

# Fluxions, Forces, and Fields

*An overview of the mathematisation of physics in Europe through the modern period*

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Zella Baig

February 11, 2021

2021-02-11

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# A Look Back

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└─ A Look Back

A Look Back

- 'Modern' physics is clearly mathematical. . .

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$$\begin{aligned}\vec{\nabla} \cdot \vec{E} &= \frac{\rho}{\epsilon_0} & \vec{\nabla} \cdot \vec{B} &= 0 \\ \vec{\nabla} \times \vec{E} &= -\frac{\partial \vec{B}}{\partial t} & \vec{\nabla} \times \vec{B} &= \mu_0 \left( \vec{J} + \epsilon_0 \frac{\partial \vec{E}}{\partial t} \right)\end{aligned}$$

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- Or even more recent:

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└─ Mathematics in Modern Physics

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$$i\hbar \frac{\partial |\psi\rangle}{\partial t} = \hat{H} |\psi\rangle$$

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└ Mathematics in Modern Physics

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$$i\hbar \frac{\partial |\psi\rangle}{\partial t} = \hat{H} |\psi\rangle$$

- But this wasn't always the case

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└ Mathematics in Modern Physics

• But this wasn't always the case

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- The *expectation* (or even requirement) that a physicist be mathematically adept only arose  $\sim$  C20

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└ Mathematics in Modern Physics

- But this wasn't always the case
- The expectation (or even requirement) that a physicist be mathematically adept only arose  $\sim$  C20

1. Mathematics within science is a somewhat recent idea - experiment was key



- Vector notation had only been around for  $\sim 50$  years!

1. We will discuss vector notation later in fact

# Tracing Back

- Let's take a convenient starting point: Einstein, special relativity, & aether theory

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└ A Look Back

└ Tracing Back

1. No real reason, but more just commonly known as a 'big' event

Tracing Back

• Let's take a convenient starting point: Einstein, special relativity, & aether theory

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- Interestingly, much of the work on length contraction was done by George Fitzgerald, who was also influenced greatly by Maxwell

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1. So we can already begin to draw these links between these (famous) people

- Maxwell himself adept at maths - 2<sup>nd</sup> Wrangler

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└─ A Look Back

└─ Beyond Maxwell

Beyond Maxwell

- Maxwell himself adept at maths - 2<sup>nd</sup> Wrangler

1. Explain what wrangler means

- Maxwell himself adept at maths - 2<sup>nd</sup> Wrangler
- 'Mentored' by William Thomson<sup>2</sup> (later Lord Kelvin)...

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└ Beyond Maxwell

1. explain this was a professional/guiding relationship

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- Physics in Thomson's day had been centred around energy (and thus dynamics)...

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## Fluxions, Forces, and Fields

### └ A Look Back

### └ Beyond Maxwell

1. Mention how we will analyse why it was dynamics which dominated energy

Beyond Maxwell

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- Physics in Thomson's day had been centred around energy (and thus dynamics)...
- ... Which followed from continental development furthered by figures such as Lagrange and Laplace...
- ... Who worked using methods derived from Newton's work on celestial motion

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1. Mention how we can now see there's a clear line of succession, and we'll be looking at how each figure influenced the next

Of course, there are other overarching themes as well:

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└─ Not Just Mathematics

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└ A Look Back

└ Not Just Mathematics

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- Baconian ideals,

1. Explain what baconianism is - empiricism, collaboration, etc.  
Science was investigated. This leads on well to the next point

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- Baconian ideals,
- Collaborative bodies such as the Royal Institute,

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- Baconian ideals,
- Collaborative bodies such as the Royal Institute,
- And (again from Newton) *hypotheses non fingo*<sup>i</sup>

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# Pre-Newtonianism

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└ Pre-Newtonianism

Pre-Newtonianism



# Natural Philosophy Pre Early Modern Period

- 'Physics' (or Natural Philosophy) focused largely on astronomy
  - the “noblest of all” mathematical disciplines<sup>3</sup>

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<sup>3</sup>Clavius, 1612.

