

**15-213**

**Machine-Level Programming III:  
Procedures  
Feb. 8, 2000**

**Topics**

- IA32 stack
- Stack-based languages
- Stack frames
- Register saving conventions
- Creating pointers to local variables

# I A32 Stack

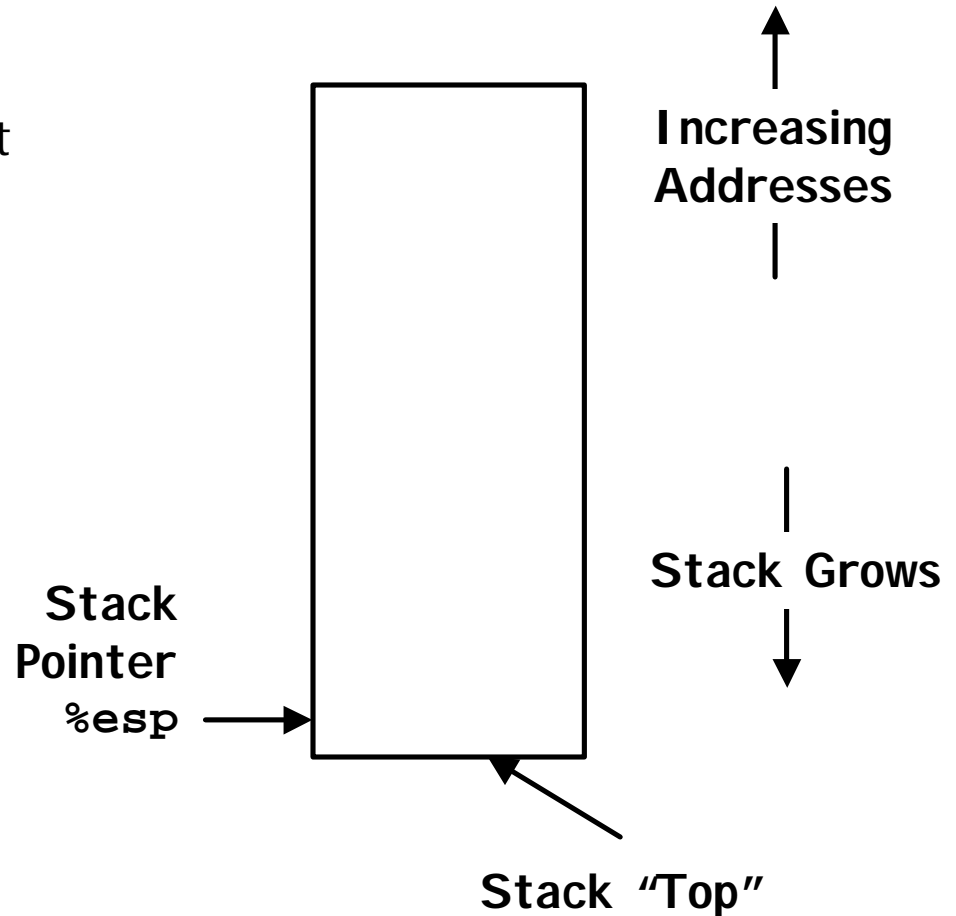
- Region of memory managed with stack discipline
- Register `%esp` indicates lowest allocated position in stack
  - i.e., address of top element

## Pushing

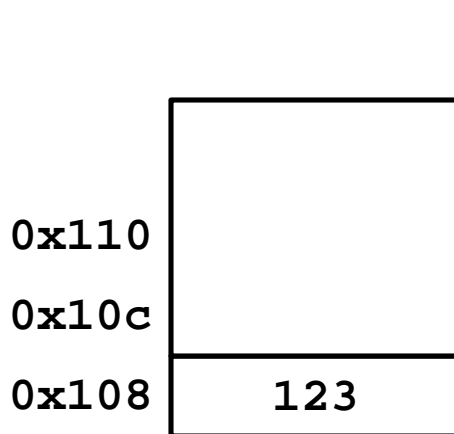
- `pushl Src`
- Fetch operand at *Src*
- Decrement `%esp` by 4
- Write operand at address given by `%esp`

## Popping

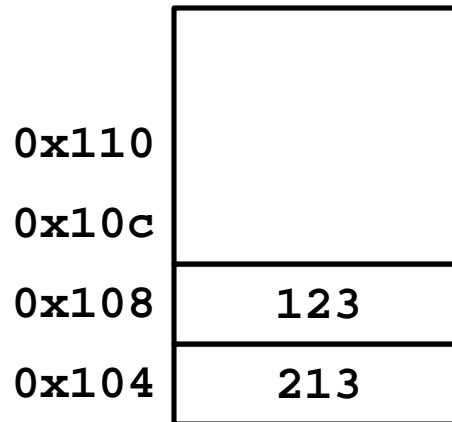
- `popl Dest`
- Read operand at address given by `%esp`
- Increment `%esp` by 4
- Write to *Dest*



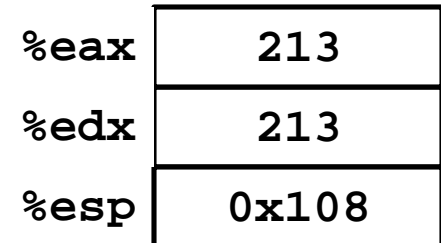
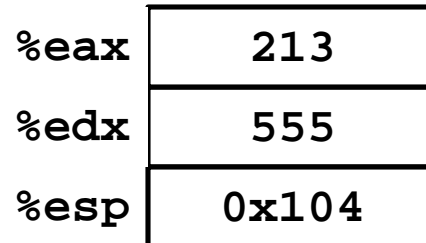
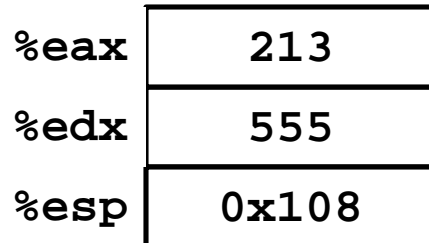
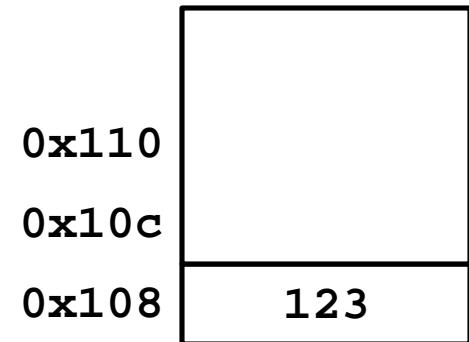
# Stack Operation Examples



`pushl %eax`



`popl %edx`



# Procedure Control Flow

Use stack to support procedure call and return

**Procedure call:**

`call label`    Push return address on stack; Jump to *label*

**Return address value**

- Address of instruction beyond `call`
- Example from disassembly

```
804854e:    e8 3d 06 00 00    call    8048b90 <main>
8048553:    50               pushl   %eax
```

