

Painter's Partition Problem

Given are N boards of length of each given in the form of array, and M painters, such that each painter takes 1 unit of time to paint 1 unit of the board.

The task is to find the **minimum time** to paint all boards under the constraints that any painter will only paint continuous sections of boards

Painter's Partition Problem

arr = [40, 30, 10, 20] $M=2$ Time to Paint = ?

$$P_1 = 40$$

$$P_2 = 60 \rightarrow 60$$

→ Paint
(Minimum)

$$P_1 = 70$$

$$P_2 = 30 \rightarrow 70$$

$$P_1 = 80$$

$$P_2 = 20 \rightarrow 80$$

[40, 30, 10, 20]

min(max(board lengths))



40

max =

Sum(board lengths)



50, 60, 70, 80, 90, 100

[min start]

54

62

$$mid = st + \frac{e-s}{2}$$

[max end]

mid

Not possible

Possible — left side

$$70 = 40 + 30$$

$$end = mid - 1$$

left side — 54



—

Right side

$$st = mid + 1$$

62

Pseudocode

st = max(arr) end = sum(arr) ans = -1

while (start <= end) {

 mid = st + (e - s / 2)

 if (IsPossible(mid)) → left

 ans = mid

 end = mid - 1

 else — Right

 st = mid + 1

 }

 return ans

}

max-allowed

bool IsPossible(arr[], n, m, mid) {

 pointers = 1, time = 0

 for (i = 0; i < n; i++) {

 if (time + arr[i] <= max Allowed Time)

 time += arr[i]

 else {

 pointer++

 time = arr[i]

 }