

COM 530500 Network Science Final Project

December 23, 2021

Institute of Communications Engineering National Tsing Hua University





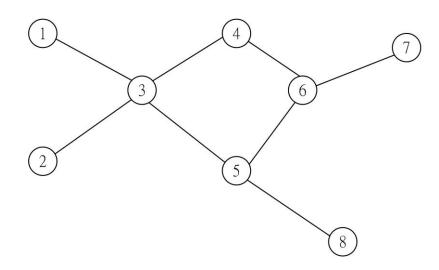
- Final Exam: Jan. 10, 2022
- Project Due: Jan. 20, 2022



Independent Cascade Model (1/7)



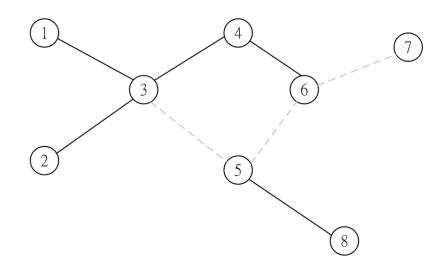
Given: adjacency matrix A, transition probability ϕ , a set of seed nodes S, and distance D.



Independent Cascade Model (2/7)



Step 1: Obtain \tilde{A} by removing edges of A, where each edge is removed with probability $1 - \phi$.



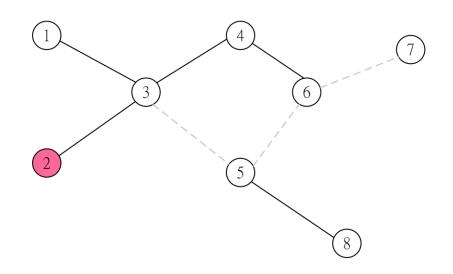
Independent Cascade Model (3/7)



Step 2: Define the $n \times 1$ seed vector x by

$$x_i = \begin{cases} 1, & \text{for } i \in S \\ 0, & \text{for } i \notin S \end{cases}$$

$$S = \{2\}$$

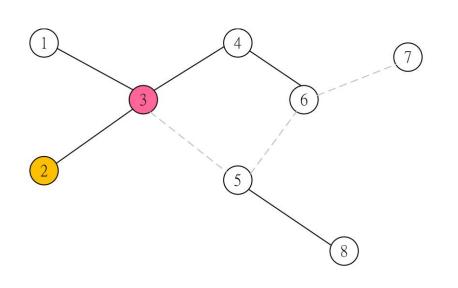


$$x = \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

Independent Cascade Model (4/7)



Step 3: Calculate $y = (\tilde{A} + I)^D x$ with the AND and the OR operations.



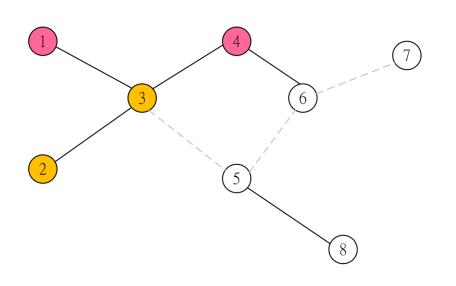
$$y = (\tilde{A} + I)x = \begin{bmatrix} 0 \\ 1 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

D=1

Independent Cascade Model (5/7)



Step 3: Calculate $y = (\tilde{A} + I)^D x$ with the AND and the OR operations.



$$D=2$$

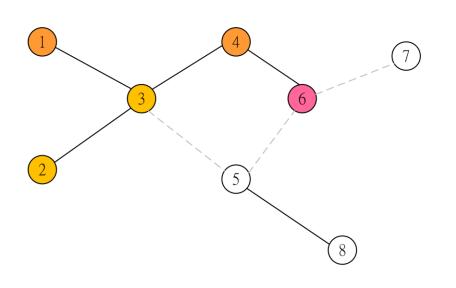
$$y = (\tilde{A} + I)^2 x = \begin{bmatrix} 1 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$



Independent Cascade Model (6/7)



Step 3: Calculate $y = (\tilde{A} + I)^D x$ with the AND and the OR operations.



$$D=3$$

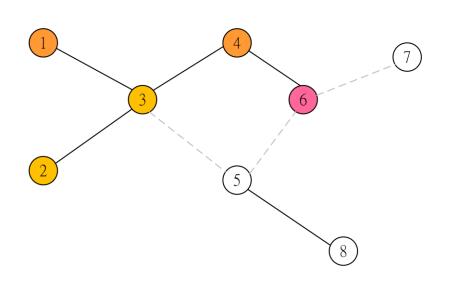
$$y = (\tilde{A} + I)^3 x = \begin{bmatrix} 1 \\ 1 \\ 0 \\ 1 \\ 0 \\ 0 \end{bmatrix}$$



Independent Cascade Model (7/7)



Step 4: Obtain the number of infected nodes by counting the number of 1's in vector y.



$$D = 3$$

$$y = \begin{bmatrix} 1\\1\\1\\0\\1\\0\\0 \end{bmatrix} \Rightarrow ||y||_1 = 5$$





Problem 1. (40%) Consider the **ego-Facebook** dataset. A node in this dataset represents a user on Facebook, and an edge between two nodes represents the relationship between two users.

- (a) (10%) List some statistical information of this dataset, such as the number of nodes, number of edges, average clustering coefficient, diameter, average degree, maximum degree, etc.
- (b) (10%) Visualize the dataset by plotting it.
- (c) (10%) Plot the degree distribution with log-log scale.
- (d) (10%) List the top 10 nodes ranked by the following centrality measures.
 - Degree centrality
 - Katz centrality
 - Eigenvector centrality
 - Betweenness centrality
 - Closeness centrality







Problem 2. (60%+bonus 10%) In this problem, we want to investigate the disease propagation by the independent cascade (IC) model in **ego-Facebook** [?] dataset. Assume the propagation probability is ϕ , and the set of seeds nodes S are randomly selected. Collect the set of infected nodes within the distance D of the seed nodes, and calculate the prevalence rate r_1 (which is defined by the ratio of the number of infected nodes to the total number of nodes). Set $\phi = 0.1, |S| = 5$, and D the diameter of the graph.







- (a) (40%) Simulate the disease propagation by IC model after removing the top 0%, 10%, 20%, ..., 50% of nodes from the following centrality measures respectively, and calculate the corresponding prevalence rate r_1 . Please plot the curves of r_1 vs. the percentage of nodes removed. (Note: Please run the simulation 100 times and average the results.)
 - Degree centrality
 - Katz centrality
 - Eigenvector centrality
 - Betweenness centrality
 - Closeness centrality
- (b) (bonus 10%) Could you find a centrality measure that achieves a better performance?
- (c) (20%) Write a report to compare and discuss the results of different centrality measures.



Summary (1/1)



Given: adjacency matrix A, transition probability ϕ , a set of seed nodes S, and distance D.

Step 1: Obtain A' by removing edges of A, where each edge is removed with probability $1 - \phi$.

Step *: Obtain \tilde{A} by removing some specific nodes and all their edges from A'.

Step 2: Define the $n \times 1$ seed vector x by $x_i = 1$ for $i \in S$ and $x_i = 0$ for $i \notin S$.

Step 3: Calculate $y = (\tilde{A} + I)^D x$ with the AND and the OR operations.

Step 4: Obtain the number of infected nodes by counting the number of 1's in vector y.

Step 5: Repeat **Step 1** to **Step 5** for 100 times, and average the results.

Step 6: Calculate the prevalence rate r_1 .