– Return address = `0x8048553`

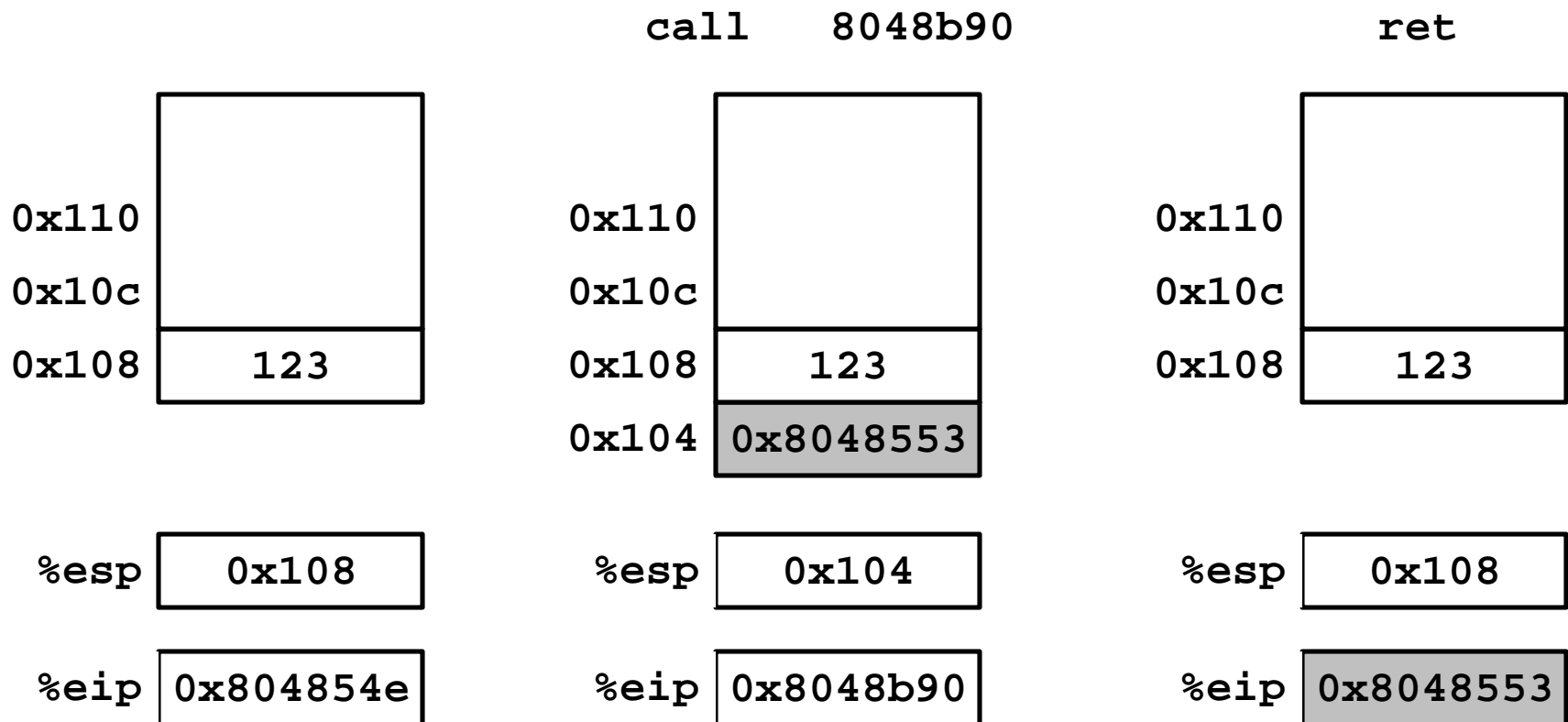
**Procedure return:**

- `ret`            Pop address from stack; Jump to address

# Procedure Call / Return Example

804854e: e8 3d 06 00 00  
8048553: 50

call 8048b90 <main>  
pushl %eax



%eip is program counter

# Stack-Based Languages

## Languages that Support Recursion

- e.g., C, Pascal, Java
- Code must be *"Reentrant"*
  - Multiple simultaneous instantiations of single procedure
- Need some place to store state of each instantiation
  - Arguments
  - Local variables
  - Return pointer

## Stack Discipline

- State for given procedure needed for limited time
  - From when called to when return
- Callee returns before caller does

## Stack Allocated in *Frames*

- state for single procedure instantiation

# Call Chain Example

## Code Structure

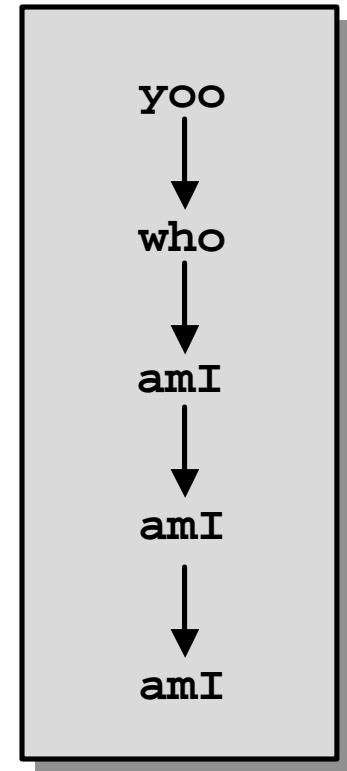
```
yoo(...)  
{  
  •  
  •  
  who();  
  •  
  •  
}
```

```
who(...)  
{  
  •  
  •  
  amI();  
  •  
  •  
}
```

```
amI(...)  
{  
  •  
  •  
  amI();  
  •  
  •  
}
```

