# Package 'MDMICA'

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Title Independent Component Analysis via Mutual Dependence Measures
Version 1.0.0
<b>Date</b> 2018-01-30
<b>Description</b> Implementation of independent component analysis methods based on mutual dependence measures in Jin, Z., and Matteson, D. S. (2017) <a href="https://arxiv.org/abs/1709.02532">https://arxiv.org/abs/1709.02532</a> and Pfister, N., et al. (2018) <a href="https://arxiv.org/abs/1709.02532">doi:10.1111/rssb.12235</a> .
<b>Depends</b> R (>= $3.4.0$ )
Imports energy (>= 1.7-0), MDMeasure (>= 1.0.0), dHSIC (>= 2.0), rBayesianOptimization (>= 1.1.0)
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Collate 'MDMICA-package.R' 'functions.R' 'mdm_ica.R'
R topics documented:
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MDMICA-package Independent Component Analysis via Mutual Dependence Measures
Description

MDMICA: A package for independent component analysis via mutual dependence measures

# **Details**

The MDMICA package provides independent component analysis methods based on mutual dependence measures.

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#### Applying mutual dependence measures

The mutual dependence measures include:

- · distance-based energy statistics
  - asymmetric measure  $\mathcal{R}_n$  based on distance covariance  $\mathcal{V}_n$
  - symmetric measure  $S_n$  based on distance covariance  $V_n$
  - simplified complete measure  $\mathcal{Q}_n^{\star}$  based on incomplete V-statistics
- · kernel-based maximum mean discrepancies
  - d-variable Hilbert–Schmidt independence criterion dHSIC<sub>n</sub> based on Hilbert–Schmidt independence criterion HSIC<sub>n</sub>

#### **Initializing local optimization methods**

The initialization methods include:

- Latin hypercube sampling
- Bayesian optimization

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 $mdm\_ica$ 

Independent Component Analysis via Mutual Dependence Measures

# **Description**

mdm\_ica performs independent component analysis by minimizing mutual dependence measures of all univariate components in X.

# Usage

```
mdm_ica(X, num_lhs = NULL, mdm_type = "comp", num_bo = NULL,
    kernel = "exp", opt_algo = "par")
```

#### **Arguments**

X A matrix or data frame, where rows represent samples, and columns represent components.

num\_lhs The number of points generated by Latin hypercube sampling. If omitted, an adaptive number is used.

mdm\_type The type of mutual dependence measures, including

- asymmetric measure  $\mathcal{R}_n$  based on distance covariance  $\mathcal{V}_n$ ;
- sym: symmectric measure  $S_n$  based on distance covariance  $V_n$ ;
- comp: simplified complete measure  $Q_n^*$  based on incomplete V-statistics;
- dhsic: d-variable Hilbert–Schmidt independence criterion dHSIC<sub>n</sub> based on Hilbert–Schmidt independence criterion HSIC<sub>n</sub>.

num\_bo The number of points evaluated by Bayesian optimization.

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kernel The kernel of the underlying Gaussian process in Bayesian optimization, including

- exp: squared exponential kernel;
- mat: Matern 5/2 kernel.

opt\_algo The algorithm of optimization, including

- def: deflation algorithm, where the components are extracted one at a time;
- par: parallel algorithm, where the components are extracted simultaneously.

#### Value

mdm\_ica returns a list including the following components:

theta The rotation angles of the estimated unmixing matrix.

W The estimated unmixing matrix.

obj The objective value of the estimated independence components.

S The estimated independence components.

#### References

Jin, Z., and Matteson, D. S. (2017). Generalizing Distance Covariance to Measure and Test Multivariate Mutual Dependence. arXiv preprint arXiv:1709.02532. https://arxiv.org/abs/1709.02532.

Pfister, N., et al. (2018). Kernel-based tests for joint independence. Journal of the Royal Statistical Society: Series B (Statistical Methodology), 80(1), 5-31. http://dx.doi.org/10.1111/rssb. 12235.

# **Examples**

```
# X is a 10 x 3 matrix with 10 samples and 3 components
X <- matrix(rnorm(10 * 3), 10, 3)

# deflation algorithm
mdm_ica(X, mdm_type = "asym", opt_algo = "def")
# parallel algorithm
mdm_ica(X, mdm_type = "asym", opt_algo = "par")

## Not run:
# bayesian optimization with exponential kernel
mdm_ica(X, mdm_type = "sym", num_bo = 1, kernel = "exp", opt_algo = "par")
# bayesian optimization with matern kernel
mdm_ica(X, mdm_type = "comp", num_bo = 1, kernel = "mat", opt_algo = "par")
## End(Not run)</pre>
```

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