

Mao Zeng

Curriculum Vitae

Contact information

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Address: JCMB 4402, Higgs Centre of Theoretical Physics, School of Physics and Astronomy,
University of Edinburgh

Education

2010 – 2015: Doctor of Philosophy in Physics, C.N. Yang Institute for Theoretical Physics, Stony Brook University, United States.

PhD Advisor: George Sterman.

Research areas: Quantum chromodynamics, Effective field theories.

2009-2010: Certificate of Advanced Study in Mathematics (Part III Mathematics), Honours pass with distinction, Cambridge University, United Kingdom.

Study area: Mathematical physics.

2006-2009: Bachelor of Arts, First-class honours, top 5 of class in all three years, Cambridge University, United Kingdom. Study area: Experimental and theoretical physics.

Employment

2021-present: Royal Society University Research Fellow, Higgs Centre of Theoretical Physics, School of Physics and Astronomy, University of Edinburgh

2021: Royal Society University Research Fellow, Department of Physics, University of Oxford, United Kingdom.

2018-2020: Postdoctoral Scholar in theoretical particle physics, Department of Physics, ETH Zurich, Switzerland.

2015-2018: Postdoctoral Scholar in theoretical particle physics, Department of Physics and Astronomy, University of California at Los Angeles, USA

Awards and Funding

2023: Frontiers of Science Award, International Congress of Basic Science, Beijing, \$25,000 award shared between 7 recipients, for work on the correspondence between scattering amplitudes and binary black hole dynamics

2023-2026: STFC Consolidated Grant, Particle Physics at the Higgs Centre, group grant for the whole Particle Physics Group at the Higgs Centre, with a significant allocation of funds for the scattering amplitudes sub-area.

2021-2025: UK Royal Society University Research Fellowship, £543,000 of initial funding, later successfully applied for £410,000 of supplemental research expenses

2018: (Declined) Marie Curie COFUND Fellowship (for postdoc position at Freiburg University, Germany; declined in favor of a regular postdoc position at ETH Zurich)

2016: President's Award to Distinguished Doctoral Student, Stony Brook University.
(Awarded annually to five doctoral graduates in all fields in the university)

2006-2010: Cambridge Overseas Scholarship, Cambridge University, UK
(Full tuition scholarship for four years of study)

2007: Percy Pemberton Prize for Distinguished Undergraduate Student, Trinity College, Cambridge University, UK
(Awarded annually to two first-year undergraduate students in Trinity College)

Publications (latest first)

48 publications, cited 4142 times as of 29 December, 2024, h index = 36, according to the database INSPIREHEP.net for high-energy physics publications.

(Links to publications on [INSPIRE](#), [arXiv](#))

1. **Zeno Capatti, Mao Zeng**
arXiv:2412.10864, Submitted 14 December 2024
Classical worldlines from scattering amplitudes
2. **Alexander Smirnov, Mao Zeng**
arXiv:2409.19099, Submitted 27 September 2024
Feynman integral reduction: balanced reconstruction of sparse rational functions and implementation on supercomputers in a co-design approach
3. **Zvi Bern, Enrico Herrmann, Radu Roiban, Michael S. Ruf, Mao Zeng**
arXiv:2408.06686, Submitted 13 August 2024
Global Bases for Nonplanar Loop Integrands, Generalized Unitarity, and the Double Copy to All Loop Orders
4. **Dogan Akpinar, Fernando Febres Cordero, Manfred Krauss, Michael S. Ruf, Mao Zeng**
arXiv:2407.19005, Submitted 26 July 2024
Spinning Black Hole Scattering at $O(G^3 S^2)$: Casimir Terms, Radial Action and Hidden Symmetry
5. **Zvi Bern, Enrico Herrmann, Radu Roiban, Michael S. Ruf, Alexander V. Smirnov, Vladimir A. Smirnov, Mao Zeng**
arXiv:2406.01554, Submitted 03 June 2024
Amplitudes, Supersymmetric Black Hole Scattering at $O(G^5)$, and Loop Integration
6. **A.V. Belitsky, A.A. Kokosinskaya, A.V. Smirnov, V.V. Voevodin, Mao Zeng**
arXiv:2402.07499, Submitted 12 Feb 2024
Efficient reduction of Feynman integrals on supercomputers

