

# Task 1

In [30]:

```
import numpy as np
import matplotlib.pyplot as plt
from matplotlib.colors import ListedColormap
import scipy.stats as scp
import math
from sklearn import cross_validation, datasets, metrics, neighbors
```

```
%matplotlib inline
%pylab inline
```

```
SIZE = 1000
```

Populating the interactive namespace from numpy and matplotlib

```
/usr/local/lib/python2.7/dist-packages/sklearn/cross_validation.py:44:
DeprecationWarning: This module was deprecated in version 0.18 in fav
or of the model_selection module into which all the refactored classes
and functions are moved. Also note that the interface of the new CV i
terators are different from that of this module. This module will be r
emoved in 0.20.
```

```
"This module will be removed in 0.20.", DeprecationWarning)
```

## Генерация данных:

In [94]:

```
classification_problem = datasets.make_classification(n_samples=10000,
                                                    n_features=2,
                                                    n_informative=2,
                                                    n_classes=4,
                                                    n_redundant=0,
                                                    n_clusters_per_class=1,
                                                    random_state=3)

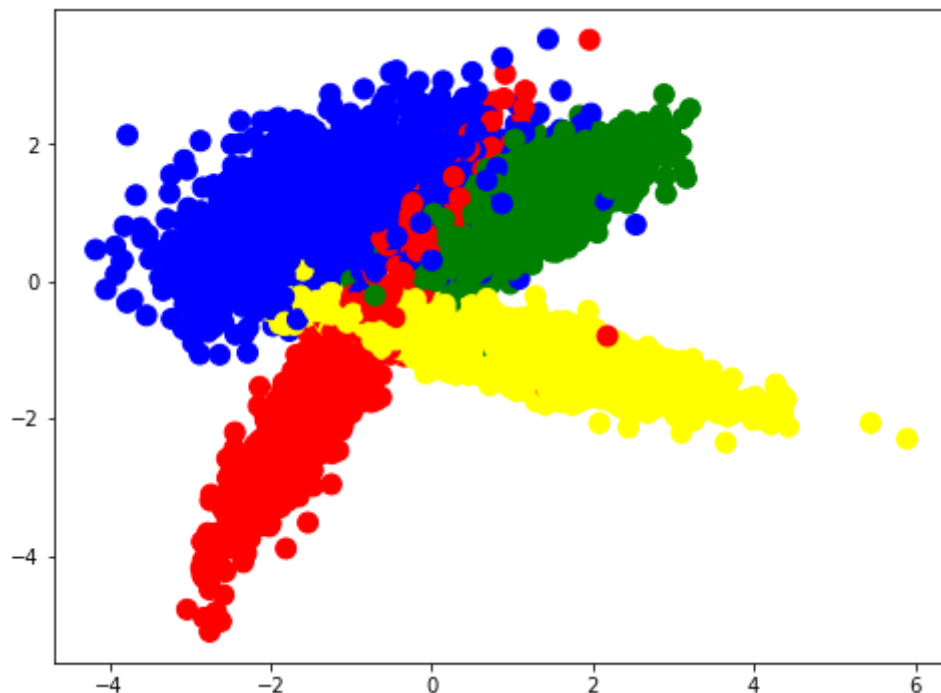
colors = ListedColormap(['red', 'blue', 'yellow', 'green'])
light_colors = ListedColormap(
    ['lightcoral', 'lightblue', 'lightyellow', 'lightgreen'])
```

In [95]:

```
pylab.figure(figsize=(8,6))
pylab.scatter(map(lambda x: x[0], classification_problem[0]),
              map(lambda x: x[1], classification_problem[0]),
              c=classification_problem[1], cmap=colors, s=100)
```

Out[95]:

<matplotlib.collections.PathCollection at 0x7f5c6b1181d0>



In [96]:

```
train_data, test_data, train_labels, test_labels
= cross_validation.train_test_split(classification_problem[0],
                                    classification_problem[1],
                                    test_size = 0.3,
                                    random_state = 1)
```

## Визуализируем разделяющие поверхности:

In [38]:

```
def get_meshgrid(data, step=.05, border=.5,):
    x_min, x_max = data[:, 0].min() - border, data[:, 0].max() + border
    y_min, y_max = data[:, 1].min() - border, data[:, 1].max() + border
    return np.meshgrid(np.arange(x_min, x_max, step),
                      np.arange(y_min, y_max, step))
```

