

# Why does Alice follow Bob?

**Filippo Menczer**

Center for Complex Networks and Systems Research  
School of Informatics and Computing  
Indiana University, Bloomington



Center for Complex Networks  
and Systems Research



SCHOOL OF Informatics and Computing

SCHOOL OF INFORMATICS AND COMPUTING

# The Role of Information Diffusion in the Evolution of Social Networks

Lilian Weng<sup>1</sup>, Jacob Ratkiewicz<sup>2</sup>, Nicola Perra<sup>3</sup>, Bruno Gonçalves<sup>4</sup>, Carlos Castillo<sup>5</sup>, Francesco Bonchi<sup>6</sup>, Rossano Schifanella<sup>7</sup>, Filippo Menczer<sup>1</sup>, Alessandro Flammini<sup>1</sup>

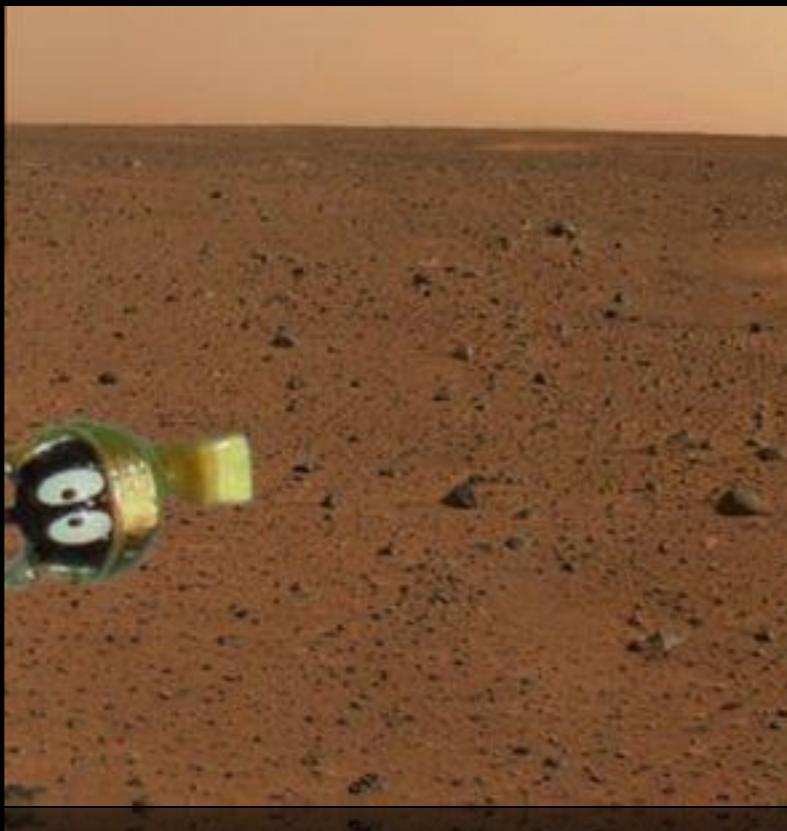
<sup>1</sup>School of Informatics and Computing, Indiana University Bloomington, USA <sup>2</sup>Google Inc.

<sup>3</sup>Laboratory for the Modeling of Biological and Socio-technical Systems, Northeastern University, USA

<sup>4</sup>Aix Marseille Université, CNRS, CPT, UMR 7332, Marseille, France

<sup>5</sup>Qatar Computing Research Institute <sup>6</sup>Yahoo! Research Barcelona

<sup>7</sup>Department of Computer Science, University of Torino, Italy



Marvin



2012.08.05 23:05

**Stamen**



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# THE ATTENTION ECONOMY

Understanding the *New Currency of Business*



THOMAS H. DAVENPORT  
JOHN C. BECK

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# THE ATTENTION ECONOMY

similar approaches to optimize the use of our attention.

Certainly the attention economy has laws of supply and demand. The most obvious one is that as the amount of information increases, the demand for attention increases. As Herbert Simon, a Nobel prize-winning economist, put it, “What information consumes is rather obvious: it consumes the attention of its recipients. Hence a wealth of information creates a poverty of attention.”<sup>14</sup> Yet the supply stays constant or even shrinks if there are fewer people available to attend to vastly more information. As

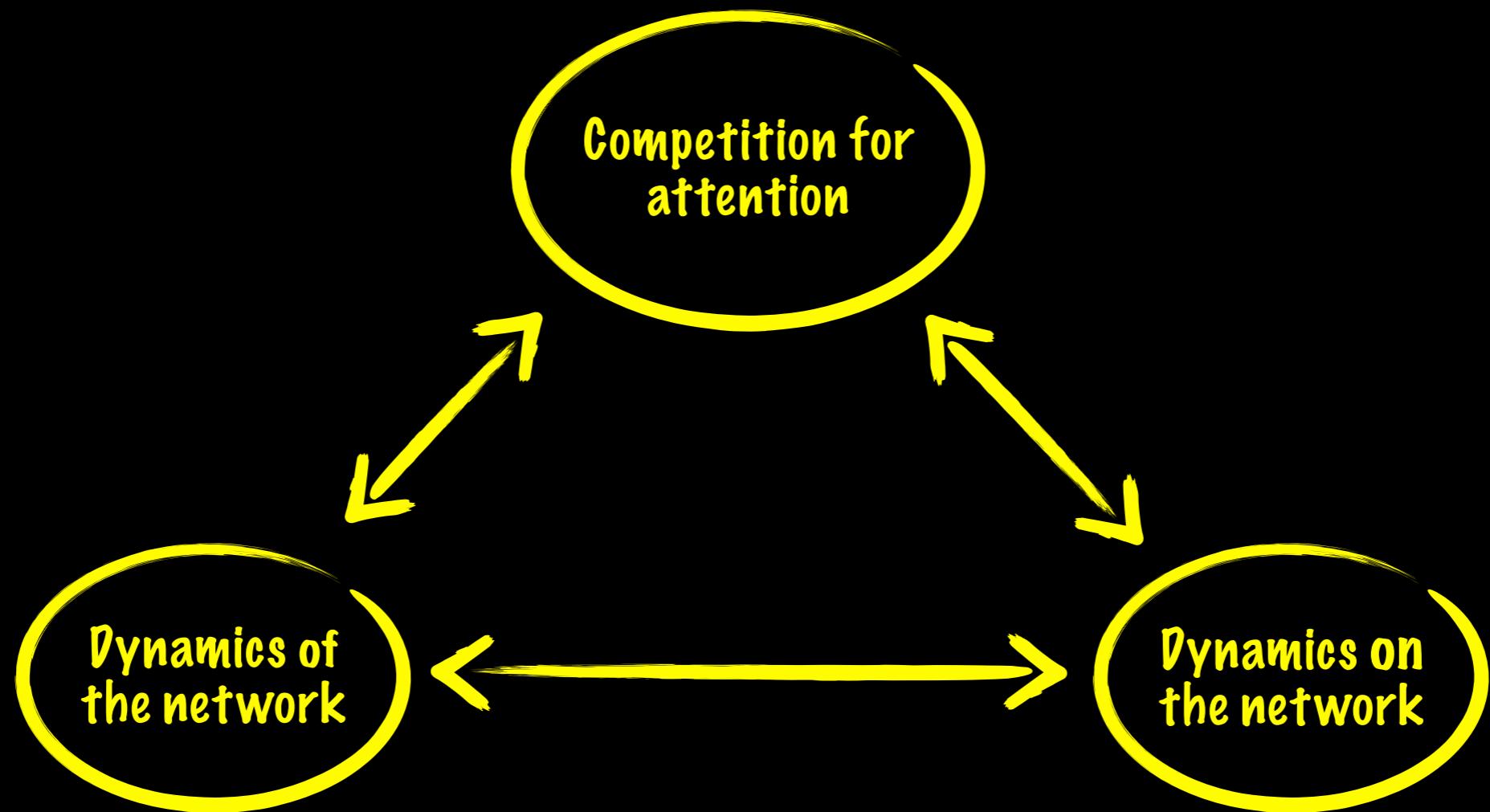
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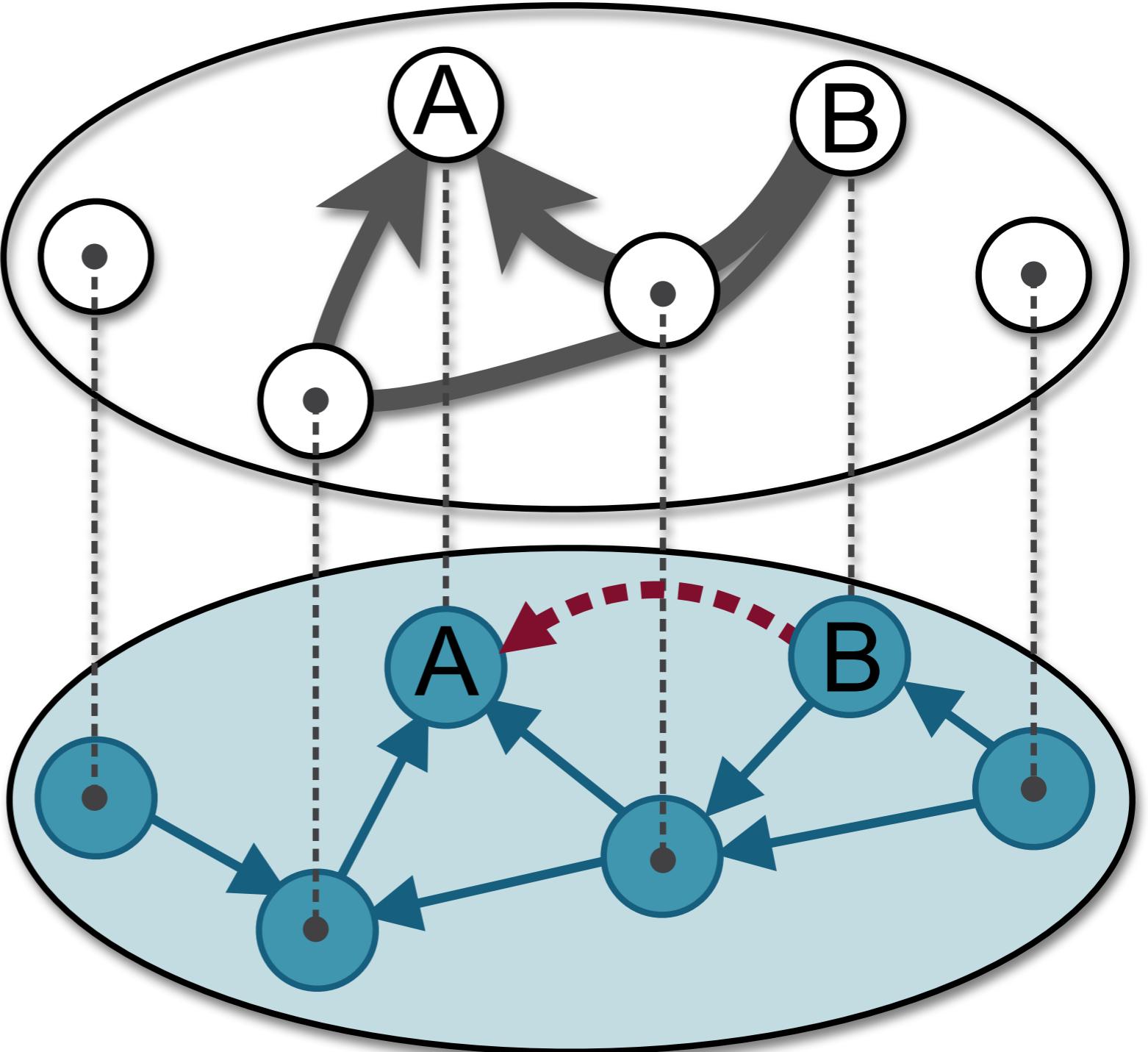
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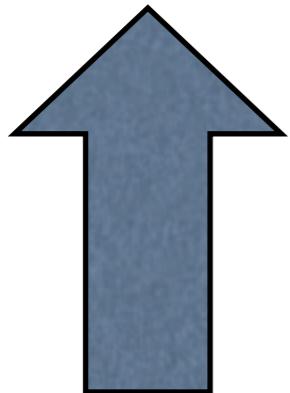
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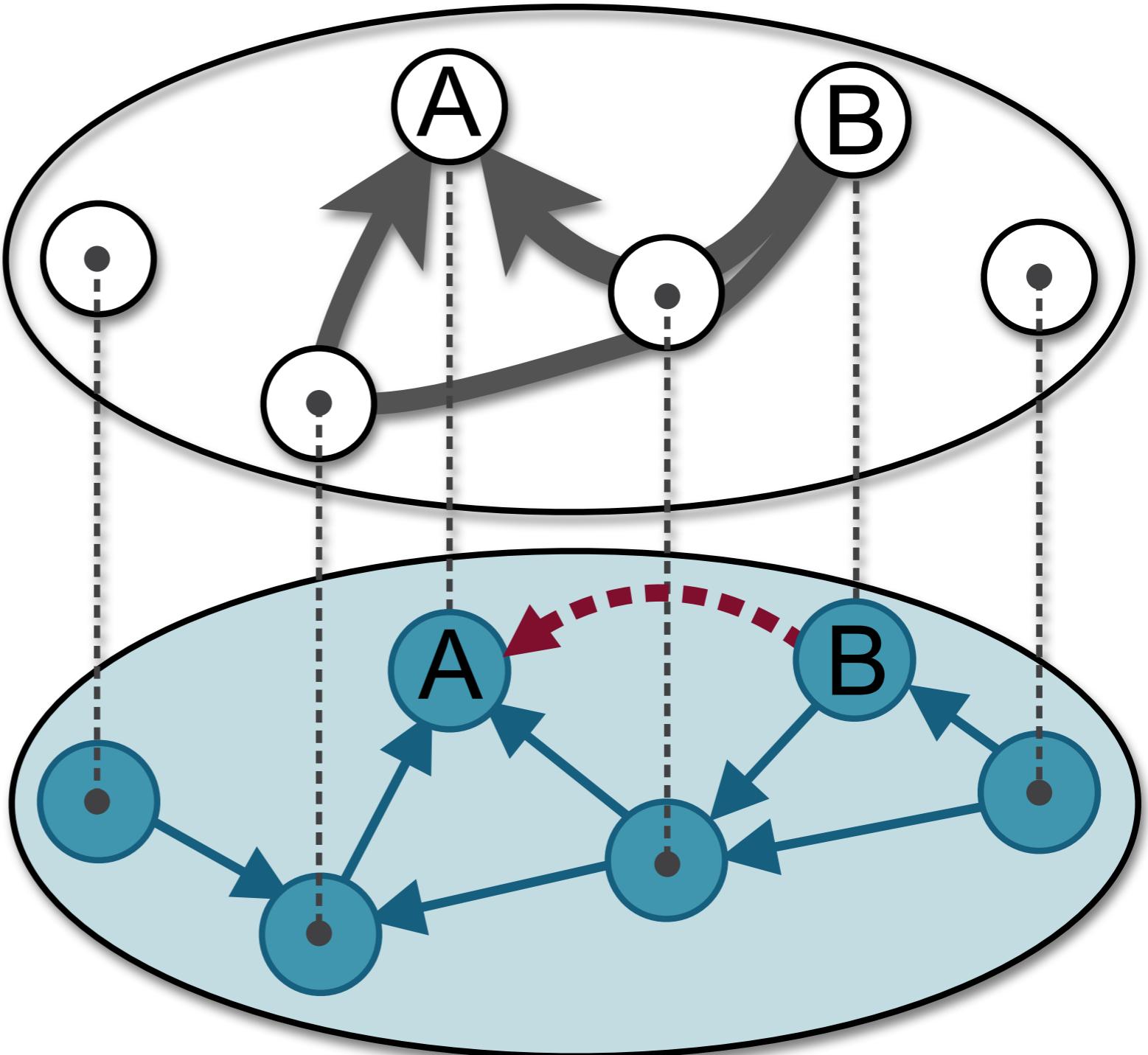
Dynamics on Network:  
Information flow



