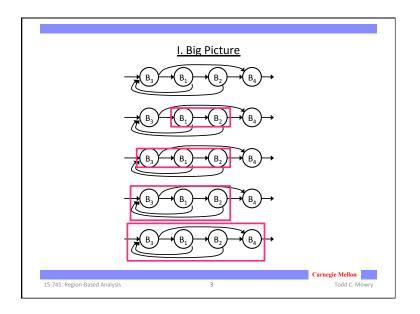
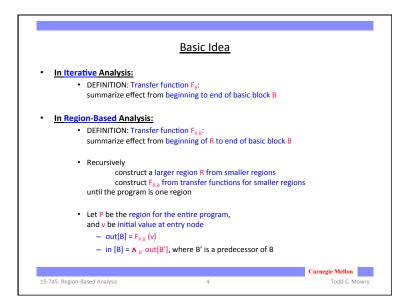
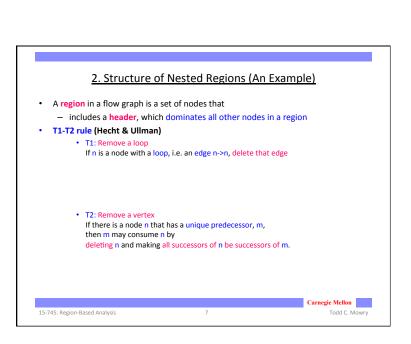
Region-Based Analysis I. Basic Idea II. Algorithm III. Optimization and Complexity IV. Comparing region-based analysis with iterative algorithms Reading: ALSU 9.7 Carnegie Mellon Todd C. Mowry 15-745: Region-Based Analysis

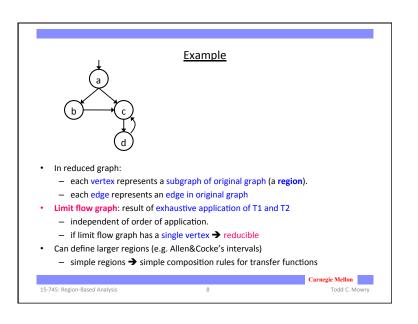


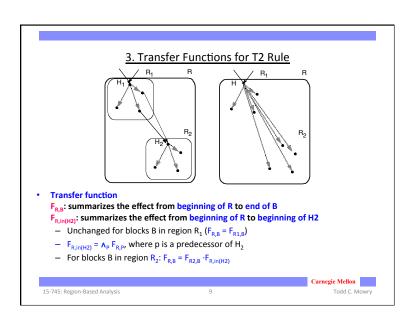
Motivation for Studying Region-Based Analysis Exploit the structure of block-structured programs in data flow · Tie in several concepts studied: - Use of structure in induction variables, loop invariant · motivated by nature of the problem • This lecture: can we use structure for speed? - Iterative algorithm for data flow • This lecture: an alternative algorithm Reducibility · all retreating edges of DFST are back edges · reducible graphs converge quickly • This lecture: algorithm exploits & requires reducibility · Usefulness in practice - Faster for "harder" analyses Useful for analyses related to structure · Theoretically interesting: better understanding of data flow Carnegie Mellon 15-745: Region-Based Analysis

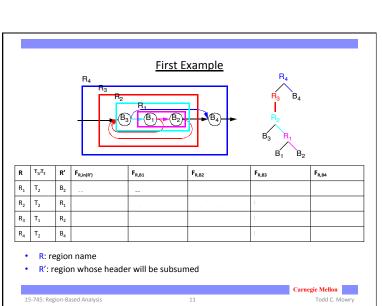


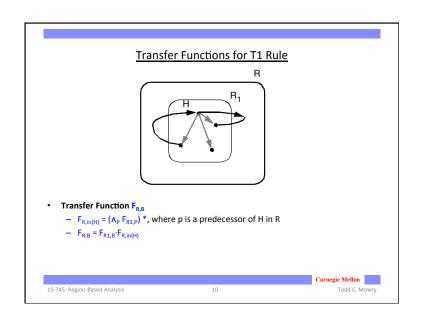
II. Algorithm 1. Operations on transfer functions 2. How to build nested regions? 3. How to construct transfer functions that correspond to the larger regions? Carnegie Mellon 15-745: Region-Based Analysis 5 Todd C. Mowry

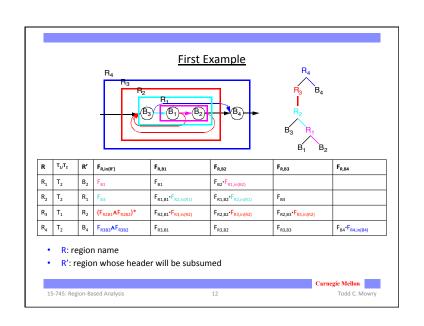


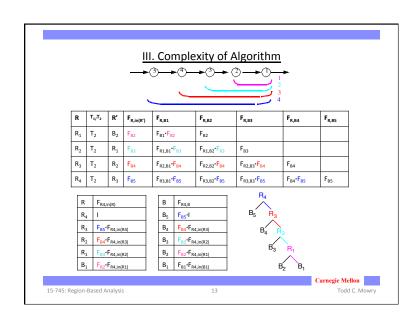












Provided to single node, then split node and continue Worst case: exponential Most graphs (including GOTO programs) are reducible Carnegic Mellon 15-745: Region-Based Analysis 15 Todd C. Mowry

Optimization • Let m = number of edges, n = number of nodes · Ideas for optimization - If we compute F_{B,B} for every region B is in, then it is very expensive - We are ultimately only interested in the entire region (E); we need to compute only $F_{E,B}$ for every B. • There are many common subexpressions between $F_{E,B1},\ F_{E,B2},\ldots$ • Number of F_{E,B} calculated = m $-\;$ Also, we need to compute $F_{R,in(R')},$ where R' represents the region whose header is subsumed. • Number of F_{R,B} calculated, where R is not final = n Total number of F_{R B} calculated: (m + n) - Data structure keeps "header" relationship • Practical algorithm: O(m log n) • Complexity: $O(m\alpha(m,n))$, α is inverse Ackermann function Carnegie Mellon 15-745: Region-Based Analysis

IV. Comparison with Iterative Data Flow Applicability Definitions of F* can make technique more powerful than iterative algorithms - Backward flow: reverse graph is not typically reducible. Requires more effort to adapt to backward flow than iterative algorithm More important for interprocedural optimization Speed Irreducible graphs · Iterative algorithm can process irreducible parts uniformly · Serious "irreducibility" can be slow with region-based analysis Reducible graph & Cycles do not add information (common) • Iterative: (depth + 2) passes depth is 2.75 average, independent of code length • Region-based analysis: Theoretically almost linear, typically O(m log n) - Reducible & Cycles add information · Iterative takes longer to converge · Region-based analysis remains the same Carnegie Mellon 15-745: Region-Based Analysis Todd C. Mowry