## **Electric Dipoles**

Analysing force and potential

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### **Important Equations**

$$W = F \cdot s \cdot \cos \theta \tag{1}$$

$$\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{Q_{source} q_{test}}{r^2} \hat{r} = \vec{E} q$$
 (2)

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} \hat{r} \left( V/m \right) \tag{3}$$

$$V = \frac{1}{4\pi\epsilon_0} \frac{Q}{r} \left( V \right) = \frac{W}{q} \tag{4}$$

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#### The Task



What is the:

- a) Force on a particle of charge q located at point  $\vec{P}$  on the x axis, as  $\vec{P}$  varies?
- b) Potential at point  $\vec{P}$  (if V at  $\infty = 0$ ) as  $\vec{P}$  varies?

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### a) The Force at $\vec{P}$

$$ec{\mathcal{E}_+} = rac{1}{4\pi\epsilon_0} rac{(+Q)}{r_+^2} \hat{r_+}$$

but we are only considering the x axis so:

$$ec{\mathcal{E}_+} = rac{1}{4\pi\epsilon_0}rac{Q}{r_+^2}\hat{x} \ 
ightarrow ec{\mathcal{F}_+} = rac{1}{4\pi\epsilon_0}rac{Qq}{r_+^2}\hat{x}$$

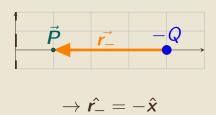
### a) The Force at $\vec{P}$

now for 
$$\vec{E}_{-}$$
:

$$\vec{E_-} = \frac{1}{4\pi\epsilon_0} \frac{(-Q)}{r_-^2} \hat{r_-}$$

 $\rightarrow$  where does  $\hat{r}_{-}$  point?

# a) The Force at $\vec{P}$



### a) The Force at $ec{P}$

so: 
$$\vec{E_{-}} = \frac{1}{4\pi\epsilon_0} \frac{(-Q)}{r_{-}^2} (-\hat{x})$$
 
$$\vec{E_{-}} = \frac{1}{4\pi\epsilon_0} \frac{Q}{r_{-}^2} \hat{x}$$
 
$$\rightarrow \vec{F_{-}} = \frac{1}{4\pi\epsilon_0} \frac{Qq}{r_{-}^2} \hat{x}$$

### The Force at $\vec{P}$

$$egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} rac{Qq}{4\pi\epsilon_0} \left(rac{1}{r_+^2} + rac{1}{r_-^2}
ight) \hat{m{x}} \left(m{N}
ight) \ &
eq 0 ext{ at origin!} \end{aligned}$$

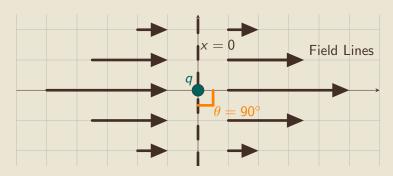
#### The Potential at $\vec{P}$

$$V_{+} = rac{1}{4\pi\epsilon_{0}} rac{(+Q)}{r_{+}} \qquad V_{-} = rac{1}{4\pi\epsilon_{0}} rac{(-Q)}{r_{-}}$$

#### The Potential at $\vec{P}$

$$V_{total}=V_{+}+V_{-}=rac{Q}{4\pi\epsilon_{0}}\left(rac{1}{r_{+}}-rac{1}{r_{-}}
ight)\;(V)$$
  $ightarrow$  is 0 at origin!

### Why Potential is 0 at the Origin



Recall that  $W = F \cdot s \cdot \cos \theta$ ; but here  $\cos \theta = \cos 90 = 0$ , so:

$$V = \frac{W}{q} = \frac{F \cdot s \cdot 0}{q} = 0 \text{ along } x = 0!$$