7. **Alexander V. Smirnov, Mao Zeng**
Comput.Phys.Commun. 302 (2024) 109261, Published May 24, 2024
FIRE 6.5: Feynman Integral Reduction with New Simplification Library
8. **Zvi Bern, Enrico Herrmann, Radu Roiban, Michael S. Ruf, Alexander V. Smirnov, Vladimir A. Smirnov, Mao Zeng**
Phys.Rev.Lett. 132 (2024) 25, 251601, Published 17 June 2024
Conservative binary dynamics at order $O(\alpha^5)$ in electrodynamics
9. **Kirill Mokrov, Alexander Smirnov, Mao Zeng**
Numerical Methods and Programming 24(4) 352-367 (2023), Published 19-10-2023
Rational Function Simplification for Integration-by-Parts Reduction and Beyond
10. **Leor Barack, Zvi Bern, Enrico Herrmann, Oliver Long, Julio Parra-Martinez, Radu Roiban, Michael S. Ruf, Chia-Hsien Shen, Mikhail P. Solon, Fei Teng, Mao Zeng**
Phys. Rev. D 108, 024025 - Published 12 July 2023
Comparison of post-Minkowskian and self-force expansions: Scattering in a scalar charge toy model
11. **Mao Zeng**
JHEP 09 (2023) 042 – Published 07 September 2023
Feynman Integrals from Positivity Constraints
12. **Michael Ruf, Zvi Bern, Julio Parra-Martinez, Chia-Hsien Shen, Mikhail Solon, Mao Zeng**
Proceedings of Science, Loops and Legs in Quantum Field Theory (LL2022) – Published 20 October, 2022
Scattering amplitudes and conservative dynamics at the fourth post-Minkowskian Order
13. **Fernando Febres Cordero, Manfred Kraus, Guanda Lin, Michael Ruf, Mao Zeng**
Phys.Rev.Lett. 130, 021601 – Published 12 January 2023
Conservative Binary Dynamics with a Spinning Black Hole at $O(G^3)$ from Scattering Amplitudes
14. **Alessandra Buonanno, Mohammed Khalil, Donal O'Connell, Radu Roiban, Mikhail P. Solon, Mao Zeng**
Contribution to 2022 Snowmass Summer Study, arXiv:2204.05194 – Submitted 11 Apr 2022
Snowmass White Paper: Gravitational Waves and Scattering Amplitudes
15. **Zvi Bern, Juan Pablo Gatica, Enrico Herrmann, Andres Luna, Mao Zeng**
JHEP 08 (2022) 131 – Published 10 Aug 2022
Scalar QED as a toy model for higher-order effects in classical gravitational scattering
16. **Zvi Bern, Julio Parra-Martinez, Radu Roiban, Michael S. Ruf, Chia-Hsien Shen, Mao Zeng**
Phys.Rev.Lett. 128, 161103 – Published 22 April 2022
Scattering Amplitudes, the Tail Effect, and Conservative Binary Dynamics at $O(G^4)$
17. **Co-authored with R. Alves Batista, M.A. Amin, G. Barenboim, N. Bartolo, D. Baumann, et al.**
arXiv:2110.10074 – Submitted 19 Oct 2021