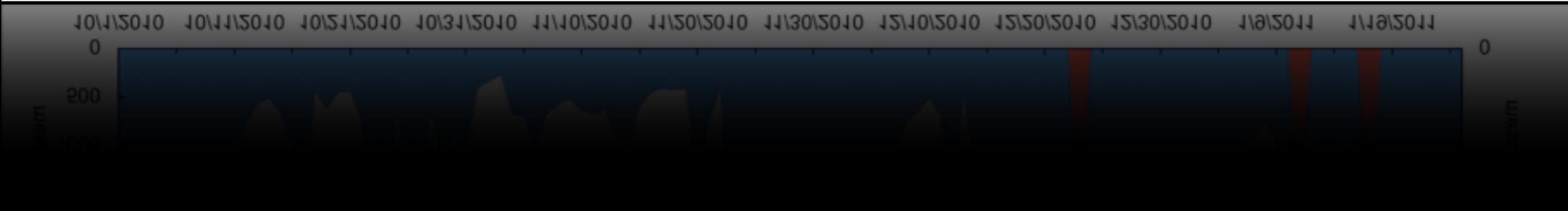
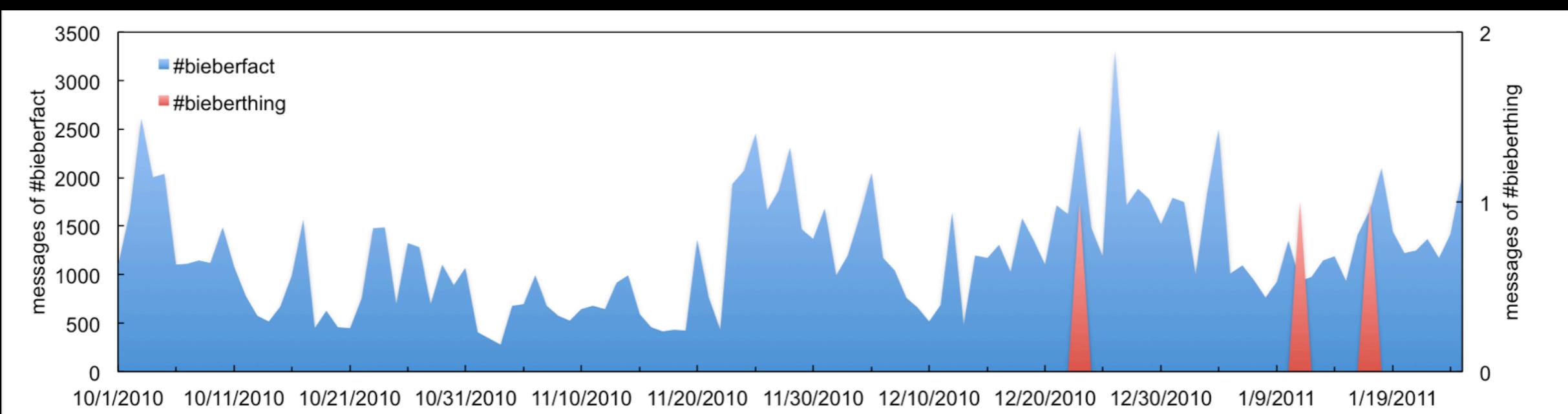
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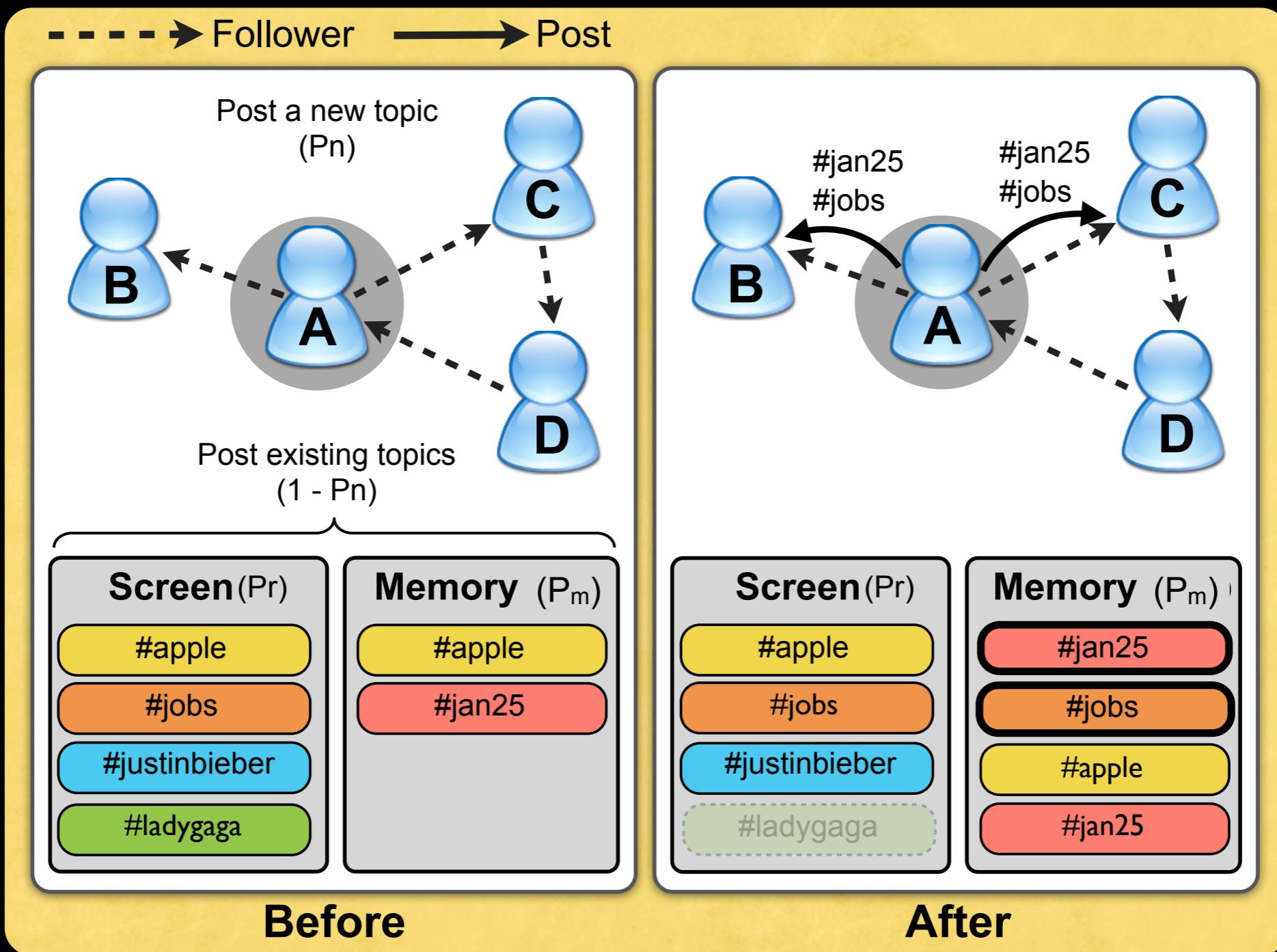
Dynamics of Network:  
Link Creation

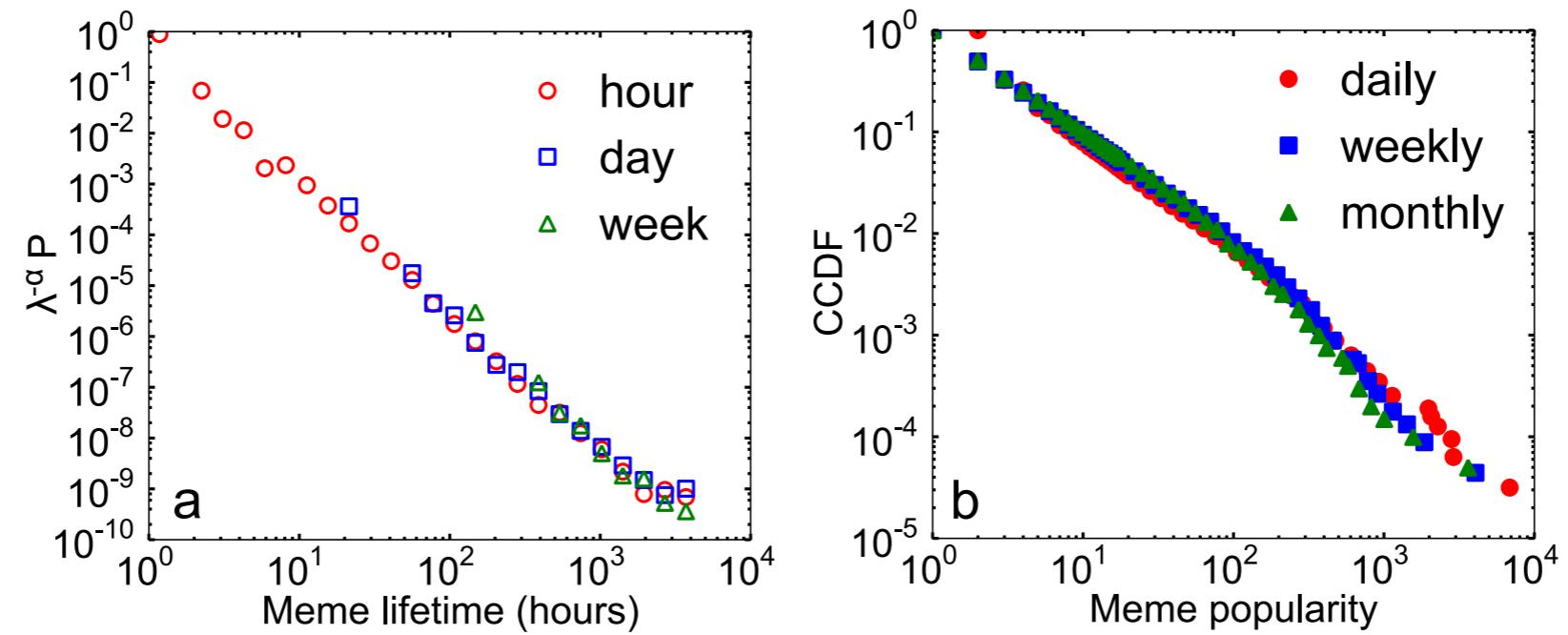


meme	popularity (number of messages)	lifetime (longest consecutive number of days)
#bieberfact	139760	145
#ieberthing	3	1

