Nonequilibrium quantum criticality of interacting Dirac fermions

Yin-Kai Yu (余荫铠)[†] Zhi Zeng (曾植)[†] Zi-Xiang Li (李自翔)^{*} Shuai Yin (阴帅)[†]

[†]School of physics, Sun Yat-Sen University, Guangzhou 510275, China.

*Beijing National Laboratory for Condensed Matter Physics & Institute of Physics, Chinese Academy of Sciences, Beijing 100190, China.

Background

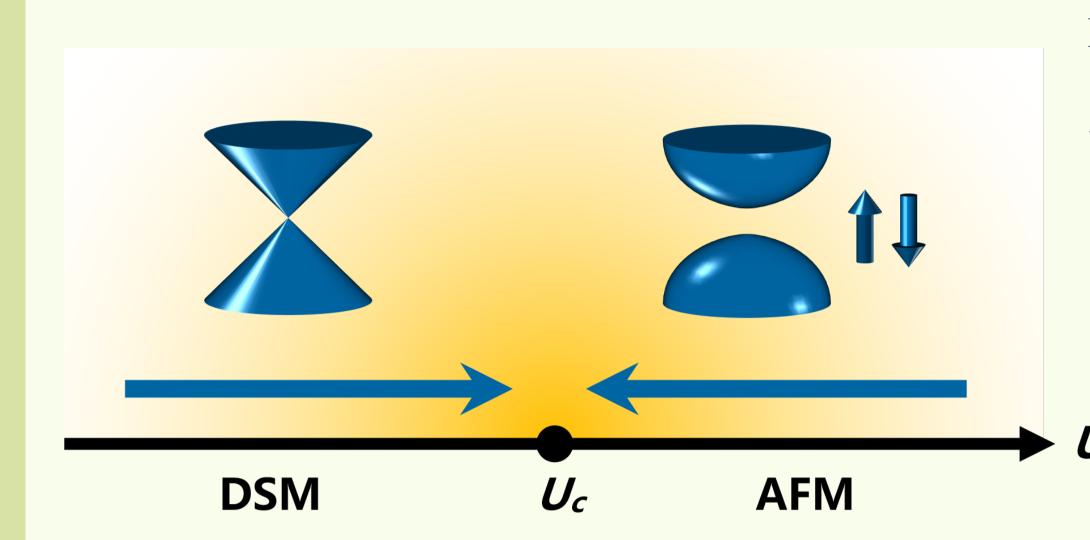
Current status in this field

- Nonequilibrium scaling has been developed in various classical or quantum systems, but rarely studied in strongly interacting fermionic systems[1–3].
- Dirac fermions with linear dispersion matter in phase transition widely in graphene, Weyl/Dirac semimetal, surface of topological insulator[4, 5].

This work

For the first time, we demonstrate the nonequilibrium dynamics of chiral Heisenberg universality class for Dirac fermions.

Model and protocol



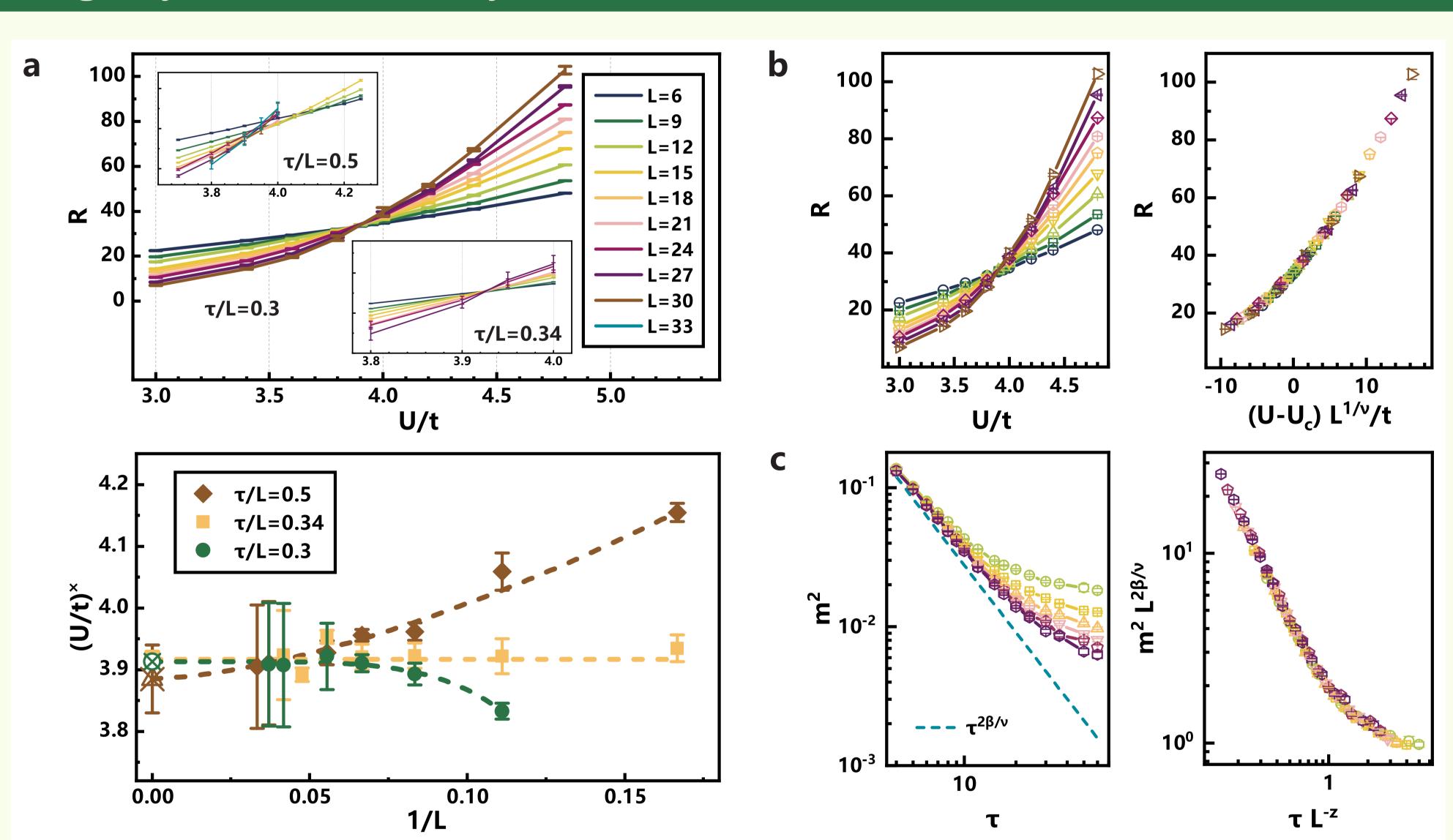
Half-filled honeycomb Hubbard model (t = 1)

$$H = -t \sum_{\langle i,i \rangle,\sigma} c_{i\sigma}^{\dagger} c_{j\sigma} + U \sum_{i} \left(n_{i\uparrow} - \frac{1}{2} \right) \left(n_{i\downarrow} - \frac{1}{2} \right).$$

Steps

- Prepare initial states of DSM and AFM.
- Quench them to the quantum critical point (QCP) U_c .
- Explore the imaginary-time relaxation by determinant quantum Monte Carlo[6].

Imaginary-time relaxation dynamics with the AFM ordered initial state



We are concerned about these observable quantities:

AFM structure factor $S(\boldsymbol{q}) = \frac{1}{L^2} \sum_{i,j} e^{i\boldsymbol{q}\cdot(\boldsymbol{r}_i-\boldsymbol{r}_j)} \langle m_i^{(z)} m_j^{(z)} \rangle$,

AFM order parameter $m^2 = S\left(\mathbf{0}\right),$

 $R = S(\mathbf{0}) / S(\Delta \mathbf{q})$. Correlation ratio

Imaginary-time correlation $A = \frac{1}{L^2} \sum_i \langle m_i^{(z)}(0) m_i^{(z)}(\tau) \rangle$.

a. Estimation of quantum critical point U_c

$$R\left(g,\tau,L\right)=f_{R}\left(gL^{1/\nu},\tau^{-1}L^{z}\right).$$

Fixed $\tau^{-1}L^z$, curves intersect at $g=U-U_c=0$.

b. Fitting for ν

Fixing $\tau^{-1}L^z = 0.3$, $R(g) = f_R(gL^{1/\nu})$, $\Rightarrow \nu = 1.17 \pm 0.07.$

 \Rightarrow QCP: $U/t = 3.91 \pm 0.03$.