18. **Enrico Herrmann, Julio Parra-Martinez, Michael S. Ruf, Mao Zeng**
JHEP 10 (2021) 148 – Published 18 Oct 2021
Radiative Classical Gravitational Observables at $O(G^3)$ from Scattering Amplitudes
19. **Enrico Herrmann, Julio Parra-Martinez, Michael S. Ruf, Mao Zeng**
Phys.Rev.Lett. 126, 201602 – Published 17 May 2021
Gravitational Bremsstrahlung from Reverse Unitarity
20. **Zvi Bern, Julio Parra-Martinez, Radu Roiban, Michael S. Ruf, Chia-Hsien Shen, Mikhail P. Solon, Mao Zeng**
(Editor's suggestion) Phys.Rev.Lett. 126, 171601 – Published 26 Apr 2021
Scattering Amplitudes and Conservative Binary Dynamics at $O(G^4)$
21. **Charalampos Anastasiou, Rayan Haindl, George Sterman, Zhou Yang, Mao Zeng**
JHEP 04 (2021) 222 – Published 22 Apr 2021
Locally finite two-loop amplitudes for off-shell multi-photon production in electron-positron annihilation
22. **Samuel Abreu, Harald Ita, Francesco Moriello, Ben Page, Wladimir Tschernow, Mao Zeng**
JHEP 11 (2020) 117 – Published 23 Nov 2020
Two-Loop Integrals for Planar Five-Point One-Mass Processes
23. **Julio Parra-Martinez, Michael Ruf, Mao Zeng**
JHEP 11 (2020) 023 – Submitted 09 November 2020
Extremal black hole scattering at $O(G^3)$: graviton dominance, eikonal exponentiation, and differential equations
24. **Zvi Bern, Andres Luna, Radu Roiban, Chia-Hsien Shen, Mao Zeng**
arXiv:2005.03071 – Submitted 06 May 2020
Spinning Black Hole Binary Dynamics, Scattering Amplitudes and Effective Field Theory
25. **Zvi Bern, Clifford Cheung, Radu Roiban, Chia-Hsien Shen, Mikhail P. Solon, Mao Zeng**
JHEP 10 (2019) 206 – Published 21 October 2019
Black Hole Binary Dynamics from the Double Copy and Effective Theory
26. **Samuel Abreu, Lance Dixon, Enrico Herrmann, Ben Page, Mao Zeng**
JHEP 1903 (2019) 123 – Published 21 March 2019
The two-loop five-point amplitude in $N=8$ supergravity
27. **Zvi Bern, Clifford Cheung, Radu Roiban, Chia-Hsien Shen, Mikhail P. Solon, Mao Zeng**
Phys. Rev. Lett. 122, 201603 – published 24 May 2019
Scattering Amplitudes and the Conservative Hamiltonian for Binary Systems at Third Post-Minkowskian Order
28. **Samuel Abreu, Lance Dixon, Enrico Herrmann, Ben Page, Mao Zeng**
Phys. Rev. Lett. 122, 121603 – published 29 Mar 2019
The two-loop five-point amplitude in $N=4$ super-Yang-Mills theory

29. **Samuel Abreu, Ben Page, Mao Zeng**
JHEP 1901 (2019) 006 – published 02 Jan 2019
Differential equations from unitarity cuts: nonplanar hexa-box integrals
30. **Samuel Abreu, Fernando Febres Cordero, Harald Ita, Ben Page, Mao Zeng**
Proceedings of Science, LL 2018 016 – Published 02 Oct 2018
Five-point two-loop amplitudes from numerical unitarity
31. **Zvi Bern, Michael Enciso, Harald Ita, Mao Zeng**
Proceedings of Science, LL2018 084 – Published 02 Oct 2018
Two-loop D-dimensional unitarity and dual conformal symmetry
32. **Ben Page, Samuel Abreu, Fernando Febres Cordero, Harald Ita, Matthieu Jaquier, Mao Zeng**
Proceedings of Science, RADCOR2017 012 – Published 02 Jul 2018
First two-loop amplitudes with the numerical unitarity method
33. **Zvi Bern, Michael Enciso, Chia-Hsien Shen, Mao Zeng**
Phys. Rev. Lett. 121, 121603 – Published 21 Sep 2018
Dual conformal structure beyond the planar limit
34. **Zvi Bern, John Joseph Carrasco, Wei-Ming Chen, Alex Edison, Henrik Johansson, Julio Parra-Martinez, Radu Roiban, Mao Zeng**
(Editor's suggestion) Phys. Rev. D. 98, 086021 – Published 19 Oct 2018
Ultraviolet properties of N=8 supergravity at five loops
35. **Samuel Abreu, Fernando Febres Cordero, Harald Ita, Ben Page, Mao Zeng**
Part of Proceedings, 53rd Rencontres de Moriond on QCD and High Energy Interactions (Moriond QCD 2018)
Computing Planar Five-Gluon Amplitudes with Numerical Unitarity
36. **Samuel Abreu, Fernando Febres Cordero, Harald Ita, Ben Page, Mao Zeng**
Phys. Rev. D 97, 116014 – Published 20 June 2018
Planar two-loop five-gluon amplitudes from numerical unitarity
37. **Zvi Bern, Michael Enciso, Harald Ita, Mao Zeng**
Phys. Rev. D 96, 096017 – Published 21 November 2017
Dual conformal symmetry, integration-by-parts reduction, differential equations and the nonplanar sector
38. **Zvi Bern, John Joseph M. Carrasco, Wei-Ming Chen, Henrik Johansson, Radu Roiban, Mao Zeng**
Phys. Rev. D 96, 126012 – Published 20 June 2018
Five-Loop Four-Point Integrand of N=8 Supergravity as a Generalized Double Copy
39. **Zvi Bern, Michael Enciso, Julio Parra-Martinez, Mao Zeng**
JHEP 05 (2017) 137 – Published 25 May 2017
Manifesting enhanced cancellations in supergravity: integrands versus integral
40. **S. Abreu, F. Febres Cordero, H. Ita, M. Jaquier, B. Page, M. Zeng**
Phys. Rev. Lett. 119, 142001 – Published 05 October 2017
Two-Loop Four-Gluon Amplitudes with the Numerical Unitarity Method