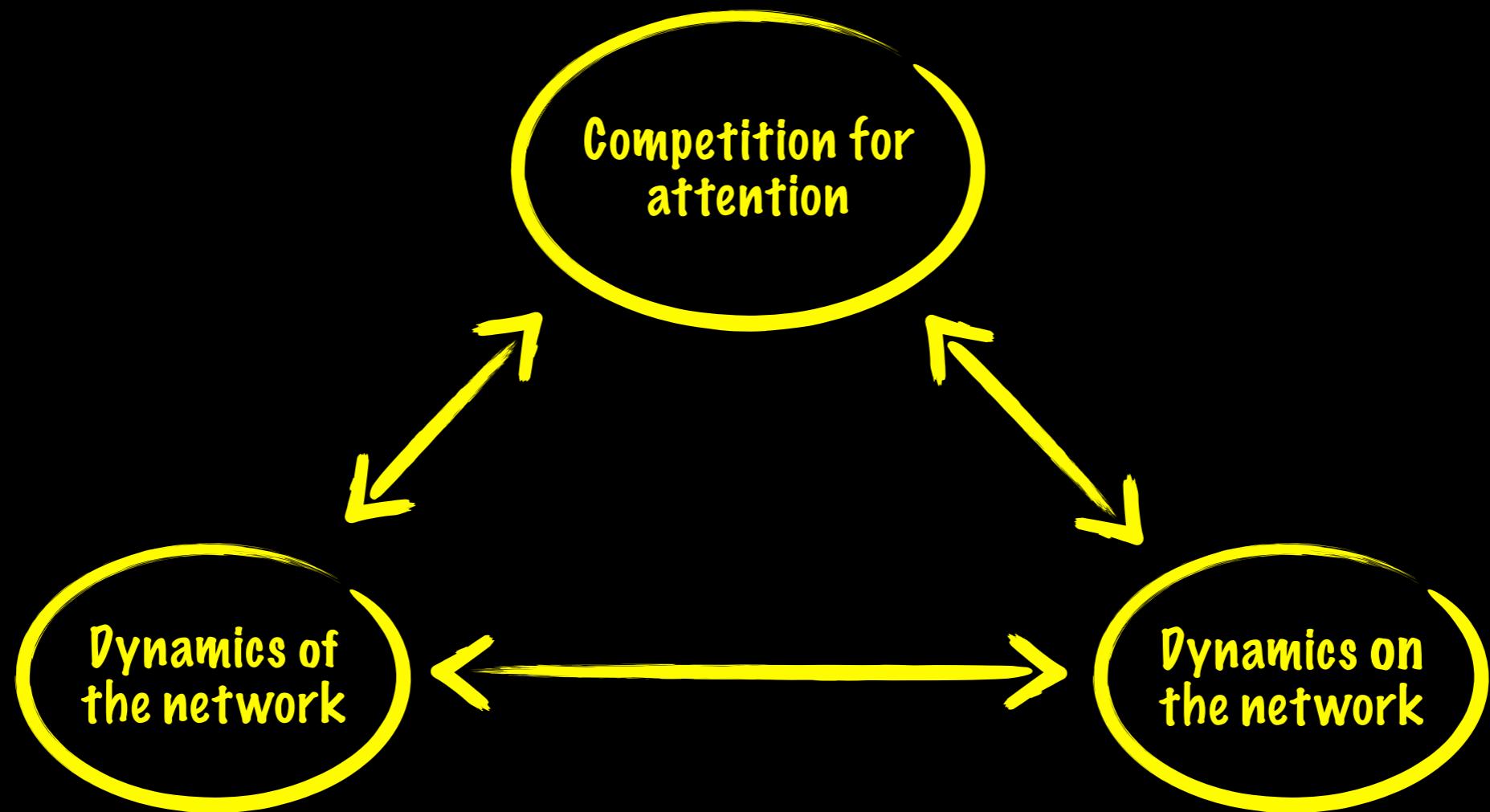


# Two key ingredients

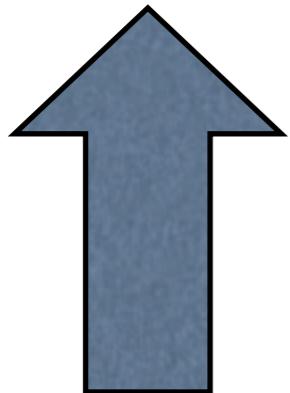




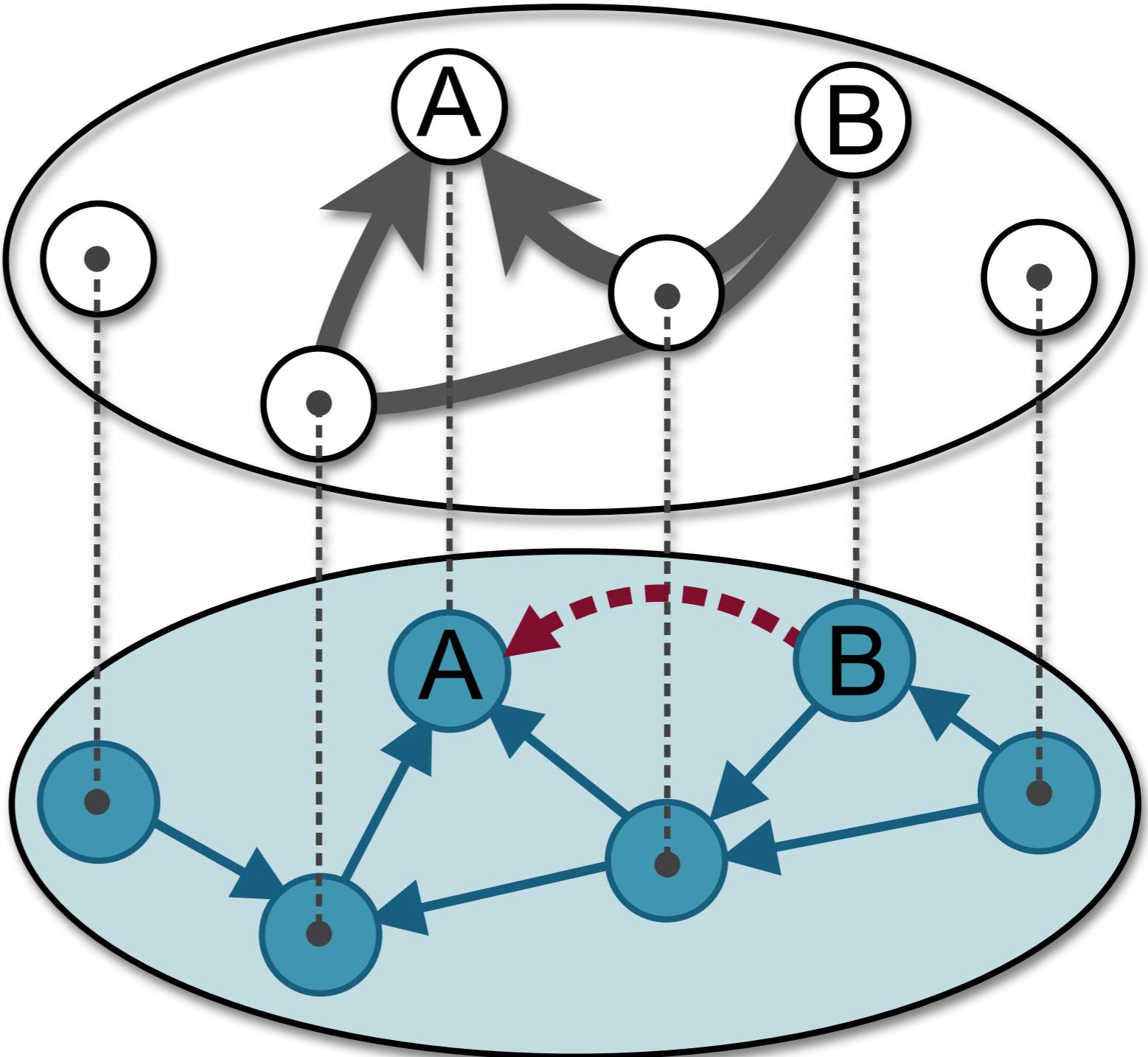
Dataset: Twitter 10% sample  
October 2010 – January 2011  
~12.5M users, ~1.3M hashtags



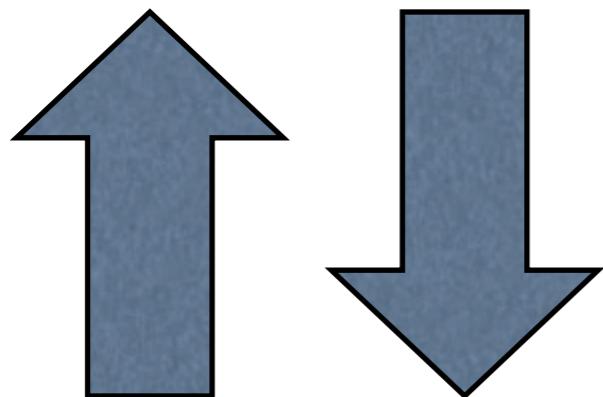
Dynamics on Network:  
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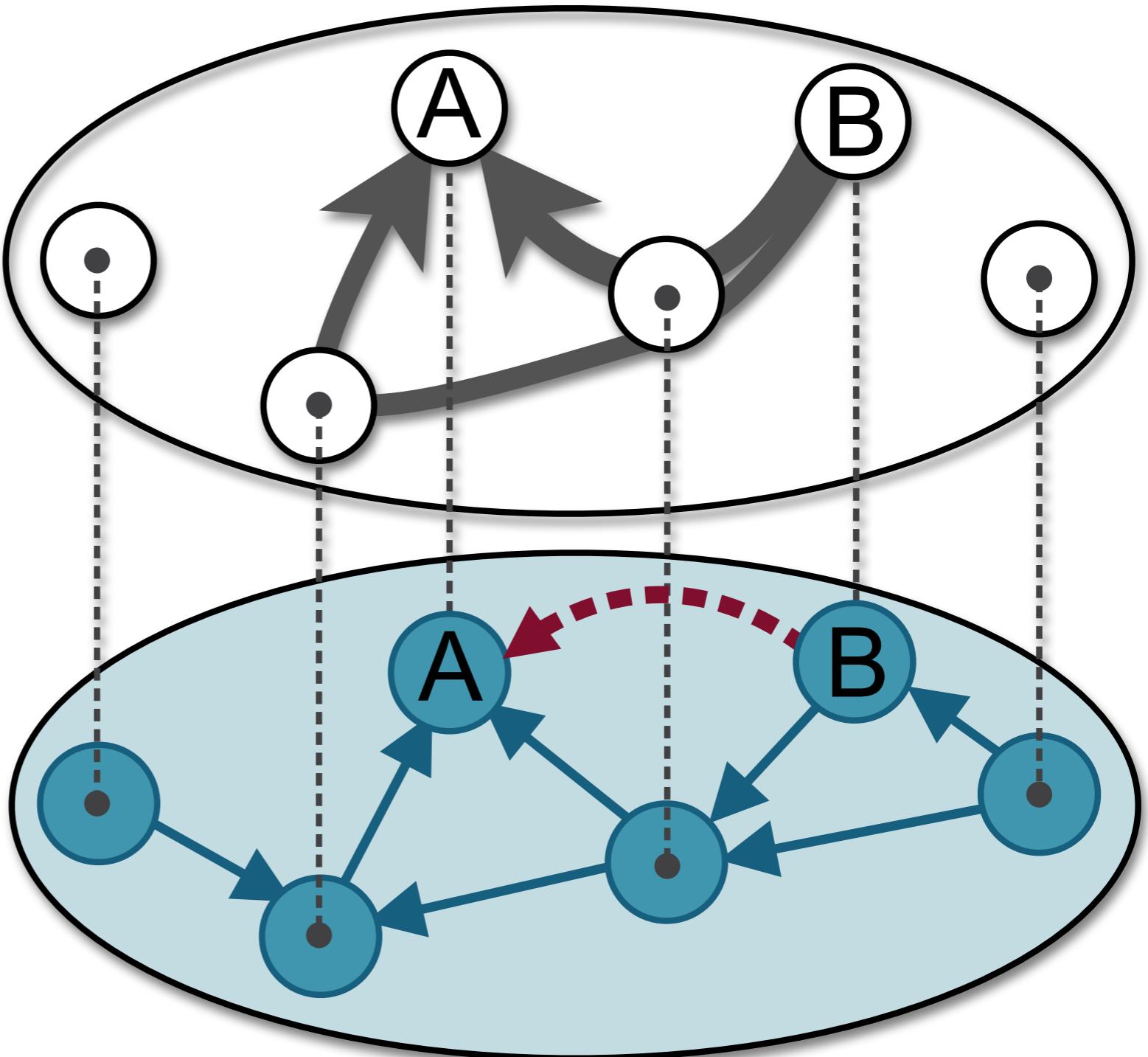
Dynamics of Network:  
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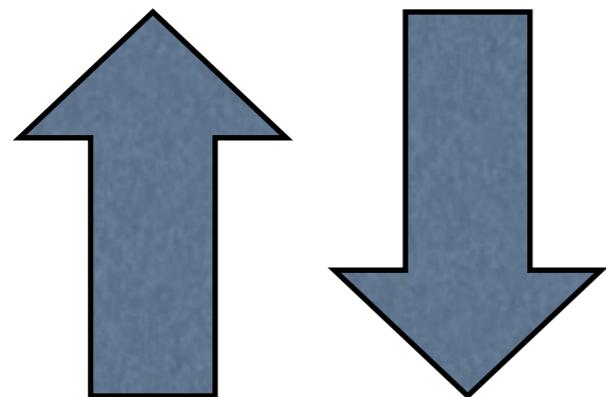
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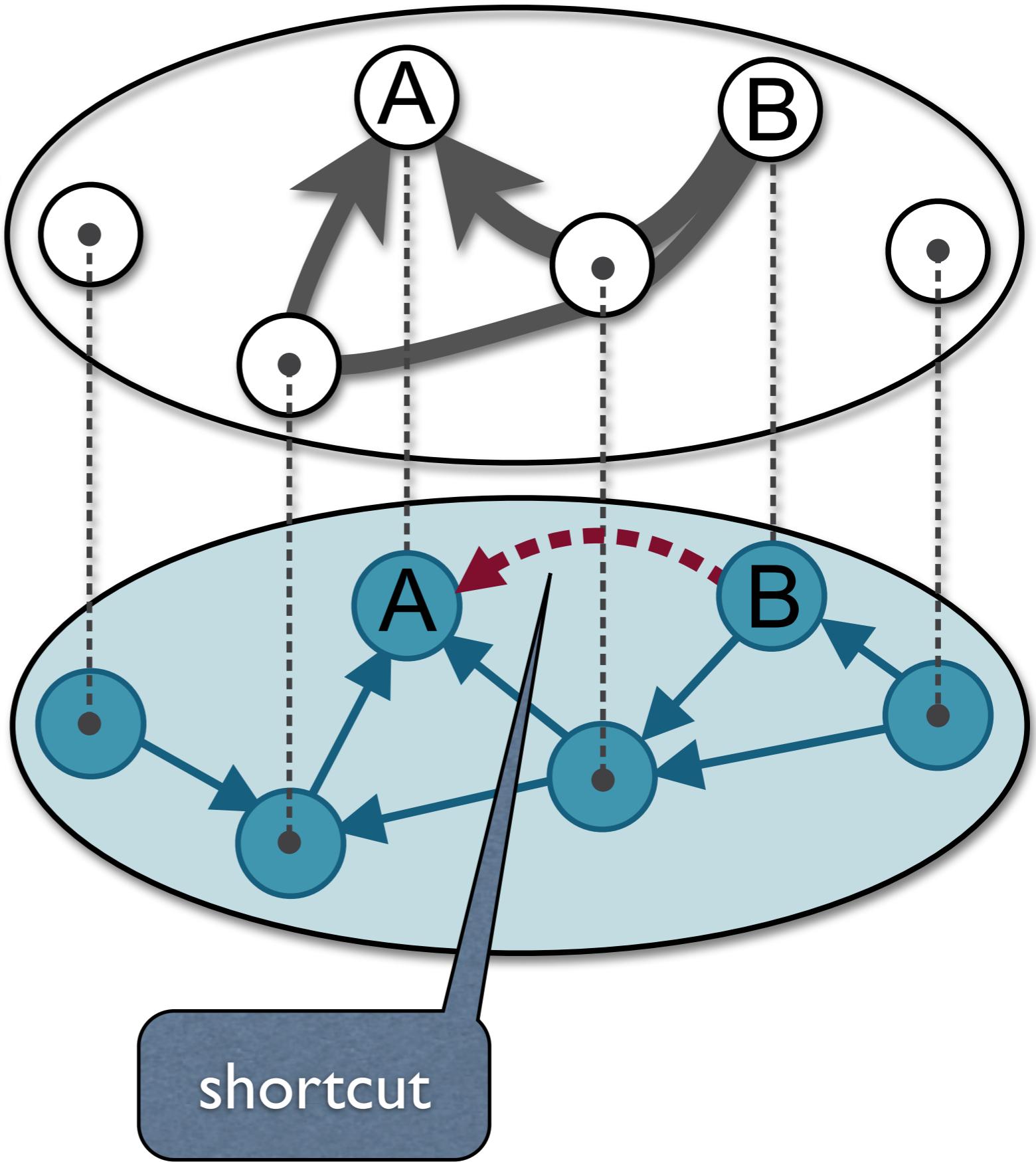
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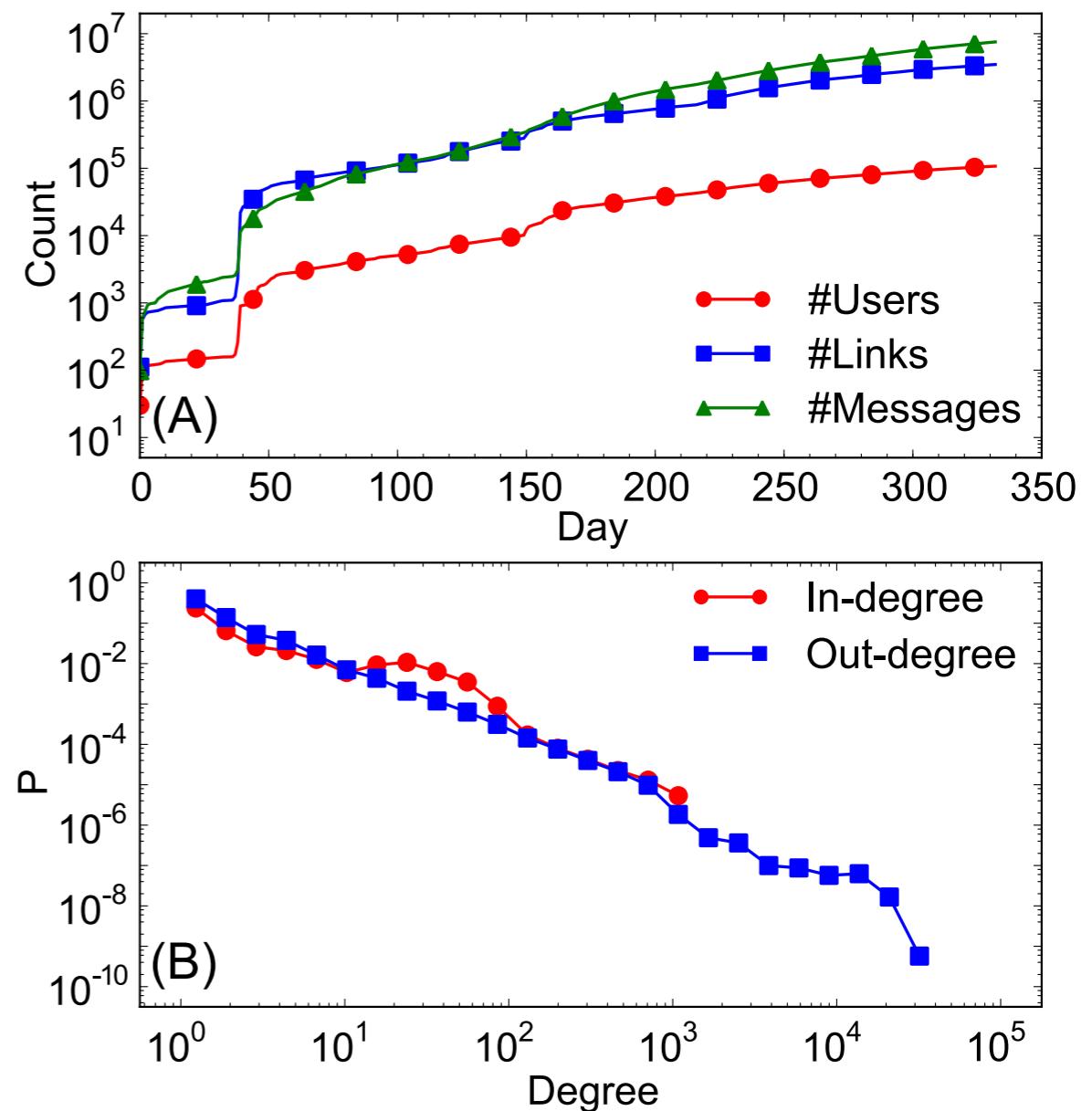


