

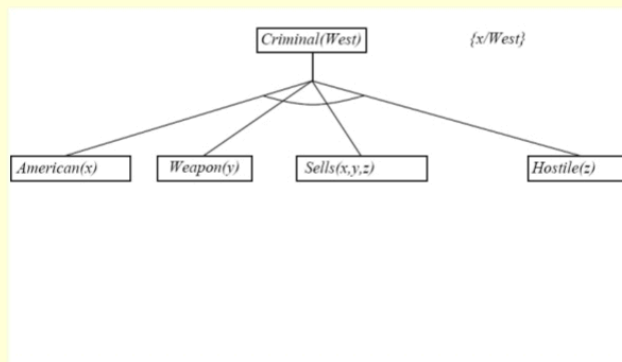
Backward Chaining

- Consider the item to be proven a goal
- Find a rule whose head is the goal (and bindings)
- Apply bindings to the body, and prove these (subgoals) in turn
- If you prove all the subgoals, increasing the binding set as you go, you will prove the item.
- Logic Programming (cprolog, on CS)

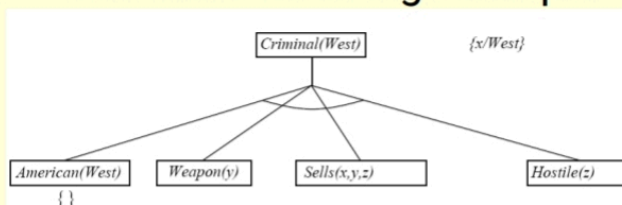
Backward Chaining Example

Criminal(West)

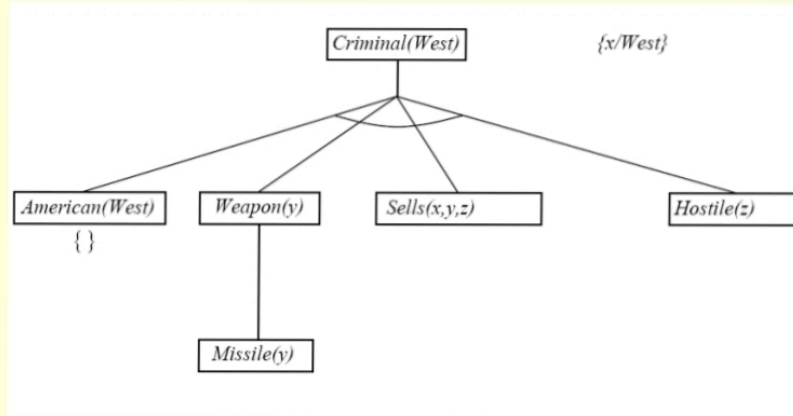
Backward Chaining Example



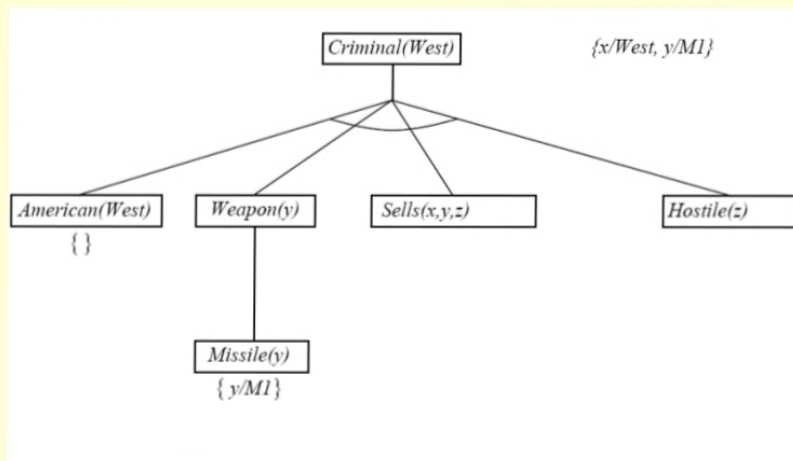
Backward Chaining Example



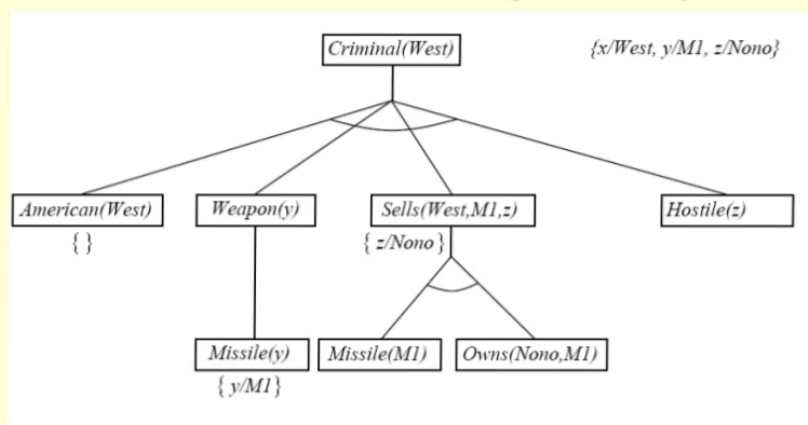
Backward Chaining Example



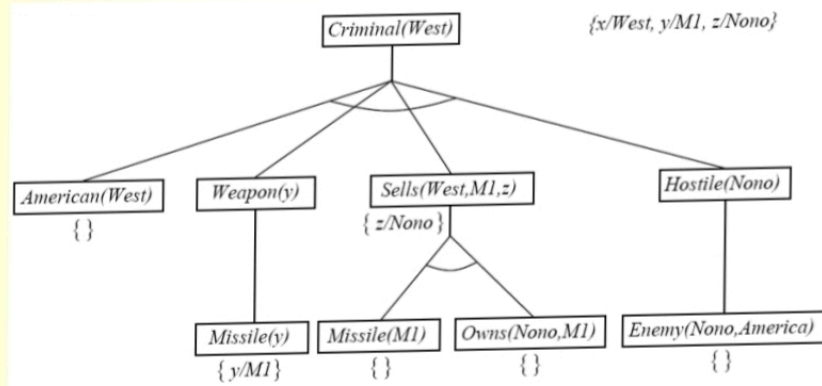
Backward Chaining Example



Backward Chaining Example



Backward Chaining Example



Backward Chaining Algorithm

```

function FOL-BC-ASK(KB, goals,  $\theta$ ) returns a set of substitutions
  inputs: KB, a knowledge base
           goals, a list of conjuncts forming a query
            $\theta$ , the current substitution, initially the empty substitution { }
  local variables: ans, a set of substitutions, initially empty

  if goals is empty then return { $\theta$ }
   $q' \leftarrow \text{SUBST}(\theta, \text{FIRST}(\text{goals}))$ 
  for each r in KB where  $\text{STANDARDIZE-APART}(r) = (p_1 \wedge \dots \wedge p_n \Rightarrow q)$ 
    and  $\theta' \leftarrow \text{UNIFY}(q, q')$  succeeds
       $\text{ans} \leftarrow \text{FOL-BC-ASK}(\text{KB}, [p_1, \dots, p_n | \text{REST}(\text{goals})], \text{COMPOSE}(\theta', \theta)) \cup \text{ans}$ 
  return ans
  
```

Properties of Backward Chaining

- Depth-first recursive proof search: space is linear in size of proof
- Incomplete due to infinite loops
 - Fix by checking current goal with every subgoal on the stack
- Inefficient due to repeated subgoals (both success and failure)
 - Fix using caching of previous results (extra space)
- Widely used without improvements for logic programming