847
6	0.0864882	-0.799728
7	-0.01254...	-0.248858
8	-0.210609	-0.567782

**X\_test - NumPy object array:**

	0	1
0	30	87000
1	38	50000
2	35	75000
3	30	79000
4	35	50000
5	27	20000
6	31	15000
7	36	144000
8	18	68000

**X\_test - NumPy object array (scaled):**

	0	1
0	-0.804802	0.504964
1	-0.01254...	-0.567782
2	-0.309641	0.157046
3	-0.804802	0.273019
4	-0.309641	-0.567782
5	-1.1019	-1.43758
6	-0.70577	-1.58254
7	-0.210609	2.15757
8	-1.99319	-0.04590...

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# Naïve Bayes – Python

- Training the Naive Bayes model on the Training set

```
32 # Training the Naive Bayes model on the Training set
33 from sklearn.naive_bayes import GaussianNB
34 classifier = GaussianNB()
35 classifier.fit(X_train, y_train)
```

GaussianNB

Definition : GaussianNB(\*, self, priors=None,  
var\_smoothing=1e-9)

Gaussian Naive Bayes (GaussianNB)

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## Naïve Bayes – Python

- Predicting the Test set results

```
37 # Predicting the Test set results  
38 y_pred = classifier.predict(X_test)
```

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## Naïve Bayes – Python

- Predicting the Test set results

The image shows two side-by-side data tables. Both are titled "y\_test - NumPy object array" and "y\_pred - NumPy object array". They both have 20 rows, indexed from 0 to 19. The first column contains the index numbers. The second column contains the values. In both tables, most values are '0'. There are three instances where the value is '1': row 7, row 18, and row 19. The table on the left has a blue background color applied to its last three rows (18 and 19). The table on the right has a blue background color applied to its 7th row (7) and 18th row (18).

	y_test - NumPy object array	y_pred - NumPy object array
0	0	0
1	0	0
2	0	0
3	0	0
4	0	0
5	0	0
6	0	0
7	1	1
8	0	0
9	0	1
10	0	0
11	0	0
12	0	0
13	0	0
14	0	0
15	0	0
16	0	0
17	0	0
18	1	1
19	0	0

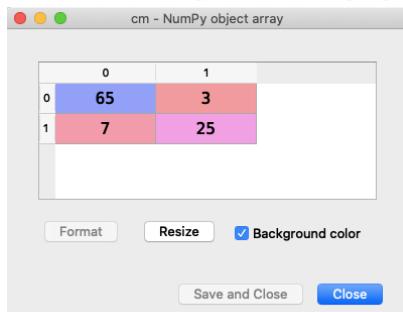
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## Naïve Bayes – Python

- Calculate the Confusion Metrix

```
40 # Making the Confusion Matrix
41 from sklearn.metrics import confusion_matrix
42 cm = confusion_matrix(y_test, y_pred)
43 print(cm)
```



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## Naïve Bayes – Python

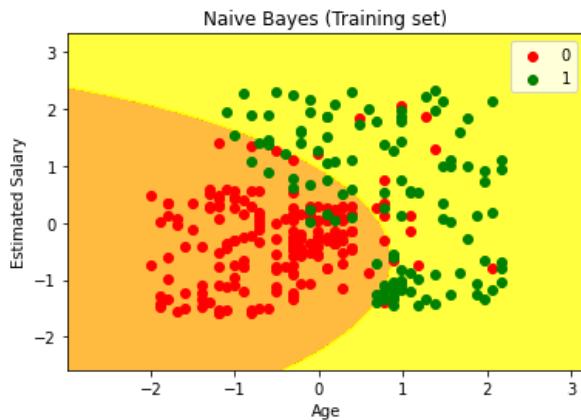
- Visualising the Training set results

```
45 # Visualising the Training set results
46 from matplotlib.colors import ListedColormap
47 X_set, y_set = X_train, y_train
48 X1, X2 = np.meshgrid(np.arange(start = X_set[:, 0].min() - 1,
49                             stop = X_set[:, 0].max() + 1, step = 0.01),
50                             np.arange(start = X_set[:, 1].min() - 1,
51                             stop = X_set[:, 1].max() + 1, step = 0.01))
52 plt.contourf(X1, X2, classifier.predict(
53     np.array([X1.ravel(), X2.ravel()]).T).reshape(X1.shape),
54     alpha = 0.75, cmap = ListedColormap(('orange', 'yellow')))
55 plt.xlim(X1.min(), X1.max())
56 plt.ylim(X2.min(), X2.max())
57 for i, j in enumerate(np.unique(y_set)):
58     plt.scatter(X_set[y_set == j, 0], X_set[y_set == j, 1],
59                 c = ListedColormap(('red', 'green'))(i), label = j)
60 plt.title('Naive Bayes (Training set)')
61 plt.xlabel('Age')
62 plt.ylabel('Estimated Salary')
63 plt.legend()
64 plt.show()
```

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## Naïve Bayes – Python

- Visualising the Training set results



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## Naïve Bayes – Python

- Visualising the Test set results

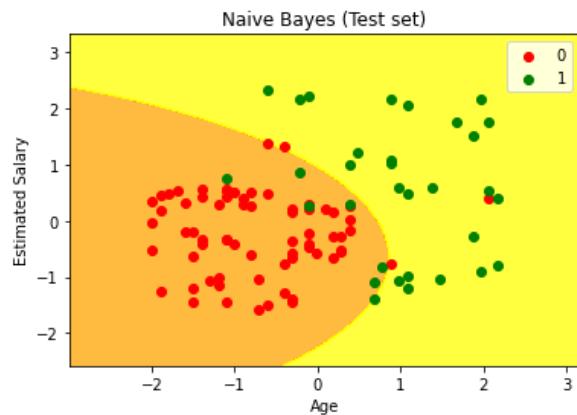
```
# Visualising the Test set results
66 from matplotlib.colors import ListedColormap
67 X_set, y_set = X_test, y_test
68 X1, X2 = np.meshgrid(np.arange(start = X_set[:, 0].min() - 1,
69                      stop = X_set[:, 0].max() + 1, step = 0.01),
70                      np.arange(start = X_set[:, 1].min() - 1,
71                      stop = X_set[:, 1].max() + 1, step = 0.01))
72 plt.contourf(X1, X2, classifier.predict(
73     np.array([X1.ravel(), X2.ravel()]).T).reshape(X1.shape),
74     alpha = 0.75, cmap = ListedColormap(('orange', 'yellow')))
75 plt.xlim(X1.min(), X1.max())
76 plt.ylim(X2.min(), X2.max())
77 for i, j in enumerate(np.unique(y_set)):
78     plt.scatter(X_set[y_set == j, 0], X_set[y_set == j, 1],
79                 c = ListedColormap(('red', 'green'))(i), label = j)
80 plt.title('Naïve Bayes (Test set)')
81 plt.xlabel('Age')
82 plt.ylabel('Estimated Salary')
83 plt.legend()
84 plt.show()
```

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## Naïve Bayes – Python



- Visualising the Test set results



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Questions ???

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