Dynamics of Network:  
Link Creation

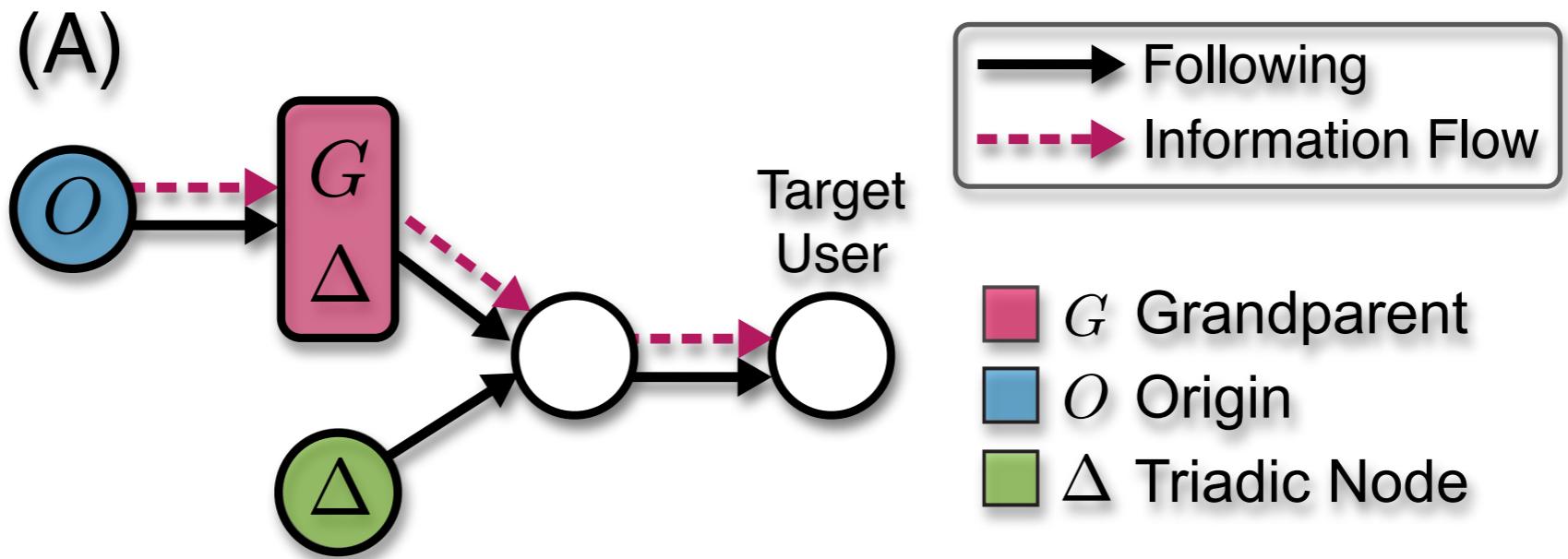


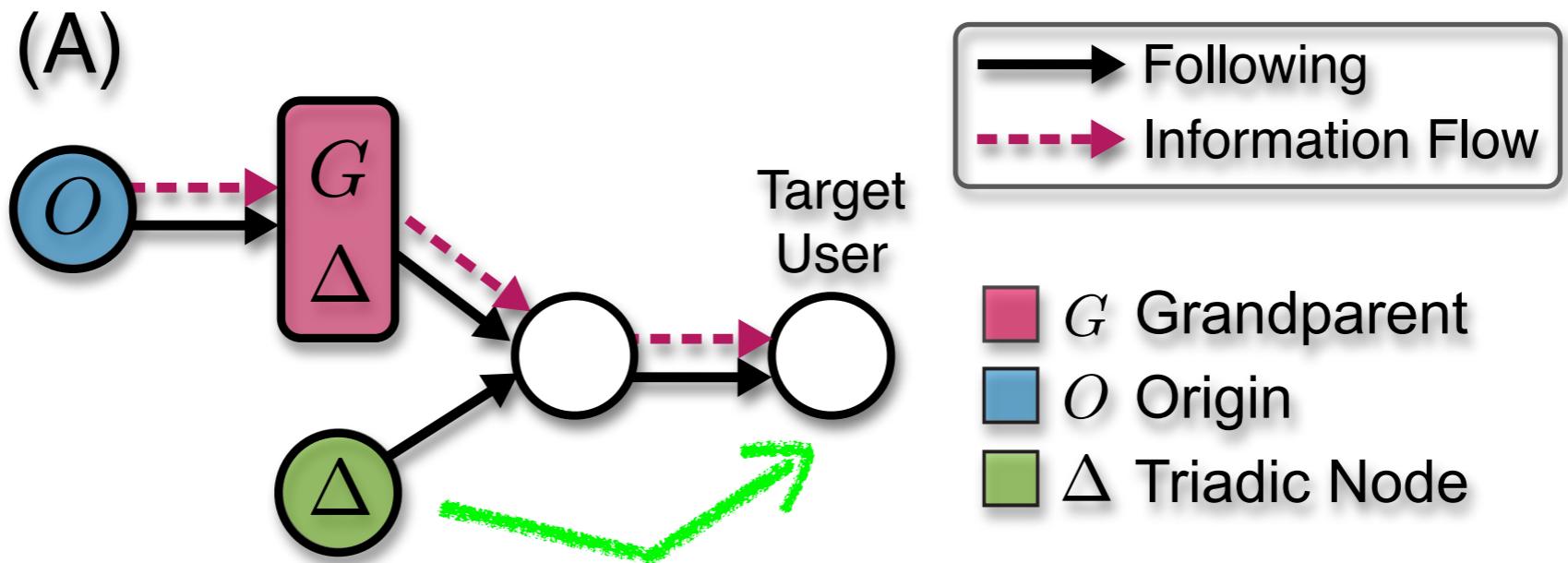
# Dataset: Yahoo! Meme

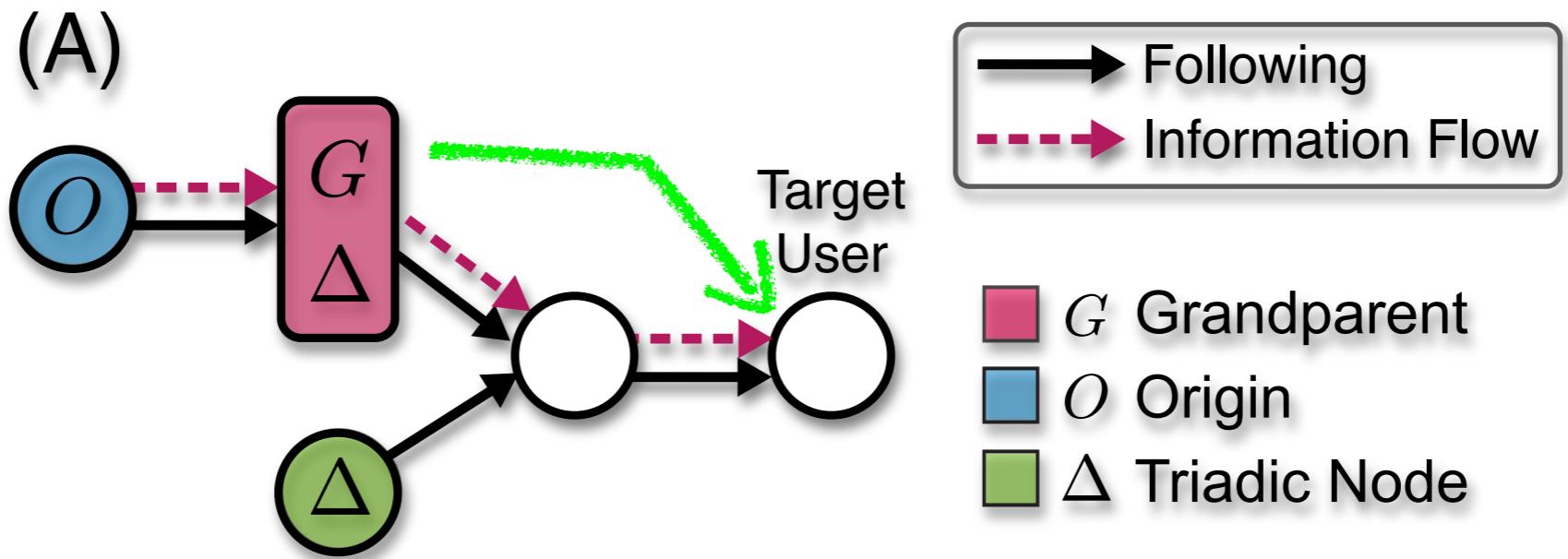
## April 2009 – March 2010

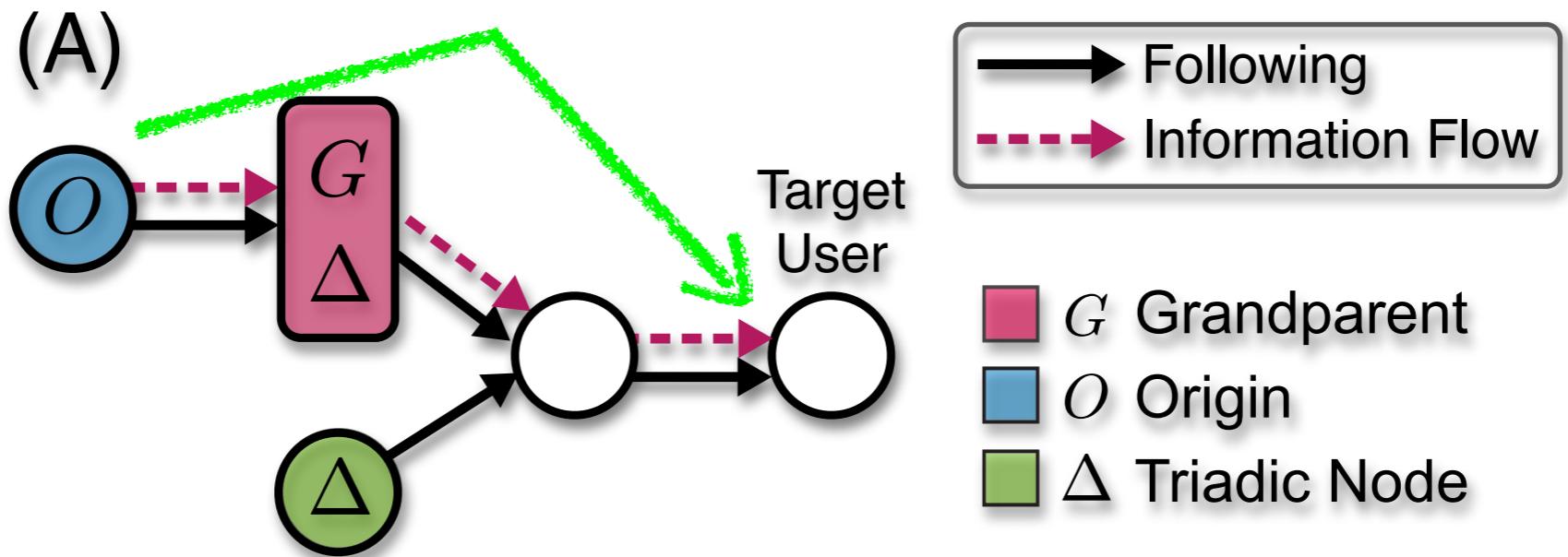


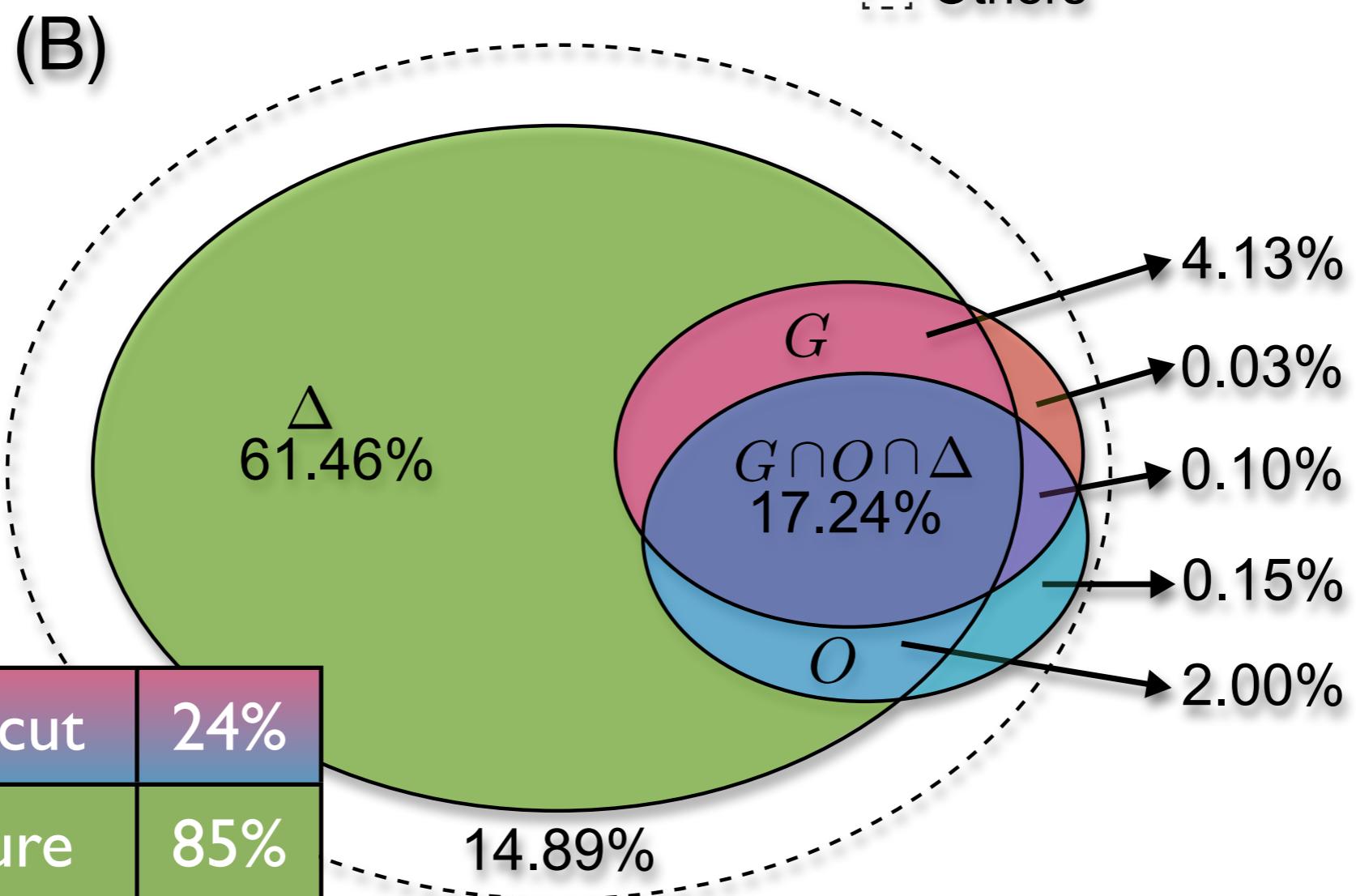
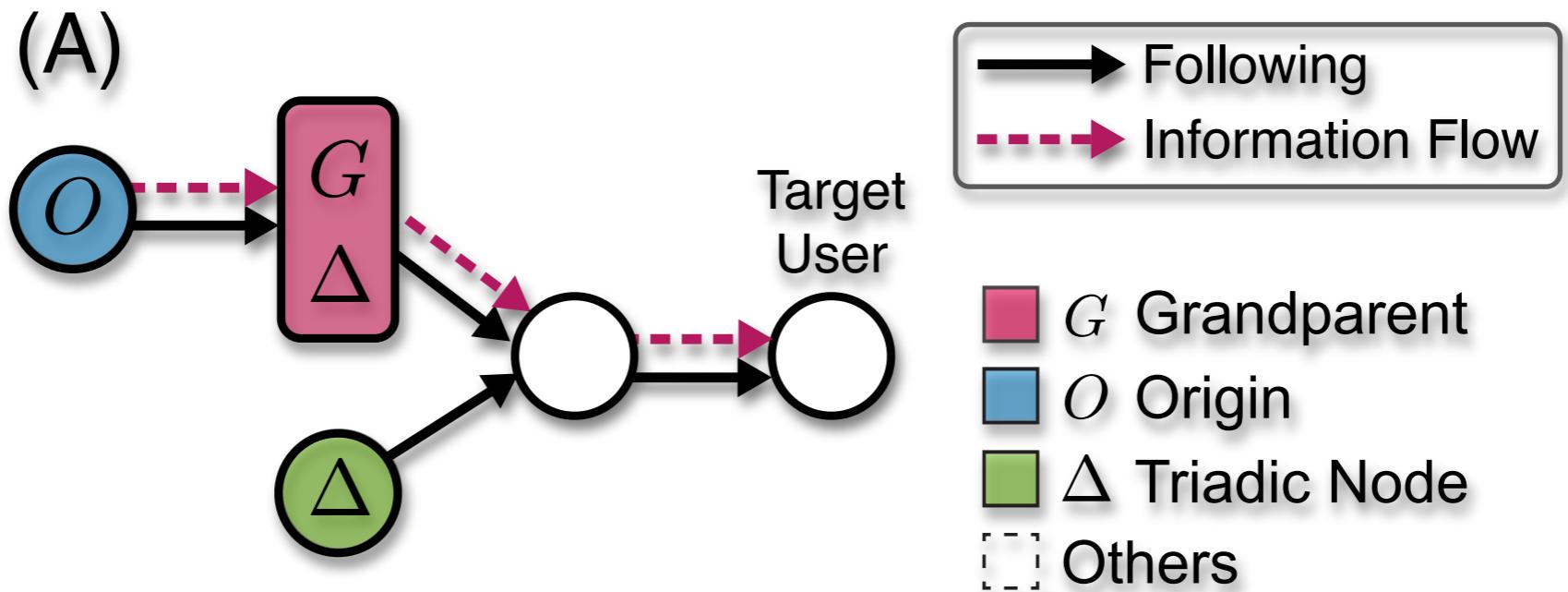
~128k users, ~3.5M links, ~7M posts











# Could this happen by chance?

$$z = \frac{S-E}{\sigma} \in \mathcal{N}(0,1)$$

# Could this happen by chance?

Actual number of links of that type in the data

Expected number of links of a certain type according to the null hypothesis (by chance). E.g., links to grandparents:

$$E_G = \sum_{\ell}^L \frac{N_G(\ell)}{N(\ell)-k(\ell)-1}$$

$$z = \frac{S-E}{\sigma} \in \mathcal{N}(0,1)$$

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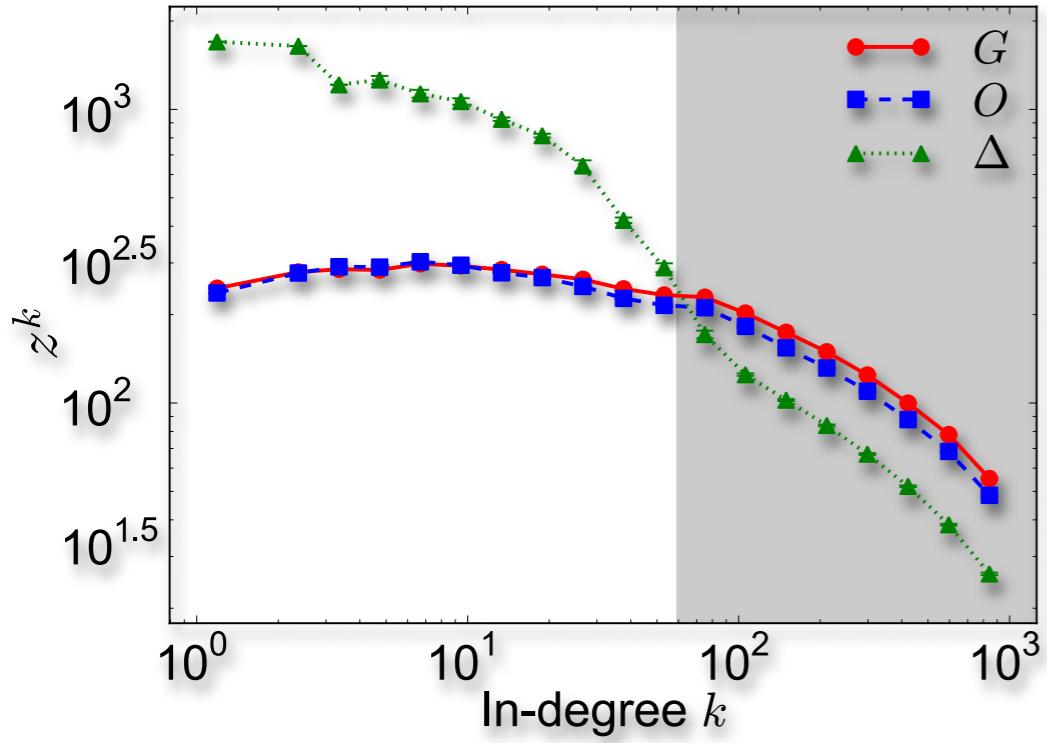
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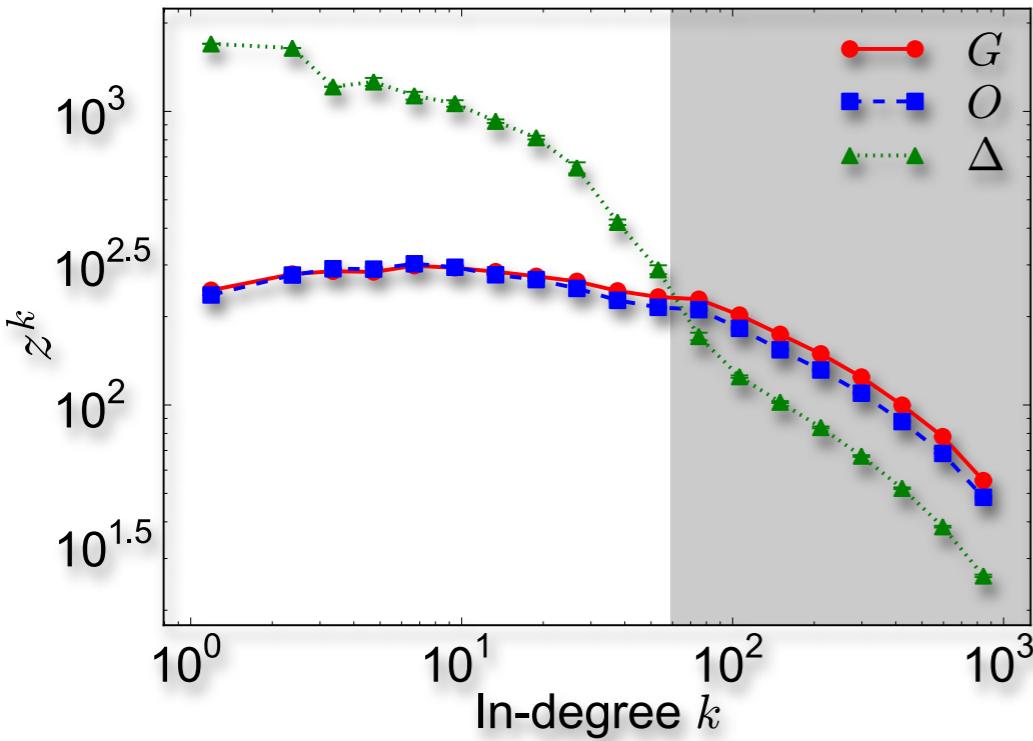
$$E_G = \sum_{\ell}^L \frac{N_G(\ell)}{N(\ell)-k(\ell)-1}$$

$$z = \frac{S-E}{\sigma} \in \mathcal{N}(0,1)$$

$z_\Delta, z_G, z_o$  very large  $\Rightarrow$  reject null hypothesis:  
links are not created randomly

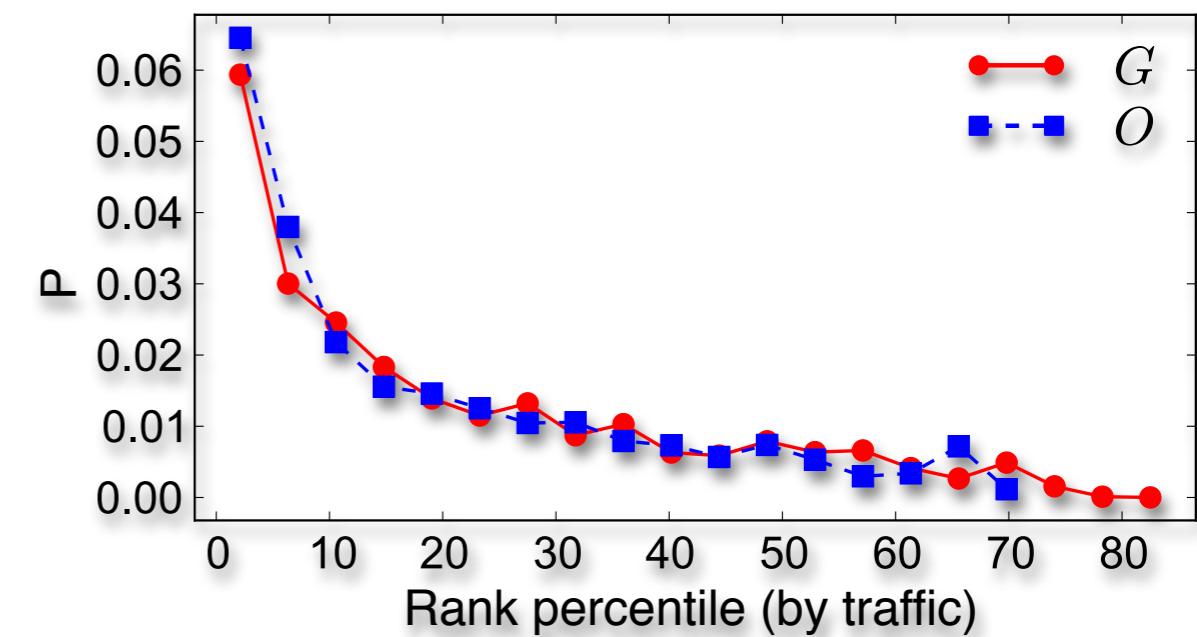


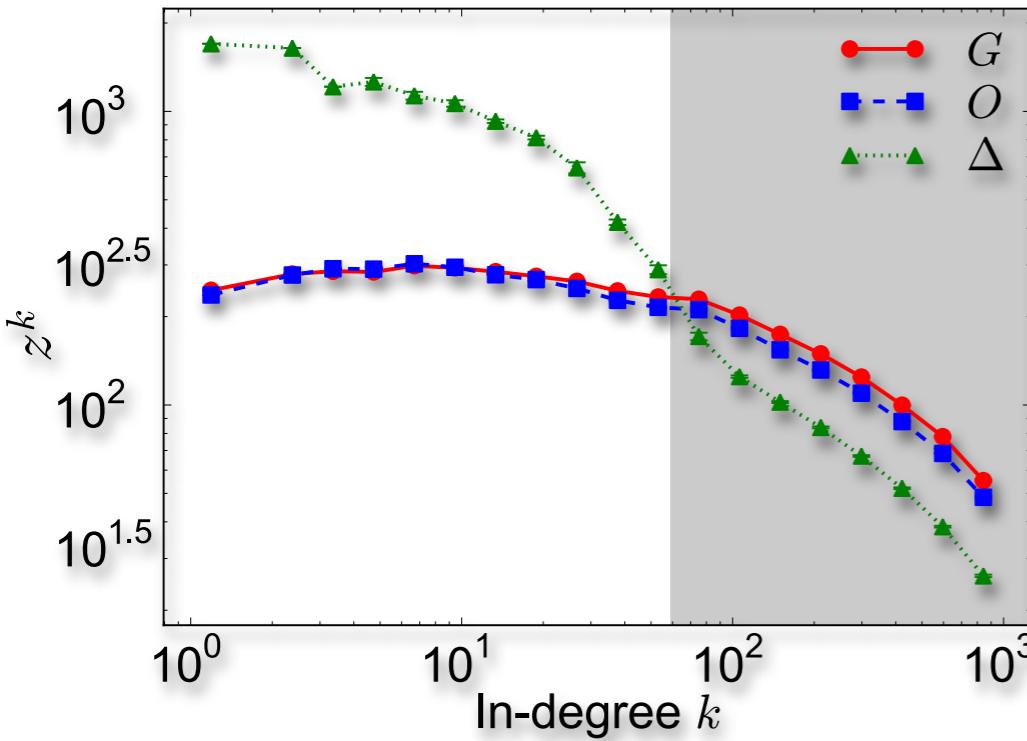
Preference for traffic-based  
shortcuts as users become  
more active



