# Information Retrieval

IR basics Boolean search, Inverted index



#### IR in 1680

- Which plays of Shakespeare contain the words:
  - Brutus AND Caesar but NOT Calpurnia
- One could grep all of Shakespeare's plays for Brutus and Caesar, then strip out lines containing Calpurnia?



#### IR in 1680

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  - grep Brutus shakespeare.txt 0.123s
  - grep Caesar shakespeare.txt 0.112s
  - grep -v Calpurnia shakespeare.txt 0.184s
  - wc shakespeare.txt
  - 124456 901325 5458199 shakespeare.txt



#### IR in 1680

- Which plays of Shakespeare contain the words:
  - Brutus AND Caesar but NOT Calpurnia
- One could grep all of Shakespeare's plays for Brutus and Caesar, then strip out lines containing Calpurnia?
- Why is that not the answer?
  - Slow (for large corpora)
  - NOT Calpurnia is non-trivial
  - Other operations (e.g., find the word Romans near countrymen) are not feasible
  - Can't do ranked retrieval (best documents to return)



# Term-document incidence

	<b>Antony and Cleopatra</b>	Julius Caesar	The Tempest	Hamlet	Othello	Macbeth
Antony	1	1	0	0	0	1
Brutus	1	1	0	1	0	0
Caesar	1	1	0	1	1	1
Calpurnia	0	1	0	0	0	0
Cleopatra	1	0	0	0	0	0
mercy	1	0	1	1	1	1
worser	1	0	1	1	1	0
			1 if play c			



### Incidence vectors

- ❖ So, we have a 0/1 vector for each term.
- To answer the query?
  - Brutus AND Caesar but NOT Calpurnia
- Bitwise AND OF the vectors for Brutus (110100), Caesar (110111), and Calpurnia (complemented=101111)
  - 110100 AND 110111 AND 101111 = 100100.



### Term-document incidence

#### Brutus AND Caesar AND (NOT Calpurnia)

	Antony and C	leopatra	Julius Caesar	The Tempest	Hamlet	Othello	Macbeth
Antony	1	_	1	0	0	0	1
Brutus	1		1	0	1	0	0
Caesar	1		1	0	1	1	1
NOT Calpurn	nia 1		0	1	1	1	1
Cleopatra	1		0	0	0	0	0
mercy	1		0	1	1	1	1
worser	1		0	1	1	1	0

110100 AND 110111 AND 101111 = 100100.



# **Answers to query**

- Antony and Cleopatra, Act III, Scene ii
  - Agrippa [Aside to DOMITIUS ENOBARBUS]:
     Why, Enobarbus, when Antony found Julius Caesar dead he cried, almost to roaring;
     and he wept when at Philippi he found Brutus slain.
- Hamlet, Act III, Scene ii
  - Lord Polonius:

I did enact Julius Caesar I was killed in the Capitol; Brutus killed me.





# Bigger collections

- Consider N = 1 million documents, each with about 1000 words.
- Avg 6 bytes/word including spaces/punctuation
  - 6GB of data in the documents.
- $\Rightarrow$  Say there are M = 500K distinct terms among these.



### Can't build the matrix

❖ 500K x 1M matrix has half-a-billion 0's and 1's.

❖ But it has no more than one thousand million 1's.





### Can't build the matrix

- ❖ 500K x 1M matrix has half-a-trillion 0's and 1's.
- ❖ But it has no more than one thousand million 1's.



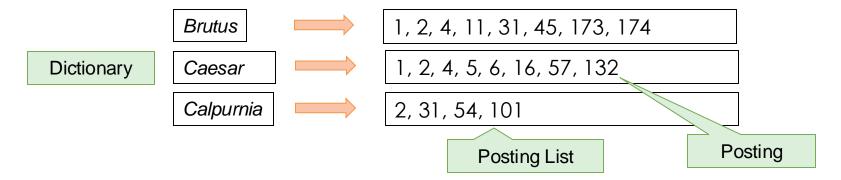
- The matrix is extremely sparse! what's a better representation?
  - Record only the "1" positions.

