

**Do backpropagation, compute loss, and optimize parameters of the following functions for 5 steps (iterations):**

$$W*3x + 4b; gt = 12; W=-2, b=2, x=1;$$

$$W*5x + 2b; gt = 10; W=4, b=-3, x=-1;$$

$$W*4x - b; gt = 15; W=5, b=-1, x=2;$$

$$W*x + 3b; gt = 20; W=6, b=1, x=2;$$

$$W*7x - 4b; gt = 29; W=15, b=10, x=-2;$$

$W * 4x - b$ ;  $gt = 15$ ;  $W = 5$ ;  $b = -1$ ;  $x = 2$ ;

**Prediction** :  $W * 4x - b = 41$

**Iteration #1 :**

MeanSquaredError :  $(prediction - gt) ** 2 = 676$

*Prediction : 41    Loss : 676*

**Optimization step :**

$w1 = w0 - \alpha * w0.grad(\text{from backpropagation}) = 5 - 0.1 * (40) = 1$

$w1 = 1$

**Optimization step :**

$b1 = b0 - \alpha * b0.grad(\text{from backpropagation}) = -1 - 0.1 * (-10) = 0$

$b1 = 0$

**Iteration #2 :**

MeanSquaredError :  $(prediction - gt) ** 2 = 4$

*Prediction : 8    Loss : 49*

**Optimization step :**

$w1 = w0 - \alpha * w0.grad(\text{from backpropagation}) = 1 - 0.1 * (-10) = 2$

$w1 = 2$

**Optimization step :**

$b1 = b0 - \alpha * b0.grad(\text{from backpropagation}) = 0 - 0.1 * (-20) = 2$

$b1 = 2$

**Iteration #3 :**

MeanSquaredError :  $(prediction - gt) ** 2 = 244$

*Prediction : 16    Loss : 244*

$w * 7x - 4b ; \quad \quad \quad gt = 29 ; \quad W = 15 ; \quad b = 10 ; \quad x = -2 ;$

**Prediction :**

$$w * 7x - 4b \Rightarrow 15 * 7 * (-2) - 4 * 10 = -250$$

**Iteration #1 :**

$$\text{MeanSquaredError} : (\text{prediction} - \text{gt}) ** 2 = (-250 - 29) ** 2 = 77,841$$

*Prediction : -250    Loss : 77,841*

**Optimization step :**

$$w1 = w0 - \text{alpha} * w0.\text{grad}(\text{from backpropagation})$$

$$w1 = 15 - 0.1 * 170 = -2$$

**Optimization step :**

$$b1 = b0 - \text{alpha} * b0.\text{grad}(\text{from backpropagation})$$

$$b1 = 10 - 0.1 * 100 = 0$$

$$\text{MeanSquaredError} : (\text{prediction} - \text{gt}) ** 2 = (28 - 29) ** 2 = 1$$

*Prediction : 28    Loss : 1*

$$w * 3x + 4b ; \quad \quad \quad gt = 12 ; \quad W = -2 ; \quad b = 2 ; \quad x = 1 ;$$

**Prediction :**

$$w * 7x - 4b \Rightarrow 2$$

**Iteration #1 :**

$$\text{MeanSquaredError} : (\text{prediction} - \text{gt}) ** 2 = 100$$

$$\text{Prediction} : 2 \quad \text{Loss} : 100$$

**Optimization step :**

$$w1 = w0 - \text{alpha} * w0.\text{grad}(\text{from backpropagation}) = -2 - 0.1 * (-70) = 5$$

$$w1 = 5$$

**Optimization step :**

$$b1 = b0 - \text{alpha} * b0.\text{grad}(\text{from backpropagation}) = 2 - 0.1 * 30 = 1$$

$$b1 = -1$$

**Iteration #2 :**

$$\text{MeanSquaredError} : (\text{prediction} - \text{gt}) ** 2 = 1$$

$$\text{Prediction} : 11 \quad \text{Loss} : 1$$

$w * 5x + 2b$  ;  $gt = 10$ ;  $W = 4$ ;  $b = -3$ ;  $x = -1$ ;

**Prediction :**

$$w * 5x + 2b = -26$$

**Iteration #1 :**

$$\text{MeanSquaredError} : (\text{prediction} - \text{gt}) ** 2 = 1296$$

*Prediction : -26    Loss : 1296*

**Optimization step :**

$$w1 = w0 - \text{alpha} * w0.\text{grad}(\text{from backpropagation}) = 4 - 0.1 * 40 = 0$$

$$w1 = 0$$

**Optimization step :**

$$b1 = b0 - \text{alpha} * b0.\text{grad}(\text{from backpropagation}) = -3 + 0.1 * 70 = 4$$

$$b1 = 4$$

**Iteration #2 :**

$$\text{MeanSquaredError} : (\text{prediction} - \text{gt}) ** 2 = 4$$

*Prediction : 8    Loss : 4*

$w * x + 3b$  ;                       $gt = 10$ ;    $W = 4$  ;    $b = -3$  ;    $x = 2$ ;

**Prediction :**

$$w * x + 3b = 15$$

**Iteration #1 :**

$$\text{MeanSquaredError : } (\text{prediction} - \text{gt}) ** 2 = 25$$

*Prediction : 15    Loss : 25*

**Optimization step :**

$$w1 = w0 - \alpha * w0.\text{grad}(\text{from backpropagation}) = 6 - 0.1 * 10 = 5$$

$$w1 = 5$$

**Optimization step :**

$$b1 = b0 - \alpha * b0.\text{grad}(\text{from backpropagation}) = 1 - 0.1 * (-20) = 3$$

$$b1 = 3$$

**Iteration #2 :**

$$\text{MeanSquaredError : } (\text{prediction} - \text{gt}) ** 2 = 1$$

*Prediction : 19    Loss : 1*