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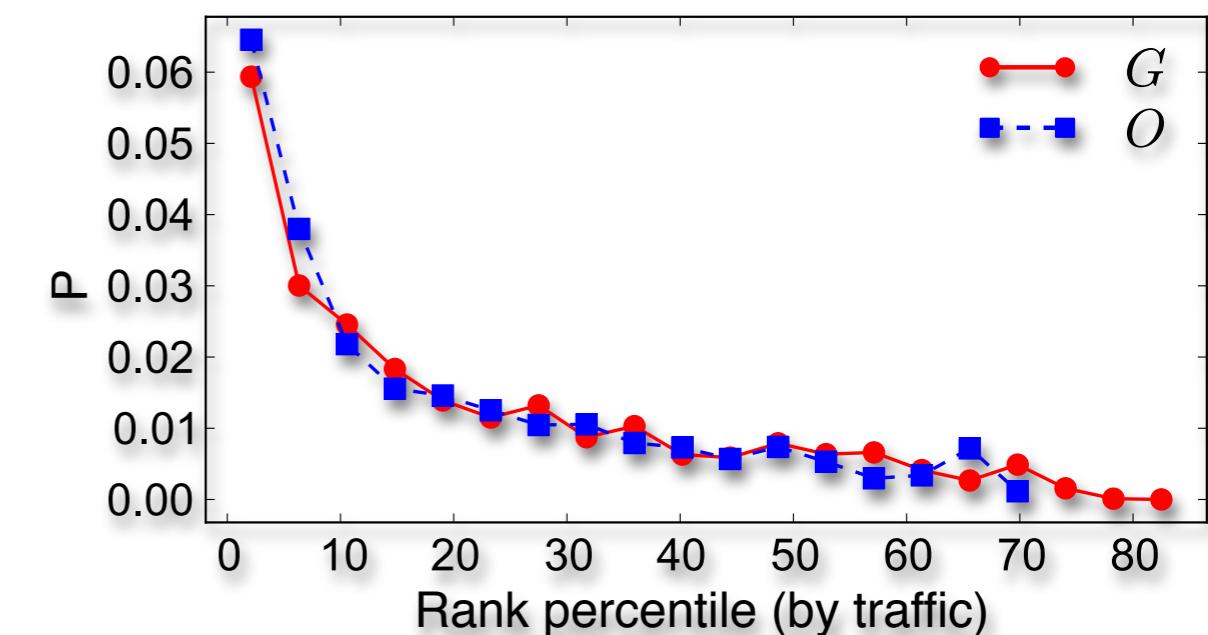
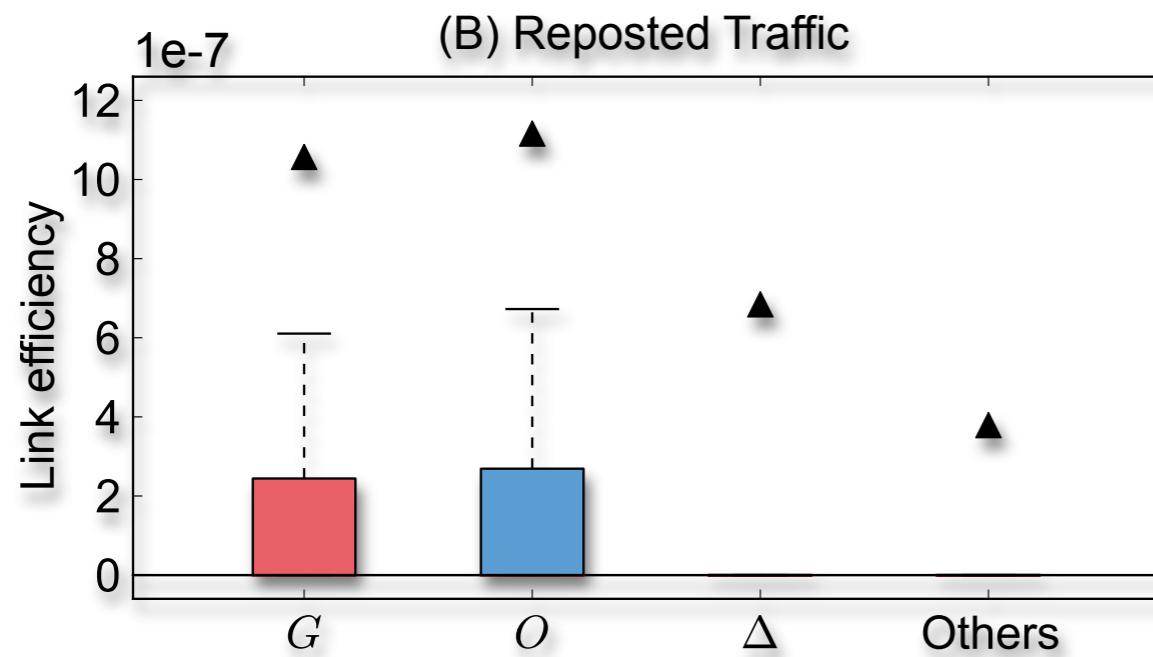
The more posts we see  
from someone, the more  
we are likely to follow them





Preference for traffic-based  
shortcuts as users become  
more active

The more posts we see  
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Shortcuts are more efficient  
at carrying messages we see  
and report

# Maximum Likelihood Estimation

# Maximum Likelihood Estimation

∀ link  $\ell$ , compute:

$f(\ell \mid \Gamma, \Theta)$  = likelihood of the target being followed by the creator according to a particular strategy  $\Gamma$ , given the network configuration  $\Theta$  at the time when  $\ell$  is created.

# Maximum Likelihood Estimation

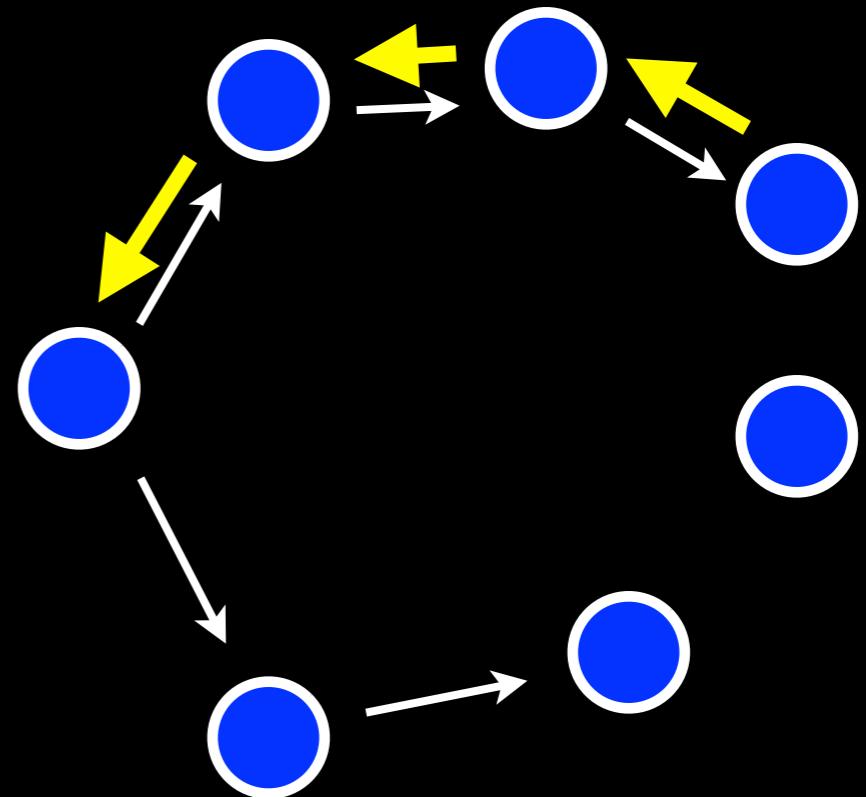
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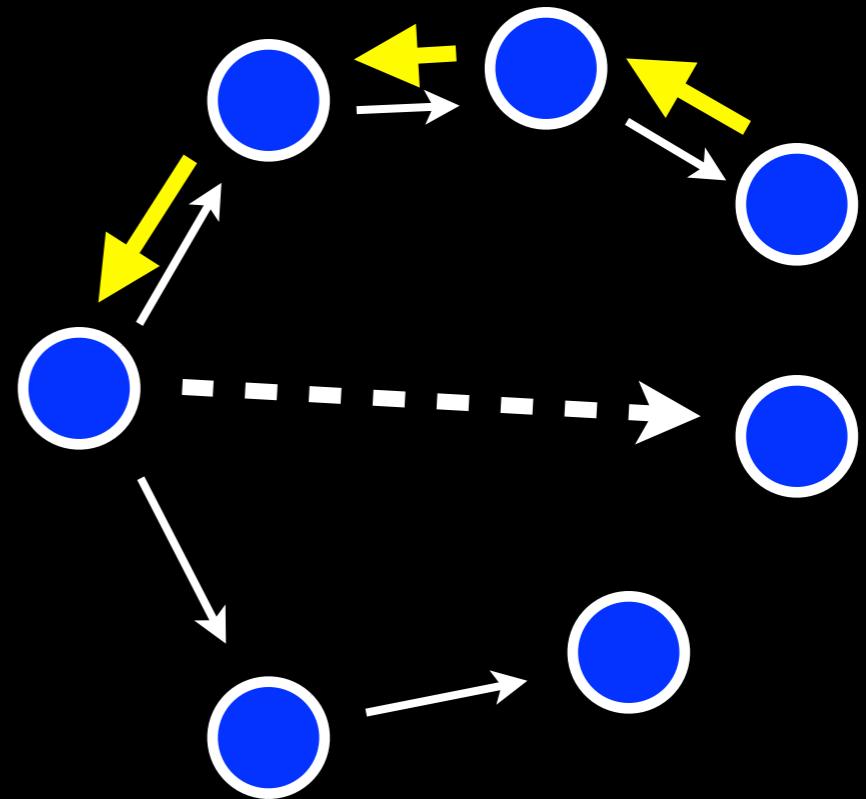
# MLE single strategies

- Random
- Triadic closure ( $\Delta$ )
- Grandparent (**G**)
- Origin (**O**)
- Traffic shortcut (**G**  $\cup$  **O**)



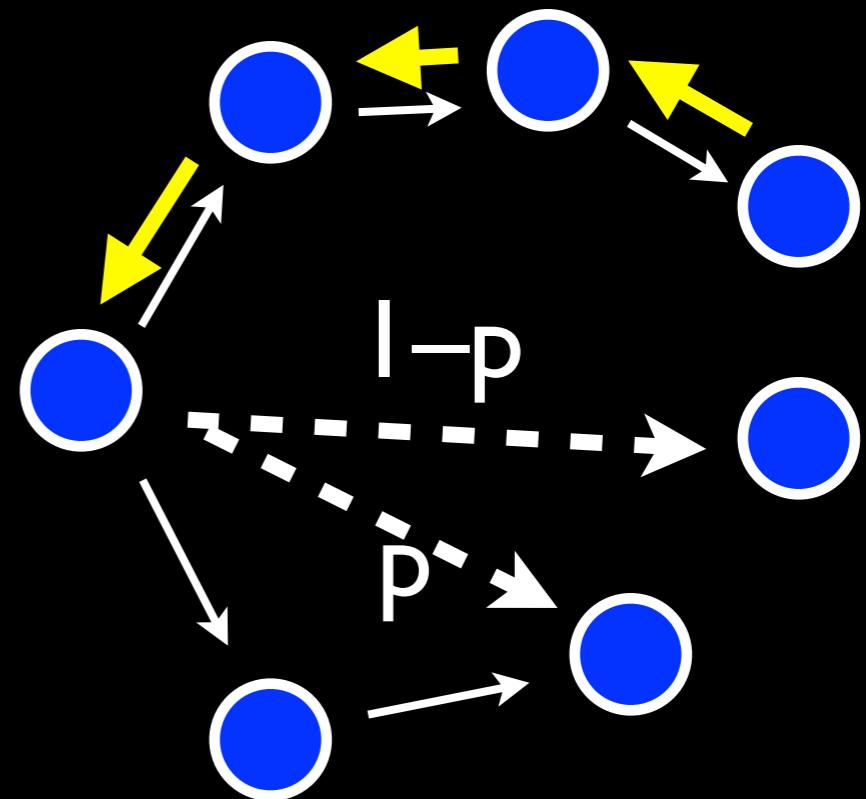
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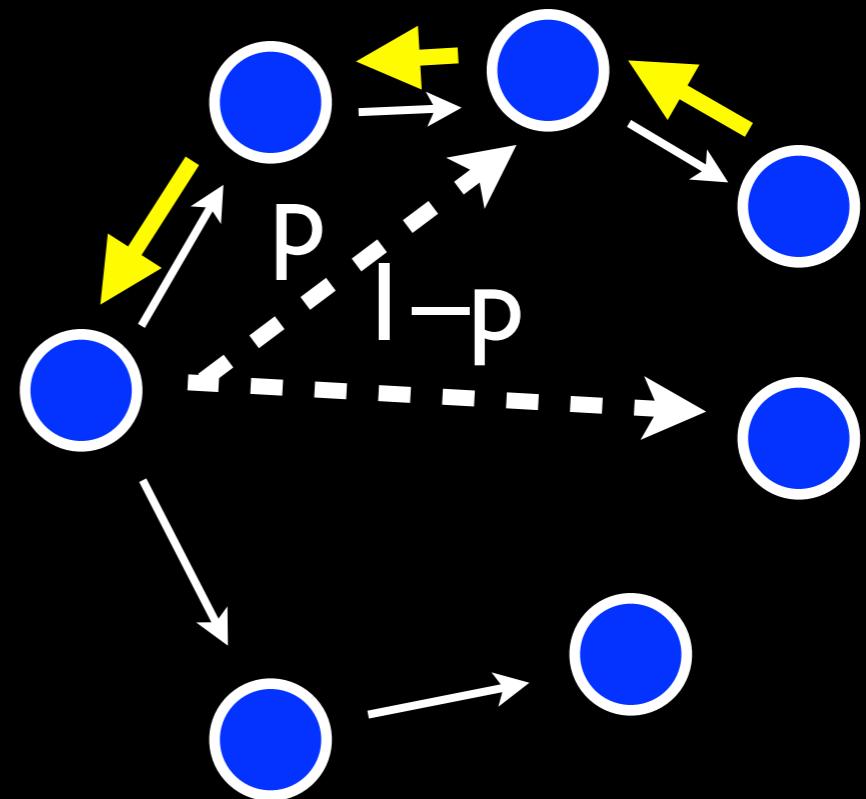
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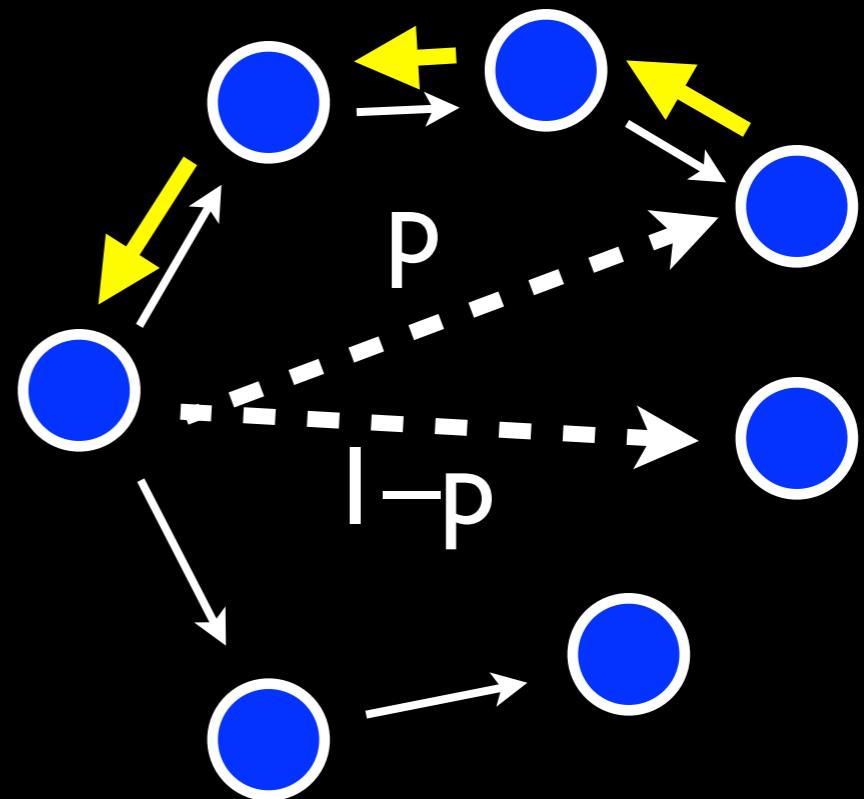
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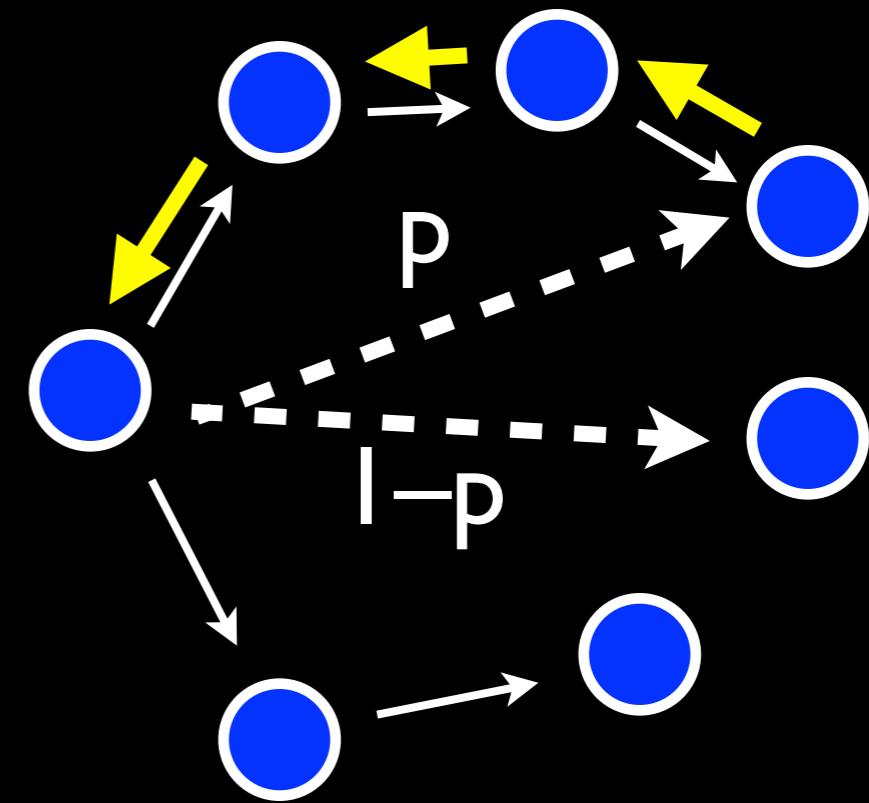
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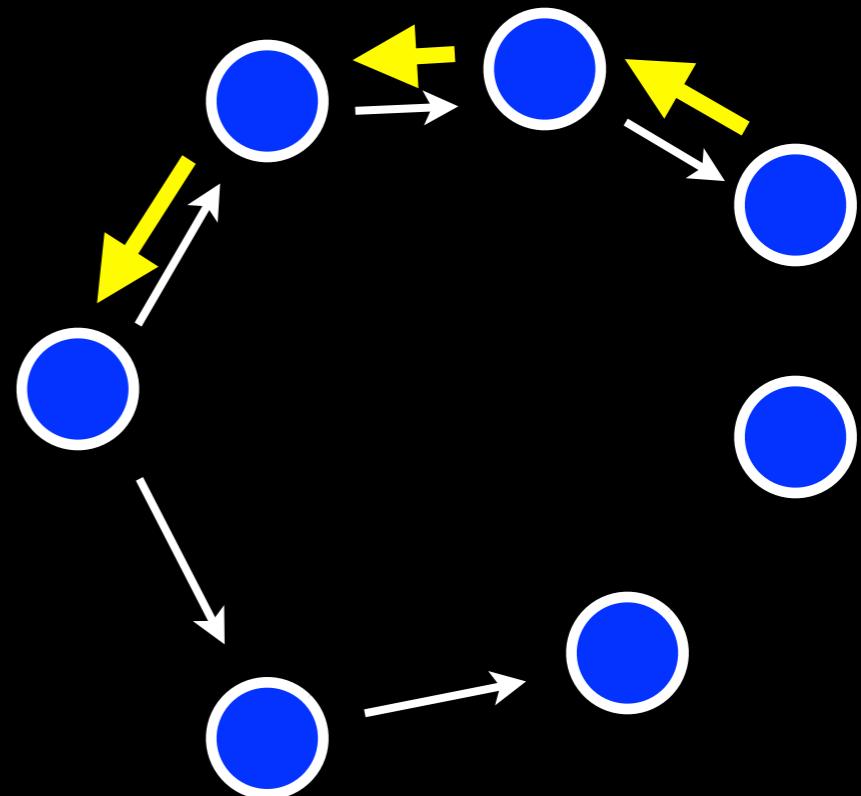