- Procedure `amI` recursive

## Call Chain



# I A32 Stack Structure

## Stack Growth

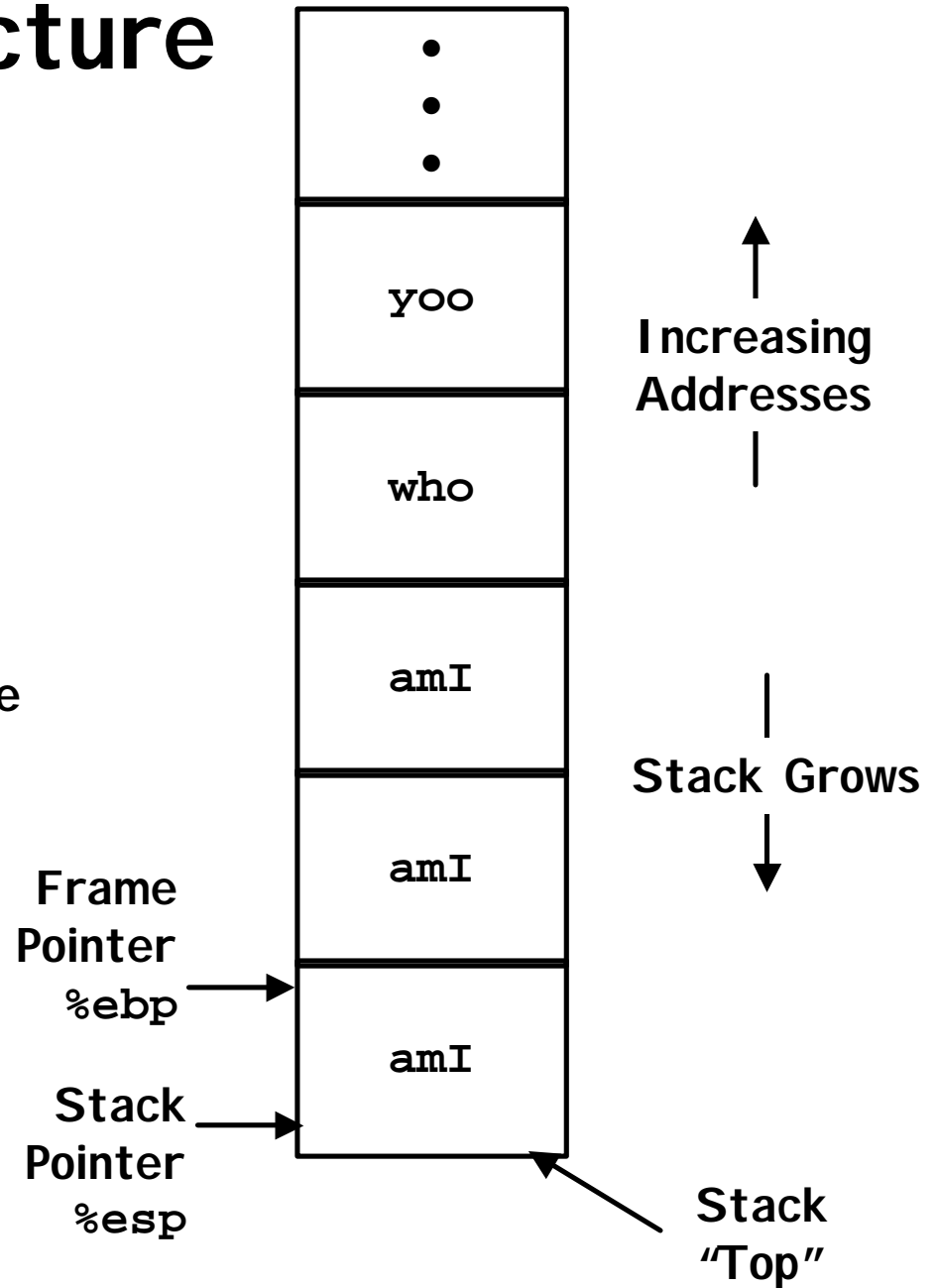
- Toward lower addresses

## Stack Pointer

- Address of next available location in stack
- Use register `%esp`

## Frame Pointer

- Start of current stack frame
- Use register `%ebp`





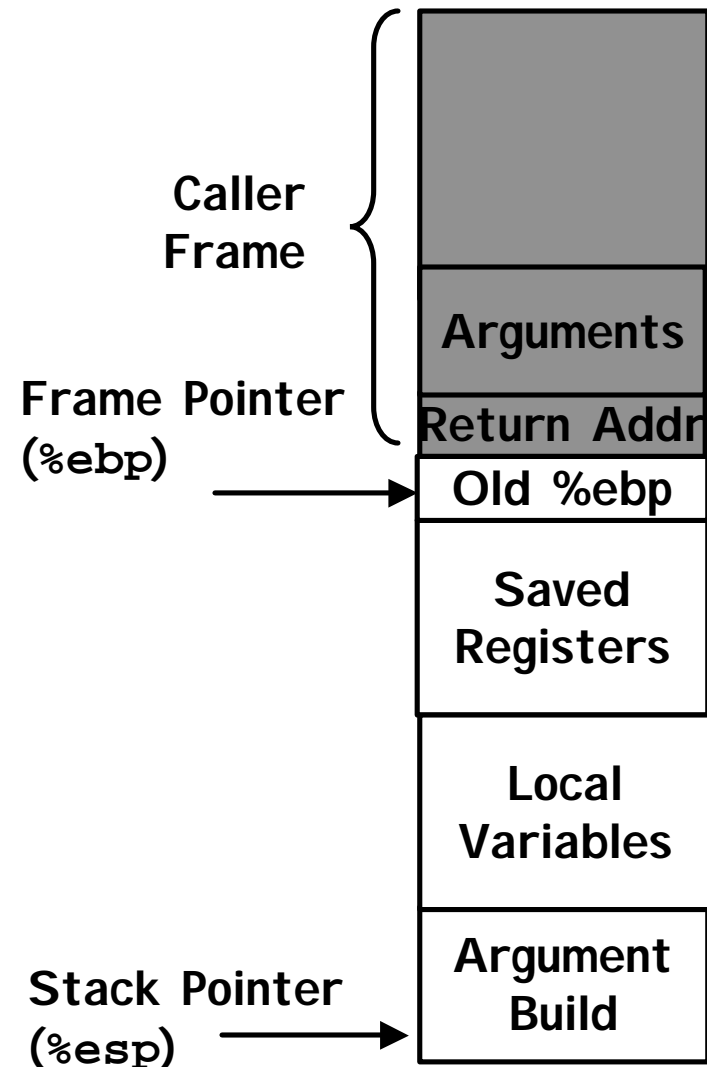
# I A32/Linux Stack Frame

## Callee Stack Frame ("Top" to Bottom)

- Parameters for called functions
- Local variables
  - If can't keep in registers
- Saved register context
- Old frame pointer

## Caller Stack Frame

- Return address
  - Pushed by `call` instruction
- Arguments for this call



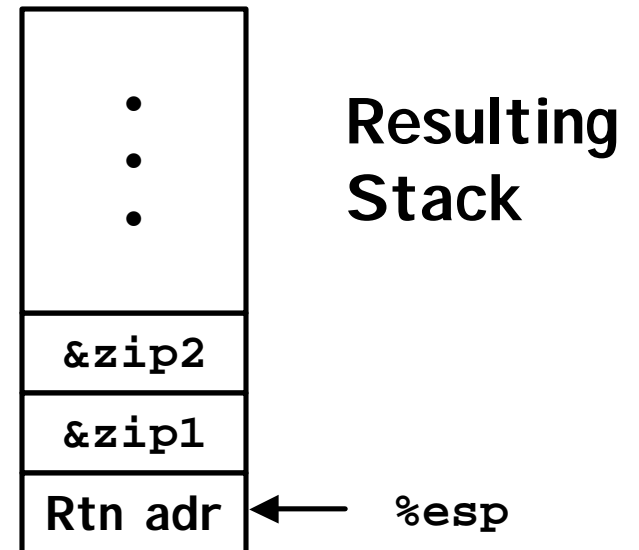
# Revisiting swap

```
int zip1 = 15213;
int zip2 = 91125;

void call_swap()
{
    swap(&zip1, &zip2);
}
```

```
void swap(int *xp, int *yp)
{
    int t0 = *xp;
    int t1 = *yp;
    *xp = t1;
    *yp = t0;
}
```

```
call_swap:
    . . .
    pushl $zip2
    pushl $zip1
    call swap
    . . .
```



# Revisiting swap

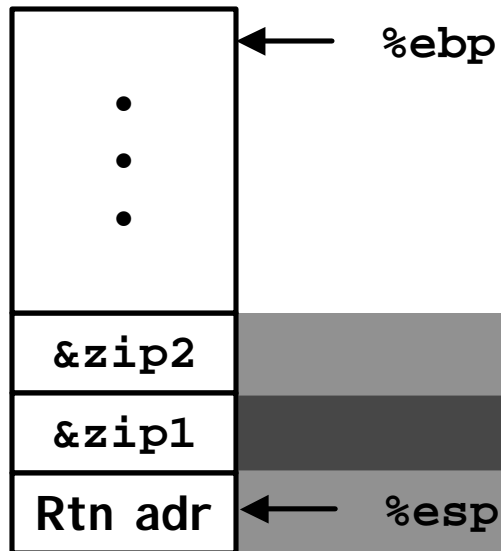
```
void swap(int *xp, int *yp)
{
    int t0 = *xp;
    int t1 = *yp;
    *xp = t1;
    *yp = t0;
}
```

swap:

pushl %ebp movl %esp,%ebp pushl %ebx	} Set Up
movl 12(%ebp),%ecx movl 8(%ebp),%edx movl (%ecx),%eax movl (%edx),%ebx movl %eax,(%edx) movl %ebx,(%ecx)	} Body
movl -4(%ebp),%ebx movl %ebp,%esp popl %ebp ret	} Finish

