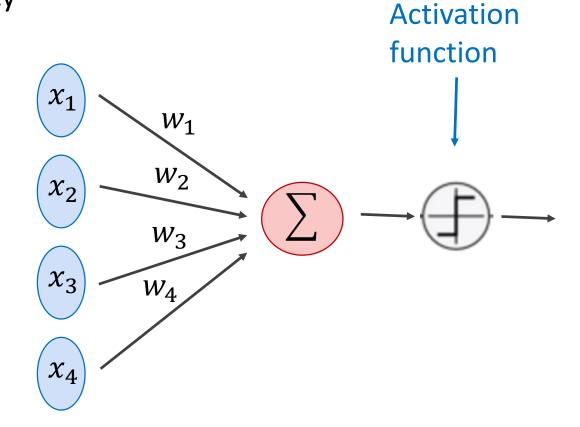
# Neural networks and CNN

Biplab Banerjee

# Perceptron Model

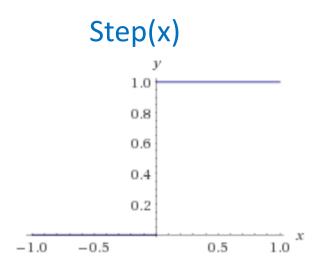
Frank Rosenblatt (1957) - Cornell University

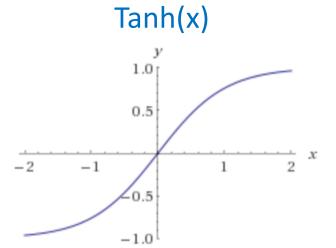
$$f(x) = \begin{cases} 1, & \text{if } \sum_{i=0}^{n} w_i x_i + b > 0 \\ 0, & \text{otherwise} \end{cases}$$

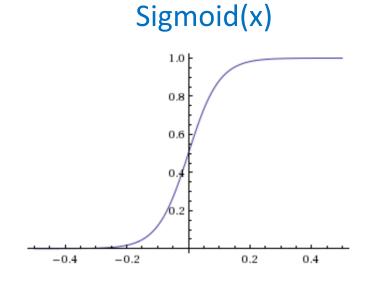


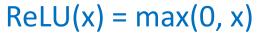
More: https://en.wikipedia.org/wiki/Perceptron

