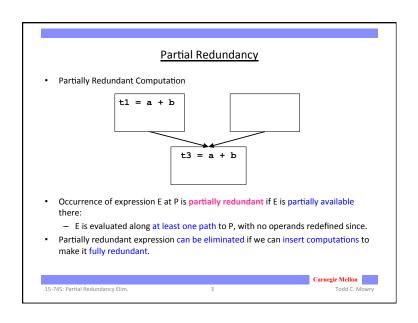
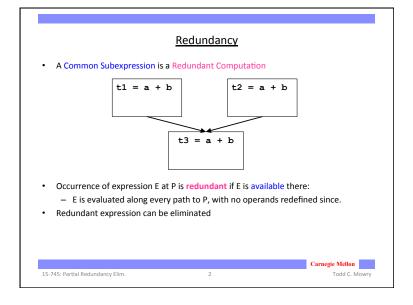
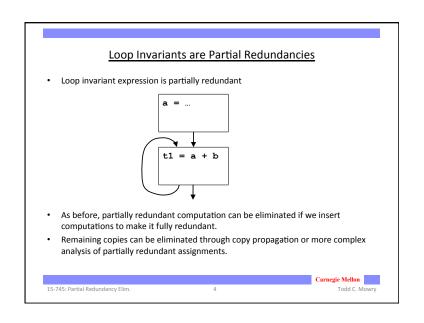
## Partial Redundancy Elimination Global code motion optimization Remove partially redundant expressions Loop invariant code motion Can be extended to do Strength Reduction No loop analysis needed Bidirectional flow problem







### Partial Redundancy Elimination

- The Method:
  - 1. Insert Computations to make partially redundant expression(s) fully
  - 2. Eliminate redundant expression(s).
- · Issues [Outline of Lecture]:
  - 1. What expression occurrences are candidates for elimination?
  - 2. Where can we safely insert computations?
  - 3. Where do we want to insert them?
- For this lecture, we assume one expression of interest, a+b.
  - In practice, with some restrictions, can do many expressions in parallel.

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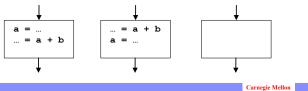
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### Finding Partially Available Expressions

- · Forward flow problem
  - Lattice = { 0, 1 }, meet is union (U), Top = 0 (not PAVAIL), entry = 0
    - PAVOUT[i] = (PAVIN[i] KILL[i]) ∪ AVLOC[i]



- · For a block,
  - Expression is locally available (AVLOC) if downwards exposed.
  - · Expression is killed (KILL) if any assignments to operands.



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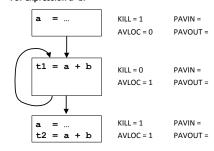
### Which Occurrences Might Be Eliminated?

- In CSE,
  - E is available at P if it is previously evaluated along every path to P, with no subsequent redefinitions of operands.
  - If so, we can eliminate computation at P.
- - E is partially available at P if it is previously evaluated along at least one path to P, with no subsequent redefinitions of operands.
  - If so, we might be able to eliminate computation at P, if we can insert computations to make it fully redundant.
- Occurrences of E where E is partially available are candidates for elimination.

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### Partial Availability Example

· For expression a+b.



· Occurrence in loop is partially redundant.

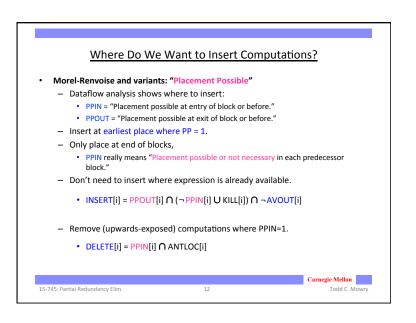
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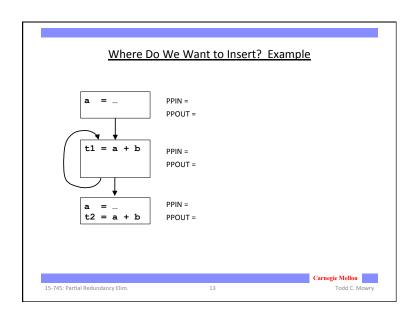
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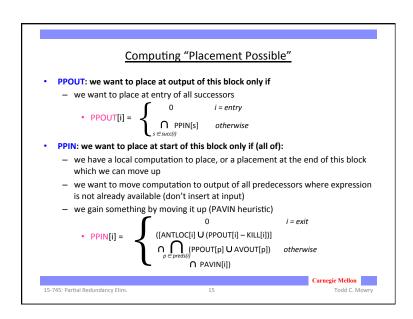
### Where Can We Insert Computations? Safety: never introduce a new expression along any path. t1 = a + b Insertion could introduce exception, change program behavior. If we can add a new basic block, can insert safely in most cases. Solution: insert expression only where it is anticipated. Performance: never increase the # of computations on any path. Under simple model, guarantees program won't get worse. Reality: might increase register lifetimes, add copies, lose.