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## Fluxions, Forces, and Fields

### └ Pre-Newtonianism

### └ Natural Philosophy Pre Early Modern Period

1. Discuss how this doesn't imply stagnation, but merely shaped how the world was viewed as well as the approach to science

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## Fluxions, Forces, and Fields

### └ Pre-Newtonianism

### └ Natural Philosophy Pre Early Modern Period

1. It still was studied, and it was rigorous, but it wasn't a science and was almost a 'plaything'

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# Isaac Newton (1642-1727)

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Fluxions, Forces, and Fields  
└ Isaac Newton (1642-1727)

Isaac Newton (1642-1727)

- Saw God as mathematical, with a fondness for geometry<sup>ii</sup>

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<sup>ii</sup>Newton's piety would greatly influence his work

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Fluxions, Forces, and Fields

└ Isaac Newton (1642-1727)

└ Newtonian Mathematical Ideals

1. Mention how in his work he would often discuss god, and the ancients
2. also bring up how his physical work is but a portion of his alchemy and other work

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1. One major reason for this was the concept of force at a distance



- Saw God as mathematical, with a fondness for geometry<sup>ii</sup>
- Would have grown up with Cartesianism (deductive reasoning), but clashed with it later in life
- Sought 'elegance' in mathematics<sup>5</sup>

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1. As well as being haughty, he was also a very petty man - bring up removing 'esteemed' to 'mr'

- The method of resolution & composition:

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Fluxions, Forces, and Fields

└ Isaac Newton (1642-1727)

└ Experimental Philosophy

Experimental Philosophy

• The method of resolution & composition:

1. Mention how sometimes it appears as if Newton himself didn't know what he meant; conflicting uses

- The method of **resolution & composition**:
  1. Observe and “come to the general properties of things”<sup>6</sup>

---

<sup>6</sup>Newton and McGuire, 1970.

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- Nature able to be quantised (e.g. fluxional calculus & Halley’s Comet)

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## Fluxions, Forces, and Fields

└ Isaac Newton (1642-1727)

└ Experimental Philosophy

1. Discuss in detail - getting measurements from Flamsteed, the royal astronomer, and applying etc

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  - Concept of forces at a distance

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- Important to note the ramifications of geometric arguments

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## Fluxions, Forces, and Fields

└ Isaac Newton (1642-1727)

### └ Experimental Philosophy

1. Religious backing, make his work iron clad as to prevent arguments against it

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- Who discovered calculus first?

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└ Isaac Newton (1642-1727)

└ Gottfried Leibniz (1646-1716)

Gottfried Leibniz (1646-1716)

- Who discovered calculus first?

1. Newton discovered first, as he claims, but leibniz published first.  
Newton quarrels as usual

# Gottfried Leibniz (1646-1716)

- Who discovered calculus first?
- Leibnizian calculus seen as inelegant

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Gottfried Leibniz (1646-1716)

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1. Again newton preferring geometry, or perhaps to cover up that he had published later as he was perfecting it

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### Fluxions, Forces, and Fields

└ Isaac Newton (1642-1727)

└ Gottfried Leibniz (1646-1716)

1. Discuss fluxions (which are adding eg a small  $dt$  term), and fluents which are both integrals and derivatives of functions of time.  
Mention sloppy notation usage

- Who discovered calculus first?
- Leibnizian calculus seen as inelegant
- Some literature suggests Newton's notation might have impeded British science
  - *The Development of Newtonian Calculus*<sup>8</sup>
  - *Dot-Age*<sup>9</sup>
  - *The History of Calculus*<sup>10</sup>

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## Fluxions, Forces, and Fields

└ Isaac Newton (1642-1727)

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1. Discuss how this isn't likely the major factor, as the next head of the royal society was very anti newton

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- Regardless, we are interested in the **physical** influences of calculus

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## Fluxions, Forces, and Fields

└ Isaac Newton (1642-1727)

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1. Newton's calculus more influential simply for the scientific ramifications - his philosophy and the discovery of Halley's comet

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<sup>9</sup>Guicciardini, 2004.

<sup>10</sup>Boyer, 2012.

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Fluxions, Forces, and Fields

└ The Dynamical Age: Continental Physics

The Dynamical Age: Continental Physics

# The Dynamical Age: Continental Physics

# Putting Calculus to Use

- Euler, Clairaut, and others applied Newton's experimental philosophy<sup>11</sup> to various problems, gradually verifying several with observations

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<sup>11</sup>Shapiro, 2004.