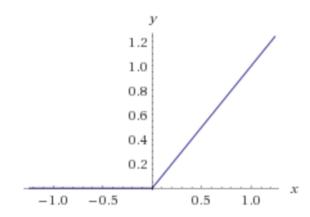
# **Activation Functions**











### Al Stats 2010

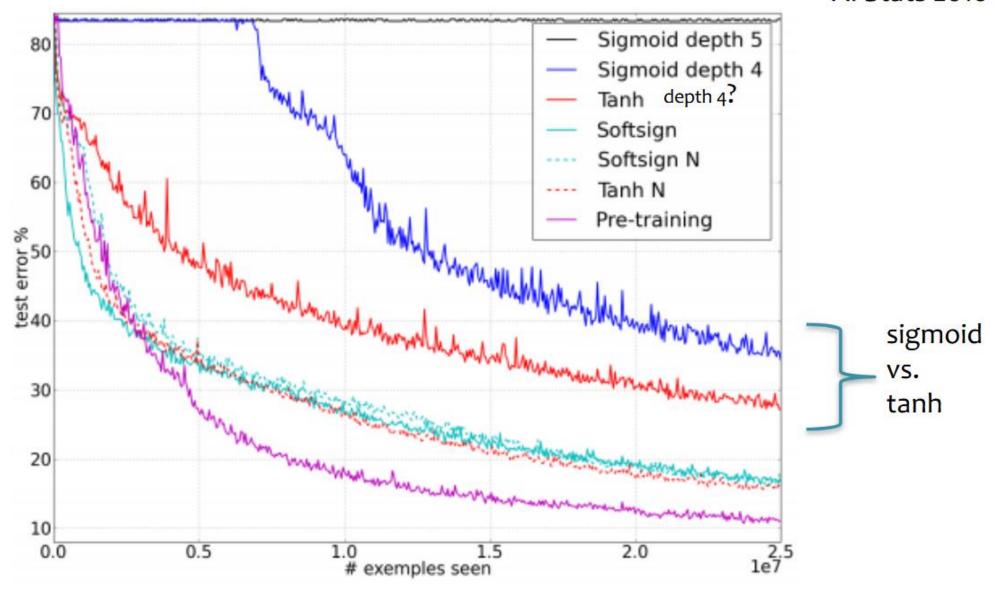
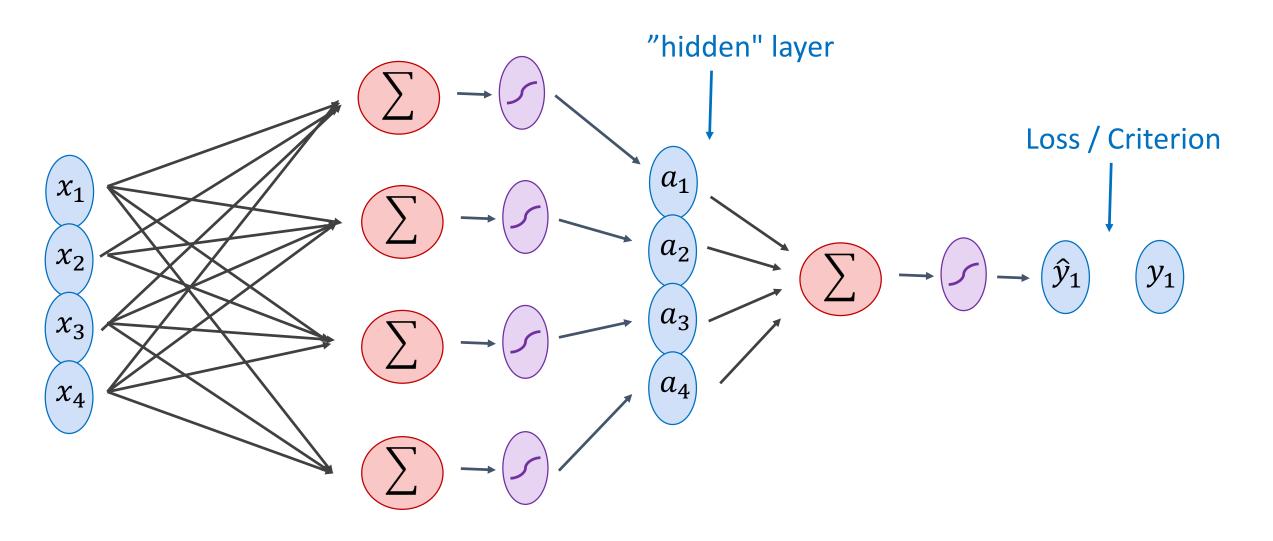


Figure from Glorot & Bentio (2010)

# Two-layer Multi-layer Perceptron (MLP)



$$x_i = [x_{i1} \ x_{i2} \ x_{i3} \ x_{i4}]$$

$$y_i = [1 \ 0 \ 0]$$

$$\hat{y}_i = \begin{bmatrix} f_c & f_d & f_b \end{bmatrix}$$

$$g_c = w_{c1}x_{i1} + w_{c2}x_{i2} + w_{c3}x_{i3} + w_{c4}x_{i4} + b_c$$

$$g_d = w_{d1}x_{i1} + w_{d2}x_{i2} + w_{d3}x_{i3} + w_{d4}x_{i4} + b_d$$

$$g_b = w_{b1}x_{i1} + w_{b2}x_{i2} + w_{b3}x_{i3} + w_{b4}x_{i4} + b_b$$

$$f_c = e^{g_c}/(e^{g_c} + e^{g_d} + e^{g_b})$$
 $f_d = e^{g_d}/(e^{g_c} + e^{g_d} + e^{g_b})$ 
 $f_b = e^{g_b}/(e^{g_c} + e^{g_d} + e^{g_b})$ 

