

Sort an Array with 0s, 1s and 2s.

Approaches

Suppose

[2, 0, 2, 1, 1, 0, 1, 2, 0, 0]

① Brute force

sort(vec.begin, vec.end())

① Brute force

② Optimized

③ Optimal

$\begin{bmatrix} O(n \log n) \\ T.C \end{bmatrix}$ $\begin{bmatrix} S.C \\ O(1) \end{bmatrix}$

② Optimized Approach $O(n)$ (2 passes)

Count of zeros, Ones, Twos
↓ ↓ ↓
4 3 3 } can be done in single loop

[2, 0, 2, 1, 1, 0, 1, 2, 0, 0]
0, 0, 0, 0 1, 1, 1 2, 2, 2

Overwriting in inner loop

$n = \text{num.size}$

count0, count1, count2

```
for(int i=0; i<n; i++) {  
    if(num[i]==0) count0++;  
    else if(num[i]==1) count1++;  
    else count2++;  
}
```

$O(n)$

int idx = 0

```
for(int i=0; i<count0; i++)  
    num[idx++] = 0
```

```
for(int i=0; i<count1; i++)  
    num[idx++] = 1
```

```
for(int i=0; i<count2; i++)  
    num[idx++] = 2
```


Optimal Approach

$O(1)$ - S.C
 $O(n)$ \rightarrow Single Pass

\rightarrow Dutch National Flag Algorithm

$[2, 0, 2, 1, 1, 0, 1, 2, 0, 0]$ high Use 3 pointers
mid $\{ \underline{0000} \quad \underline{111} \quad \underline{222} \}$
 $0 - l-1 \quad l - m-1 \quad m+1 - n-1$
(low, mid, high)

$m - h$
 \rightarrow Gap \rightarrow Used for Unsorted Elements

0s \rightarrow 0 to low-1

1s \rightarrow low to mid-1

Unsorted = (mid - high)

2s \rightarrow high+1 to n-1

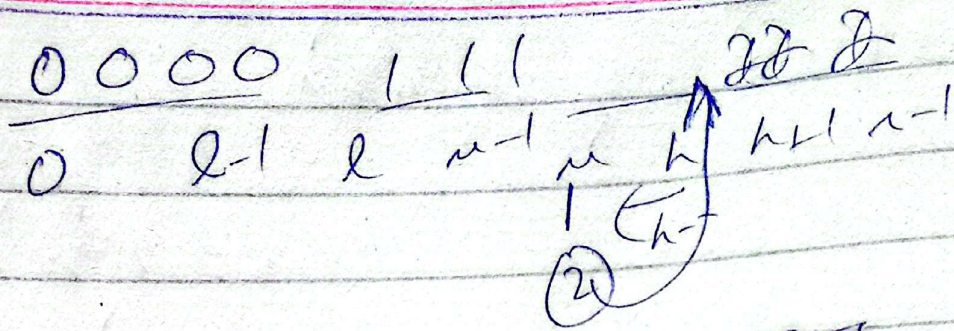
$\underline{0000} \quad \underline{111} \quad \underline{222}$
 $0 \quad l-1 \quad l \quad m-1 \quad m \quad h \quad m+1 \quad n-1$

~~0000~~

$\text{swap}(A[l], A[m])$
low++
mid++

$\underline{0000} \quad \underline{111} \quad \underline{222}$
 $0 \quad l-1 \quad l \quad m-1 \quad m \quad h \quad m+1 \quad n-1$
 mid++

mid++



swap($A[h], A[n]$)
 $h--;$

Pseudocode

mid = 0, high = n-1, low = 0

while (mid <= high) {

if ($A[mid] == 0$)

swap($A[low], A[mid]$)
 mid++, low++

else if ($A[mid] == 1$) mid++

else

swap($A[high], A[mid]$)
 high--

}