

Ph291E Lab 4 – Bessel & Telescope

Zeshui Song
The Cooper Union

November 13, 2025

1 Purpose

Using Bessel's method to determine the focal lengths of two different converging lenses, we will construct a simple refracting telescope using these lenses and determine its magnification both experimentally and theoretically.

2 Data

Approximate Focal Lengths

$$f_1 =$$

$$f_2 =$$

Measurements for Bessel's Method Calculations for Focal Lengths

Table 1: Bessel's Method Data for Lens 1

D (cm)	d (cm)	Random Error D (mm)	Random Error d (mm)	Inst. Error (mm)
2.180				
2.190				
2.185				
2.185				
2.195				
2.180	0.005	0.002	0.002	0.0005
Mean D				7.66 mm
Mean d				7.66 mm

Table 2: Bessel's Method Data for Lens 2

D (cm)	d (cm)	Random Error D (mm)	Random Error d (mm)	Inst. Error (mm)
2.180				
2.190				
2.185				
2.185				
2.195				
2.180	0.005	0.002	0.002	0.0005
Mean D				7.66 mm
Mean d				7.66 mm

Approximate Angular Magnification

3 Calculations

Length D Sample Calculations

Mean Calculation:

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$\bar{x} = \frac{1}{6}(2.180 + 2.190 + 2.185 + 2.185 + 2.195 + 2.180)$$

$$\bar{x} = 2.1858 \text{ mm}$$

Standard Deviation:

$$S_x = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2}$$

$$S_x = \sqrt{\frac{1}{6-1} \left[(2.180 - 2.1858)^2 + (2.190 - 2.1858)^2 + \cdots + (2.180 - 2.1858)^2 \right]}$$

$$S_x = 0.005845 \text{ mm}$$

Standard Deviation of the Mean (SDOM):

$$\sigma_{\bar{x}} = \frac{S_x}{\sqrt{n}}$$

$$\sigma_{\bar{x}} = \frac{0.005845}{\sqrt{6}}$$

$$\sigma_{\bar{x}} = 0.0023863 \text{ mm}$$

The same procedure was applied to calculate the mean, standard deviation and standard deviation of the mean for the remaining measurements.

Bessel's Method Calculations for Lens 1

$$f = \frac{D^2 - d^2}{4D}$$

$$f = \frac{(90.0)^2 - (30.0)^2}{4(90.0)}$$

$$f = 36.67 \text{ cm}$$

Error Propagation for Bessel's Method (Lens 1)

Since the measurements of D and d are independent, we can use the independent error propagation formula:

$$\delta f = \sqrt{\left(\frac{\partial f}{\partial D} \delta D\right)^2 + \left(\frac{\partial f}{\partial d} \delta d\right)^2}$$

$$\delta f = \sqrt{\left(\frac{D^2 + d^2}{4D^2} \delta D\right)^2 + \left(-\frac{d}{2D} \delta d\right)^2}$$

Chosen uncertainties: $\delta D = 0.05 \text{ mm}$ (random, larger than instrumental) and $\delta d = 0.005 \text{ mm}$ (instrumental, larger than random).

$$\delta f = \sqrt{\left(\frac{(90.0)^2 + (30.0)^2}{4(90.0)^2} (0.05)\right)^2 + \left(-\frac{30.0}{2(90.0)} (0.005)\right)^2}$$

$$\delta f = 0.0142 \text{ cm}$$

Angular Magnification

$$m_{\theta} = -\frac{f_{obj}}{f_{eye}}$$

$$m_{\theta} = -\frac{36.67}{10.0}$$

$$m_{\theta} = -3.667$$

Error Propagation for Angular Magnification

Since the measurements of f_{obj} and f_{eye} are independent, we can use the independent error propagation formula:

$$\delta m_\theta = \sqrt{\left(\frac{\partial m_\theta}{\partial f_{obj}} \delta f_{obj}\right)^2 + \left(\frac{\partial m_\theta}{\partial f_{eye}} \delta f_{eye}\right)^2}$$

$$\delta m_\theta = \sqrt{\left(-\frac{1}{f_{eye}} \delta f_{obj}\right)^2 + \left(\frac{f_{obj}}{f_{eye}^2} \delta f_{eye}\right)^2}$$

Chosen uncertainties: $\delta f_{obj} = 0.0142$ cm (from previous calculation) and $\delta f_{eye} = 0.05$ cm (instrumental).

$$\delta m_\theta = \sqrt{\left(-\frac{1}{10.0}(0.0142)\right)^2 + \left(\frac{36.67}{(10.0)^2}(0.05)\right)^2}$$

$$\delta m_\theta = 0.0191$$

4 Results

5 Conclusion

6 Answers to questions

Question 1