# swap Setup

Entering  
Stack



Offset

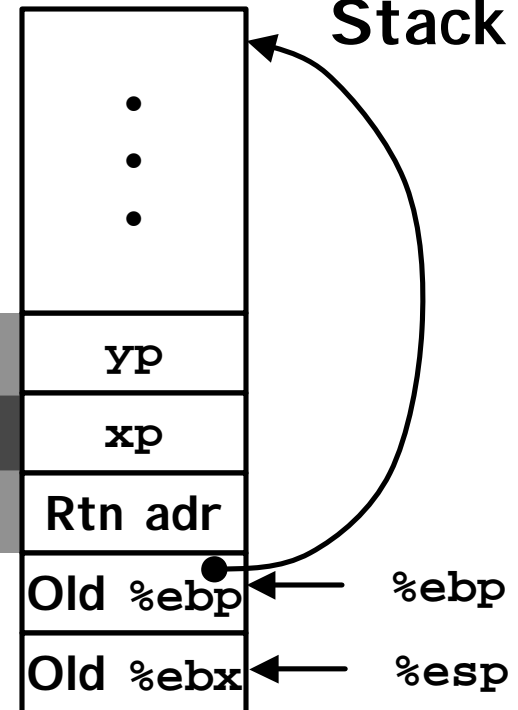
12

8

4

0

Resulting  
Stack

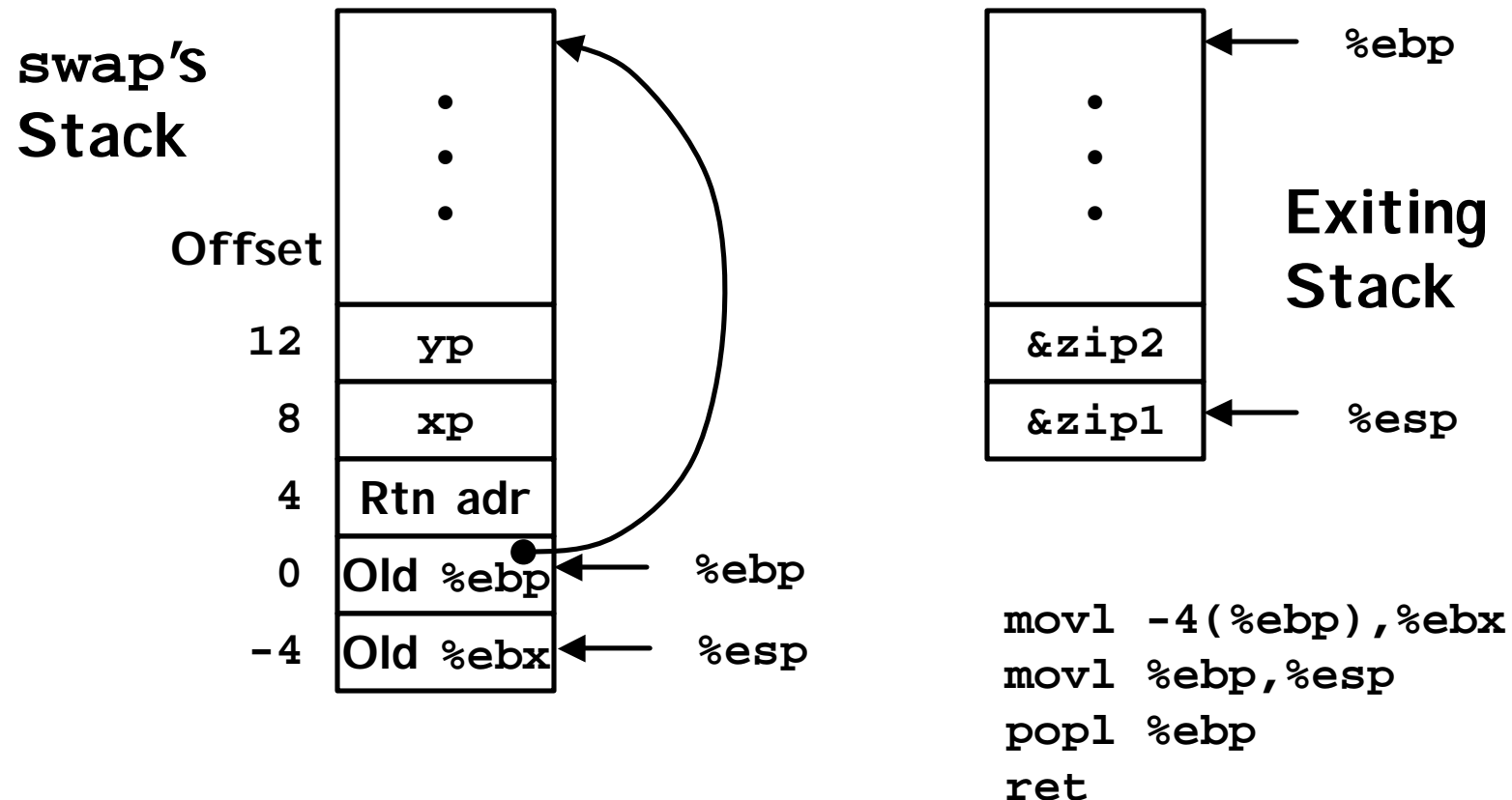


swap:

```

pushl %ebp
movl %esp,%ebp
pushl %ebx
    
```

# swap Finish



## Observation

- Saved & restored register %ebx
- Didn't do so for %eax, %ecx, or %edx

# Register Saving Conventions

When procedure *yoo* calls *who*:

- *yoo* is the *caller*, who is the *callee*

Can Register be Used for Temporary Storage?

*yoo*:

```
• • •  
movl $15213, %edx  
call who  
addl %edx, %eax  
• • •  
ret
```

*who*:

```
• • •  
movl 8(%ebp), %edx  
addl $91125, %edx  
• • •  
ret
```

- Contents of register `%edx` overwritten by *who*

## Conventions

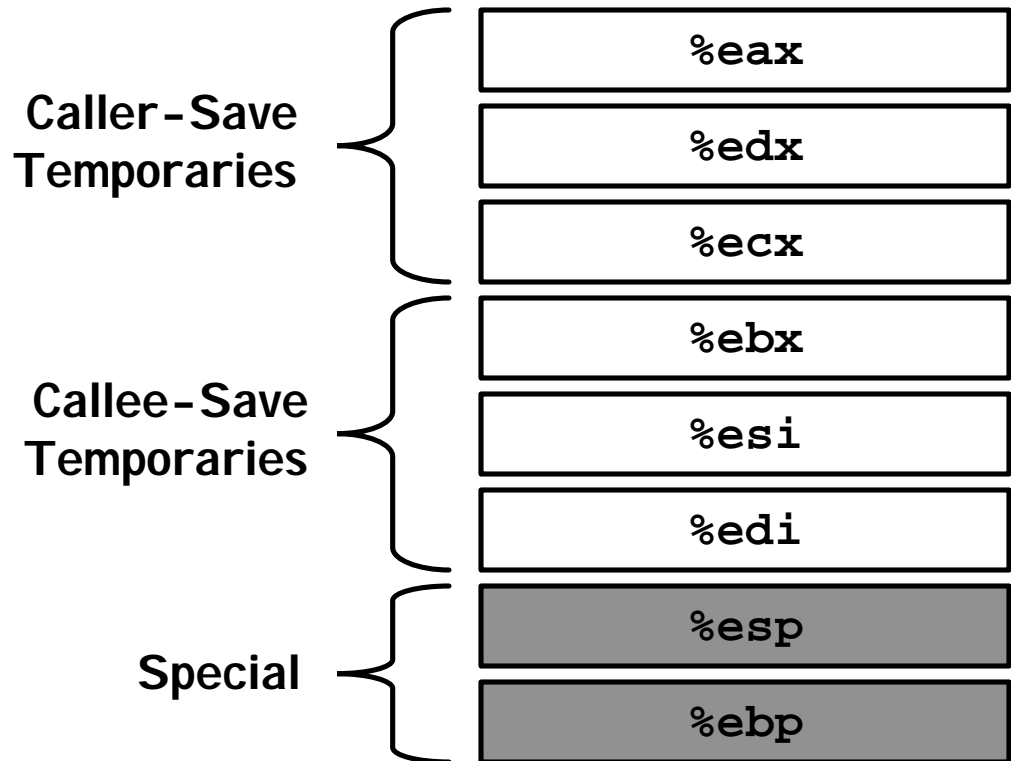
- “Caller Save”
  - Caller saves temporary in its frame before calling
- “Callee Save”
  - Callee saves temporary in its frame before using

# I A32/Linux Register Usage

- Surmised by looking at code examples

## Integer Registers

- Two have special uses  
`%ebp`, `%esp`
- Three managed as callee-save  
`%ebx`, `%esi`, `%edi`
  - Old values saved on stack prior to using
- Three managed as caller-save  
`%eax`, `%ecx`, `%edx`
  - Do what you please, but expect any callee to do so, as well
- Register `%eax` also stores returned value



# Recursive Factorial

```
int rfact(int x)
{
    int rval;
    if (x <= 1)
        return 1;
    rval = rfact(x-1);
    return rval * x;
}
```

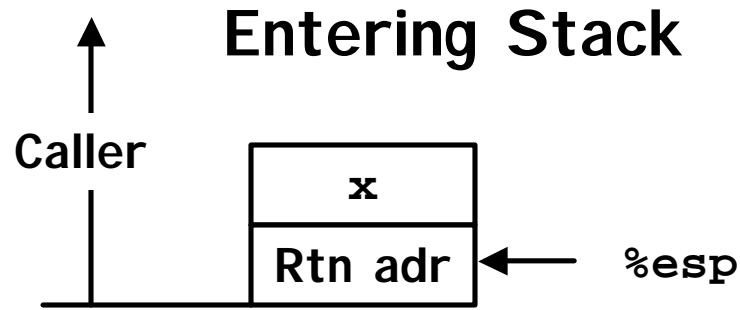
## Complete Assembly

- Assembler directives
  - Lines beginning with “.”
  - Not of concern to us
- Labels
  - .Lxx
- Actual instructions