c. Fitting for β/ν

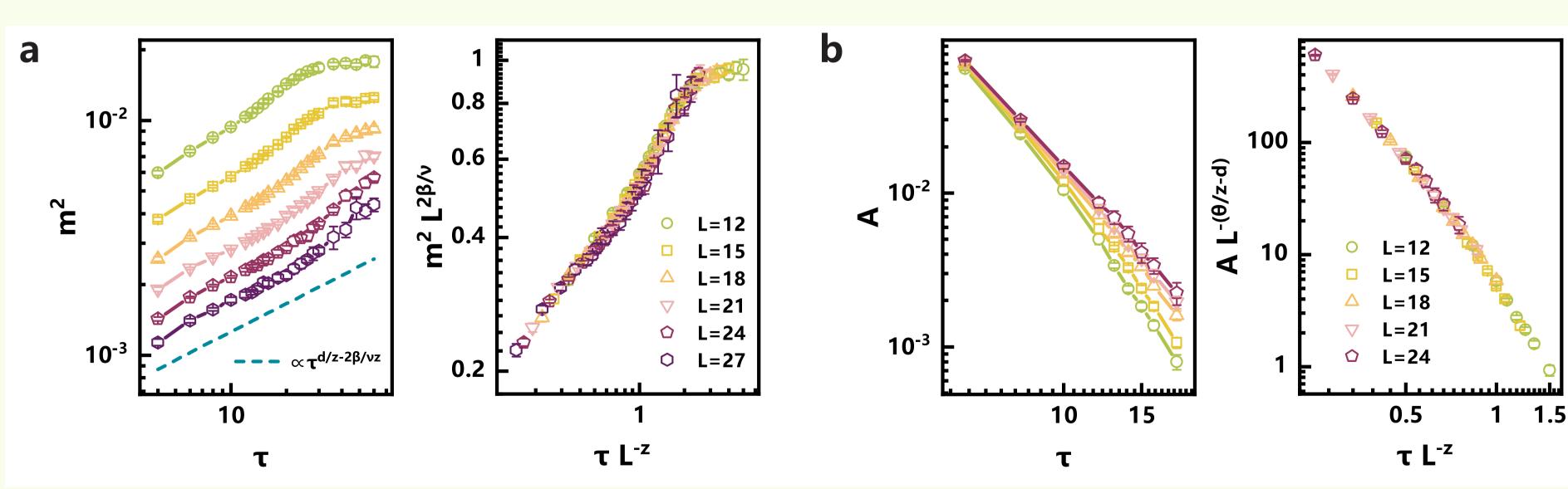
Saturated AFM initialized, g = 0 set,

$$m^2= au^{-2eta/
u z}f_{m^2}\left(au^{-1}L^z
ight),$$

 $\Rightarrow \beta/\nu = 0.80 \pm 0.03.$

Limit $\tau L^{-z} \to 0$, $m^2 \sim \tau^{-2\beta/\nu z} + \tau^{-2\beta/\nu z} \mathcal{O}(\tau L^{-z})$.

Imaginary-time relaxation dynamics with the disordered initial state



a. Examination for β/ν

Initial DSM at g = 0. Here we take $\beta/\nu = 0.80$,

 $m^2=L^{-d} au^{d/z-2eta/
u z}f_{m^2}\left(au^{-1}L^z
ight).$

Compare with zero-order approximation $m^2 \sim \tau^{d/z - 2\beta/\nu z}$.

b. Fitting for θ

Random initial state at q = 0,

 $A = L^{\theta z - d} f_A \left(\tau^{-1} L^z \right).$

 $\Rightarrow \theta = -0.84 \pm 0.04$.

Discussion and conclusion

Comparison with previous works

model	method	U_c/t	eta/ u	θ
honeycomb	QMC (present)	3.91(3)	0.80(3)	-0.84(4)
honeycomb	QMC[5]	3.85(2)	0.75(2)	-
honeycomb	QMC[4]	3.77(4)	0.8(1)	-
Gross-Neveu	$4 - \epsilon (1st order)[7]$	-	0.945	-
Gross-Neveu	$4 - \epsilon$ (2nd order)[7]	-	0.985	-
Gross-Neveu	FRG[8]	-	1.008	-

Conclusion

- A negative critical initial slip exponent $\theta = -0.84(4)$ for chiral Heisenberg universality class.
- An efficient dynamic QMC method to determine the critical point and critical exponents.
- A new avenue for numerical studies on nonequilibrium quantum criticality of fermionic systems.



Contact

Shuai Yin: yinsh6@mail.sysu.edu.cn Zi-Xiang Li: zixiangli@iphy.ac.cn

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