$$x_i = [x_{i1} \ x_{i2} \ x_{i3} \ x_{i4}]$$

$$y_i = [1 \ 0 \ 0]$$

$$\hat{y}_i = [f_c \quad f_d \quad f_b]$$

$$g_c = w_{c1}x_{i1} + w_{c2}x_{i2} + w_{c3}x_{i3} + w_{c4}x_{i4} + b_c$$

$$g_d = w_{d1}x_{i1} + w_{d2}x_{i2} + w_{d3}x_{i3} + w_{d4}x_{i4} + b_d$$

$$g_b = w_{b1}x_{i1} + w_{b2}x_{i2} + w_{b3}x_{i3} + w_{b4}x_{i4} + b_b$$

$$w = \begin{bmatrix} w_{c1} & w_{c2} & w_{c3} & w_{c4} \\ w_{d1} & w_{d2} & w_{d3} & w_{d4} \\ w_{b1} & w_{b2} & w_{b3} & w_{b4} \end{bmatrix}$$

$$b = [b_c \quad b_d \quad b_b]$$

$$f_c = e^{g_c}/(e^{g_c} + e^{g_d} + e^{g_b})$$
 $f_d = e^{g_d}/(e^{g_c} + e^{g_d} + e^{g_b})$ 
 $f_b = e^{g_b}/(e^{g_c} + e^{g_d} + e^{g_b})$ 

$$x_i = [x_{i1} \ x_{i2} \ x_{i3} \ x_{i4}]$$

$$y_i = [1 \ 0 \ 0]$$

$$\hat{y}_i = \begin{bmatrix} f_c & f_d & f_b \end{bmatrix}$$

$$g = wx^T + b^T$$

$$w = \begin{bmatrix} w_{c1} & w_{c2} & w_{c3} & w_{c4} \\ w_{d1} & w_{d2} & w_{d3} & w_{d4} \\ w_{b1} & w_{b2} & w_{b3} & w_{b4} \end{bmatrix}$$

$$b = [b_c \quad b_d \quad b_b]$$

$$f_c = e^{g_c}/(e^{g_c} + e^{g_d} + e^{g_b})$$
 $f_d = e^{g_d}/(e^{g_c} + e^{g_d} + e^{g_b})$ 
 $f_b = e^{g_b}/(e^{g_c} + e^{g_d} + e^{g_b})$ 

$$x_i = [x_{i1} \ x_{i2} \ x_{i3} \ x_{i4}]$$

$$y_i = [1 \ 0 \ 0]$$

$$\hat{y}_i = [f_c \quad f_d \quad f_b]$$

$$g = wx^T + b^T$$

$$w = \begin{bmatrix} w_{c1} & w_{c2} & w_{c3} & w_{c4} \\ w_{d1} & w_{d2} & w_{d3} & w_{d4} \\ w_{b1} & w_{b2} & w_{b3} & w_{b4} \end{bmatrix}$$

$$b = [b_c \quad b_d \quad b_b]$$

$$f = softmax(g)$$

$$x_i = [x_{i1} \ x_{i2} \ x_{i3} \ x_{i4}]$$

$$y_i = [1 \ 0 \ 0]$$

$$\hat{y}_i = [f_c \quad f_d \quad f_b]$$

$$f = softmax(wx^T + b^T)$$

# Two-layer MLP + Softmax

$$x_i = [x_{i1} \ x_{i2} \ x_{i3} \ x_{i4}]$$

$$y_i = [1 \ 0 \ 0]$$

$$\hat{y}_i = [f_c \quad f_d \quad f_b]$$

$$a_1 = sigmoid(w_{[1]}x^T + b_{[1]}^T)$$
  
 $f = softmax(w_{[2]}x^T + b_{[2]}^T)$ 

# N-layer MLP + Softmax

$$x_i = [x_{i1} \ x_{i2} \ x_{i3} \ x_{i4}]$$

$$y_i = [1 \ 0 \ 0]$$

$$\hat{y}_i = [f_c \quad f_d \quad f_b]$$

$$a_1 = sigmoid(w_{[1]}x^T + b_{[1]}^T)$$

$$a_2 = sigmoid(w_{[2]}a_1^T + b_{[2]}^T)$$

. . .

$$a_k = sigmoid(w_{[k]}a_{k-1}^T + b_{[k]}^T)$$

...

$$f = softmax(w_{[n]}a_{n-1}^T + b_{[n]}^T)$$

# How to train the parameters?

$$x_i = [x_{i1} \ x_{i2} \ x_{i3} \ x_{i4}]$$

$$y_i = [1 \ 0 \ 0]$$

$$\hat{y}_i = [f_c \quad f_d \quad f_b]$$

$$a_1 = sigmoid(w_{[1]}x^T + b_{[1]}^T)$$

$$a_2 = sigmoid(w_{[2]}a_1^T + b_{[2]}^T)$$

• • •

$$a_k = sigmoid(w_{[k]}a_{k-1}^T + b_{[k]}^T)$$

...

$$f = softmax(w_{[n]}a_{n-1}^T + b_{[n]}^T)$$

# How to train the parameters?

$$x_i = [x_{i1} \ x_{i2} \ x_{i3} \ x_{i4}]$$

$$y_i = [1 \ 0 \ 0]$$

$$\hat{y}_i = [f_c \quad f_d \quad f_b]$$

$$a_1 = sigmoid(w_{[1]}x^T + b_{[1]}^T)$$

$$a_2 = sigmoid(w_{[2]}a_1^T + b_{[2]}^T)$$

...

$$a_k = sigmoid(w_{[k]}a_{k-1}^T + b_{[i]}^T)$$

...

$$f = softmax(w_{[n]}a_{n-1}^T + b_{[n]}^T)$$

$$l = loss(f, y)$$

We can still use SGD

We need!

$$rac{\partial l}{\partial w_{[k]ij}} \qquad rac{\partial l}{\partial b_{[k]i}}$$

### Regression:

- Use the same objective as Linear Regression
- Quadratic loss (i.e. mean squared error)

### Classification:

- Use the same objective as Logistic Regression
- Cross-entropy (i.e. negative log likelihood)
- This requires probabilities, so we add an additional "softmax" layer at the end of our network

# Forward Backward $J = \frac{1}{2}(y-y^*)^2 \qquad \qquad \frac{dJ}{dy} = y-y^*$ Cross Entropy $J = y^*\log(y) + (1-y^*)\log(1-y) \qquad \frac{dJ}{dy} = y^*\frac{1}{y} + (1-y^*)\frac{1}{y-1}$

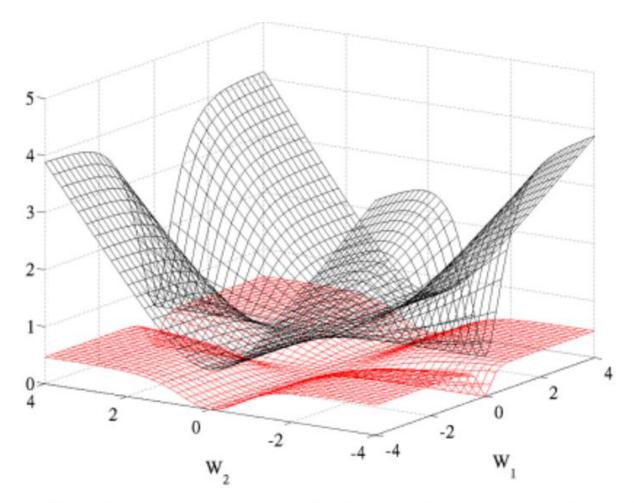


Figure 5: Cross entropy (black, surface on top) and quadratic (red, bottom surface) cost as a function of two weights (one at each layer) of a network with two layers,  $W_1$  respectively on the first layer and  $W_2$  on the second, output layer.

# Background

# A Recipe for Machine Learning

1. Given training data:

$$\{oldsymbol{x}_i, oldsymbol{y}_i\}_{i=1}^N$$

### 2. Choose each of these:

Decision function

$$\hat{\boldsymbol{y}} = f_{\boldsymbol{\theta}}(\boldsymbol{x}_i)$$

Loss function

$$\ell(\hat{oldsymbol{y}}, oldsymbol{y}_i) \in \mathbb{R}$$

3. Define goal:

$$oldsymbol{ heta}^* = rg\min_{oldsymbol{ heta}} \sum_{i=1}^N \ell(f_{oldsymbol{ heta}}(oldsymbol{x}_i), oldsymbol{y}_i)$$

4. Train with SGD:

(take small steps opposite the gradient)

$$\boldsymbol{\theta}^{(t+1)} = \boldsymbol{\theta}^{(t)} - \eta_t \nabla \ell(f_{\boldsymbol{\theta}}(\boldsymbol{x}_i), \boldsymbol{y}_i)$$

### Finite Difference Method

- Pro: Great for testing implementations of backpropagation
- Con: Slow for high dimensional inputs / outputs
- Required: Ability to call the function f(x) on any input x

### 2. Symbolic Differentiation

- Note: The method you learned in high-school
- Note: Used by Mathematica / Wolfram Alpha / Maple
- Pro: Yields easily interpretable derivatives
- Con: Leads to exponential computation time if not carefully implemented
- Required: Mathematical expression that defines f(x)

### 3. Automatic Differentiation - Reverse Mode

- Note: Called Backpropagation when applied to Neural Nets
- Pro: Computes partial derivatives of one output  $f(x)_i$  with respect to all inputs  $x_j$  in time proportional to computation of f(x)
- Con: Slow for high dimensional outputs (e.g. vector-valued functions)
- Required: Algorithm for computing f(x)

### 4. Automatic Differentiation - Forward Mode

- Note: Easy to implement. Uses dual numbers.
- Pro: Computes partial derivatives of all outputs  $f(x)_i$  with respect to one input  $x_j$  in time proportional to computation of f(x)
- Con: Slow for high dimensional inputs (e.g. vector-valued x)
- Required: Algorithm for computing f(x)

Given  $f: \mathbb{R}^A \to \mathbb{R}^B, f(\mathbf{x})$ 

Compute  $\frac{\partial f(\mathbf{x})_i}{\partial x_j} \forall i, j$ 

The centered finite difference approximation is:

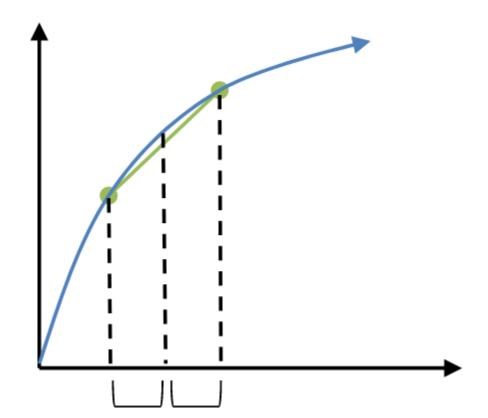
$$\frac{\partial}{\partial \theta_i} J(\boldsymbol{\theta}) \approx \frac{(J(\boldsymbol{\theta} + \epsilon \cdot \boldsymbol{d}_i) - J(\boldsymbol{\theta} - \epsilon \cdot \boldsymbol{d}_i))}{2\epsilon}$$

where  $d_i$  is a 1-hot vector consisting of all zeros except for the ith

entry of  $d_i$ , which has value 1.

### **Notes:**

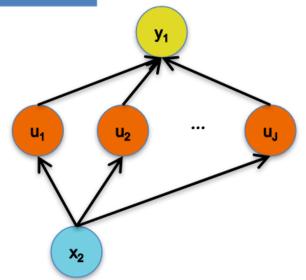
- Suffers from issues of floating point precision, in practice
- Typically only appropriate to use on small examples with an appropriately chosen epsilon



# Backpropagation – repeated application of chain rule

Given: y = g(u) and u = h(x).

Chain Rule:  $\frac{dy_i}{dx_k} = \sum_{j=1}^J \frac{dy_i}{du_j} \frac{du_j}{dx_k}, \quad \forall i, k$ 



### **Forward Computation**

- 1. Write an **algorithm** for evaluating the function y = f(x). The algorithm defines a directed acyclic graph, where each variable is a node (i.e. the "computation graph")
- 2. Visit each node in topological order. For variable  $u_i$  with inputs  $v_1, \dots, v_N$ 
  - a. Compute  $u_i = g_i(v_1, ..., v_N)$
  - b. Store the result at the node

### **Backward Computation**

- Initialize all partial derivatives dy/du<sub>j</sub> to 0 and dy/dy = 1.
   Visit each node in reverse topological order.
- - For variable  $u_i = g_i(v_1, ..., v_N)$
  - a. We already know dy/du
  - b. Increment dy/dv<sub>j</sub> by (dy/du<sub>i</sub>)(du<sub>i</sub>/dv<sub>j</sub>) (Choice of algorithm ensures computing (du<sub>i</sub>/dv<sub>i</sub>) is easy)

**Simple Example:** The goal is to compute  $J = \cos(\sin(x^2) + 3x^2)$ on the forward pass and the derivative  $\frac{dJ}{dx}$  on the backward pass.

$$J = cos(u)$$

$$u = u_1 + u_2$$

$$u_1 = sin(t)$$

$$u_2 = 3t$$

$$t = x^2$$

Forward Backward 
$$J = cos(u) \quad \frac{dJ}{du} += -sin(u)$$

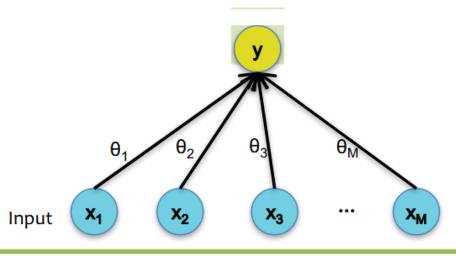
$$u = u_1 + u_2 \quad \frac{dJ}{du_1} += \frac{dJ}{du} \frac{du}{du_1}, \quad \frac{du}{du_1} = 1 \qquad \frac{dJ}{du_2} += \frac{dJ}{du} \frac{du}{du_2}, \quad \frac{du}{du_2} = 1$$

$$u_1 = sin(t) \quad \frac{dJ}{dt} += \frac{dJ}{du_1} \frac{du_1}{dt}, \quad \frac{du_1}{dt} = cos(t)$$

$$u_2 = 3t \qquad \frac{dJ}{dt} += \frac{dJ}{du_2} \frac{du_2}{dt}, \quad \frac{du_2}{dt} = 3$$

$$t = x^2 \qquad \frac{dJ}{dx} += \frac{dJ}{dt} \frac{dt}{dx}, \quad \frac{dt}{dx} = 2x$$

### Logistic Regression



### **Forward**

$$J = y^* \log y + (1 - y^*) \log(1 - y)$$

$$y = \frac{1}{1 + \exp(-a)}$$

$$a = \sum_{j=0}^{D} \theta_j x_j$$

### **Backward**

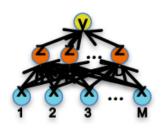
$$J = y^* \log y + (1 - y^*) \log(1 - y) \quad \frac{dJ}{dy} = \frac{y^*}{y} + \frac{(1 - y^*)}{y - 1}$$

$$\frac{dJ}{da} = \frac{dJ}{dy}\frac{dy}{da}, \frac{dy}{da} = \frac{\exp(-a)}{(\exp(-a) + 1)^2}$$

$$\frac{dJ}{d\theta_j} = \frac{dJ}{da} \frac{da}{d\theta_j}, \, \frac{da}{d\theta_j} = x_j$$

$$\frac{dJ}{dx_j} = \frac{dJ}{da}\frac{da}{dx_j}, \, \frac{da}{dx_j} = \theta_j$$

### Neural Network



### Forward

$$J = y^* \log y + (1 - y^*) \log(1 - y) \quad \frac{dJ}{dy} = \frac{y^*}{y} + \frac{(1 - y^*)}{y - 1}$$

$$y = \frac{1}{1 + \exp(-b)}$$
$$b = \sum_{j=0}^{D} \beta_j z_j$$

$$z_j = \frac{1}{1 + \exp(-a_j)}$$
$$a_j = \sum_{i=0}^{M} \alpha_{ji} x_i$$

### Backward

$$\frac{dJ}{dy} = \frac{y^*}{y} + \frac{(1-y^*)}{y-1}$$

$$dJ \quad dJ \, dy \, dy \quad \exp$$

$$\frac{dJ}{db} = \frac{dJ}{dy}\frac{dy}{db}, \frac{dy}{db} = \frac{\exp(-b)}{(\exp(-b) + 1)^2}$$

$$\frac{dJ}{d\beta_j} = \frac{dJ}{db} \frac{db}{d\beta_j}, \ \frac{db}{d\beta_j} = z_j$$