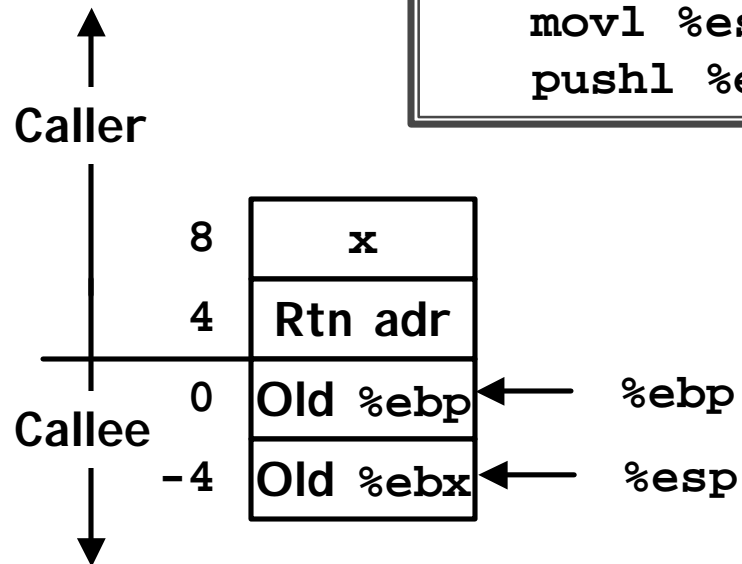
```
.globl rfact
.type
rfact,@function
rfact:
    pushl %ebp
    movl %esp,%ebp
    pushl %ebx
    movl 8(%ebp),%ebx
    cmpl $1,%ebx
    jle .L78
    leal -1(%ebx),%eax
    pushl %eax
    call rfact
    imull %ebx,%eax
    jmp .L79
    .align 4
.L78:
    movl $1,%eax
.L79:
    movl -4(%ebp),%ebx
    movl %ebp,%esp
    popl %ebp
    ret
```



# Rfact Stack Setup



```
rfact:
    pushl %ebp
    movl %esp,%ebp
    pushl %ebx
```



# Rfact Body

```
movl 8(%ebp),%ebx    # ebx = x
cmpl $1,%ebx         # Compare x : 1
jle .L78             # If <= goto Term
leal -1(%ebx),%eax   # eax = x-1
pushl %eax           # Push x-1
call rfact           # rfact(x-1)
imull %ebx,%eax      # rval * x
jmp .L79             # Goto done
.L78:                # Term:
    movl $1,%eax     # return val = 1
.L79:                # Done:
```

```
int rfact(int x)
{
    int rval;
    if (x <= 1)
        return 1;
    rval = rfact(x-1);
    return rval * x;
}
```

## Registers

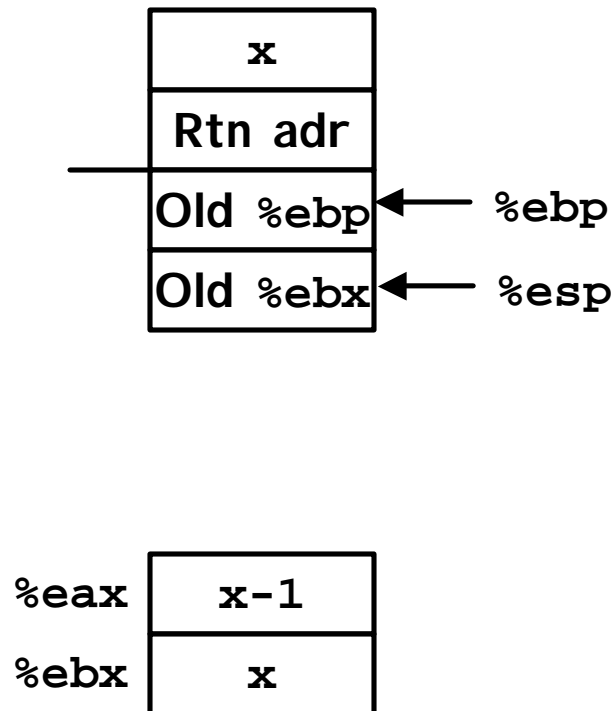
**\$ebx** Stored value of x

**\$eax**

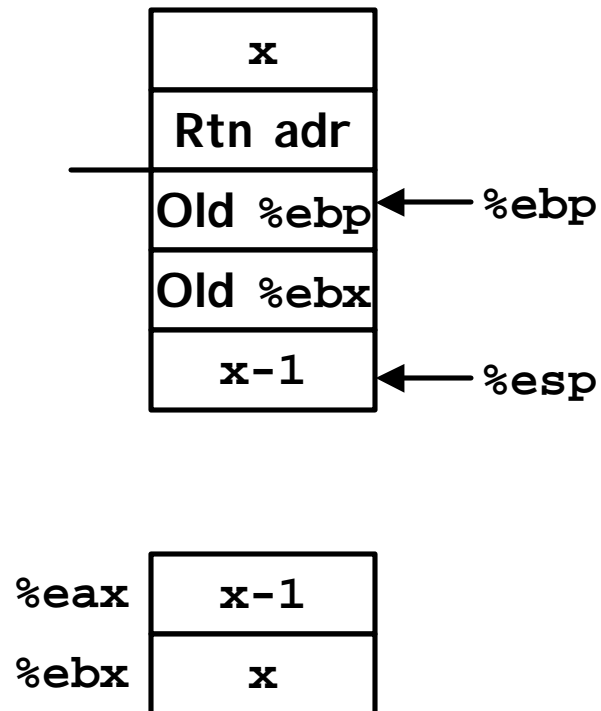
- Temporary value of **x-1**
- Returned value from **rfact(x-1)**
- Returned value from this call

# Rfact Recursion

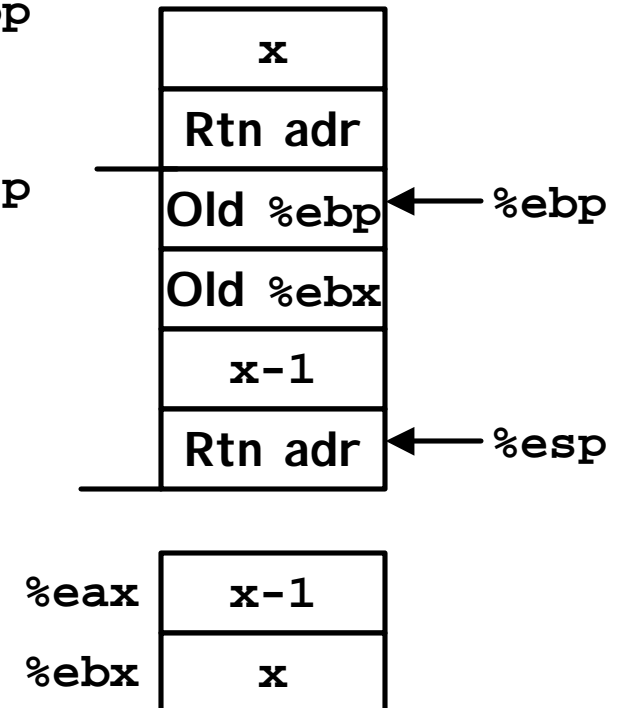
```
leal -1(%ebx), %eax
```



```
pushl %eax
```

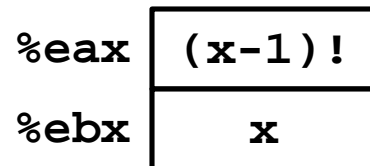
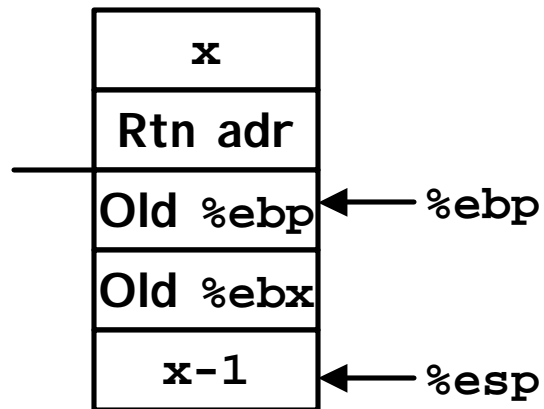


```
call rfact
```

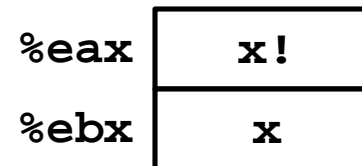
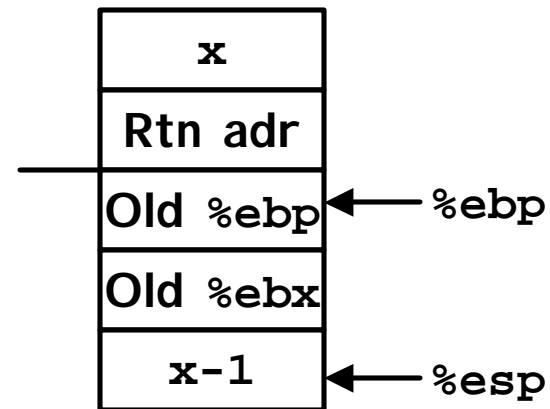