Example:

$$\log \mathcal{L}_G(p) = \sum_{\mathbf{1}_G(\ell)=1} \ln \left( \frac{p}{N_G(\ell)} + \frac{1-p}{N(\ell) - k(\ell) - 1} \right) + \sum_{\mathbf{1}_G(\ell)=0} \ln \frac{1-p}{N(\ell) - k(\ell) - 1}.$$

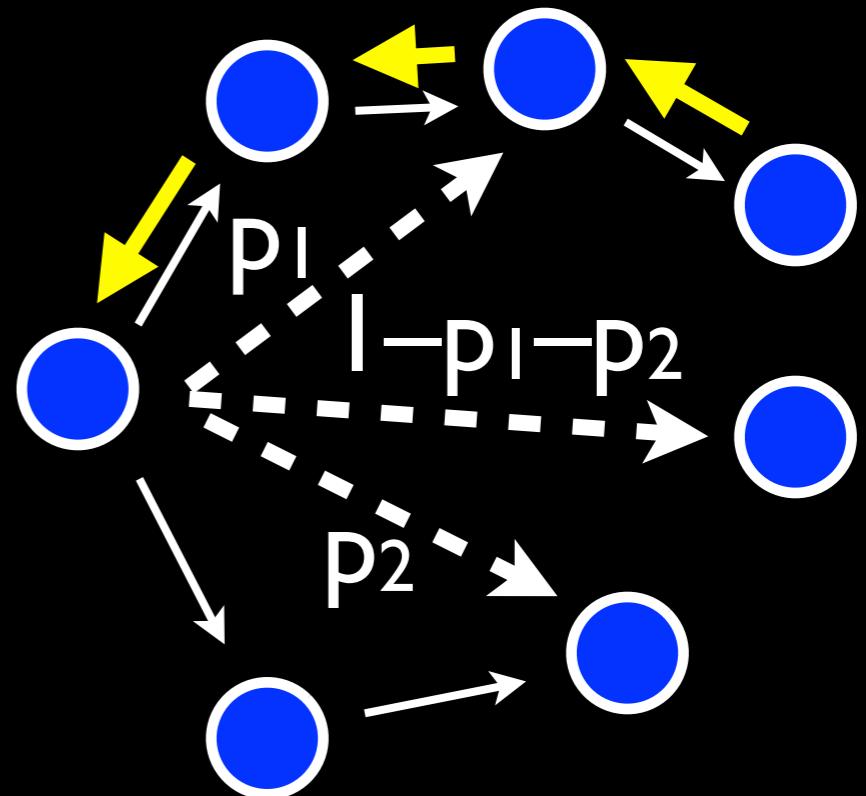
# MLE combined strategies

- Grandparent or triadic closure ( $\mathbf{G} + \Delta$ )
- Origin or triadic closure ( $\mathbf{O} + \Delta$ )
- Traffic shortcut or triadic closure ( $\mathbf{G} \cup \mathbf{O} + \Delta$ )



# MLE combined strategies

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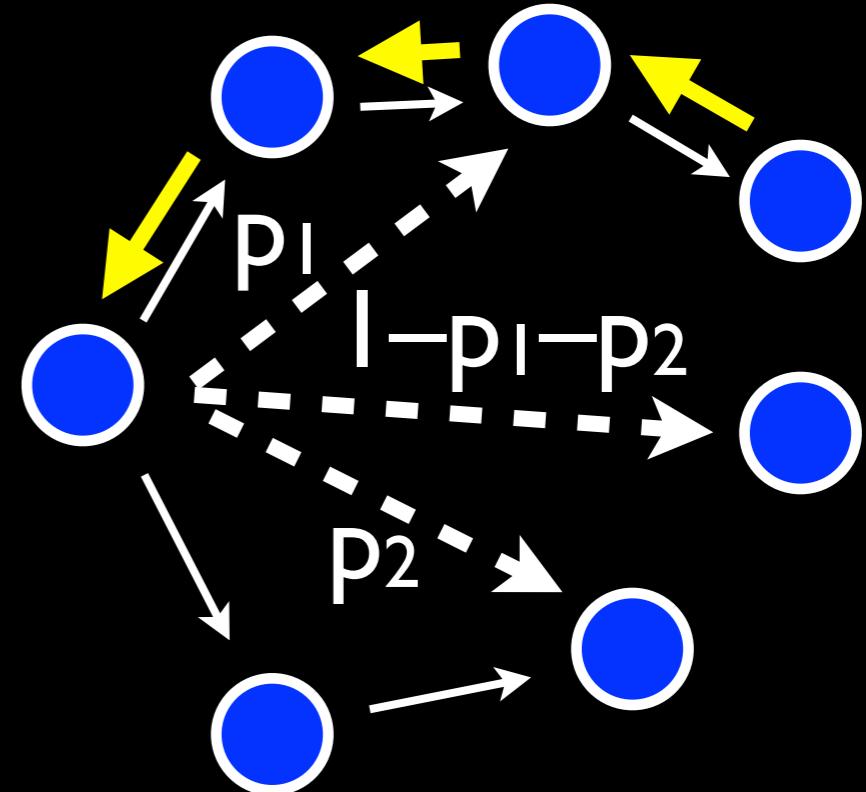


# MLE combined strategies

- Grandparent or triadic closure (**G + Δ**)
- Origin or triadic closure (**O + Δ**)
- Traffic shortcut or triadic closure (**G ∪ O + Δ**)

Example:

$$\begin{aligned} \log \mathcal{L}_{G+\Delta}(p_1, p_2) &= \log \prod_{\ell=1}^L [p_1 f(\ell|G, \Theta) + p_2 f(\ell|\Delta, \Theta) \\ &\quad + (1 - p_1 - p_2) f(\ell|\text{Rand}, \Theta)] \\ &= \sum_{\substack{1_G(\ell)=1 \\ 1_\Delta(\ell)=1}} \log \left( \frac{p_1}{N_G(\ell)} + \frac{p_2}{N_\Delta(\ell)} + \frac{1 - p_1 - p_2}{N(\ell) - k(\ell) - 1} \right) \\ &\quad + \sum_{\substack{1_G(\ell)=1 \\ 1_\Delta(\ell)=0}} \log \left( \frac{p_1}{N_G(\ell)} + \frac{1 - p_1 - p_2}{N(\ell) - k(\ell) - 1} \right) \\ &\quad + \sum_{\substack{1_G(\ell)=0 \\ 1_\Delta(\ell)=1}} \log \left( \frac{p_2}{N_\Delta(\ell)} + \frac{1 - p_1 - p_2}{N(\ell) - k(\ell) - 1} \right) \\ &\quad + \sum_{\substack{1_G(\ell)=0 \\ 1_\Delta(\ell)=0}} \log \frac{1 - p_1 - p_2}{N(\ell) - k(\ell) - 1}. \end{aligned}$$

