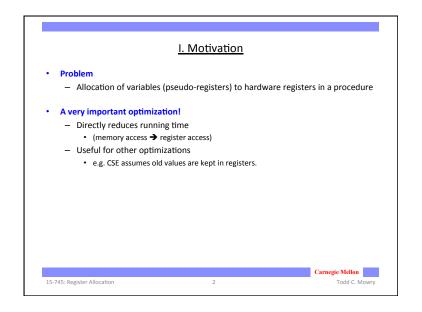
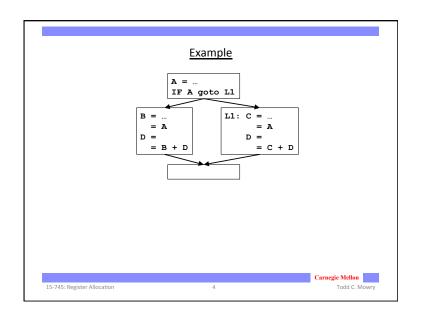
Lecture 15 Register Allocation & Spilling I. Introduction II. Abstraction and the Problem III. Algorithm IV. Spilling Reading: ALSU 8.8.4

Solution Find an allocation for all pseudo-registers, if possible. If there are not enough registers in the machine, choose registers to spill to memory Carnegie Mellon 15-745: Register Allocation 3 Todd C. Mowry





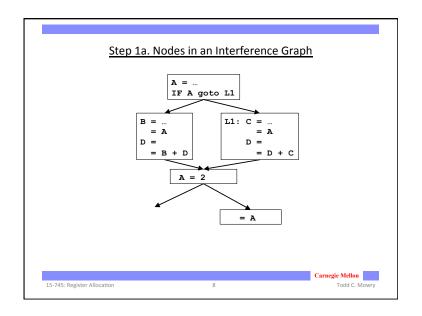
II. An Abstraction for Allocation & Assignment Intuitively Two pseudo-registers interfere if at some point in the program they cannot both occupy the same register. Interference graph: an undirected graph, where nodes = pseudo-registers there is an edge between two nodes if their corresponding pseudo-registers interfere What is not represented Extent of the interference between uses of different variables Where in the program is the interference

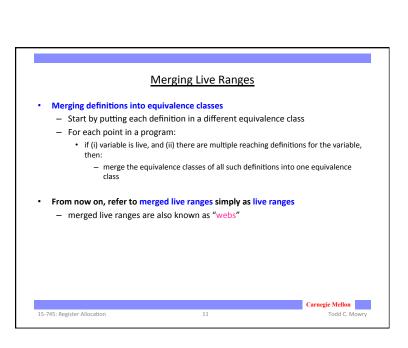
15-745: Register Allocation

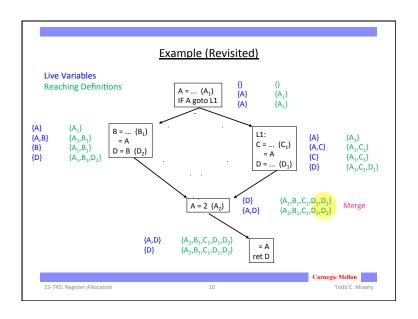
Todd C. Mowry

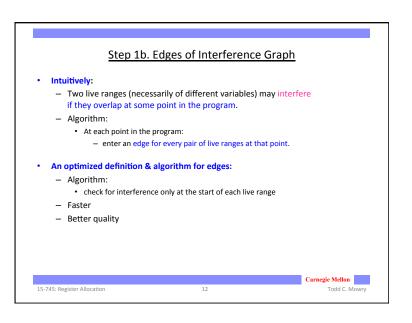
III. Algorithm Step 1. Build an interference graph a. refining notion of a node b. finding the edges Step 2. Coloring - use heuristics to try to find an n-coloring • Success: - colorable and we have an assignment • Failure: - graph not colorable, or - graph is colorable, but it is too expensive to color

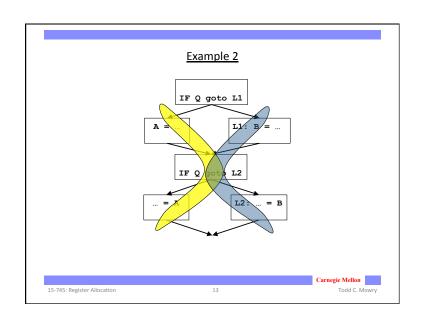
Register Allocation and Coloring • A graph is n-colorable if: - every node in the graph can be colored with one of the n colors such that two adjacent nodes do not have the same color. • Assigning n register (without spilling) = Coloring with n colors - assign a node to a register (color) such that no two adjacent nodes are assigned same registers(colors) • Is spilling necessary? = Is the graph n-colorable? • To determine if a graph is n-colorable is NP-complete, for n>2 - Too expensive - Heuristics