41. **Mao Zeng**
JHEP 06 (2017) 121 – Published 22 June 2017
Differential equations on unitarity cut surfaces
42. **Sally Dawson, Ye Li, Prerit Jaiswal, Harikrishnan Ramani, and Mao Zeng**
Phys. Rev. D 94, 114014 – Published 15 December 2016
Resummation of jet veto logarithms at partial $N^3\text{LL}+\text{NNLO}$ for WW production at the LHC
43. **Mao Zeng**
JHEP 10 (2015) 189 – Published 28 October 2015
Drell-Yan Process with Jet Vetoes: breaking of generalized factorization
44. **Sally Dawson, Ian M. Lewis and Mao Zeng**
Phys. Rev. D 91, 074012 (2015) – Published 07 April 2015
The Usefulness of EFT for Boosted Higgs Production
45. **Sally Dawson, Ian M. Lewis and Mao Zeng**
Phys. Rev. D 90, 093007 (2014) – Published 25 November 2014
Effective Field Theory for Higgs Plus Jet Production
46. **Patrick Meade, Harikrishnan Ramani and Mao Zeng**
Phys. Rev. D 90, 114006 (2014) – Published 01 December 2014
Transverse Momentum Resummation effects in WW measurements
47. **George Sterman and Mao Zeng**
JHEP 05 132 (2014) – Published 28 May 2014
Quantifying Comparisons of Threshold Resummations
48. **Sally Dawson, Ian M. Lewis and Mao Zeng**
Phys. Rev. D 88, 054028 – Published 26 September 2013
Threshold Resummed and Approximate Next-to-next-to-leading Order Results for WW Pair Production at the LHC

Talks and Presentations (latest first)

1. *Finite classical observables from amplitudes and the emergent worldline*, Theoretical Physics seminar at Queen Mary University of London, 28 Nov 2024
2. *Unity of scattering amplitude and worldline approaches to binary dynamics*, Theoretical Physics seminar at Scuola Normale Superiore, Pisa, Italy, 14 Nov 2024
3. *Collider Methods for Gravitational Wave Physics*, Particle Phenomenology Seminar at the University of Liverpool, 13 Mar 2024
4. *Scattering Amplitudes and Gravitational Wave Physics, remote*, Theoretical Particle Physics Seminar at the University of Sussex, 06 Nov
5. *Lectures on Gravitational Binary dynamics from Scattering Amplitudes*, 6th School of Analytic Computing in High-Energy and Gravitational Theoretical Physics, Atrani, Italy, 12-13 Oct 2023