# Rfact Result

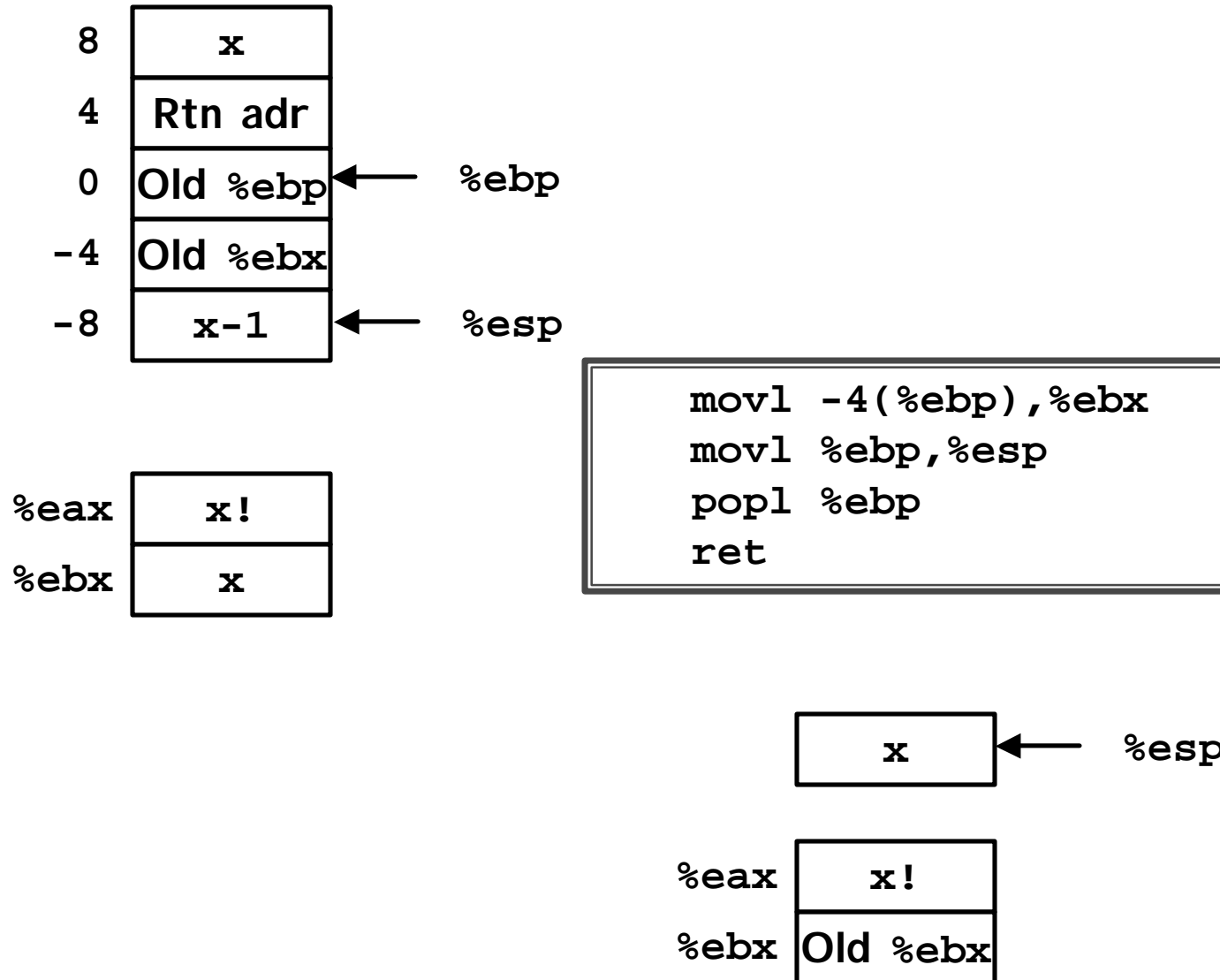
Return from Call



`imull %ebx,%eax`



# Rfact Completion



# Pointer Code

## Recursive Procedure

```
void s_helper
(int x, int *accum)
{
    if (x <= 1)
        return;
    else {
        int z = *accum * x;
        *accum = z;
        s_helper (x-1, accum);
    }
}
```

## Top-Level Call

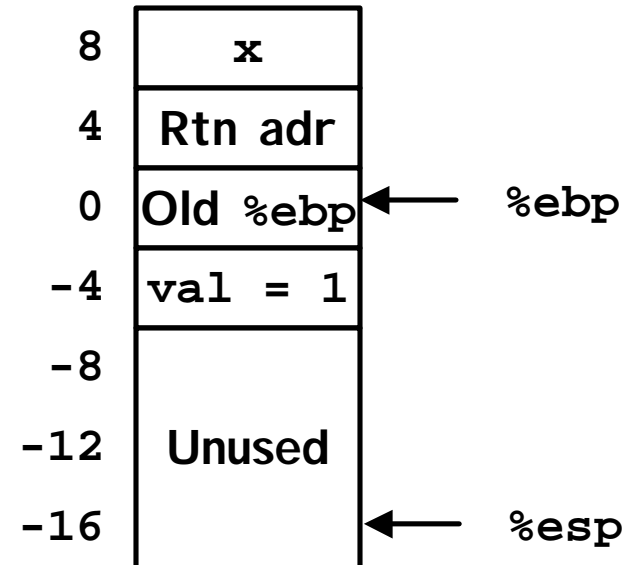
```
int sfact(int x)
{
    int val = 1;
    s_helper(x, &val);
    return val;
}
```

- Pass pointer to update location
- Uses tail recursion
  - But GCC only partially optimizes it

# Creating & Initializing Pointer

## Initial part of sfact

```
_sfact:
    pushl %ebp          # Save %ebp
    movl %esp,%ebp      # Set %ebp
    subl $16,%esp       # Add 16 bytes
    movl 8(%ebp),%edx    # edx = x
    movl $1,-4(%ebp)    # val = 1
```



## Using Stack for Local Variable

- Variable `val` must be stored on stack
  - Need to create pointer to it
- Compute pointer as `-4(%ebp)`
- Push on stack as second argument

```
int sfact(int x)
{
    int val = 1;
    s_helper(x, &val);
    return val;
}
```

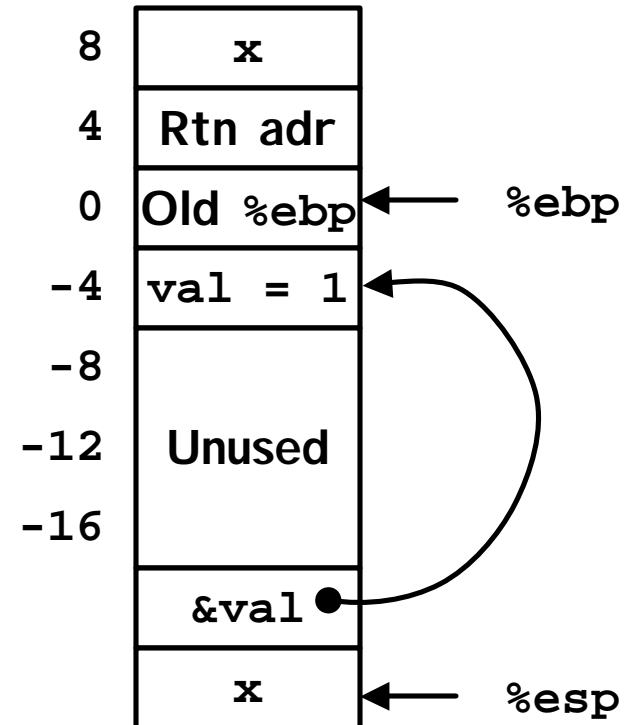
# Passing Pointer

## Calling s\_helper from sfact

```
leal -4(%ebp),%eax # Compute &val
pushl %eax          # Push on stack
pushl %edx          # Push x
call _s_helper      # call
movl -4(%ebp),%eax  # Return val
...                # Finish
```

```
int sfact(int x)
{
    int val = 1;
    s_helper(x, &val);
    return val;
}
```