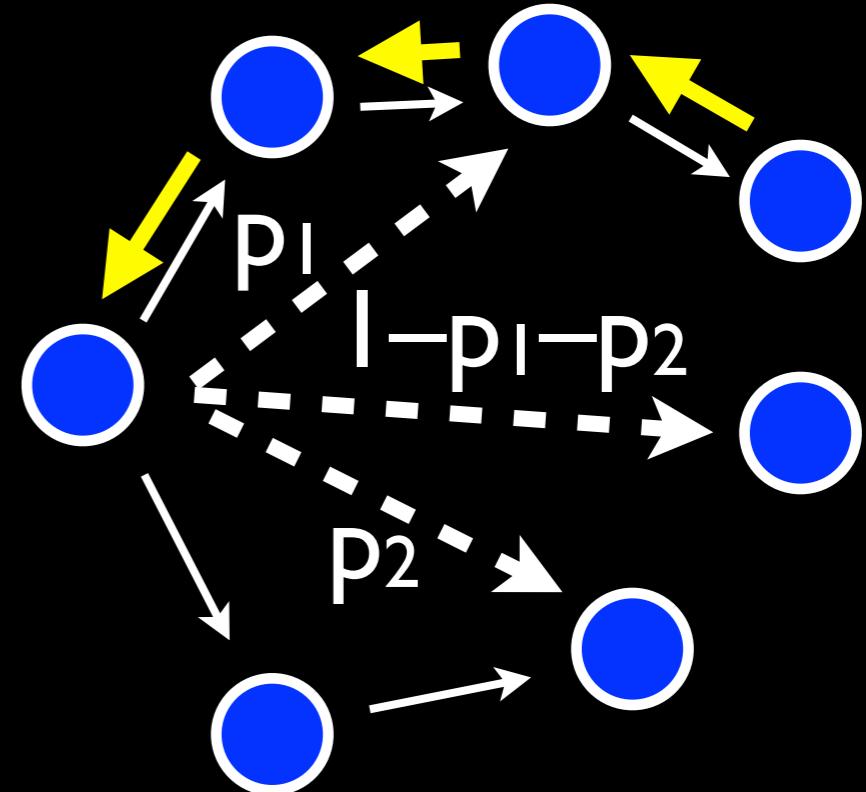


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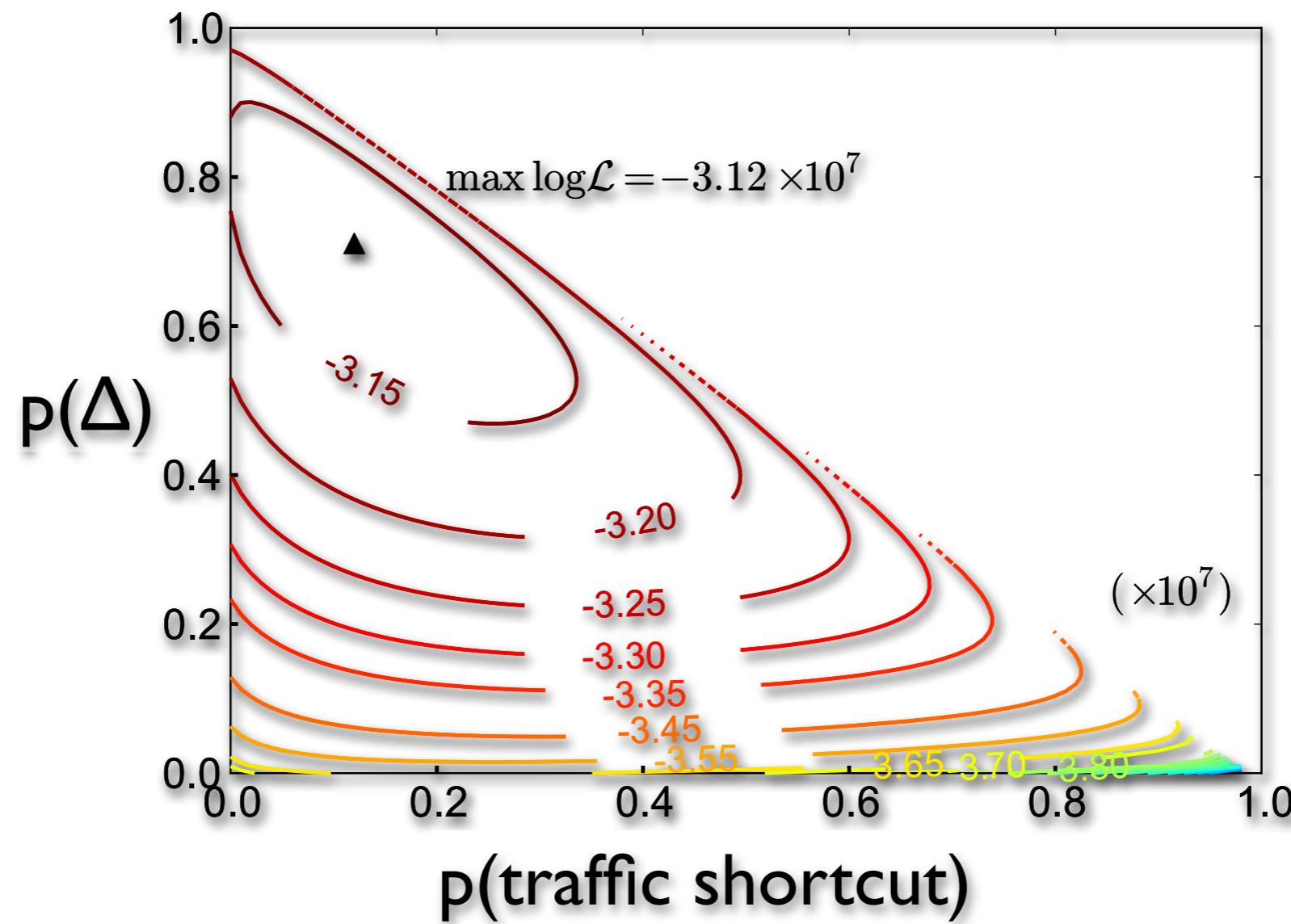
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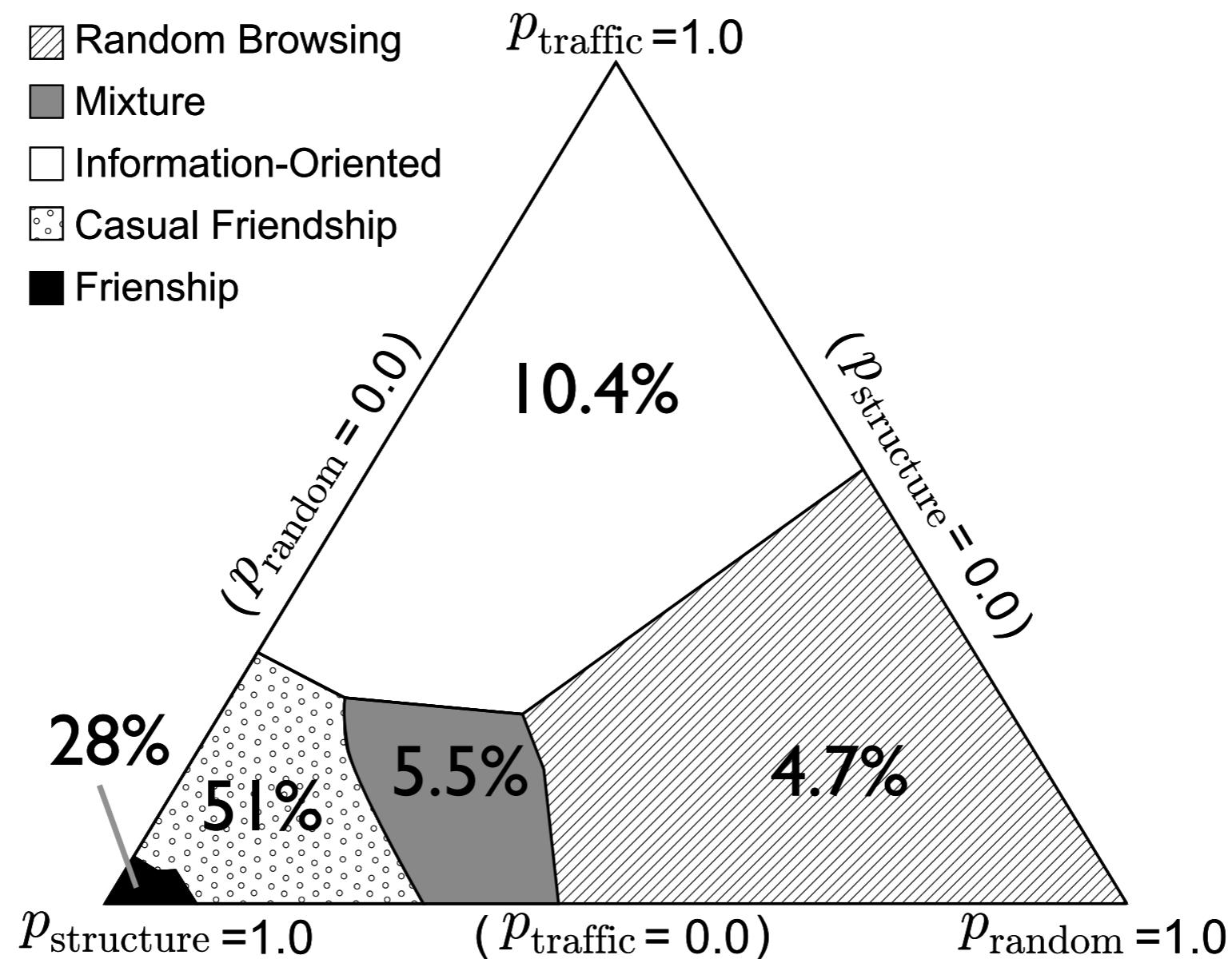
# Maximum Likelihood

**( $\mathbf{G} \cup \mathbf{O} + \Delta$ )**



# Maximum Likelihood

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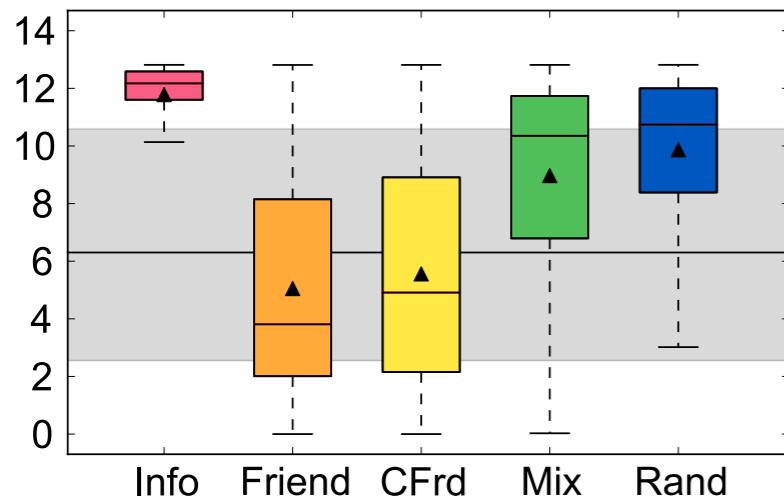


longer lived

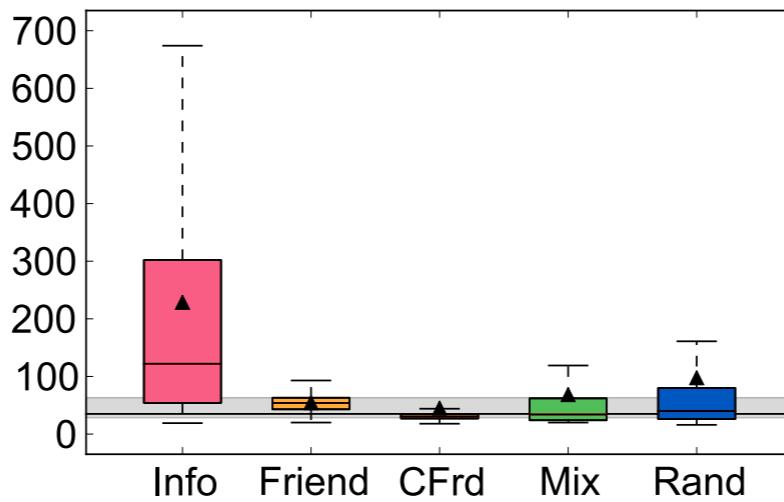
follow more

more  
followers

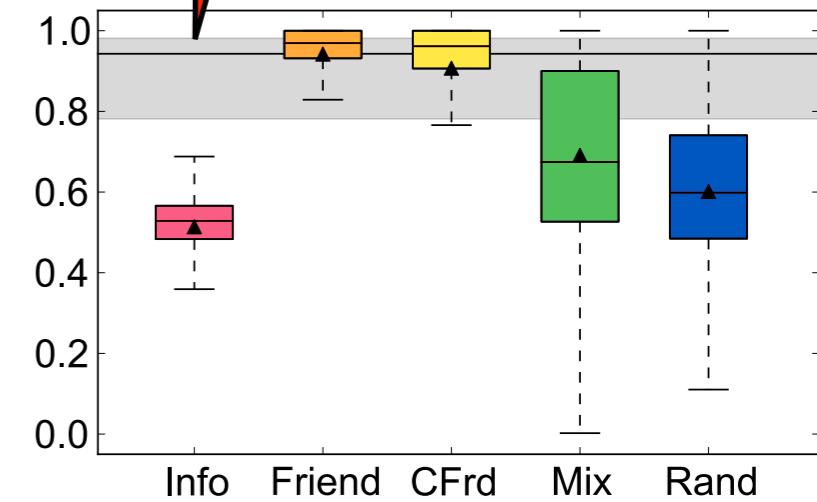
(D) Lifetime



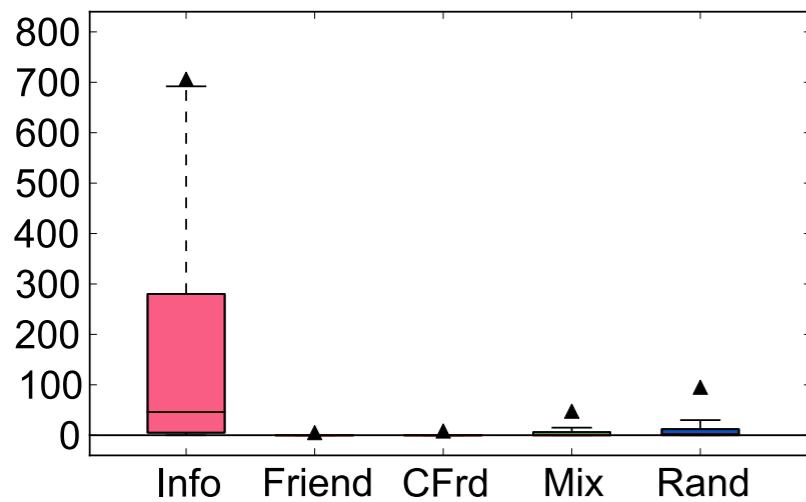
(E) In-degree



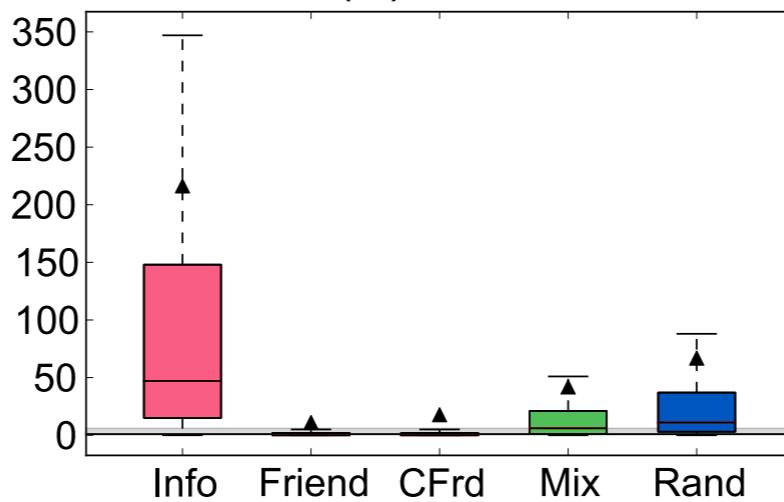
(F) In-degree ratio



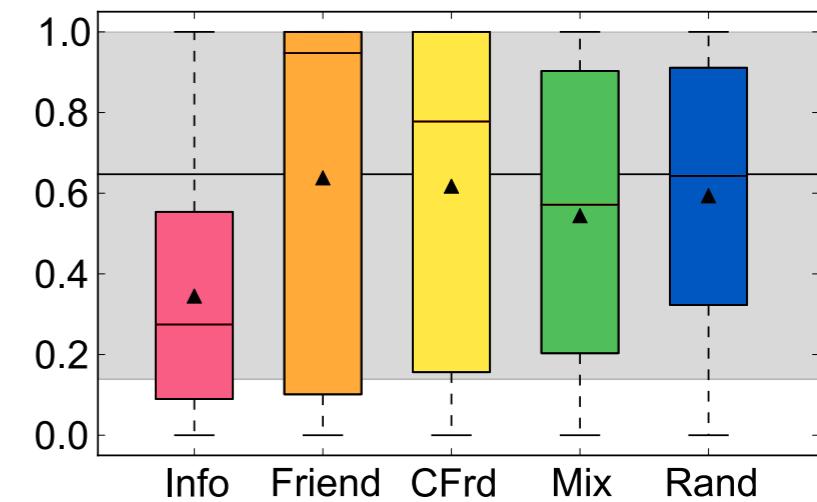
(G) Reposted



(H) Posts



(I) Post ratio



influential

active

spreaders



As users become more active, more popular, and more influential, they make the network more “efficient” by shortening the distance between producers and consumers of information.



Lilian Weng<sup>1</sup>, Jacob Ratkiewicz<sup>2</sup>, Nicola Perra<sup>3</sup>, Bruno Gonçalves<sup>4</sup>, Carlos Castillo<sup>5</sup>, Francesco Bonchi<sup>6</sup>, Rossano Schifanella<sup>7</sup>, Filippo Menczer<sup>1</sup>, Alessandro Flammini<sup>1</sup>

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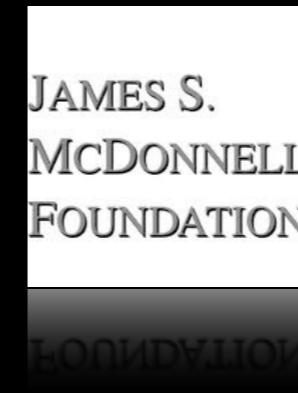
<sup>3</sup>Laboratory for the Modeling of Biological and Socio-technical Systems, Northeastern University, USA

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<sup>7</sup>Department of Computer Science, University of Torino, Italy

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