

Binary Number System

Binary Number System is the most important number system in the context of computer.

Number System

In the Number System, we generally have the numbers on the basis of which we perform the calculations.

Decimal \rightarrow 0-9 Dec (Base 10)
10 dig 10

Binary \rightarrow 0-1 Binary (Base 2)
2 dig 2

Octal \rightarrow 0-7 Octal (Base 8)
8 dig 8

Hexadecimal \rightarrow 0-15 Hexa (Base 16)
0-9-A,B,C,D,E,F decimal 16
10,11,12,13,14,15

Conversions

① \rightarrow Decimal to Binary | Binary to Decimal

For Example

42

$$\begin{array}{r|l} 2 & 42 \\ \hline 2 & 21-0 \\ 2 & 10-1 \\ 2 & 5-0 \\ 2 & 2-1 \\ 2 & 1-0 \end{array}$$

(101010)₂

(101010)₂

$$\begin{array}{cccccc} 5 & 4 & 3 & 2 & 1 & 0 \\ 2^5 & 2^4 & 2^3 & 2^2 & 2^1 & 2^0 \end{array}$$

$$32 + 16 + 8 + 4 + 2 + 1$$

check which one is ON/OFF

OR

$$1 \times 32 + 0 \times 16 + 1 \times 8 + 0 \times 4 +$$

$$1 \times 2 + 1 \times 0$$

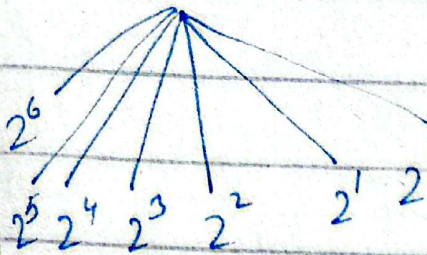
$$= 32 + 8 + 2$$

42

m

A simple logic for Binary Conversion as well.

$$42 - 32 = 10 - 8 = 2 - 2 = 0$$



As we know some spaces will be occupied by it

64 32 16 8 4 2 1

89 ✓ 89 ✓ 89 ✓ 0

1 0 1 0

→ (101010)₂

Can be verified as well.

Code logic

Decimal to Binary

decNum

ans = 0 → Binary Number

pow = 1 → 10⁰ → 10¹ → 10² → 10³

while (decNum > 0) {

rem = decNum % 2

decNum = decNum / 2

ans += (rem * pow)

pow = pow * 10

}
ans

Binary to Decimal

binum = binary Number given

ans = 0

pow = 1/2⁰

while (binum > 0) {

rem = binum % 10

ans += binum * pow

binum /= 10

pow *= 2

}
ans

Two's Complement

As we know int takes 4 bytes

- int \rightarrow 4 bytes \rightarrow 8 bits = 1 byte \rightarrow 32 bits.

$$\text{int } n = 10 \rightarrow (1010)_2$$

In memory

32 bits (Allocated)
In case of +ve number \rightarrow 1010

$$\text{int } n = -10$$

In the backend

① Binary

$$10 = (1010)$$

② Prefix with a zero

01010

↓

Most (MS)
Significant

MS $\rightarrow 0 \rightarrow +ve$
 $\rightarrow 1 \rightarrow -ve$

③ 1's Complement

$$0 \rightarrow 1 \quad 1 \rightarrow 0$$

01010

10101

④ Now Added 1

10101

$$\begin{array}{r} 10101 \\ + 1 \\ \hline (10110)_2 \end{array}$$

Final form
to be stored

$$(10110)_2$$

Now, we must know that the particular binary form is of a negative number.

So,

10110

① 1's Complement

01001

0(1001)

↳ Extracting it as it represents the direction.

01001

+1

01010

$$0(1010) \rightarrow (10)_{10}$$

$$(-10)_{10}$$