Inverted index



#### **Inverted index**

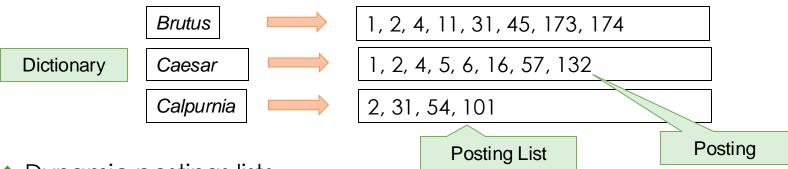
- $\diamond$  For each term  $t_i$ , we must store a list of all documents that contain  $t_i$ .
  - Identify each by a docID, a document serial number





#### Inverted index

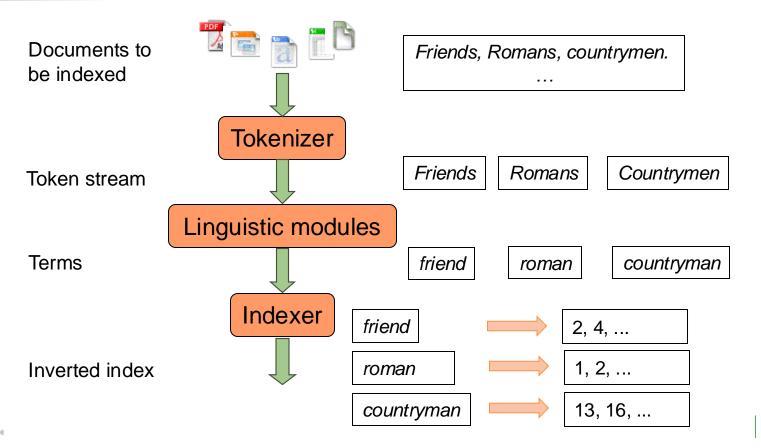
- $\diamond$  For each term  $t_i$ , we must store a list of all documents that contain  $t_i$ .
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- Dynamic postings lists
  - On disk, a continuous run of postings
    - E.g., comma-separated in a text file
  - In memory, linked lists or variable-length arrays
    - Some tradeoffs in size/ease of insertion

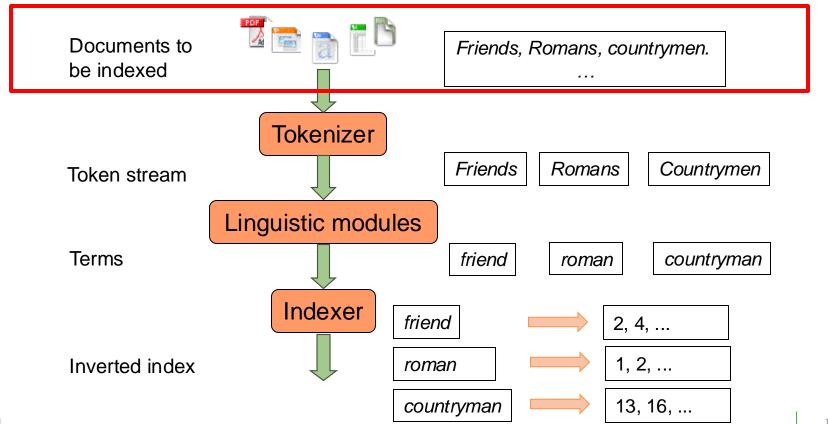


### Inverted index construction





### Inverted index construction



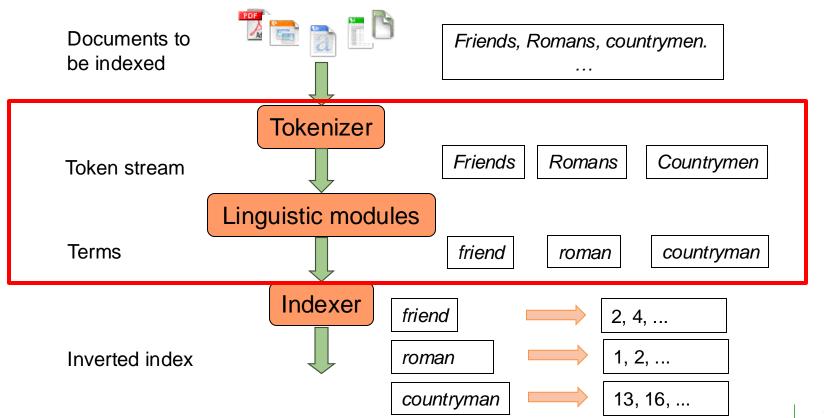


#### **Documents**

- What is a unit document?
  - A file?
  - Documents within a file? (e.g. XML, CSV)
  - An email? (Perhaps one of many in a single mbox file)
    - What about an email with 5 attachments?
  - A group of files (e.g., PPT or LaTeX split over HTML pages)
- What format is it in?
  - pdf/word/excel/html?
- What language is it in?
- What character set is in use?



### Inverted index construction





# Initial stages of text processing

#### Tokenization

- Cut character sequence into word tokens
  - Deal with "John's", a state-of-the-art solution

#### Normalization

- Map text and query term to same form
  - You want U.S.A. and USA to match

#### Stemming

- We may wish different forms of a root to match
  - authorize, authorization

#### Stop words

- We may omit very common words (or not)
  - the, a, to, of



### idea

- Replace next slides by naïve algorithm
- Discuss limitations
- Present alternative



# Indexer steps: Token sequence

#### Sequence of pairs

- (Modified token, Document ID)

#### Doc 1

I did enact Julius Caesar I was killed i' the Capitol; Brutus killed me.

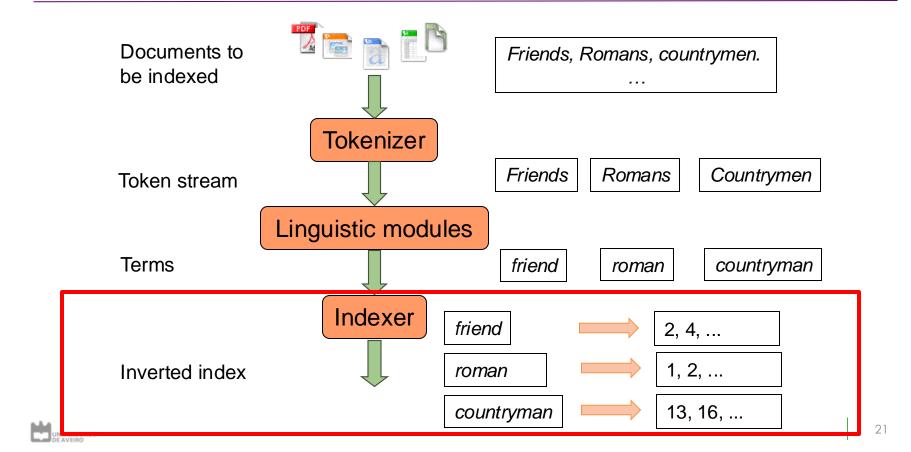
#### Doc 2

So let it be with Caesar. The noble Brutus hath told you Caesar was ambitious

Term	docID
I	1
did	1
enact	1
julius	1
caesar	1
l	1
was	1
killed	1
l'	1
the	1
capitol	1
brutus	1
killed	1
me	1
so	2
let	2
it	2
be	2
with	2
caesar	2
the	2
noble	2
brutus	2
hath	2
told	2
you	2
caesar	2
was	2
ambitious	2



### Inverted index construction



# **Indexer steps: Sort**

- Sort by terms
  - And then docID

Core indexing step

1	1
did	1
enact	1
julius	1
caesar	1
I	1
was	1
killed	1
i'	1
the	1
capitol	1
brutus	1
killed	1
me	1
so	2
let	2
it	2 2 2 2
be	2
with	2
caesar	2
the	2
noble	2
brutus	2
hath	2
told	2
you	2 2 2 2
caesar	2
was	2
ambitious	2

Term	docID
ambitious	2
be	2
brutus	1
brutus	2
capitol	1
caesar	1 1 2 2 1 1
caesar	2
caesar	2
did	1
enact	1
hath	1
I	1
I	1
i'	1
it	2
julius	1
killed	1
killed	1
let	2
me	1
noble	2
so	2
the	1
the	2
told	2
you	2
was	2 1 2 2 1 2 2 2 2 1 1 2 2 2 2 2 2 2 2 2
was	2
with	2



# Indexer steps: Sort

- Sort by terms
  - And then docID



- Need to keep information for a given term together
- Avoid changing / rewriting index on disk

Term	docID
I	1
did	1
enact	1
julius	1
caesar	1
1	1
was	1
killed	1
i'	1
the	1
capitol	1
brutus	1
killed	1
me	1
so	2
let	2
it	2
be	2
with	2
caesar	2
the	2
noble	2
brutus	2
hath	2
told	2
you	1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
caesar	2
was	2
ambitious	2