In [42]:

```

def plot_decision_surface(estimator, train_data, train_labels,
                           test_data, test_labels,
                           colors = colors, light_colors = light_colors):
    #fit model
    estimator.fit(train_data, train_labels)

    #set figure size
    pyplot.figure(figsize = (16, 6))

    #plot decision surface on the train data
    pyplot.subplot(1,2,1)
    xx, yy = get_meshgrid(train_data)
    mesh_predictions = np.array(
        estimator.predict(np.c_[xx.ravel(), yy.ravel()])).reshape(xx.shape)
    pyplot.pcolormesh(
        xx, yy, mesh_predictions, cmap = light_colors)
    pyplot.scatter(
        train_data[:, 0], train_data[:, 1], c = train_labels, s = 100, cmap = colors)
    pyplot.title(
        'Train data, accuracy={:.2f}'
        .format(metrics.accuracy_score(train_labels,
                                        estimator.predict(train_data))))

    #plot decision surface on the test data
    pyplot.subplot(1,2,2)
    pyplot.pcolormesh(xx, yy, mesh_predictions, cmap = light_colors)
    pyplot.scatter(test_data[:, 0], test_data[:, 1],
                   c = test_labels, s = 100, cmap = colors)
    pyplot.title('Test data, accuracy={:.2f}'
                 .format(metrics.accuracy_score(test_labels,
                                                estimator.predict(test_data))))

```

In [45]:

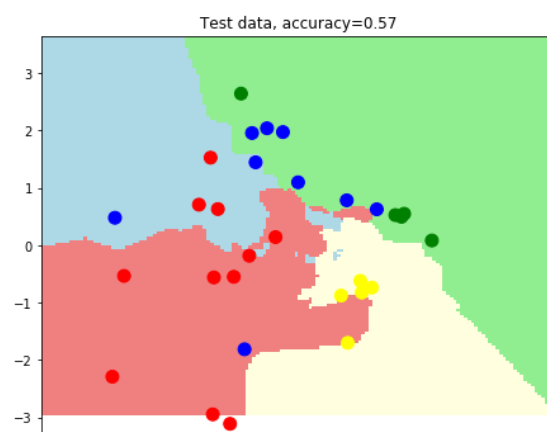
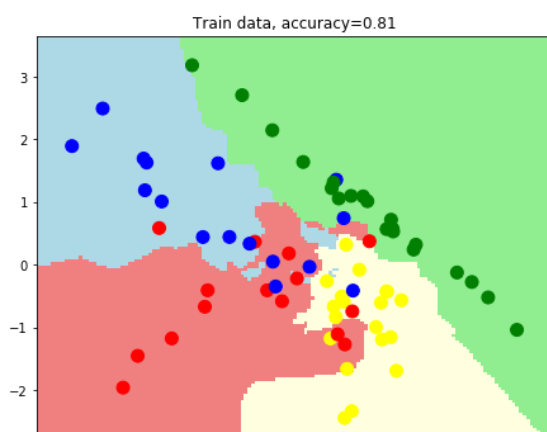
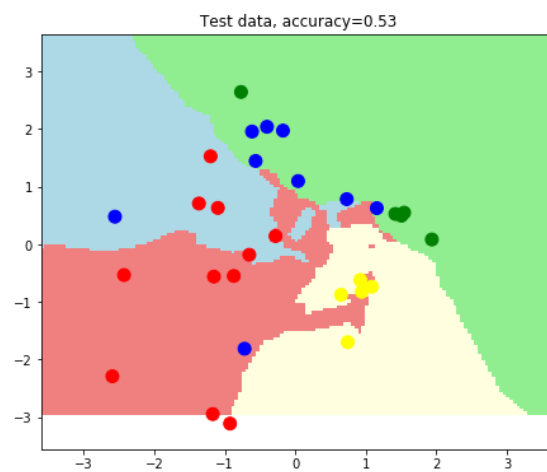
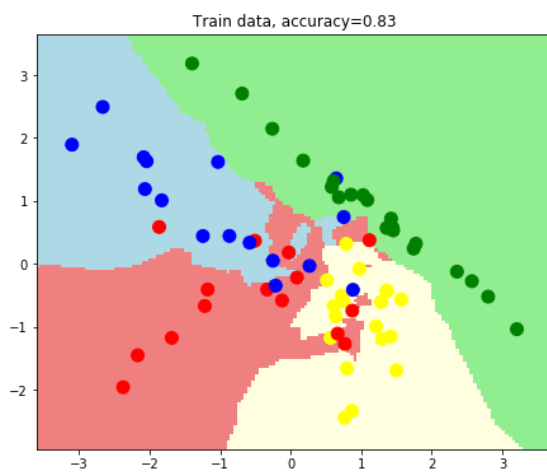
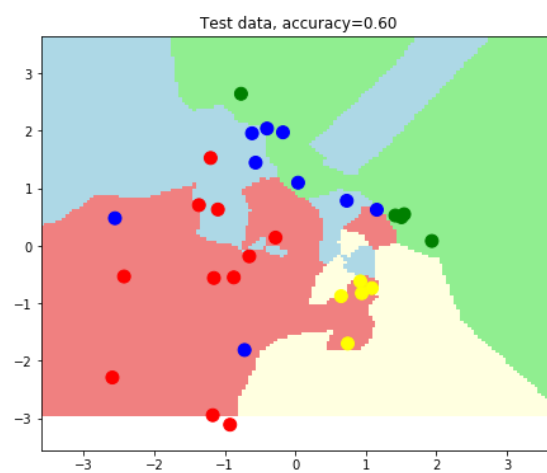
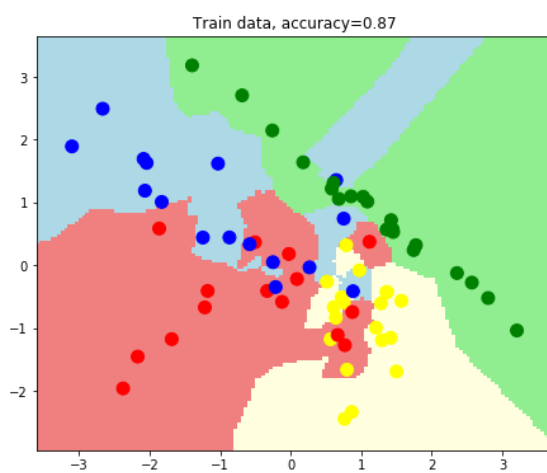
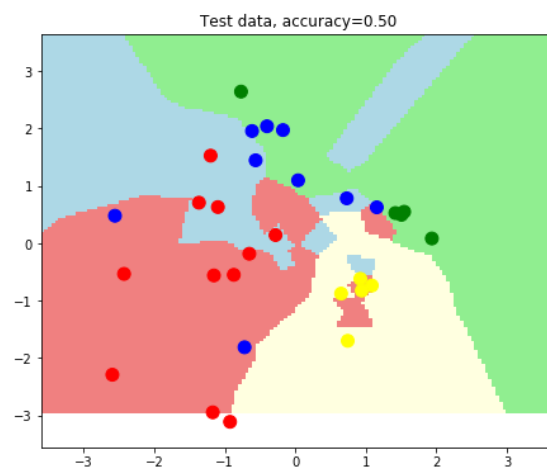
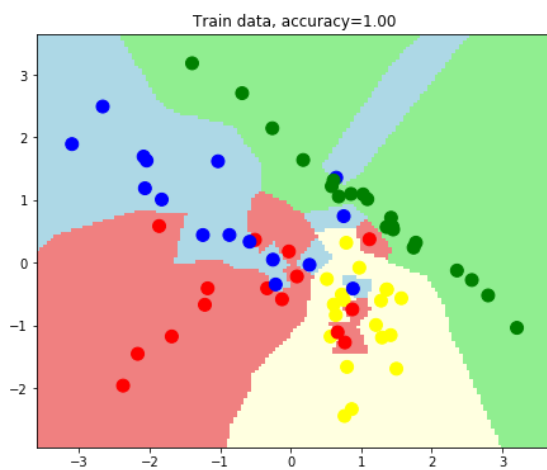
```

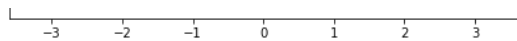
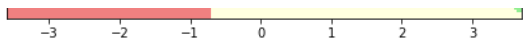
def plot_surface_with_k_neighbours(k):
    estimator = neighbors.KNeighborsClassifier(n_neighbors=k)
    plot_decision_surface(
        estimator, train_data, train_labels, test_data, test_labels)

