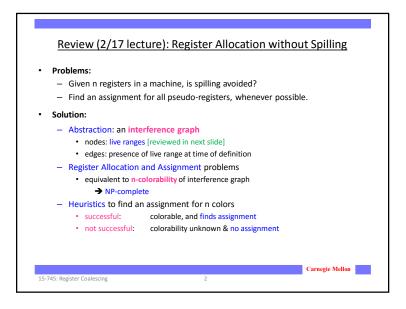
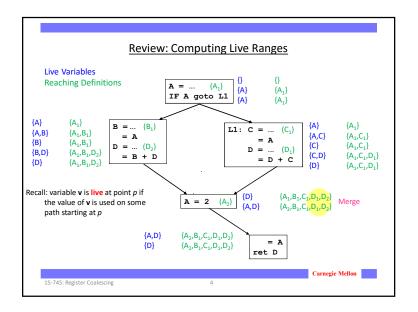
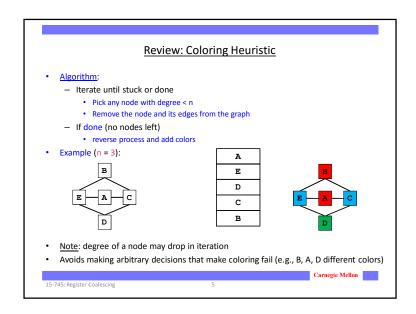
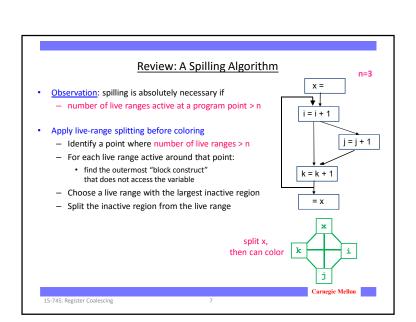
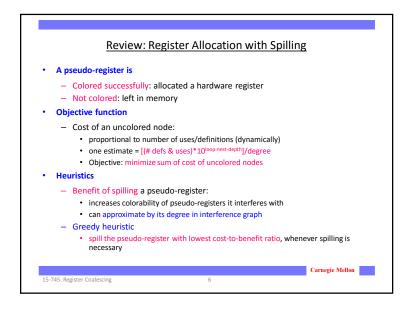
Lecture 23 Register Allocation: Coalescing Phillip B. Gibbons 15-745: Register Coalescing Carnegie Mellon 1