### **Anticipation Example** · For expression a+b. a = ... KILL = 1 ANTIN = ANTLOC = 0 ANTOUT = t1 = a + bKILL = 0ANTIN = ANTLOC = 1 ANTOUT = KILL = 1 ANTIN = a = ... ANTLOC = 0 ANTOUT = t2 = a + b· Expression is anticipated at end of first block. · Computation may be safely inserted there. Carnegie Mellon 15-745: Partial Redundancy Elim. Todd C. Mown

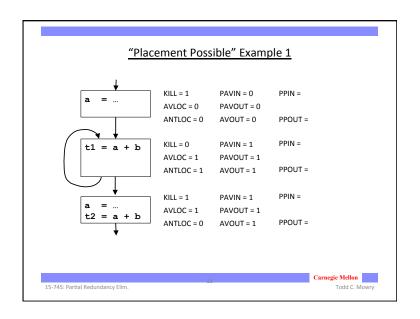
# Finding Anticipated Expressions • Backward flow problem - Lattice = {0, 1}, meet is intersection (\(\Omega\), top = 1 (ANT), exit = 0 • ANTIN[i] = ANTLOC[i] \(\Omega\) (ANTOUT[i] - KILL[i]) • ANTOUT[i] = \(\begin{array}{c} 0 & i = exit \\ \cdot \ANTIN[s] & otherwise \end{array} • For a block, • Expression locally anticipated (ANTLOC) if upwards exposed. \(\omega\) = a + b \(\omega\) a = ... \(\omega\) = a + b \(\omega\) a = ... \(\omega\) = a + b \(\omega\) a = ... \(\omega\) Todd C. Mowry

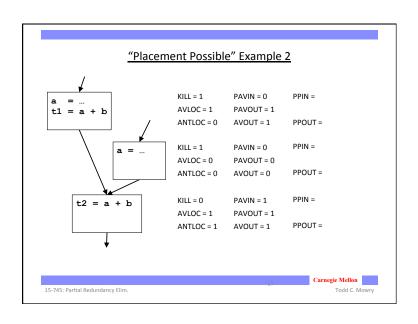


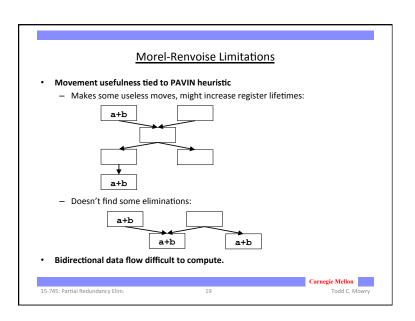




### Formulating the Problem . PPOUT: we want to place at output of this block only if we want to place at entry of all successors • PPIN: we want to place at input of this block only if (all of): - we have a local computation to place, or a placement at the end of this block which we can move up we want to move computation to output of all predecessors where expression is not already available (don't insert at input) - we can gain something by placing it here (PAVIN) · Forward or Backward? - BOTH! · Problem is bidirectional, but lattice {0, 1} is finite, so - as long as transfer functions are monotone, it converges. Carnegie Mellon 15-745: Partial Redundancy Elim. 14 Todd C. Mowry







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### Related Work

- · Don't need heuristic
  - Dhamdhere, Drechsler-Stadel, Knoop,et.al.
  - use restricted flow graph or allow edge placements.
- Data flow can be separated into unidirectional passes
  - Dhamdhere, Knoop, et. al.
- · Improvement still tied to accuracy of computational model
  - Assumes performance depends only on the number of computations along any path.
  - Ignores resource constraint issues: register allocation, etc.
  - Knoop, et.al. give "earliest" and "latest" placement algorithms which begin to address this.
- Further issues:
  - more than one expression at once, strength reduction, redundant assignments, redundant stores.

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15-745: Partial Redundancy Elim.

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