

We use induction.

When  $n = 1$ , the equation becomes  $2 = 2^2 - 2$ , obviously it is true.

Assume  $n = k$ , we have

$$\sum_{i=1}^n 2^i = 2^{n+1} - 2$$

When  $n = k + 1$ ,

$$\begin{aligned}\sum_{i=1}^{n+1} 2^i &= \left(\sum_{i=1}^n 2^i\right) + 2^{n+1} \\ &= (2^{n+1} - 2) + 2^{n+1} \\ &= 2^{n+1} + 2^{n+1} - 2 \\ &= 2^{n+2} - 2\end{aligned}$$

It satisfies the assumption.

Hence, it's proved true.