

# BreadthFirstPaths.java

Below is the syntax highlighted version of [BreadthFirstPaths.java](#) from §4.1 Undirected Graphs.

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/*****
 *  Compilation:  javac BreadthFirstPaths.java
 *  Execution:    java BreadthFirstPaths G s
 *  Dependencies: Graph.java Queue.java Stack.java StdOut.java
 *  Data files:   https://algs4.cs.princeton.edu/41graph/tinyCG.txt
 *                https://algs4.cs.princeton.edu/41graph/tinyG.txt
 *                https://algs4.cs.princeton.edu/41graph/mediumG.txt
 *                https://algs4.cs.princeton.edu/41graph/largeG.txt
 *
 *  Run breadth first search on an undirected graph.
 *  Runs in  $O(E + V)$  time.
 *
 *  % java Graph tinyCG.txt
 *  6 8
 *  0: 2 1 5
 *  1: 0 2
 *  2: 0 1 3 4
 *  3: 5 4 2
 *  4: 3 2
 *  5: 3 0
 *
 *  % java BreadthFirstPaths tinyCG.txt 0
 *  0 to 0 (0): 0
 *  0 to 1 (1): 0-1
 *  0 to 2 (1): 0-2
 *  0 to 3 (2): 0-2-3
 *  0 to 4 (2): 0-2-4
 *  0 to 5 (1): 0-5
 *
 *  % java BreadthFirstPaths LargeG.txt 0
 *  0 to 0 (0): 0
 *  0 to 1 (418): 0-932942-474885-82707-879889-971961-...
 *  0 to 2 (323): 0-460790-53370-594358-780059-287921-...
 *  0 to 3 (168): 0-713461-75230-953125-568284-350405-...
 *  0 to 4 (144): 0-460790-53370-310931-440226-380102-...
 *  0 to 5 (566): 0-932942-474885-82707-879889-971961-...
 *  0 to 6 (349): 0-932942-474885-82707-879889-971961-...
 *
 *****/

/**
 *  The {@code BreadthFirstPaths} class represents a data type for finding
 *  shortest paths (number of edges) from a source vertex s
 *  (or a set of source vertices)
 *  to every other vertex in an undirected graph.
 *
 *  <p>
 *  This implementation uses breadth-first search.
 *  The constructor takes &Theta;(V + E) time in the
 *  worst case, where V is the number of vertices and E
 *  is the number of edges.
 *  Each instance method takes &Theta;(1) time.
 *  It uses &Theta;(V) extra space (not including the graph).
 *
 *  <p>
 *  For additional documentation,

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* see <a href="https://algs4.cs.princeton.edu/41graph">Section 4.1</a>
* of <i>Algorithms, 4th Edition</i> by Robert Sedgewick and Kevin Wayne.
*
* @author Robert Sedgewick
* @author Kevin Wayne
*/
public class BreadthFirstPaths {
    private static final int INFINITY = Integer.MAX_VALUE;
    private boolean[] marked; // marked[v] = is there an s-v path
    private int[] edgeTo; // edgeTo[v] = previous edge on shortest s-v path
    private int[] distTo; // distTo[v] = number of edges shortest s-v path

    /**
     * Computes the shortest path between the source vertex {@code s}
     * and every other vertex in the graph {@code G}.
     * @param G the graph
     * @param s the source vertex
     * @throws IllegalArgumentException unless {@code 0 <= s < V}
     */
    public BreadthFirstPaths(Graph G, int s) {
        marked = new boolean[G.V()];
        distTo = new int[G.V()];
        edgeTo = new int[G.V()];
        validateVertex(s);
        bfs(G, s);

        assert check(G, s);
    }

    /**
     * Computes the shortest path between any one of the source vertices in {@code sources}
     * and every other vertex in graph {@code G}.
     * @param G the graph
     * @param sources the source vertices
     * @throws IllegalArgumentException if {@code sources} is {@code null}
     * @throws IllegalArgumentException if {@code sources} contains no vertices
     * @throws IllegalArgumentException unless {@code 0 <= s < V} for each vertex
     *         {@code s} in {@code sources}
     */
    public BreadthFirstPaths(Graph G, Iterable<Integer> sources) {
        marked = new boolean[G.V()];
        distTo = new int[G.V()];
        edgeTo = new int[G.V()];
        for (int v = 0; v < G.V(); v++)
            distTo[v] = INFINITY;
        validateVertices(sources);
        bfs(G, sources);
    }

    // breadth-first search from a single source
    private void bfs(Graph G, int s) {
        Queue<Integer> q = new Queue<Integer>();
        for (int v = 0; v < G.V(); v++)
            distTo[v] = INFINITY;
        distTo[s] = 0;
        marked[s] = true;
        q.enqueue(s);

        while (!q.isEmpty()) {
            int v = q.dequeue();
            for (int w : G.adj(v)) {
                if (!marked[w]) {
                    edgeTo[w] = v;
                    distTo[w] = distTo[v] + 1;
                }
            }
        }
    }
}

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        marked[w] = true;
        q.enqueue(w);
    }
}

// breadth-first search from multiple sources
private void bfs(Graph G, Iterable<Integer> sources) {
    Queue<Integer> q = new Queue<Integer>();
    for (int s : sources) {
        marked[s] = true;
        distTo[s] = 0;
        q.enqueue(s);
    }
    while (!q.isEmpty()) {
        int v = q.dequeue();
        for (int w : G.adj(v)) {
            if (!marked[w]) {
                edgeTo[w] = v;
                distTo[w] = distTo[v] + 1;
                marked[w] = true;
                q.enqueue(w);
            }
        }
    }
}

/**
 * Is there a path between the source vertex {@code s} (or sources) and vertex {@code v}?
 * @param v the vertex
 * @return {@code true} if there is a path, and {@code false} otherwise
 * @throws IllegalArgumentException unless {@code 0 <= v < V}
 */
public boolean hasPathTo(int v) {
    validateVertex(v);
    return marked[v];
}

/**
 * Returns the number of edges in a shortest path between the source vertex {@code s}
 * (or sources) and vertex {@code v}?
 * @param v the vertex
 * @return the number of edges in such a shortest path
 *         (or {@code Integer.MAX_VALUE} if there is no such path)
 * @throws IllegalArgumentException unless {@code 0 <= v < V}
 */
public int distTo(int v) {
    validateVertex(v);
    return distTo[v];
}

/**
 * Returns a shortest path between the source vertex {@code s} (or sources)
 * and {@code v}, or {@code null} if no such path.
 * @param v the vertex
 * @return the sequence of vertices on a shortest path, as an Iterable
 * @throws IllegalArgumentException unless {@code 0 <= v < V}
 */
public Iterable<Integer> pathTo(int v) {
    validateVertex(v);
    if (!hasPathTo(v)) return null;
    Stack<Integer> path = new Stack<Integer>();
    int x;
    for (x = v; distTo[x] != 0; x = edgeTo[x])

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        path.push(x);
    path.push(x);
    return path;
}

// check optimality conditions for single source
private boolean check(Graph G, int s) {

    // check that the distance of s = 0
    if (distTo[s] != 0) {
        StdOut.println("distance of source " + s + " to itself = " + distTo[s]);
        return false;
    }

    // check that for each edge v-w dist[w] <= dist[v] + 1
    // provided v is reachable from s
    for (int v = 0; v < G.V(); v++) {
        for (int w : G.adj(v)) {
            if (hasPathTo(v) != hasPathTo(w)) {
                StdOut.println("edge " + v + "-" + w);
                StdOut.println("hasPathTo(" + v + ") = " + hasPathTo(v));
                StdOut.println("hasPathTo(" + w + ") = " + hasPathTo(w));
                return false;
            }
            if (hasPathTo(v) && (distTo[w] > distTo[v] + 1)) {
                StdOut.println("edge " + v + "-" + w);
                StdOut.println("distTo[" + v + "] = " + distTo[v]);
                StdOut.println("distTo[" + w + "] = " + distTo[w]);
                return false;
            }
        }
    }

    // check that v = edgeTo[w] satisfies distTo[w] = distTo[v] + 1
    // provided v is reachable from s
    for (int w = 0; w < G.V(); w++) {
        if (!hasPathTo(w) || w == s) continue;
        int v = edgeTo[w];
        if (distTo[w] != distTo[v] + 1) {
            StdOut.println("shortest path edge " + v + "-" + w);
            StdOut.println("distTo[" + v + "] = " + distTo[v]);
            StdOut.println("distTo[" + w + "] = " + distTo[w]);
            return false;
        }
    }

    return true;
}

// throw an IllegalArgumentException unless {@code 0 <= v < V}
private void validateVertex(int v) {
    int V = marked.length;
    if (v < 0 || v >= V)
        throw new IllegalArgumentException("vertex " + v + " is not between 0 and " + (V-1));
}

// throw an IllegalArgumentException if vertices is null, has zero vertices,
// or has a vertex not between 0 and V-1
private void validateVertices(Iterable<Integer> vertices) {
    if (vertices == null) {
        throw new IllegalArgumentException("argument is null");
    }
    int vertexCount = 0;
    for (Integer v : vertices) {

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        vertexCount++;
        if (v == null) {
            throw new IllegalArgumentException("vertex is null");
        }
        validateVertex(v);
    }
    if (vertexCount == 0) {
        throw new IllegalArgumentException("zero vertices");
    }
}

/**
 * Unit tests the {@code BreadthFirstPaths} data type.
 *
 * @param args the command-line arguments
 */
public static void main(String[] args) {
    In in = new In(args[0]);
    Graph G = new Graph(in);
    // StdOut.println(G);

    int s = Integer.parseInt(args[1]);
    BreadthFirstPaths bfs = new BreadthFirstPaths(G, s);

    for (int v = 0; v < G.V(); v++) {
        if (bfs.hasPathTo(v)) {
            StdOut.printf("%d to %d (%d): ", s, v, bfs.distTo(v));
            for (int x : bfs.pathTo(v)) {
                if (x == s) StdOut.print(x);
                else StdOut.print("-" + x);
            }
            StdOut.println();
        }
        else {
            StdOut.printf("%d to %d (-): not connected\n", s, v);
        }
    }
}
}

```