APDE: **Charpit:** $F(p,q,u,x,y)=0$ with $u_x=p, u_y=q$. Then via $F_x, F_y, \& p_y=q_x \to p_\tau=-F_x-pF_u$, $q_\tau=-F_y-qF_u, u_\tau=pF_p+qF_q$. Also, $u0_s=p_0x0_s+q_0y0_s; F_0=0$. **Riemann:** $\int_D RLu-uL^*R=\int_D \partial_x\left(Ru_y+auR\right)+\partial_y\left(-uR_x+buR\right)=\int_{\partial D} dy\left(Ru_y+Rau\right)+dx\left(uR_x-buR\right)$. Expand over triangle going B-P-A (B at bottom right) $\to$ need $R_x=bR@y=\eta, R_y=aR@x=\xi, R(P)=1, L^*R=0$. **Canonical:** For $au_{xx}+2bu_{xy}+cu_{yy}=f$, we need Cauchy-Kowalevski s.t. first derivs defined: $x':=\frac{dx}{ds}$ s.t. on Γ $p_0'=x_0'u_{xx}+y_0'u_{xy}, q_0'=x_0'u_{xy}+y_0'u_{yy}$. Use these 3, solve det A!=0 s.t. $ay_0'^2-2bx_0'y_0'+cx_0'^2\neq 0$. Solve quadratic s.t. $b^2>ac\to h, b^2<ac\to e, b^2=ac\to p$. H: $\lambda_1,\lambda_2\to\xi,\eta$. E: $\lambda=\lambda_R\pm i\lambda_I; \lambda_R\to\xi, \lambda_I\to\eta$. P: $\lambda_1\to\xi$, choose η independent e.g. xy, x^2. **Green's Fn:** For $u_{xx}+u_{yy}+au_x+bu_y+cu=f$ we have $\int_D GLu-uL^*G=\int_D\left(u_xG\right)_x+\left(u_yG\right)_y-\left(uG_x\right)_x-\left(uG_y\right)_y+\left(auG\right)_x+\left(auG\right)_y=\int_D \boldsymbol{\nabla}\cdot\left(u_nG-uG_n\right)+\boldsymbol{\nabla}\cdot\left((a\,b)^T\hat{n}Gu\right)=\int_{\partial D}u_nG-uG_n+(a\,b)^T\hat{n}Gu=\int_{\partial D}-uG_n$.
SAM: **Dists:** Need linearity and continuity: $\exists N, C$ s.t. $|(u,\phi)|\leq C\sum_{m\leq N}\max_{in[-X,X]}|\phi^{(m)}|$