```

In [52]:

```
for i in range(1,5):  
    plot_surface_with_k_neighbours(i)
```





## Теперь построим график ассигуры от количества соседей:

In [97]:

```
def get_accuracy(estimator, train_data, train_labels, test_data, test_labels,
                  colors = colors, light_colors = light_colors):

    estimator.fit(train_data, train_labels)
    return [metrics.accuracy_score(train_labels, estimator.predict(train_data)),
            metrics.accuracy_score(test_labels, estimator.predict(test_data))]

def get_accuracy_for_k_neighbours(k):
    estimator = neighbors.KNeighborsClassifier(n_neighbors=k)
    return get_accuracy(estimator, train_data,
                        train_labels, test_data, test_labels)

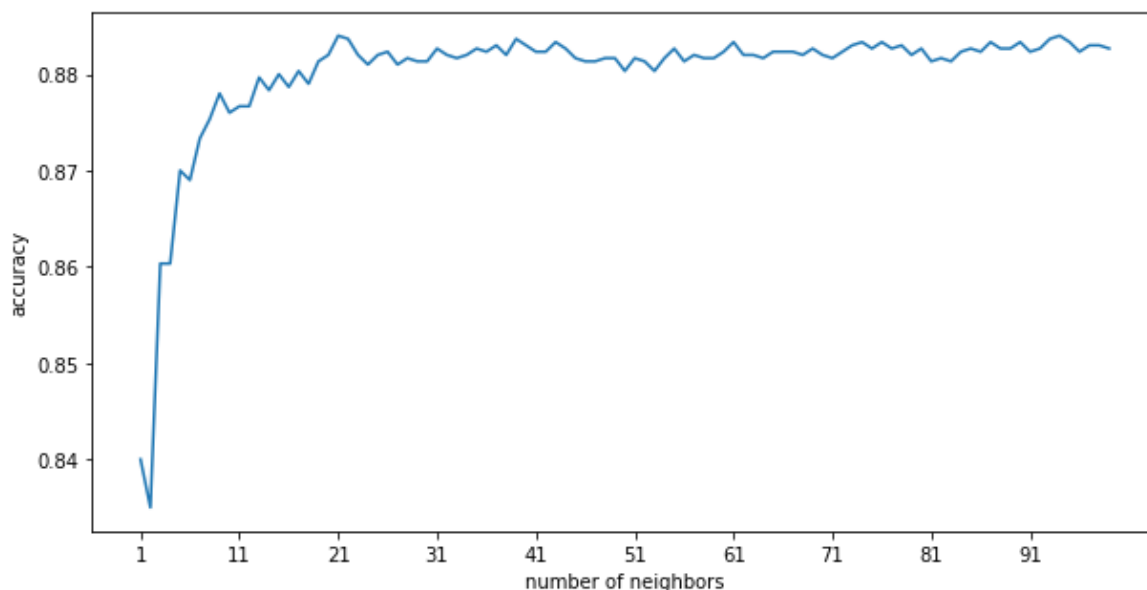
def get_accuracy_array():
    result = []
    for i in range(1,100):
        result.append(get_accuracy_for_k_neighbours(i))
    return np.array(result)
```

In [98]:

```
accuracy = (get_accuracy_array())[:,1]
```

In [100]:

```
fig = plt.figure(figsize=[10, 5])
plt.plot(np.arange(1, 100), accuracy)
plt.xlabel('number of neighbors')
plt.ylabel('accuracy')
plt.xticks(np.arange(1,100)[::10])
plt.show()
```



Как мы видим, наилучшая ассигура получается при  $n = 20$

## Task 2

In [84]:

```
from sklearn import datasets
from sklearn.model_selection import cross_val_score
from sklearn import naive_bayes
```