6. *Adding FUEL to FIRE for faster IBP*, “MathemAmplitudes 2023: QFT at the Computational Frontier” conference at Padova University, Italy, 26 Sep 2023
7. *Feynman integrals from positivity constraints, remote*, Seminar at the University of Colorado Boulder, Nuclear Theory Group, 07 Sep 2023
8. *Overview: scattering amplitudes and the gravitational two-body problem*, Gravitational Waves meet Amplitudes in the Southern Hemisphere, ICTP-SAIFR, Brazil, 15 Aug 2023
9. *Scattering Amplitudes and Gravitational Wave Physics*, Frontiers of Science Lecture for receiving an award at the First International Congress of Basic Science, Beijing, 20 Jul 2023
10. *Feynman integrals from positivity constraints*, LoopFest XXI conference, SLAC National Accelerator Laboratory, 27 Jun 2023
11. *Feynman integrals from positivity constraints, remote*, Amplitudes Seminar at Bonn University, 11 May 2023
12. *Feynman integrals from positivity constraints, remote*, Peking University HEP Seminar, 02 Feb, 2023
13. *A new method for evaluating Feynman integrals*, Zurich Phenomenology Workshop, 12 Jan, 2023
14. *Electrodynamics as toy model for binary gravitational dynamics at higher orders*, remote, Physics in Intense Fields Conference 2022 (PIF22), Plymouth University, 31 Aug, 2022
15. *Multi-loop integrals for binary dynamics*, Workshop on From Scattering Amplitudes to Gravitational-Wave Predictions for Compact Binaries, University of Zurich, 14 Jul, 2022
16. *Spinning binary black holes & 2-loop scattering amplitudes*, remote, Seminar at Institute of Theoretical Physics, Chinese Academy of Science, 30 Jun, 2022
17. *Multi-loop scattering amplitudes and gravitational binary dynamics*, remote, Colloquium at CERN Department of Theoretical Physics, 02 Mar, 2022
18. *Multi-loop scattering amplitudes and gravitational binary dynamics*, Seminar at Kings College London, 26 Jan, 2022.
19. *Amplitudes, Loops, and Gravity*, Seminar at Queen Mary University of London, remote, 11 Nov, 2021.
20. *Conservative and radiative binary dynamics from scattering amplitudes*, remote, Amplitudes 2021 International Conference, Michigan State University, 18 Aug, 2021.
21. *Particle physics methods for gravitational wave physics*, remote, Qingdao Summer School in Particle Physics Theory, Qingdao University, China, Jul 13, 2021
22. *Importing perturbative QCD methods into gravitational wave physics*, remote, Radcor-LoopFest 2021 Conference, Florida State University, May 20, 2021.
23. *Integrals for post-Minkowskian classical dynamics*, remote, GGI Workshop on Gravitational Scattering, Inspiral, and Radiation, May 12, 2021

24. *Gravitational physics from scattering amplitudes and collider methods*, remote, Colloquium at University of Oxford, Apr 30, 2021
25. *Third-post-Minkowskian binary dynamics from KMOC formalism*, remote, UCLA / AEI Potsdam joint journal club, Mar 09, 2021
26. *New results for gravitational binary dynamics from scattering amplitudes*, remote, Seminar at Nordita, Feb 16, 2021
27. *New results for gravitational binary dynamics from QFT amplitudes*, remote, Seminar at Mathematical Institute, University of Oxford, Jan 26, 2021
28. *Locally finite representation of 2-loop amplitudes*, remote, Seminar at University of Edinburgh, Oct 22, 2020
29. *Factorization and subtraction of singularities of 2-loop amplitudes*, remote, Seminar at Peking University, Oct 13, 2020
30. *NNLO subtraction for numerical integration of virtual amplitudes*, remote, QCD@LHC-X Conference, CERN, Sep 10, 2020
31. *Towards 4th-Post-Minkowskian Potential*, QCD Meets Gravity Conference, University of California at Los Angeles, Dec 10, 2019
32. *Black Hole Binary Dynamics from Scattering Amplitudes*, Seminar at Zurich University, Dec 03, 2019
33. *Orbital Dynamics from double copy and EFT*, RadCor 2019 – 14th International Symposium on Radiative Corrections, 11 September 2019
34. *Generalized unitarity and numerical ansatzes for 2-loop 5-point amplitudes*, LoopFest XVIII Conference, Fermilab, August 13, 2019
35. *Generalized unitarity and frontiers of perturbative QFT*, Seminar at SLAC National Accelerator Laboratory, August 08, 2019
36. *High-multiplicity Frontier for Amplitudes at the LHC*, Annual Meeting of the Institute of Theoretical Physics, Chinese Academy of Science, Beijing, April 29, 2019
37. *Loop amplitudes from unitarity and ansatz*, Particle Physics Seminar at the Institute for Theoretical Physics, ETH Zurich, February 26, 2019
38. *The high-multiplicity frontier for two-loop QCD*, Workshop on Amplitudes in the LHC Era, Galileo Galilei Institute for Theoretical Physics, Florence, October 29, 2018
39. *Five-loop UV properties of $N=8$ supergravity*, International Workshop on High Precision for Hard Processes, Albert-Ludwigs-Universitat Freiburg, October 03, 2018
40. *Calculating supergravity divergences at high loop orders*, Amplitudes 2018 International Conference, SLAC National Accelerator Laboratory, June 20, 2018
41. *Integral reduction and five-loop supergravity*, Workshop on Taming the Complexity of Multiloop Integrals, June 05, 2018
42. *Two-loop D-dimensional unitarity and dual conformal symmetry*, 14th Workshop on Loops and Legs in Quantum Field Theory, St. Goar, Germany, May 04, 2018