## Stack at time of call





# Using Pointer

```
void s_helper
(int x, int *accum)
{
    • • •
    int z = *accum * x;
    *accum = z;
    • • •
}
```

```
• • •
movl %ecx,%eax    # z = x
imull (%edx),%eax # z *= *accum
movl %eax,(%edx)  # *accum = z
• • •
```

- Register `%ecx` holds `x`
- Register `%edx` holds `accum`
  - Use access `(%edx)` to reference memory

# Multi-Way Recursion

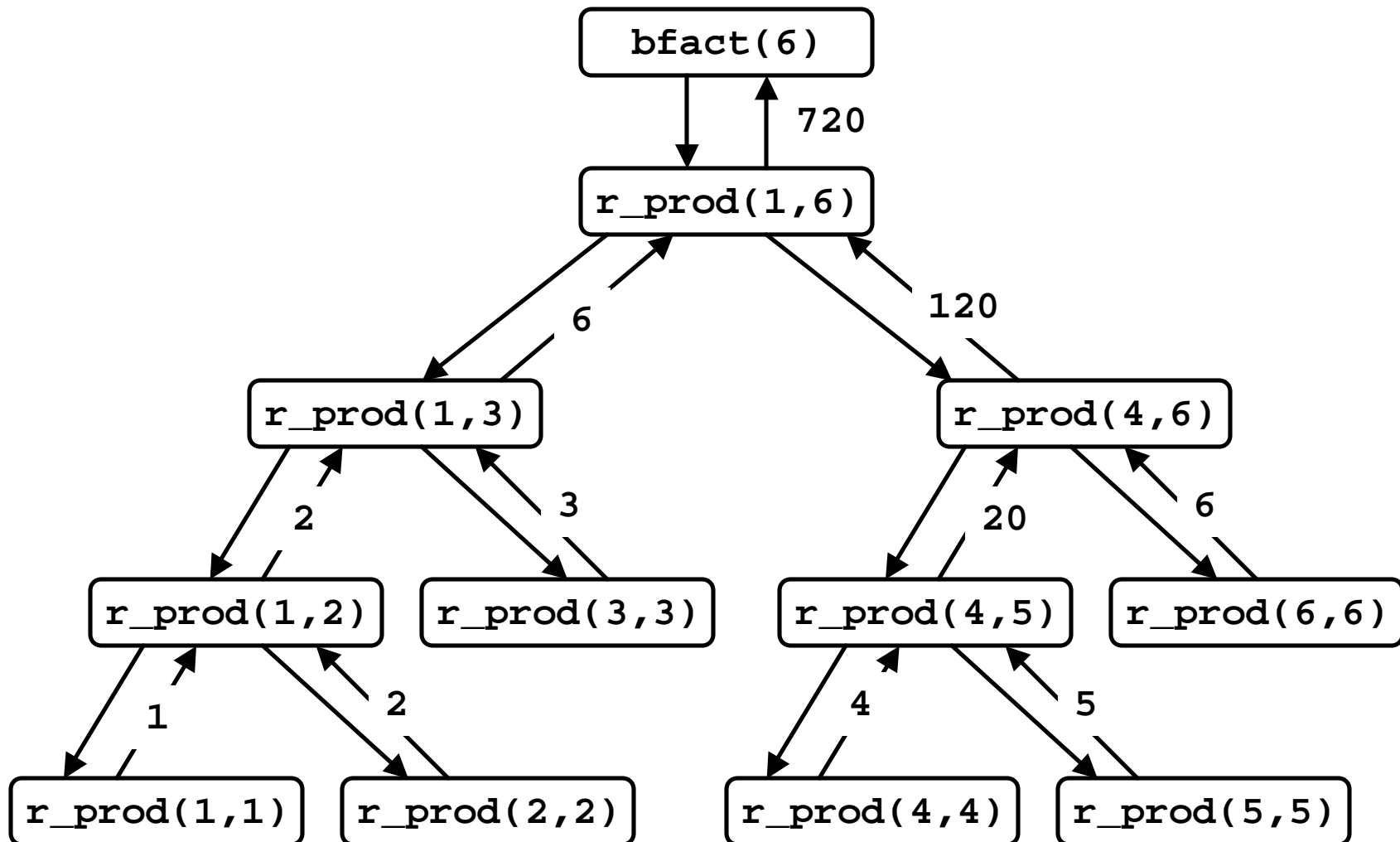
```
int r_prod
(int from, int to)
{
    int middle;
    int prodA, prodB;
    if (from >= to)
        return from;
    middle = (from + to) >> 1;
    prodA = r_prod(from, middle);
    prodB = r_prod(middle+1, to);
    return prodA * prodB;
}
```

## Top-Level Call

```
int bfact(int x)
{
    return r_prod(1,x);
}
```

- Compute product  $x * (x+1) * \dots * (y-1) * y$
- Split into two ranges:
  - Left:  $x * (x+1) * \dots * (m-1) * m$
  - Right:  $(m+1) * \dots * (y-1) * y$
$$m = \lfloor (x+y)/2 \rfloor$$
- No real advantage algorithmically

# Binary Splitting Example



# Multi-Way Recursive Code

## Stack Frame

12	from
8	to
4	Rtn Adr
0	Old \$ebp
-4	Old \$edi
-8	Old \$esi
-12	Old \$ebx

\$eax

from

return values

## Callee Save Regs.

\$ebx middle

\$edi to

\$esi prodA

\_r\_prod:

• • •

# Setup

movl 8(%ebp),%eax # eax = from

movl 12(%ebp),%edi # edi = to

cmpl %edi,%eax # from : to

jge L8 # if >= goto done

leal (%edi,%eax),%ebx # from + to

sarl \$1,%ebx # middle

pushl %ebx # 2nd arg: middle

pushl %eax # 1st arg: from

call \_r\_prod # 1st call

pushl %edi # 2nd arg: to

movl %eax,%esi # esi = ProdA

incl %ebx # middle + 1

pushl %ebx # ... 1st arg

call \_r\_prod # 2nd call

imull %eax,%esi # ProdA \* ProdB

movl %esi,%eax # Return value

L8:

# done:

• • •

# Finish

# Multi-Way Recursive Code Finish

12	from	L8:	# done:
8	to	leal -12(%ebp),%esp	# Set Stack Ptr
4	Rtn Adr	popl %ebx	# Restore %ebx
0	Old \$ebp	popl %esi	# Restore %esi
-4	Old \$edi	popl %edi	# Restore %edi
-8	Old \$esi	movl %ebp,%esp	# Restore %esp
-12	Old \$ebx	popl %ebp	# Restore %ebp
-16	Arg 2	ret	# Return
-20	Arg 1		