In [67]:

```
digits = datasets.load_digits()
```

In [68]:

```
digits
```

Out[68]:

```
{'DESCR': "Optical Recognition of Handwritten Digits Data Set\n=====\n\nNotes\n----\nData Set Characteristics:\n      :Number of Instances: 5620\n      :Number of Attributes: 64\n      :Attribute Information: 8x8 image of integer pixels in the range 0..16.\n      :Missing Attribute Values: None\n      :Creator: E. Alpaydin (alpaydin '@' boun.edu.tr)\n      :Date: July; 1998\n\nThis is a copy of the test set of the UCI ML hand-written digits datasets\nhttp://archive.ics.uci.edu/ml/datasets/Optical+Recognition+of+Handwritten+Digits\n\nThe data set contains images of hand-written digits: 10 classes where each class refers to a digit.\n\nPreprocessing programs made available by NIST were used to extract normalized bitmaps of handwritten digits from a preprinted form. From a total of 43 people, 30 contributed to the training set and different 13 to the test set. 32x32 bitmaps are divided into nonoverlapping blocks of 4x4 and the number of on pixels are counted in each block. This generates an input matrix of 8x8 where each element is an integer in the range 0..16. This reduces dimensionality and gives invariance to small distortions.\n\nFor info on NIST preprocessing routines, see M. D. Garriss, J. L. Blue, G. T. Candela, D. L. Dimmick, J. Geist, P. J. Grother, S. A. Janet, and C. L. Wilson, NIST Form-Based Handprint Recognition System, NISTIR 5469, 1994.\n\nReferences\n-----\n- C. Kaynak (1995) Methods of Combining Multiple Classifiers and Their Applications to Handwritten Digit Recognition, MSc Thesis, Institute of Graduate Studies in Science and Engineering, Bogazici University.\n- E. Alpaydin, C. Kaynak (1998) Cascading Classifiers, Kybernetika.\n- Ken Tang and Ponnuthurai N. Suganthan and Xi Yao and A. Kai Qin. Linear dimensionality reduction using relevance weighted LDA. School of Electrical and Electronic Engineering Nanyang Technological University. 2005.\n- Claudio Gentile. A New Approximate Maximal Margin Classification Algorithm. NIPS. 2000.\n",
  'data': array([[ 0.,  0.,  5., ...,  0.,  0.,  0.],
                [ 0.,  0.,  0., ..., 10.,  0.,  0.],
                [ 0.,  0.,  0., ..., 16.,  9.,  0.],
                ...,
                [ 0.,  0.,  1., ...,  6.,  0.,  0.],
                [ 0.,  0.,  2., ..., 12.,  0.,  0.],
                [ 0.,  0., 10., ..., 12.,  1.,  0.])),
  'images': array([[[ 0.,  0.,  5., ...,  1.,  0.,  0.],
                    [ 0.,  0., 13., ..., 15.,  5.,  0.],
                    [ 0.,  3., 15., ..., 11.,  8.,  0.],
                    ...,
                    [ 0.,  4., 11., ..., 12.,  7.,  0.],
                    [ 0.,  2., 14., ..., 12.,  0.,  0.],
                    [ 0.,  0.,  6., ...,  0.,  0.,  0.]],
                   [[ 0.,  0.,  0., ...,  5.,  0.,  0.],
                    [ 0.,  0.,  0., ...,  9.,  0.,  0.],
                    [ 0.,  0.,  3., ...,  6.,  0.,  0.],
                    ...,
                    [ 0.,  0.,  1., ...,  6.,  0.,  0.],
                    [ 0.,  0.,  1., ...,  6.,  0.,  0.],
                    [ 0.,  0.,  0., ..., 10.,  0.,  0.]],
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                    [ 0.,  0.,  8., ..., 16.,  0.,  0.],
                    ...,
                    [ 0.,  9., 16., ...,  0.,  0.,  0.],
                    [ 0.,  3., 13., ..., 11.,  5.,  0.],
                    [ 0.,  0.,  0., ..., 16.,  9.,  0.]])]
```



```

...,
[[ 0.,  0.,  1., ...,  1.,  0.,  0.],
 [ 0.,  0., 13., ...,  2.,  1.,  0.],
 [ 0.,  0., 16., ..., 16.,  5.,  0.],
...,
 [ 0.,  0., 16., ..., 15.,  0.,  0.],
 [ 0.,  0., 15., ..., 16.,  0.,  0.],
 [ 0.,  0.,  2., ...,  6.,  0.,  0.]],

[[ 0.,  0.,  2., ...,  0.,  0.,  0.],
 [ 0.,  0., 14., ..., 15.,  1.,  0.],
 [ 0.,  4., 16., ..., 16.,  7.,  0.],
...,
 [ 0.,  0.,  0., ..., 16.,  2.,  0.],
 [ 0.,  0.,  4., ..., 16.,  2.,  0.],
 [ 0.,  0.,  5., ..., 12.,  0.,  0.]],

[[ 0.,  0., 10., ...,  1.,  0.,  0.],
 [ 0.,  2., 16., ...,  1.,  0.,  0.],
 [ 0.,  0., 15., ..., 15.,  0.,  0.],
...,
 [ 0.,  4., 16., ..., 16.,  6.,  0.],
 [ 0.,  8., 16., ..., 16.,  8.,  0.],
 [ 0.,  1.,  8., ..., 12.,  1.,  0.] ]]),
'target': array([0, 1, 2, ..., 8, 9, 8]),
'target_names': array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])}

```

In [69]:

```
breast = datasets.load_breast_cancer()
```

In [73]:

```
breast
```

Out[73]:

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```
f Two Linearly Inseparable Sets",\nOptimization Methods and Software
1, 1992, 23-34].\n\nThis database is also available through the UW CS
ftp server:\n\nftp ftp.cs.wisc.edu\ncd math-prog/cpo-dataset/machine-
learn/WDBC/\n\nReferences\n-----\n    - W.N. Street, W.H. Wolberg
and O.L. Mangasarian. Nuclear feature extraction \n    for breast tu
mor diagnosis. IS&T/SPIE 1993 International Symposium on \n    Electr
onic Imaging: Science and Technology, volume 1905, pages 861-870,\n
    San Jose, CA, 1993.\n    - O.L. Mangasarian, W.N. Street and W.H. Wol
berg. Breast cancer diagnosis and \n    prognosis via linear programm
ing. Operations Research, 43(4), pages 570-577, \n    July-August 199
5.\n    - W.H. Wolberg, W.N. Street, and O.L. Mangasarian. Machine lear
ning techniques\n    to diagnose breast cancer from fine-needle aspir
ates. Cancer Letters 77 (1994) \n    163-171.\n',
'data': array([[ 1.79900000e+01,  1.03800000e+01,  1.22800000e+02,
...,
                2.65400000e-01,  4.60100000e-01,  1.18900000e-01],
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  2.43000000e-01,  3.61300000e-01,  8.75800000e-02],
...,
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  1.41800000e-01,  2.21800000e-01,  7.82000000e-02],
[ 2.06000000e+01,  2.93300000e+01,  1.40100000e+02, ...,
  2.65000000e-01,  4.08700000e-01,  1.24000000e-01],
[ 7.76000000e+00,  2.45400000e+01,  4.79200000e+01, ...,
  0.00000000e+00,  2.87100000e-01,  7.03900000e-02]]),
'feature_names': array(['mean radius', 'mean texture', 'mean perimete
r', 'mean area',
                        'mean smoothness', 'mean compactness', 'mean concavity',
                        'mean concave points', 'mean symmetry', 'mean fractal dimensio
n',
                        'radius error', 'texture error', 'perimeter error', 'area erro
r',
                        'smoothness error', 'compactness error', 'concavity error',
                        'concave points error', 'symmetry error', 'fractal dimension e
rror',
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                        'worst smoothness', 'worst compactness', 'worst concavity',
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sion']),
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0, 1,
```