$$\frac{dJ}{dz_i} = \frac{dJ}{db} \frac{db}{dz_i}, \frac{db}{dz_i} = \beta_j$$

$$\frac{dJ}{da_j} = \frac{dJ}{dz_j} \frac{dz_j}{da_j}, \frac{dz_j}{da_j} = \frac{\exp(-a_j)}{(\exp(-a_j) + 1)^2}$$

$$\frac{dJ}{d\alpha_{ji}} = \frac{dJ}{da_j} \frac{da_j}{d\alpha_{ji}}, \frac{da_j}{d\alpha_{ji}} = x_i$$

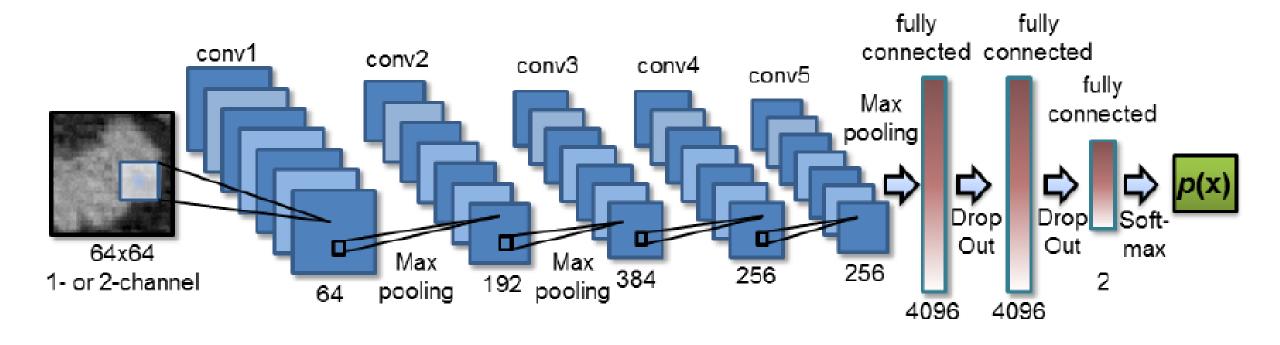
$$\frac{dJ}{dx_i} = \frac{dJ}{da_j} \frac{da_j}{dx_i}, \ \frac{da_j}{dx_i} = \sum_{j=0}^{D} \alpha_{ji}$$

# Two-layer Neural Network – Forward Pass

```
# Setup the input variable x.
img, label = trainset[0]
x = imq.view(1, 1 * 28 * 28)
# Setup the number of inputs, hidden neurons, and outputs.
nInputs = 1 * 28 * 28
nHidden = 512
nOutputs = 10
# Create the model here.
linear fn1 = toynn Linear(nInputs, nHidden)
relu fn = toynn ReLU()
linear fn2 = toynn Linear(nHidden, nOutputs)
# Make predictions.
x = linear fn1.forward(x)
x = relu fn.forward(x)
x = linear fn2.forward(x)
# Show the prediction scores for each class.
# Yes, pytorch tensors already come with a softmax function.
# We need it here because we hard-coded the softmax inside
# the loss function.
print(x.softmax(dim = 1))
```

# Two-layer Neural Network – Backward Pass

```
# Create the model here.
linear fn1 = toynn Linear(nInputs, nHidden)
relu fn = toynn ReLU()
linear fn2 = toynn Linear(nHidden, nOutputs)
loss fn = toynn CrossEntropyLoss()
# Make predictions (forward pass).
a = linear fn1.forward(x)
z = relu fn.forward(a)
vhat = \overline{linear} fn2.forward(z)
# Compute loss.
loss = loss fn.forward(yhat, label)
yhat grads = loss fn.backward(yhat, label)
# Compute gradients (backward pass).
z grads = linear fn2.backward(z, yhat grads)
a grads = relu fn.backward(a, z grads)
x grads = linear fn1.backward(x, a grads)
# Update parameters:
learningRate = 0.2
linear fnl.weight.add (-learningRate, linear fnl.weight grads)
linear fnl.bias.add (-learningRate, linear fnl.bias grads)
linear fn2.weight.add (-learningRate, linear fn2.weight grads)
linear fn2.bias.add (-learningRate, linear fn2.bias grads)
```