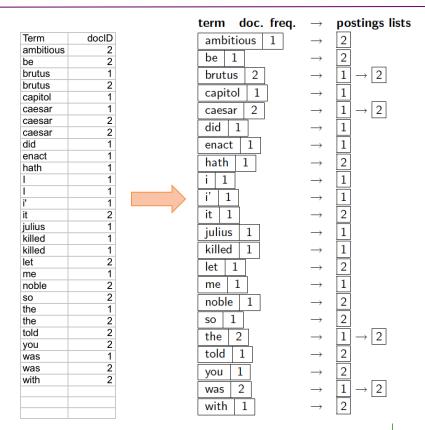




# Indexer steps: Dictionary & Postings

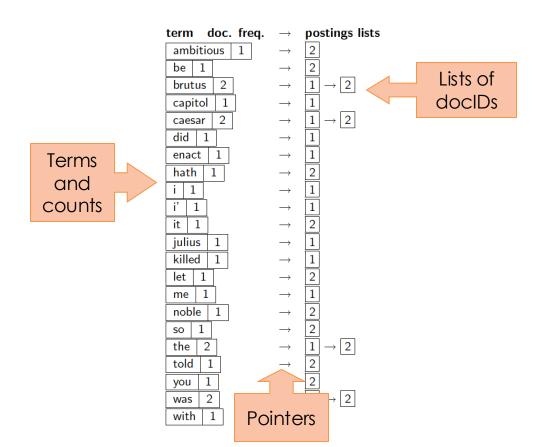
- Multiple term entries in a single document are merged.
- Split into Dictionary and Postings
- Doc. frequency information is added.







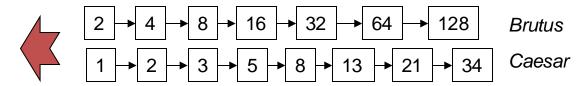
# Where do we pay in storage?





# **Query processing: AND**

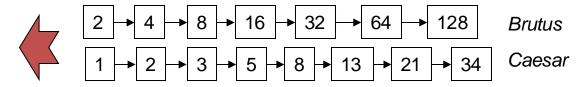
- Consider processing the query:
  - Brutus AND Caesar
- Locate Brutus in the Dictionary and retrieve its postings.
- Locate Caesar in the Dictionary and retrieve its postings.
- "Merge" the two postings:





# **Query processing: AND**

- Consider processing the query:
  - Brutus AND Caesar
- Locate Brutus in the Dictionary and retrieve its postings.
- Locate Caesar in the Dictionary and retrieve its postings.
- "Merge" the two postings:



- Walk through the two postings simultaneously, in time linear in the total number of posting entries
- If the list lengths are x and y, the merge takes O(x+y) operations.
  - Crucial: postings sorted by docID.



## Merge algorithm

```
INTERSECT(p_1, p_2)
 1 answer \leftarrow \langle \rangle
 2 while p_1 \neq \text{NIL} and p_2 \neq \text{NIL}
     do if doclD(p_1) = doclD(p_2)
             then ADD(answer, doclD(p_1))
 5
                    p_1 \leftarrow next(p_1)
                    p_2 \leftarrow next(p_2)
             else if doclD(p_1) < doclD(p_2)
                       then p_1 \leftarrow next(p_1)
 8
 9
                       else p_2 \leftarrow next(p_2)
10
      return answer
```



### Boolean queries: Exact match

- The Boolean retrieval model is being able to ask a query that is a Boolean expression:
  - Boolean Queries are queries using AND, OR and NOT to join query terms
    - Views each document as a set of words
    - Is precise: document matches condition or not.
  - Perhaps the simplest model to build an IR system
- Primary commercial retrieval tool
  - Email, library catalog, Mac OS X Spotlight



# Boolean queries: More general merges

#### Exercise:

- Adapt the merge for the queries:
  - Brutus AND NOT Caesar
  - Brutus OR NOT Caesar
- Can we still run through the merge in time O(x+y)?
- What can we achieve?



# Merging

- What about an arbitrary Boolean formula?
  - (Brutus OR Caesar) AND NOT
  - (Antony OR Cleopatra)
- Can we always merge in "linear" time?
  - Linear in what?
- Can we do better?



# **Query optimization**

- What is the best order for query processing?
- Consider a query that is an AND of n terms.
  - Brutus AND Calpurnia AND Caesar
- For each of the n terms, get its postings, then AND them together.

Brutus	1, 2, 4, 11, 31, 45, 173, 174
Caesar	1, 2, 4, 5, 6, 16, 57, 132
Calpurnia	2, 31, 54, 101



# **Query optimization**

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- Process in order of increasing frequency:
  - start with the smallest set, then keep cutting further.
    - This is why we kept document freq. in the dictionary



## More general optimization

- e.g., (madding OR crowd) AND (ignoble OR strife)
  - Get documents' frequencies (DF) for all terms.
  - Estimate the size of each OR by the sum of its DF(conservative).
  - Process in increasing order of OR sizes.

#### Exercise:

Recommend a query processing order for

(tangerine OR trees) AND (marmalade OR skies) AND (kaleidoscope OR eyes)

Term	Freq
eyes	213312
kaleidoscope	87009
marmalade	107913
skies	271658
tangerine	46653
trees	316812



### This lesson

- Boolean indexing and search
- Term-document matrix
- Inverted index
- Inverted index construction

