# Package 'CMDMeasure'

# February 9, 2018

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| Title Conditional Mean Dependence Measures via Energy Statistics  |
| Version 1.0.0   |
| Date 2018-01-30   |
| <b>Description</b> Implementation of conditional mean dependence measures and conditional mean independence tests in Shao, X., and Zhang, J. (2014) <a href="https://doi.org/10.1080/01621459.2014.887012">doi:10.1080/01621459.2014.887012</a> and Park, T., et al. (2015) <a href="https://doi.org/10.1214/15-EJS1047">doi:10.1214/15-EJS1047</a> . |
| <b>Depends</b> R (>= 3.4.0)   |
| <b>Suggests</b> testthat (>= 2.0.0), energy (>= 1.7-0)  |
| License GPL (>= 2)  |
| LazyData true   |
| RoxygenNote 6.0.1   |
| Collate 'CMDMeasure-package.R' 'functions.R' 'cmdm.R' 'cmdm_test.R'   |
| R topics documented:  |
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| CMDMeasure-package Conditional Mean Dependence Measures via Energy Statistics   |
| Description   |

CMDMeasure: A package for mutual dependence measures via energy statistics

## **Details**

The CMDMeasure package provides measures of conditional mean dependence and tests of conditional mean independence.

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#### Measuring conditional mean dependence

The conditional mean dependence measures include:

- asymmetric measure  $\mathcal{R}_n$  based on distance covariance  $\mathcal{V}_n$
- symmetric measure  $\mathcal{S}_n$  based on distance covariance  $\mathcal{V}_n$
- complete measure  $Q_n$  based on complete V-statistics
- simplified complete measure  $\mathcal{Q}_n^{\star}$  based on incomplete V-statistics
- asymmetric measure  $\mathcal{J}_n$  based on complete measure  $\mathcal{Q}_n$
- simplified asymmetric measure  $\mathcal{J}_n^{\star}$  based on simplified complete measure  $\mathcal{Q}_n^{\star}$
- symmetric measure  $\mathcal{I}_n$  based on complete measure  $\mathcal{Q}_n$
- simplified symmetric measure  $\mathcal{I}_n^\star$  based on simplified complete measure  $\mathcal{Q}_n^\star$

## Testing conditional mean independence

The conditional mean independence tests based on the conditional mean dependence measures are implemented as permutation tests.

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```

MDD

Mutual Dependence Measures

## **Description**

cmdm measures mutual dependence of all components in X, where each component contains one variable (univariate) or more variables (multivariate).

#### Usage

```
MDD(x, y)
```

## **Arguments**

| X | A matrix or data frame, where rows represent samples, and columns represent |
|---|---|
|   | variables.  |

y A matrix or data frame, where rows represent samples, and columns represent variables.

#### Value

cmdm returns a list including the following components:

stat The value of the mutual dependence measure.

dist The distances between all components from all samples.

MDD2

#### References

Shao, X., and Zhang, J. (2014). Martingale difference correlation and its use in high-dimensional variable screening. Journal of the American Statistical Association, 109(507), 1302-1318. https://arxiv.org/abs/1709.02532.

Park, T., Shao, X., and Yao, S. (2015). Partial martingale difference correlation. Electronic Journal of Statistics, 9(1), 1492-1517. https://arxiv.org/abs/1709.02532.

## **Examples**

```
# X, Y is a 10 x 3 matrix with 10 samples and 3 variables X <- matrix(rnorm(10 * 3), 10, 3) Y <- matrix(rnorm(10 * 3), 10, 3) # assume X = (X1, X2) where X1 is 1-dim, X2 is 2-dim MDD(X, Y)
```

MDD2

Mutual Dependence Measures

## **Description**

cmdm measures mutual dependence of all components in X, where each component contains one variable (univariate) or more variables (multivariate).

## Usage

```
MDD2(x, y)
```

### **Arguments**

x A matrix or data frame, where rows represent samples, and columns represent

y A matrix or data frame, where rows represent samples, and columns represent variables.

## Value

cmdm returns a list including the following components:

stat The value of the mutual dependence measure.

dist The distances between all components from all samples.

#### References

Shao, X., and Zhang, J. (2014). Martingale difference correlation and its use in high-dimensional variable screening. Journal of the American Statistical Association, 109(507), 1302-1318. https://arxiv.org/abs/1709.02532.

Park, T., Shao, X., and Yao, S. (2015). Partial martingale difference correlation. Electronic Journal of Statistics, 9(1), 1492-1517. https://arxiv.org/abs/1709.02532.

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## Examples

```
# X, Y is a 10 x 3 matrix with 10 samples and 3 variables X <- matrix(rnorm(10 * 3), 10, 3) Y <- matrix(rnorm(10 * 3), 10, 3) # assume X = (X1, X2) where X1 is 1-dim, X2 is 2-dim MDD(X, Y)
```

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