43. *Unitarity cuts beyond loop integrands*, Seminar at SLAC National Accelerator Laboratory, December 01, 2017.
44. *Unitarity cuts and loop amplitudes in QCD and supersymmetric theories*, Seminar at UC Los Angeles, October 03, 2017.
45. *QCD at the LHC using new theoretical tools in scattering amplitudes*, Seminar at Lawrence Berkeley National Laboratory, Sep 20, 2017.
46. *Unitarity cuts and UV divergences*, Scattering Amplitudes and Beyond Workshop, Kavli Institute for Theoretical Physics, UC Santa Barbara, Jun 29, 2017.
47. *Differential equations and integration by parts from unitarity*, LoopFest XVI Workshop, Argonne National Laboratory, Jun 02, 2017
48. *Towards multi-jet production at NNLO*, Topical Workshop on QCD Structure of Nucleons in the Modern Era, UC Los Angeles, May 06, 2017.
49. *New integration-by-parts techniques for gravity amplitudes*, QCD Meets Gravity Workshop, UC Los Angeles, Dec 05, 2016.
50. *Partial N³LL + NNLO resummation for WW production under a jet veto*, LoopFest XV Conference, University at Buffalo, Aug 16, 2016
51. *Same title as above*, Seminar UC San Diego, Jun 14, 2016.
52. *Same title as above*, Seminar at Harvard University, May 10, 2016.
53. *Jet vetoes and discrete symmetries*, QCD Factorization Workshop, University at Buffalo, Nov 03, 2015.
54. *Drell-Yan Process with Jet Vetoes: Breaking of Generalized Factorization*, The 12th International Symposium on Radiative Corrections and LoopFest XIV, UC Los Angeles, Jun 17, 2015.
55. *Transverse Momentum Resummation effects in WW measurements*, PITT-PACC Workshop on QCD and Beyond at Colliders, Pittsburgh University, Nov 14, 2014.
56. *Same title as above*, Seminar at Argonne National Laboratory, Nov 12, 2014.
57. *Same title as above*, Phenomenology / Experiment Joint Seminar, Stony Brook University, Sep 29, 2014.
58. *Effective Field Theory for Higgs plus Jet Production*, Seminar at Brookhaven National Laboratory, Sep 26, 2014.
59. *Transverse Momentum Resummation effects in WW measurements*, remote, ATLAS Collaboration Standard Model Plenary Meeting, Aug 14, 2014.
60. *Parton Luminosity Shapes and Threshold Resummation in SCET and Direct QCD*, XIth Annual Workshop on Soft-Collinear Effective Theory, Technical University of Munich, Mar 26, 2014.

Teaching

Fall 2010 and Spring 2011: graduate Teaching Assistant for PHY 277 Computation for Physics and Astronomy, Stony Brook University

Summer 2011 and Fall 2011: graduate Teaching Assistant for PHY 124 Physics for the Life Sciences II, Stony Brook University

Spring 2011: graduate Teaching Assistant for PHY 512 Quantum Mechanics II, Stony Brook University

Fall 2018: Teaching Coordinator for Quantum Field Theory I, ETH Zurich (postdoc appointment)

2018-2019: Supervision of master student thesis, ETH Zurich (postdoc appointment)

2022-: Lecturer for Computer Simulations, course for 2nd year undergraduate physics students, Edinburgh University

2021-: Project supervisor of Mphys program at Edinburgh University. Two Mphys students supervised so far.

2022-: PhD student supervision. Two PhD students currently under supervision.

2023:- Supervisor for summer project of exchange undergraduate student from Nankai University, China

2024-: Project supervisor of Msc program at Edinburgh University. Three Msc students supervised so far.

2024:- Project supervisor of Senior Honours Mathematical Physics Program, University of Edinburgh. One current student under supervision.