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Fluxions, Forces, and Fields

└ The Dynamical Age: Continental Physics

└ Putting Calculus to Use

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# Putting Calculus to Use

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Fluxions, Forces, and Fields

└ The Dynamical Age: Continental Physics

└ Putting Calculus to Use

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  - Clairaut's work on the three-body problem particularly important

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  - Clairaut's work on the three-body problem particularly important

---

<sup>11</sup>Shapiro, 2004.

1. This showed that newton's work really was quite important - it had allowed for major work towards the problem which had stumped many other mathematicians. Lent credit to newton

# Putting Calculus to Use

- Euler, Clairaut, and others applied Newton's experimental philosophy<sup>11</sup> to various problems, gradually verifying several with observations
  - Clairaut's work on the three-body problem particularly important
- Development of Lagrangian mechanics & applications to further contexts (such as the motion of sound)

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## Fluxions, Forces, and Fields

### └ The Dynamical Age: Continental Physics

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- The rise of French scientific dominance

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Fluxions, Forces, and Fields

└ The Dynamical Age: Continental Physics

└ Laplacian Physics

Laplacian Physics

- The rise of French scientific dominance

1. Discuss napoleons upbringing - had laplace as a teacher, was fond of mathematics

- The rise of French scientific dominance
- Physics spearheaded by Laplace in early C19, who took an "astronomical view of nature"<sup>12</sup>

---

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- Prevalence of central-force based models, for even minute scales<sup>13</sup>

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<sup>12</sup>Merz, 1896.

<sup>13</sup>Fox, 1974.

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## Fluxions, Forces, and Fields

### └ The Dynamical Age: Continental Physics

#### └ Laplacian Physics

1. these had traditionally been the bread and butter of newtonian calculus

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## Fluxions, Forces, and Fields

### └ The Dynamical Age: Continental Physics

#### └ Laplacian Physics

1. Allowed for great development of ideas internationally

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- Development of light, heat, and electromagnetic theory with various contestants (e.g. Fourier) - via Laplacian methods

---

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Fluxions, Forces, and Fields

└ The Dynamical Age: Continental Physics

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# Energy Physics

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Fluxions, Forces, and Fields  
└─ Energy Physics

Energy Physics



## William Thomson (1824-1907)

- Ideas of *vis-viva* around since Leibniz, *caloric* furthered by e.g. Carnot in early C19

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Fluxions, Forces, and Fields

└ Energy Physics

└ William Thomson (1824-1907)

William Thomson (1824-1907)

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1. Energy ideas were floating around - it being created, being a fluid, etc

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- Natural philosophy shifted towards a focus on (conservation of) energy - in particular heat<sup>14</sup>

---

<sup>14</sup>Smith, 1978.

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Fluxions, Forces, and Fields

└ Energy Physics

└ William Thomson (1824-1907)

1. Many reasons for this - perhaps discuss steam engines, practical applications. Baconianism - applications of science to improving lives

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  - Appealing due to **all** physics being related (perhaps even dynamically!)

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<sup>14</sup>Smith, 1978.  
<sup>15</sup>Thomson, 1851.

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<sup>15</sup>Thomson, 1851.

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## Fluxions, Forces, and Fields

### └ Energy Physics

### └ William Thomson (1824-1907)

1. Thomson knew there was something relating heat and energy, investigated it

- Together, they publish *Treatise on Natural Philosophy*:<sup>16</sup> the first high-level **mathematically-inclined** physics textbook<sup>iii</sup>, as well as a synthesis of their work on energy

---

<sup>16</sup>Thomson and Tait, 1867.

<sup>iii</sup>In fact, 'energy' as a concept was not taught much *at all*

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Fluxions, Forces, and Fields

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# James Maxwell (1831-1879)

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Fluxions, Forces, and Fields

└ James Maxwell (1831-1879)

James Maxwell (1831-1879)



- Both mathematically inclined Scottish physicists (contrasting to e.g. Faraday)<sup>18</sup>

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<sup>18</sup>Gooding and James, 1985.

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Fluxions, Forces, and Fields

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1. Thomson busy with other pursuits, told to read on faraday as thomson (and the world) recognised his brilliance
2. faraday the opposite of a mathematician - almost all practical work, but amazing experimenter; give brief overview

- Both mathematically inclined Scottish physicists (contrasting to e.g. Faraday)<sup>18</sup>
- Thomson guided Maxwell's intellectual pursuits both directly and indirectly:
  - “The discussion of the various forms of energy . . . constitutes the whole of physical science”<sup>19</sup>

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<sup>18</sup>Gooding and James, 1985.

<sup>19</sup>Maxwell, 1877.

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## Fluxions, Forces, and Fields

└ James Maxwell (1831-1879)

└ Maxwell & Thomson

1. Quote from several years later but you can see how Thomson influenced Maxwell

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  - “The discussion of the various forms of energy . . . constitutes the whole of physical science”<sup>19</sup>
- On electromagnetism, pondered the nature of the 'store' of energy, e.g. in his *Dynamical Theory*<sup>20</sup>

---

<sup>18</sup>Gooding and James, 1985.

<sup>19</sup>Maxwell, 1877.

<sup>20</sup>Maxwell, 1865.

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## Fluxions, Forces, and Fields

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<sup>19</sup>Maxwell, 1877.

<sup>20</sup>Maxwell, 1865.

- Faraday had done groundbreaking work on electromagnetism, but almost entirely qualitative

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Fluxions, Forces, and Fields

└ James Maxwell (1831-1879)

└ Electromagnetism

Electromagnetism

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- Maxwell reticent to attribute any physical cause; *Faraday's Lines*<sup>21</sup> makes no claim of physicality

---

<sup>21</sup>Maxwell, 1856.

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## Fluxions, Forces, and Fields

└ James Maxwell (1831-1879)

└ Electromagnetism

1. Instead claims to be a mathematical model which he uses to develop Faraday's work

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- *Dynamical Theory* made little note of aether as it was mathematically unnecessary

---

<sup>21</sup>Maxwell, 1856.

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## Fluxions, Forces, and Fields

└ James Maxwell (1831-1879)

└ Electromagnetism

1. This was interesting given how much of a headache aether theory had caused EM models

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- *Physical Lines*<sup>22</sup> - first postulates light being electromagnetic, as well as displacement current

---

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<sup>23</sup>Maxwell, 1873.

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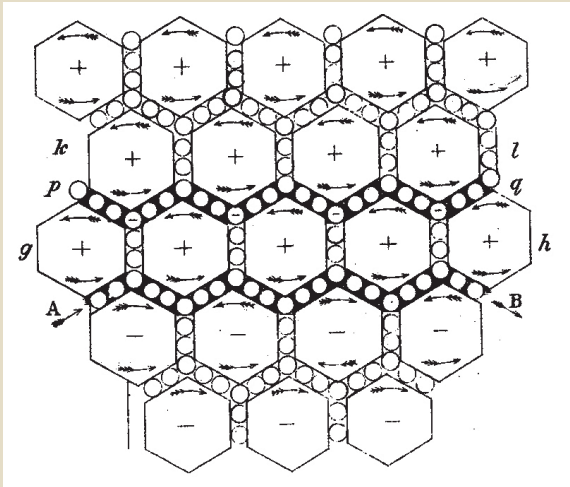
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<sup>23</sup>Maxwell, 1873.

# Vortex Model



**Figure 1:** Maxwell's 'vortex & idle-wheel' model, in *Physical Lines*

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Fluxions, Forces, and Fields  
└ James Maxwell (1831-1879)

└ Vortex Model

Vortex Model

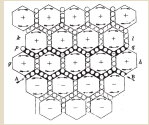


Figure 1: Maxwell's 'vortex & idle-wheel' model, in *Physical Lines*

1. Describe the motion of the wheels and current particles; explain how it led to the curl dependence

- Greatly develops vector calculus out of necessity for his mechanical models

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Fluxions, Forces, and Fields

└ James Maxwell (1831-1879)

└ Maxwell & Vectors

Maxwell & Vectors

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Fluxions, Forces, and Fields

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- Greatly develops ~~vector~~ calculus out of necessity for his mechanical models
- Modern formulation only introduced in 1884, by Heaviside<sup>24</sup>

---

<sup>24</sup>Hunt, 2012.