## Stack

- After making recursive calls, still has two arguments on top

## Finishing Code

- Moves stack pointer to start of saved register area
- Pops registers

# Mutual Recursion

## Top-Level Call

```
int lrfact(int x)
{
    int left = 1;
    return
        left_prod(&left, &x);
}
```

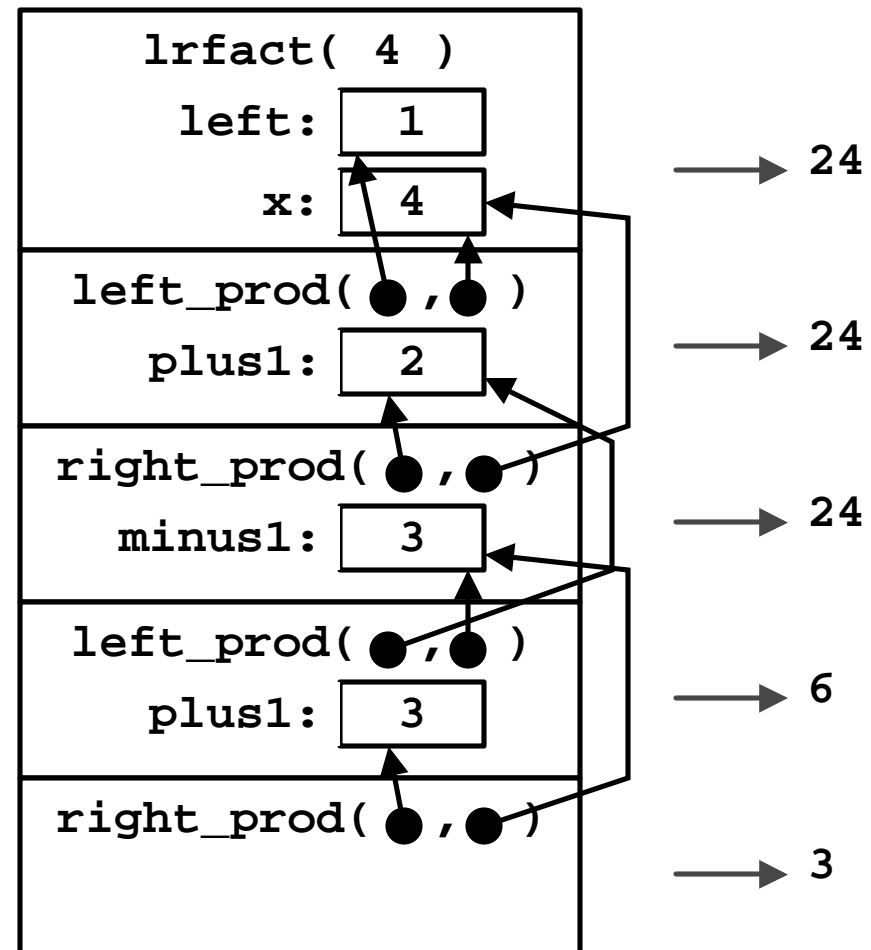
```
int left_prod
(int *leftp, int *rightp)
{
    int left = *leftp;
    if (left >= *rightp)
        return left;
    else {
        int plus1 = left+1;
        return left *
            right_prod(&plus1, rightp);
    }
}
```

```
int right_prod
(int *leftp, int *rightp)
{
    int right = *rightp;
    if (*leftp == right)
        return right;
    else {
        int minus1 = right-1;
        return right *
            left_prod(leftp, &minus1);
    }
}
```

# Mutually Recursive Execution Example

## Calling

- Recursive routines pass two arguments
  - Pointer to own local variable
  - Pointer to caller's local variable



# Implementation of lrfact

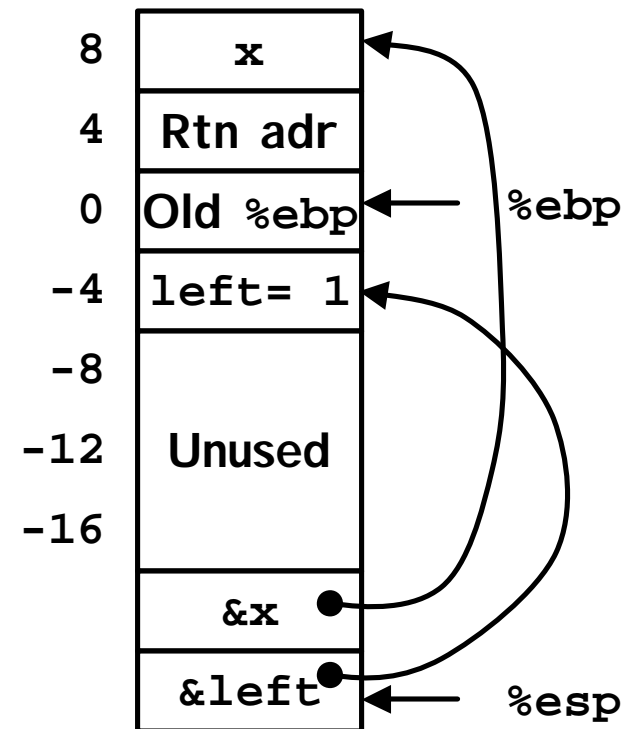
## Call to Recursive Routine

```
int left = 1;  
return left_prod(&left, &x);
```

## Code for Call

```
leal 8(%ebp),%edx # edx = &x  
pushl %edx        # push &x  
leal -4(%ebp),%eax # eax = &left  
pushl %eax        # push &left  
call _left_prod   # Call
```

## Stack at time of call





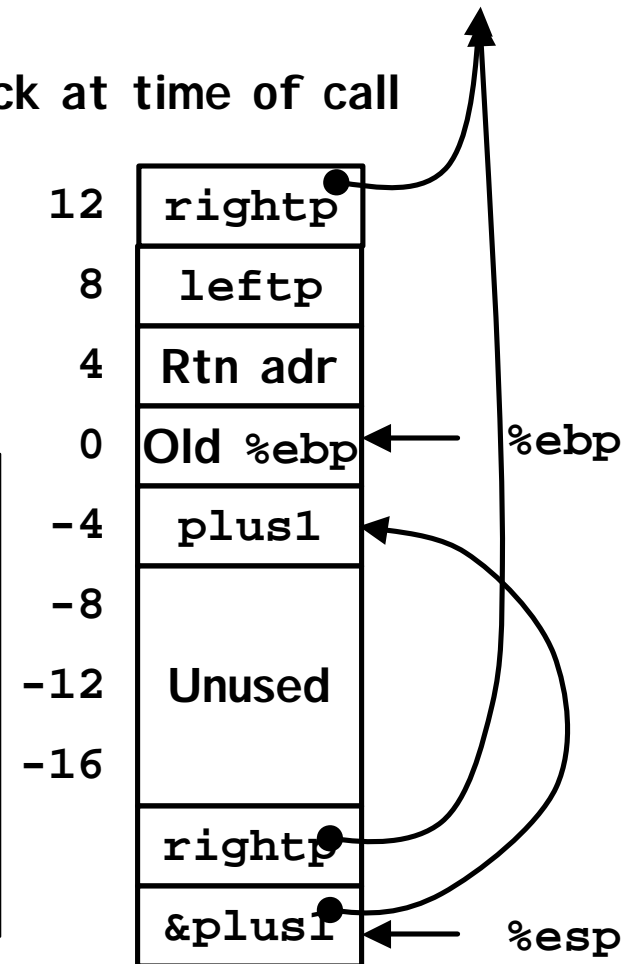
# Implementation of left\_prod

## Call to Recursive Routine

```
int plus1 = left+1;  
return left *  
    right_prod(&plus1, rightp);
```

```
# %ebx holds left  
# %edx holds rightp  
leal 1(%ebx),%ecx # left+1  
movl %ecx,-4(%ebp) # Store in plus1  
pushl %edx        # Push rightp  
leal -4(%ebp),%eax # &plus1  
pushl %eax        # Push &plus1  
call _right_prod  # Call
```

Stack at time of call



# Tail Recursion

## Tail Recursive Procedure

```
int t_helper
  (int x, int val)
{
  if (x <= 1)
    return val;
  return
    t_helper(x-1, val*x);
}
```

## General Form

```
t_helper(x, val)
{
  • • •
  return
    t_helper(Xexpr, Vexpr)
}
```

## Top-Level Call

```
int tfact(int x)
{
  return t_helper(x, 1);
}
```

## Form

- Directly return value returned by recursive call

## Consequence

- Can convert into loop

# Removing Tail Recursion

## Optimized General Form

```
t_helper(x, val)
{
  start:
    • • •
    val = Vexpr;
    x = Xexpr;
    goto start;
}
```

## Resulting Code

```
int t_helper
(int x, int val)
{
  start:
    if (x <= 1)
      return val;
    val = val*x;
    x = x-1;
    goto start;
}
```

## Effect of Optimization

- Turn recursive chain into single procedure
- No stack frame needed
- Constant space requirement
  - Vs. linear for recursive version

# Generated Code for Tail Recursive Proc.

## Optimized Form

```
int t_helper
(int x, int val)
{
  start:
  if (x <= 1)
    return val;
  val = val*x;
  x = x-1;
  goto start;
}
```

## Code for Loop

```
# %edx = x
# %ecx = val
L53:                                # start:
    cmpl $1,%edx                    # x : 1
    jle L52                         # if <= goto done
    movl %edx,%eax                  # eax = x
    imull %ecx,%eax                 # eax = val * x
    decl %edx                       # x--
    movl %eax,%ecx                  # val = val * x
    jmp L53                         # goto start
L52:                                # done:
```

## Registers

\$edx x

\$ecx val

# Main Ideas

## Stack Provides Storage for Procedure Instantiation

- Save state
- Local variables
- Any variable for which must create pointer

## Assembly Code Must Manage Stack

- Allocate / deallocate by decrementing / incrementing stack pointer
- Saving / restoring register state

## Stack Adequate for All Forms of Recursion

- Multi-way
- Mutual