



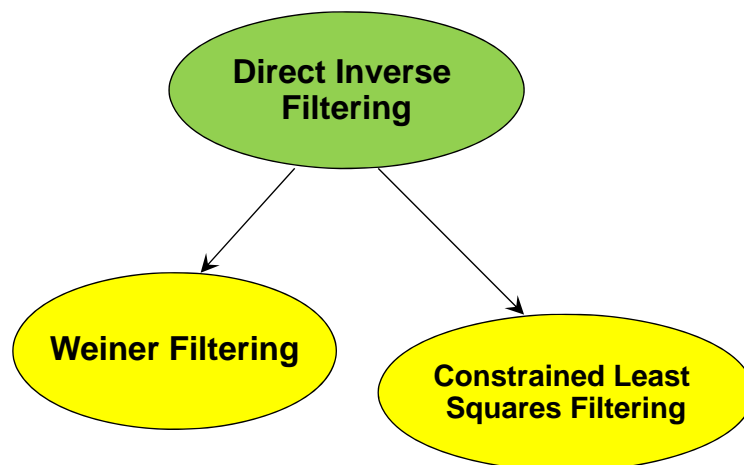
Image Processing

Image Restoration (Part II)

Pattern Recognition and Image Processing Laboratory (Since 2012)



Approaches for Image Restoration



Note: - These approaches are **linear image restoration**.
- PSF (Point Spread Function) is available.

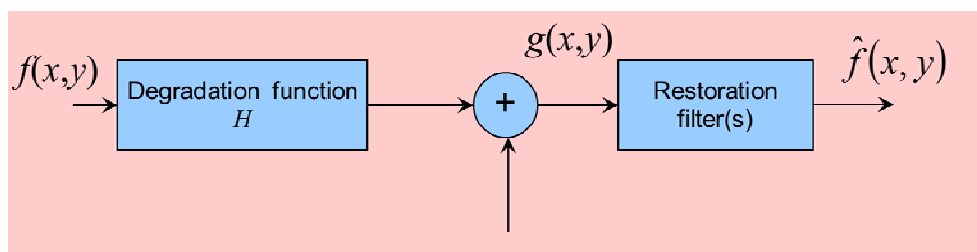
Approaches for Image Restoration

Lucy-Richardson
Algorithm

Blind
Deconvolution

Note: - These approaches are **nonlinear** image restoration.
- PSF is **NOT** available.

Direct Invert Filtering



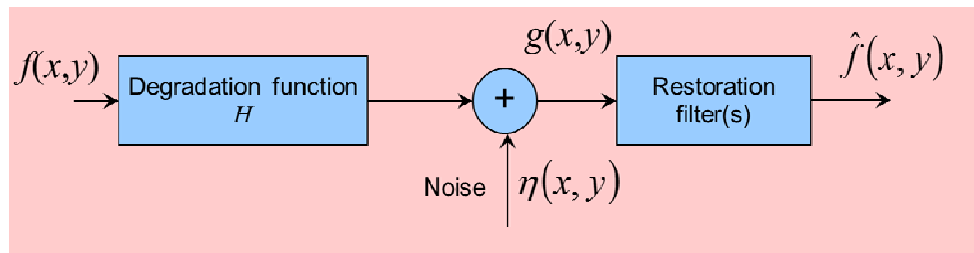
Degradation Eq

$$G(u,v) = H(u,v)F(u,v)$$

$$\hat{F}(u,v) = \frac{G(u,v)}{H(u,v)}$$

Restoration Eq

Direct Invert Filtering



Degradation Eq

$$G(u, v) = H(u, v)F(u, v) + N(u, v)$$

$$\hat{F}(u, v) = F(u, v) + \frac{N(u, v)}{H(u, v)}$$

Restoration Eq

Wiener Filtering

$$\hat{F}(u, v) = \left[\frac{1}{H(u, v)} \frac{|H(u, v)|^2}{|H(u, v)|^2 + S_{\eta}(u, v) / S_f(u, v)} \right] G(u, v)$$

(Note: In the original image, a green oval highlights the denominator term $|H(u, v)|^2 + S_{\eta}(u, v) / S_f(u, v)$, and an arrow points from the '0' in the denominator of the simplified equation below to this term.)

$$\hat{F}(u, v) = \frac{G(u, v)}{H(u, v)}$$

Direct Inverse Filtering



Wiener Filtering

```
>> fr = deconwnr(g, PSF) % Direct Inverse Filter  
>> fr = deconwnr(g, PSF, NSPR) % Parametric Weiner Filter  
>> fr = deconwnr(g, PSF, NACORR, FACORR) % Weiner Filter with  
                                         % Autocorrelation  
  
>> degrad5_5 % See demonstration
```



Constrained Least Squares Filtering

$$\hat{F}(u, v) = \left[\frac{H^*(u, v)}{|H(u, v)|^2 + \gamma |P(u, v)|^2} \right] G(u, v)$$

An arrow points from the '0' in the denominator to the term $\gamma |P(u, v)|^2$, which is highlighted in a green oval.

$$\hat{F}(u, v) = \frac{G(u, v)}{H(u, v)}$$

Direct Inverse F
iltering



Iterative Nonlinear Restoration Using the Lucy-Richardson Algorithm

>> degrad5_9 % See demonstration



Blind Deconvolution

One of the most difficult problems in image restoration is obtaining a suitable estimation of the PSF to use in restoration algorithm.



Blind Deconvolution

Image restoration methods that are **NOT** based on specific knowledge of the PSF are called “blind deconvolution” algorithm.



Blind Deconvolution

>> degrad5_10 % See demonstration