```

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1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1]),
'target_names': array(['malignant', 'benign'],
dtype='|S9')}
```

In [90]:

```
def get_number_of_operations(method, d_set):
    return np.mean(cross_val_score(method, d_set.data, d_set.target))
```

In [92]:

```
print('digits dataset:')
print('bernulli accuracy = {:.2f}'.format(
    get_number_of_operations(naive_bayes.BernoulliNB(), digits)))
print('multinomial accuracy = {:.2f}'.format(
    get_number_of_operations(naive_bayes.MultinomialNB(), digits)))
print('gaussian accuracy = {:.2f}'.format(
    get_number_of_operations(naive_bayes.GaussianNB(), digits)))
```

```
digits dataset:
bernulli accuracy = 0.83
multinomial accuracy = 0.87
gaussian accuracy = 0.82
```

In [93]:

```
print('breast_canser dataset:')
print('bernulli accuracy = {:.2f}'.format(
    get_number_of_operations(naive_bayes.BernoulliNB(), breast)))
print('multinomial accuracy = {:.2f}'.format(
    get_number_of_operations(naive_bayes.MultinomialNB(), breast)))
print('gaussian accuracy = {:.2f}'.format(
    get_number_of_operations(naive_bayes.GaussianNB(), breast)))
```

```
breast_canser dataset:
bernulli accuracy = 0.63
multinomial accuracy = 0.89
gaussian accuracy = 0.94
```

Итак, максимально качество на датасете digits: 0.87 на датасете breast\_canser: 0.94

Из наших данных верны следующие пункты: (b)

## Task 3

### Сгенерируем выборку точек

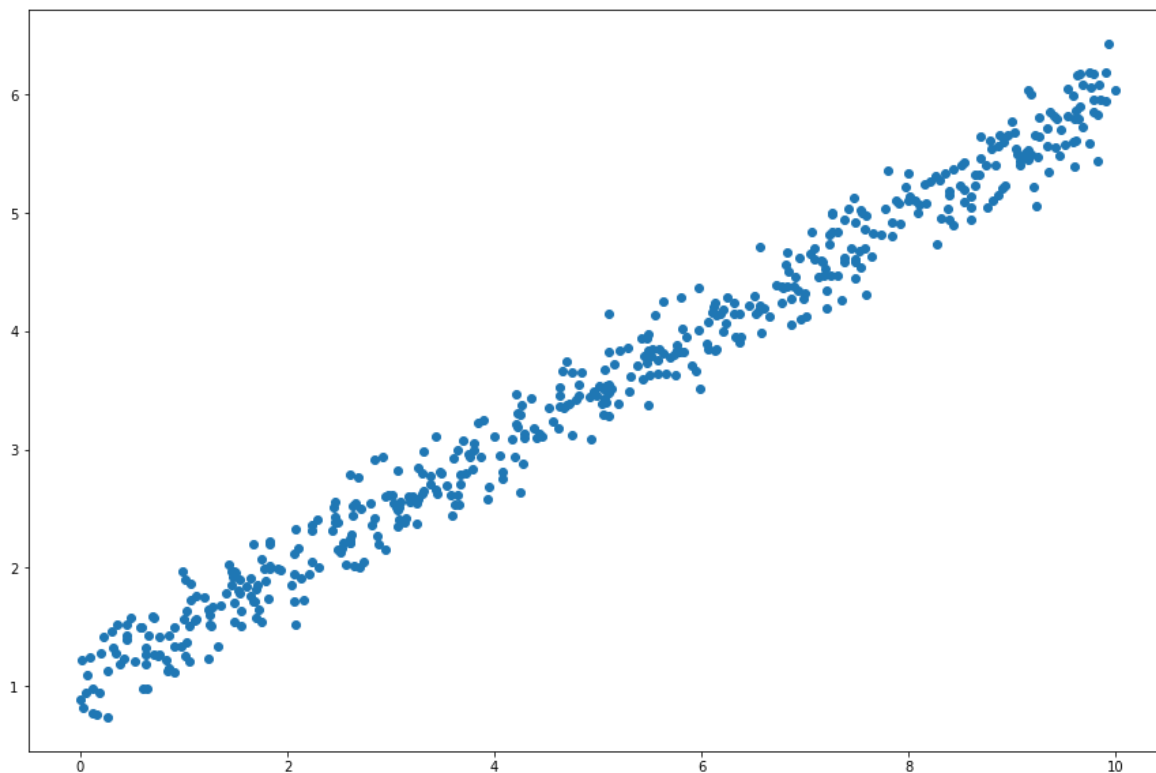
In [107]:

```
A = 0
SCALE = 0.2
SIZE = 500

eps = np.array(scp.norm.rvs(loc=A, scale=SCALE, size=SIZE))
sampleX = np.array(scp.uniform.rvs(loc=0, scale=10, size=SIZE))
sampleY = sampleX * 0.5 + 1 + eps
```

In [108]:

```
fig = plt.figure(figsize=[15, 10])
plt.scatter(sampleX, sampleY)
plt.show()
```



## Построим оценки

In [110]:

```
from scipy.optimize import minimize
```

In [129]:

```
def func(args, x):
    k, b = args
    return k * x + b

def func_mean_squares(args):
    k, b = args
    return ((k * sampleX + b - sampleY) ** 2).mean()

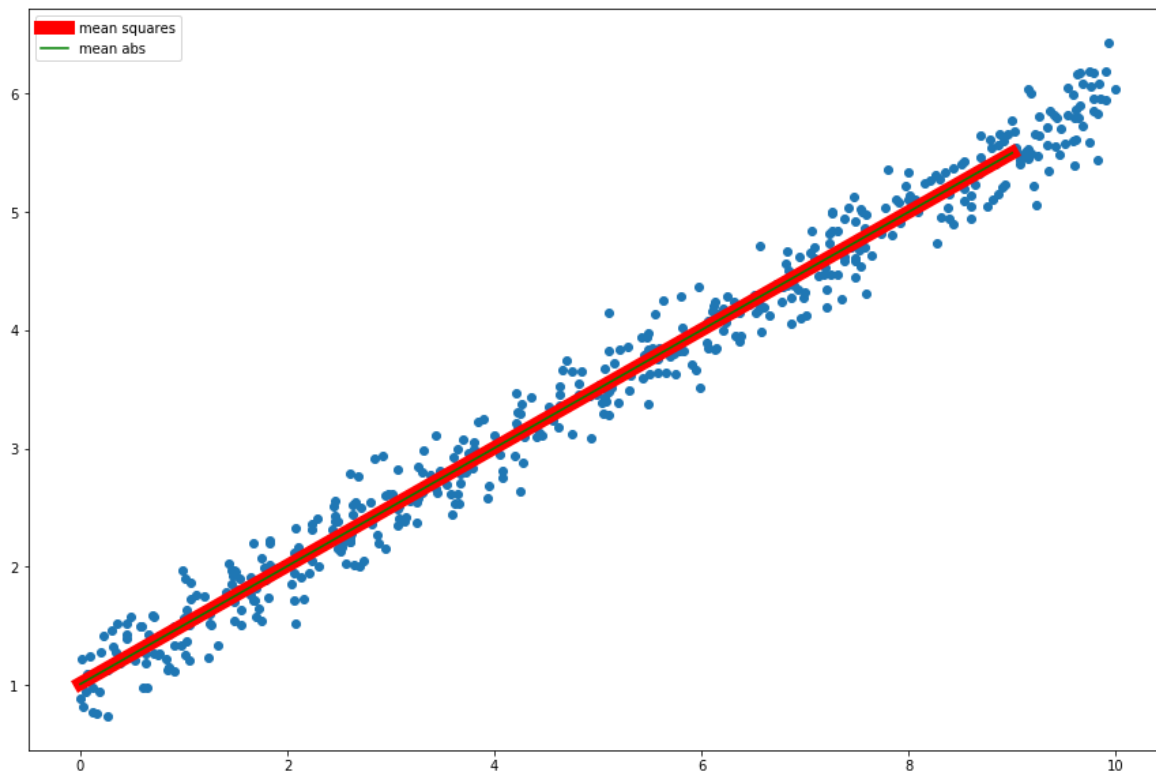
def func_mean_abs(args):
    k, b = args
    return np.mean(np.fabs(k * sampleX + b - sampleY))
```

In [130]:

```
bnds = ((0, 10), (-10, 10))
res_mean_squares = minimize(func_mean_squares, (2, 0), bounds=bnds)
res_mean_abs = minimize(func_mean_abs, (2, 0), bounds=bnds)
```

In [135]:

```
fig = plt.figure(figsize=[15, 10])
plt.scatter(sampleX, sampleY)
plt.plot(np.arange(10), func(res_mean_squares.x, np.arange(10)),
         linewidth=10, color='red', label=r'mean squares')
plt.plot(np.arange(10), func(res_mean_abs.x, np.arange(10)),
         color='green', label=r'mean abs')
plt.legend()
plt.show()
```



## Добавим выбросы

In [136]:

```
newEps = np.array(scp.norm.rvs(loc=A, scale=SCALE, size=75))
newX = np.array(scp.uniform.rvs(loc=0, scale=10, size=75))
newY = -1 + newEps
```

In [137]:

```
sampleX = np.append(sampleX, newX)
sampleY = np.append(sampleY, newY)
```

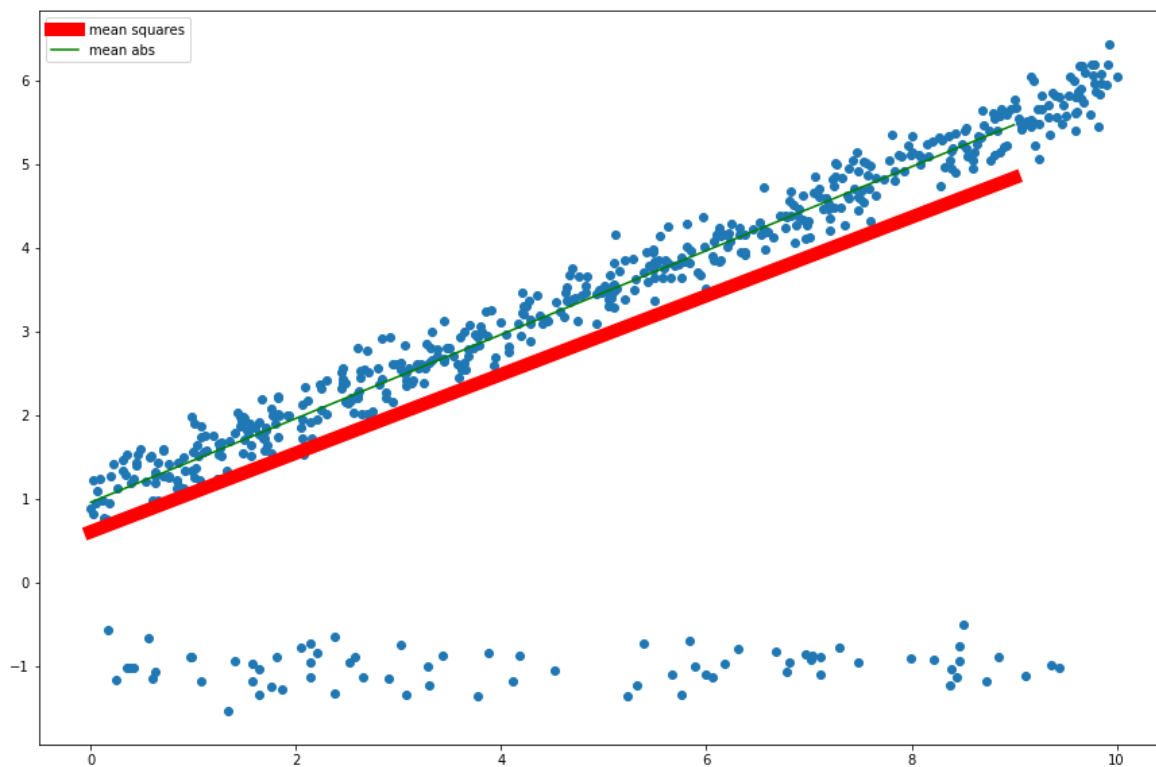
In [138]:

```
bnds = ((0, 10), (-10, 10))
res_mean_squares = minimize(func_min_squares, (2, 0), bounds=bnds)
res_mean_abs = minimize(func_min_abs, (2, 0), bounds=bnds)
```



In [139]:

```
fig = plt.figure(figsize=[15, 10])
plt.scatter(sampleX, sampleY)
plt.plot(np.arange(10), func(res_mean_squares.x, np.arange(10)),
         linewidth=10, color='red', label=r'mean squares')
plt.plot(np.arange(10), func(res_mean_abs.x, np.arange(10)),
         color='green', label=r'mean abs')
plt.legend()
plt.show()
```



Как мы видим, метод минимизации среднего квадрата отклонения более подвержен влиянию выбросов.

In [ ]: