

The coefficients in potential at LO is collected to a matrix, i.e.,

$$\begin{array}{c}
 K^- p \quad \Sigma^+ \pi^- \quad \Sigma^0 \pi^0 \quad \bar{K}^0 n \quad \Sigma^- \pi^+ \quad \Lambda \pi^0 \\
 \begin{pmatrix}
 K^- p \\
 \Sigma^+ \pi^- \\
 \Sigma^0 \pi^0 \\
 \bar{K}^0 n \\
 \Sigma^- \pi^+ \\
 \Lambda \pi^0
 \end{pmatrix}
 \begin{pmatrix}
 2 & 1 & \frac{1}{2} & 1 & 0 & \frac{\sqrt{3}}{2} \\
 1 & 2 & 2 & 0 & 0 & 0 \\
 \frac{1}{2} & 2 & 0 & \frac{1}{2} & 2 & 0 \\
 1 & 0 & \frac{1}{2} & 2 & 1 & -\frac{\sqrt{3}}{2} \\
 0 & 0 & 2 & 1 & 2 & 0 \\
 \frac{\sqrt{3}}{2} & 0 & 0 & -\frac{\sqrt{3}}{2} & 0 & 0
 \end{pmatrix}
 \end{array} \quad (1)$$

The  $D_{ij}$  and  $L_{ij}$  in the NLO potential are given by

$$\begin{array}{c}
 K^- p \quad \Sigma^+ \pi^- \quad \Sigma^0 \pi^0 \quad \bar{K}^0 n \quad \Sigma^- \pi^+ \quad \Lambda \pi^0 \\
 \begin{pmatrix}
 K^- p \\
 \Sigma^+ \pi^- \\
 \Sigma^0 \pi^0 \\
 \bar{K}^0 n \\
 \Sigma^- \pi^+ \\
 \Lambda \pi^0
 \end{pmatrix}
 \begin{pmatrix}
 4(b_0 + b_D)m_K^2 & (b_D - b_F)\mu_1^2 & \frac{(b_D - b_F)\mu_1^2}{2} & 2(b_D + b_F)m_K^2 & 0 & -\frac{(b_D + 3b_F)\mu_1^2}{2\sqrt{3}} \\
 (b_D - b_F)\mu_1^2 & 4(b_0 + b_D)m_\pi^2 & 0 & 0 & 0 & 0 \\
 \frac{(b_D - b_F)\mu_1^2}{2} & 0 & 4(b_0 + b_D)m_\pi^2 & \frac{(b_D - b_F)\mu_1^2}{2} & 0 & 0 \\
 2(b_D + b_F)m_K^2 & 0 & \frac{(b_D - b_F)\mu_1^2}{2} & 4(b_0 + b_D)m_K^2 & (b_D - b_F)\mu_1^2 & \frac{(b_D + 3b_F)\mu_1^2}{2\sqrt{3}} \\
 0 & 0 & 0 & (b_D - b_F)\mu_1^2 & 4(b_0 + b_D)m_\pi^2 & 0 \\
 -\frac{(b_D + 3b_F)\mu_1^2}{2\sqrt{3}} & 0 & 0 & \frac{(b_D + 3b_F)\mu_1^2}{2\sqrt{3}} & 0 & \frac{4(3b_0 + b_D)m_\pi^2}{3}
 \end{pmatrix}
 \end{array} \quad (2)$$

and,

$$\begin{array}{c}
 K^- p \quad \Sigma^+ \pi^- \quad \Sigma^0 \pi^0 \quad \bar{K}^0 n \quad \Sigma^- \pi^+ \quad \Lambda \pi^0 \\
 \begin{pmatrix}
 K^- p \\
 \Sigma^+ \pi^- \\
 \Sigma^0 \pi^0 \\
 \bar{K}^0 n \\
 \Sigma^- \pi^+ \\
 \Lambda \pi^0
 \end{pmatrix}
 \begin{pmatrix}
 2d_2 + d_3 + 2d_4 & -d_1 + d_2 + d_3 & \frac{-d_1 - d_2 + 2d_3}{2} & d_1 + d_2 + d_3 & -2d_2 + d_3 & \frac{-\sqrt{3}(d_1 + d_2)}{2} \\
 -d_1 + d_2 + d_3 & 2d_2 + d_3 + 2d_4 & -2d_2 + d_3 & -2d_2 + d_3 & -4d_2 + 2d_3 & 0 \\
 \frac{-d_1 - d_2 + 2d_3}{2} & -2d_2 + d_3 & 2(d_3 + d_4) & \frac{-d_1 - d_2 + 2d_3}{2} & -2d_2 + d_3 & 0 \\
 d_1 + d_2 + d_3 & -2d_2 + d_3 & \frac{-d_1 - d_2 + 2d_3}{2} & 2d_2 + d_3 + 2d_4 & -d_1 + d_2 + d_3 & \frac{-\sqrt{3}(d_1 + d_2)}{2} \\
 -2d_2 + d_3 & -4d_2 + 2d_3 & -2d_2 + d_3 & -d_1 + d_2 + d_3 & 2d_2 + d_3 + 2d_4 & 0 \\
 \frac{-\sqrt{3}(d_1 + d_2)}{2} & 0 & 0 & \frac{-\sqrt{3}(d_1 + d_2)}{2} & 0 & 2d_4
 \end{pmatrix}
 \end{array} \quad (3)$$