Algorithm Analysis

CSI 5301

## Assignment 6.1: BBST Select

Due: Fri June 17, 2022 11:59pm

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# Description: Print the ith order statistic from a list of numbers after implementing a Balanced Binary Search Tree for those numbers.

# Data Structure: vector<int>, Binary Search tree

Node Class with following properties:

int value, int height, node leftChild and Node rightChild

System Implementation Details:

* Save the current height of the node as a property in the Node class so that we can calculate balance factor to maintain a balanced BST. (see Algorithm)
* Assumptions: Input are strictly integers and No duplicate values
* Given ‘N’ numbers are inserted one by one to the BBST so that the height of BST is logN
* Once the BBST is formed for N, perform a In-order traversal as push the value from each node as we traverse through. This results in a vector of ‘N’ elements which is sorted.
* SELECT subroutine will then return the element at (i-1) in this sorted vector. This value is the ith smallest value. This subroutine will take O(n).
  + If we stop the traversal once we populate the ith element (once we have traversed i nodes by performing in-order traversal) we can stop the traversal as that will be the ith order statistic and run time in this case will be O(i).

# Algorithm:

1) Read the std input lines and push numbers from first line to a vector<int> and int variable ith

2) Insert the numbers as nodes creating a Balanced Binary Search Tree

1. Recursively insert the number as a leaf node and adjust nodes as in normal BST insertion maintaining the BST invariant
2. Update the height of this parent node
3. Calculate the balance factor of this parent node and check if this node is imbalanced now.
4. Balance factor is the difference between the height of left and right child nodes
5. For a BST to be BBST, magnitude of balance factor can’t be greater than 1
6. Handle imbalanced scenarios by rotating the sub-tree at this parent Node

3) Perform a in-order traversal and push the node values to another vector<int> sortedNumbers

4) Print the integer at (ith-1) position on sortedNumbers vector

# Analysis:

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| --- | --- |
| Input N | Vector<int> numbers  int ith  (implicitly derived from 1st and 2nd lines in cin) |
| Basic Operation | Read from input stream  vector operations  Tree height and balance factor calculations  Recursion |
| Recurrence relation | for SELECT subroutine |
| Run-time analysis (Big O) | for insertion and balancing on BST  for in-order traversal  **for overall program to perform SELECT subroutine** |

**References:**

1. <https://www.geeksforgeeks.org/avl-tree-set-1-insertion/>
2. <https://www.youtube.com/watch?v=1QSYxIKXXP4>
3. <https://github.com/williamfiset/Algorithms/blob/master/src/main/java/com/williamfiset/algorithms/datastructures/balancedtree/AVLTreeRecursive.java>