# Maxwell & Vectors

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## Fluxions, Forces, and Fields

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- Greatly develops ~~vector~~ calculus out of necessity for his mechanical models
- Modern formulation only introduced in 1884, by Heaviside<sup>24</sup>
  - From 20 equations to 4

---

<sup>24</sup>Hunt, 2012.

└ James Maxwell (1831-1879)

└ Maxwell & Vectors

1. Discuss how there were various other parameters each representing components of fields along certain axes
2. Also mention how this led to conceptual complexity - dealing with so many interconnected equations

- Greatly develops ~~vector~~ calculus out of necessity for his mechanical models
- Modern formulation only introduced in 1884, by Heaviside<sup>24</sup>
  - From 20 equations to 4

- Greatly develops ~~vector~~ calculus out of necessity for his mechanical models
- Modern formulation only introduced in 1884, by Heavyside<sup>24</sup>
  - From 20 equations to 4
- Vector notation itself only introduced in 1843, by Hamilton, with a 'recognisable' form appearing later that century via Clifford, Gibbs, and Heavyside<sup>25</sup>

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<sup>25</sup>Crowe, 1994.

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## Fluxions, Forces, and Fields

└ James Maxwell (1831-1879)

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1. Discuss how this was brought about with textbook usage by Clifford and Gibbs mainly, when lecturing in the US. Heavyside was mainly consolidating Maxwell's work

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Fluxions, Forces, and Fields

└ Aether Theory & Special Relativity

Aether Theory & Special Relativity

## Aether Theory & Special Relativity



- Following Maxwell's work, electromagnetism became dominant<sup>26</sup>

---

<sup>26</sup>Hunt, 1994.

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Fluxions, Forces, and Fields

└ Aether Theory & Special Relativity

└ The First Cracks

1. Dominant in the sense it led to an explosion of work around electromagnetism, light, and energy.

- Following Maxwell's work, electromagnetism became dominant<sup>26</sup>
- The nature of the aether<sup>iv</sup> was hotly debated due to conflicting theories and results (often from the same experiment)

<sup>26</sup>Hunt, 1994.  
<sup>iv</sup>In fact, Newton's initial work necessitated a vacuum in space

# The First Cracks

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## Fluxions, Forces, and Fields

### └ Aether Theory & Special Relativity

#### └ The First Cracks

1. Discuss michelson morley experiment and conflicting results - stokes' dragging hypotheses, fizeaus water experiment etc.

- Following Maxwell's work, electromagnetism became dominant<sup>26</sup>
- The nature of the aether<sup>iv</sup> was hotly debated due to conflicting theories and results (often from the same experiment)
- Following inconsistencies with Maxwell's equations & Fizeau's experiment Lorentz develops ideas of 'local time' & 'corresponding states' (co-ordinate transforms - *but only of EM waves*)

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  - A **purely** mathematical construction<sup>27</sup>

<sup>26</sup>Hunt, 1994.

<sup>27</sup>Brown, 2005.

<sup>iv</sup>In fact, Newton's initial work necessitated a vacuum in space

1. Stress this point - Lorentz was seemingly not aware of the physical connotations; had merely shown that this was a hypothesis that could work. Also had funnily enough made a factor of 2 error in his work

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# Henri Poincaré (1854-1912)

- Willing to ignore aether hypotheses, as mathematically unnecessary<sup>28</sup>

<sup>28</sup>Poincaré, Blondin, and Neculcea, 1901.

<sup>29</sup>Poincaré and Halsted, 1929.

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- Fluxions, Forces, and Fields
  - └ Aether Theory & Special Relativity
    - └ Henri Poincaré (1854-1912)

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1. He may also have been unwilling to let go of the idea of aether theory, or alternatively he may not have actually grasped the ramifications of what this implied for aether theory

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# Conclusion

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## To Sum Up...

- Initial shift with Newton's development of *experimental philosophy* and quantisation of nature

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- The final steps away from the aether - after thousands of years

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└ Conclusion

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1. discuss how we have had a massive shift in just the period of a few hundred years - can link it with the explosive rate of human growth as well. Discuss how it has led to so much advance in science and mathematics, as the lines between the two are blurred.

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**Thank You**

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