

Count Inversion Problem

arr = {6, 3, 5, 2, 7}
1, 1, 1, 1, 1 = 5

Pairs (arr[i], arr[j])

① $i < j$

② $arr[i] > arr[j]$

Brute Force Approach

Check all the possible pairs

```
for (i = 0 to n) {  
  for (j = i + 1 to n; j++) {  
    if (arr[i] > arr[j])
```

invcnt++

} } ANS = 5

T.C = $O(n^2)$

Optimal Approach (Merge Sort)

arr = {1, 3, 5, 10, 2, 6, 8, 9}

[1 | 3 | 5 | 10]

[2 | 6 | 8 | 9]

[1 | 2 | 3 | 5 | 6 | 8 | 9 | 10]

Inversion
Counts

if (arr[i] < arr[j])

swap = arr[i]

else \rightarrow arr[i] > arr[j]

invCount += (mid - i + 1)

invCount = {0 + 3 + 1 + 1 + 1} \rightarrow (6)

Changes to be done in the Merge logic
in Merge step

Use a variable invCount = 0

In else part \rightarrow invCount += (mid - i + 1)
return invCount

In the mergesort — main part.

① — leftCount

② — rightCount

Total = LC + RC + invCount

T.C = $O(n \log n)$

S.C = $O(1)$