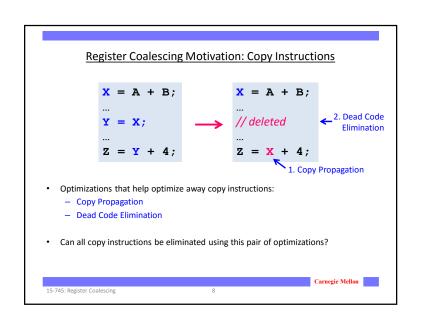


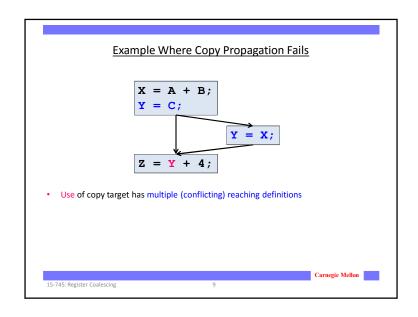


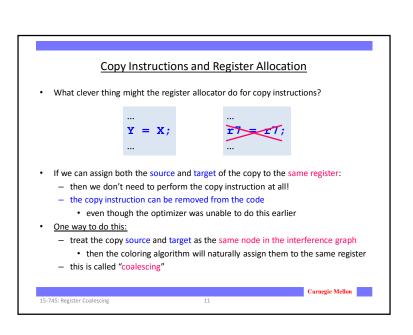


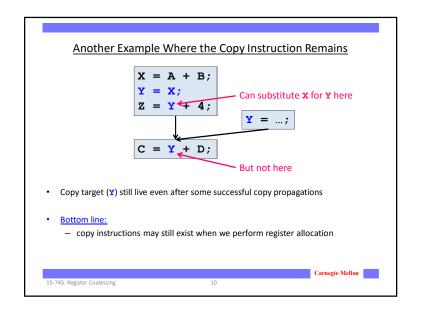


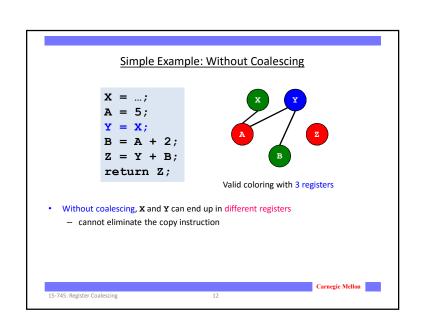


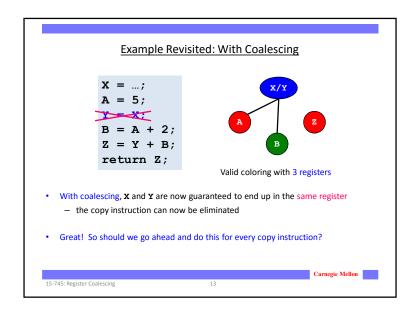


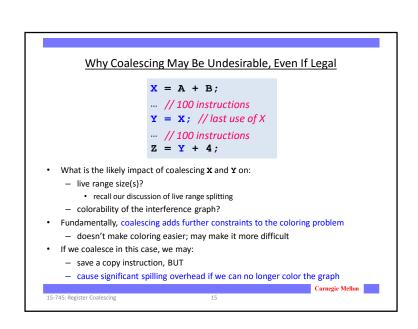


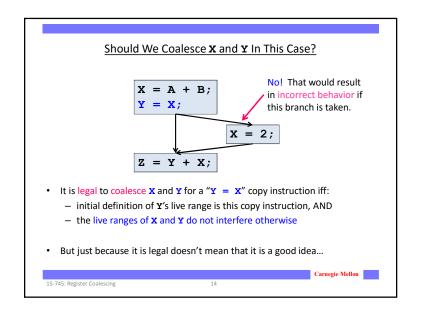


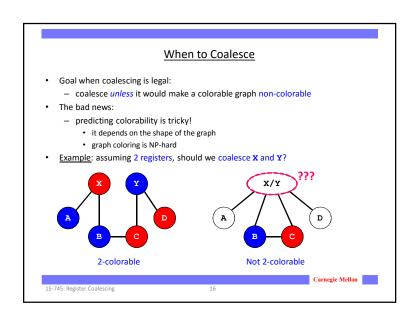








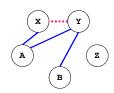




Representing Coalescing Candidates in the Interference Graph

- To decide whether to coalesce, we augment the interference graph
- Coalescing candidates are represented by a new type of interference graph edge:
 - dotted lines: coalescing candidates
 - · try to assign vertices the same color
 - (unless that is problematic, in which case they can be given different colors)
 - solid lines: interference
 - vertices must be assigned different colors





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Simple and Safe Coalescing Algorithm

- We can safely coalesce nodes **X** and **Y** if (|**X**| + |**Y**|) < N
 - Note: |x| = degree of node x counting interference (not coalescing) edges

Example:



(|X| + |Y|) = (1 + 2) = 3



Degree of coalesced node can be no larger than 3

- if N >= 4, it would always be safe to coalesce these two nodes
 - this cannot cause new spilling that would not have occurred with the original graph
- if N < 4, it is unclear

How can we (safely) be more aggressive than this?

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How Do We Know When Coalescing Will Not Cause Spilling?

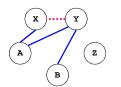
- Key insight:
 - Recall from the coloring algorithm:
 - we can always successfully N-color a node if its degree is < N
- · To ensure that coalescing does not cause spilling:
 - check that the degree < N invariant is still locally preserved after coalescing
 - if so, then coalescing won't cause the graph to become non-colorable
- - We do NOT need to determine whether the full graph is colorable or not
 - Just need to check that coalescing does not cause a colorable graph to become non-colorable

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What About This Example?

- Assume N = 3
- Is it safe to coalesce x and y?



(|x| + |y|) = (1 + 2) = 3(Not less than N)

• Notice: X and Y share a common (interference) neighbor: node A

- hence the degree of the coalesced X/Y node is actually 2 (not 3)
- therefore coalescing **X** and **Y** is guaranteed to be safe when N = 3
- · How can we adjust the algorithm to capture this?

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Another Helpful Insight • Colors are not assigned until nodes are popped off the stack - nodes with degree < N are pushed on the stack first - when a node is popped off the stack, we know that it can be colored • because the number of potentially conflicting neighbors must be < N • Spilling only occurs if there is no node with degree < N to push on the stack • Example: (N=2) B T IX | = 5 |Y |

