$$\{\max\{|x|,|y|\} = 1\}$$

$$f(x,y) = \left(\frac{x}{\sqrt{x^2 + y^2}}, \frac{y}{\sqrt{x^2 + y^2}}\right)$$

$$f^{-1}(x,y) = \left(\frac{x}{\max\{|x|,|y|\}}, \frac{y}{\max\{|x|,|y|\}}\right)$$