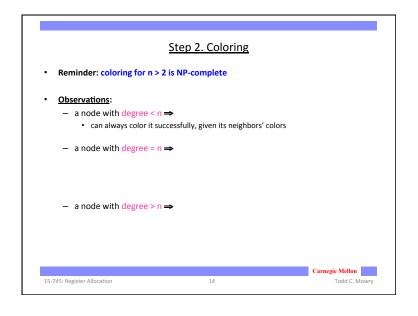




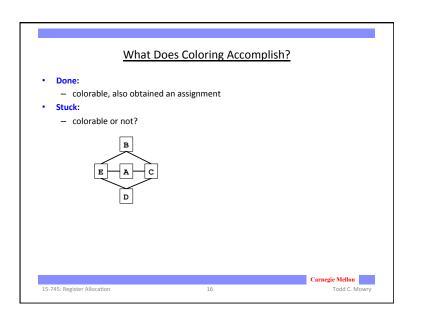








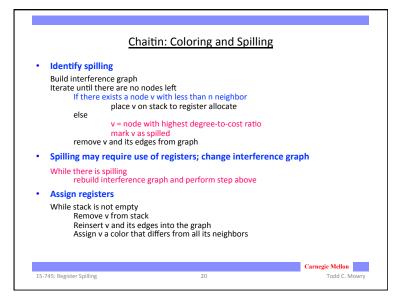
Coloring Algorithm • Algorithm: - Iterate until stuck or done • Pick any node with degree < n • Remove the node and its edges from the graph - If done (no nodes left) • reverse process and add colors • Example (n = 3): • Note: degree of a node may drop in iteration • Avoids making arbitrary decisions that make coloring fail | Carnegie Mellon | Todd C. Mowry



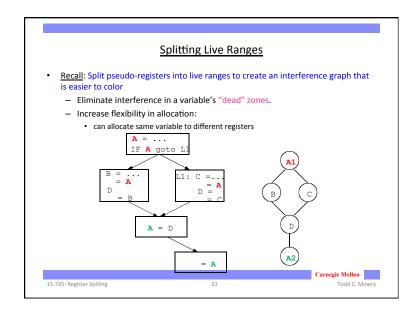
Extending Coloring: Design Principles A pseudo-register is - Colored successfully: allocated a hardware register - Not colored: left in memory · Objective function - Cost of an uncolored node: · proportional to number of uses/definitions (dynamically) · estimate by its loop nesting - Objective: minimize sum of cost of uncolored nodes Heuristics Benefit of spilling a pseudo-register: · increases colorability of pseudo-registers it interferes with · can approximate by its degree in interference graph Greedy heuristic · spill the pseudo-register with lowest cost-to-benefit ratio, whenever spilling is necessary Carnegie Mellon 15-745: Register Spilling Todd C. Mowry

Review: Coloring Algorithm (Without Spilling) · Attempt to Color Graph Build interference graph Iterate until there are no nodes left If there exists a node v with less than n neighbor place v on stack to register allocate else return (coloring heuristics fail) remove v and its edges from graph Assign registers While stack is not empty Remove v from stack Reinsert v and its edges into the graph Assign v a color that differs from all its neighbors Carnegie Mellon 15-745: Register Spilling Todd C. Mown

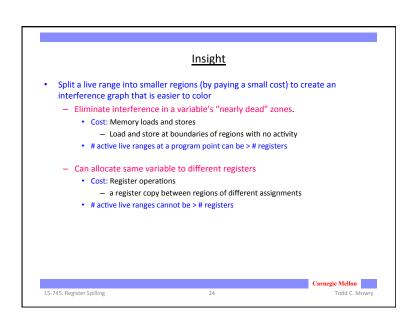
Spilling to Memory • CISC architectures - can operate on data in memory directly - memory operations are slower than register operations • RISC architectures - machine instructions can only apply to registers - Use • must first load data from memory to a register before use - Definition • must first compute RHS in a register • store to memory afterwards - Even if spilled to memory, needs a register at time of use/definition

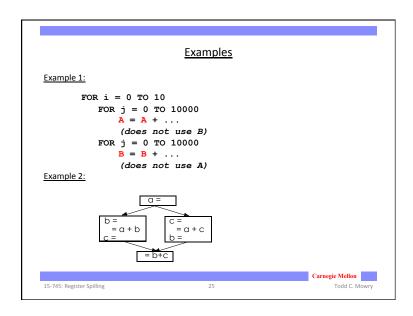


Spilling • What should we spill? - Something that will eliminate a lot of interference edges - Something that is used infrequently - Maybe something that is live across a lot of calls? • One Heuristic: - spill cheapest live range (aka "web") - Cost = [(# defs & uses)*10|oop-nest-depth]/degree



Quality of Chaitin's Algorithm Giving up too quickly An optimization: "Prioritize the coloring" Still eliminate a node and its edges from graph Do not commit to "spilling" just yet Try to color again in assignment phase. Carnegie Mellon Todd C. Mowry





One Algorithm • Observation: spilling is absolutely necessary if - number of live ranges active at a program point > n • Apply live-range splitting before coloring - Identify a point where number of live ranges > n - For each live range active around that point: • find the outermost "block construct" that does not access the variable - Choose a live range with the largest inactive region - Split the inactive region from the live range

Live Range Splitting When do we apply live range splitting? Which live range to split? Where should the live range be split? How to apply live-range splitting with coloring? Advantage of coloring: defers arbitrary assignment decisions until later When coloring fails to proceed, may not need to split live range degree of a node >= n does not mean that the graph definitely is not colorable Interference graph does not capture positions of a live range