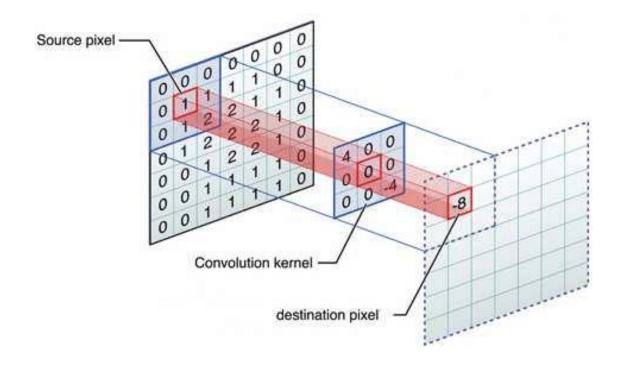


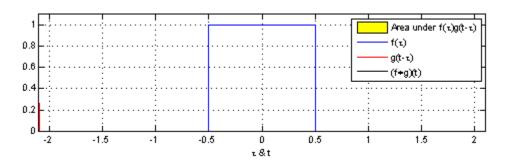
# Basic building blocks of the CNN architecture

- Input layer
- Convolutional layer
- Fully connected layer
- Loss layer

- Convolutional layer
  - Convolutional kernel
  - Pooling layer
  - Non-linearity

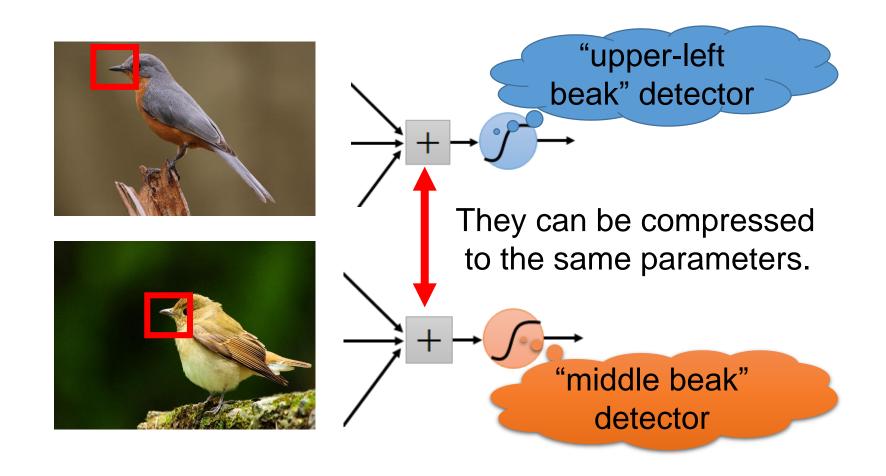
# Convolution operation



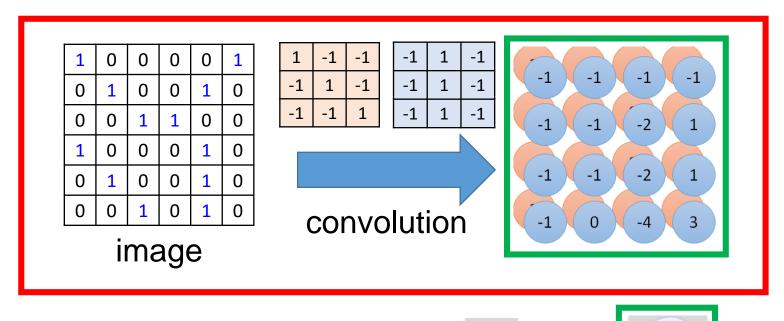


Same pattern appears in different places: They can be compressed!

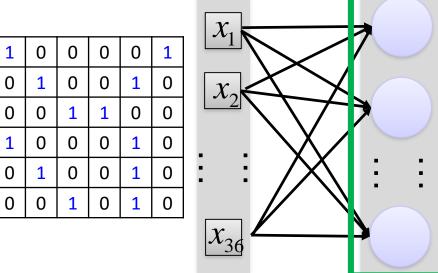
What about training a lot of such "small" detectors and each detector must "move around".



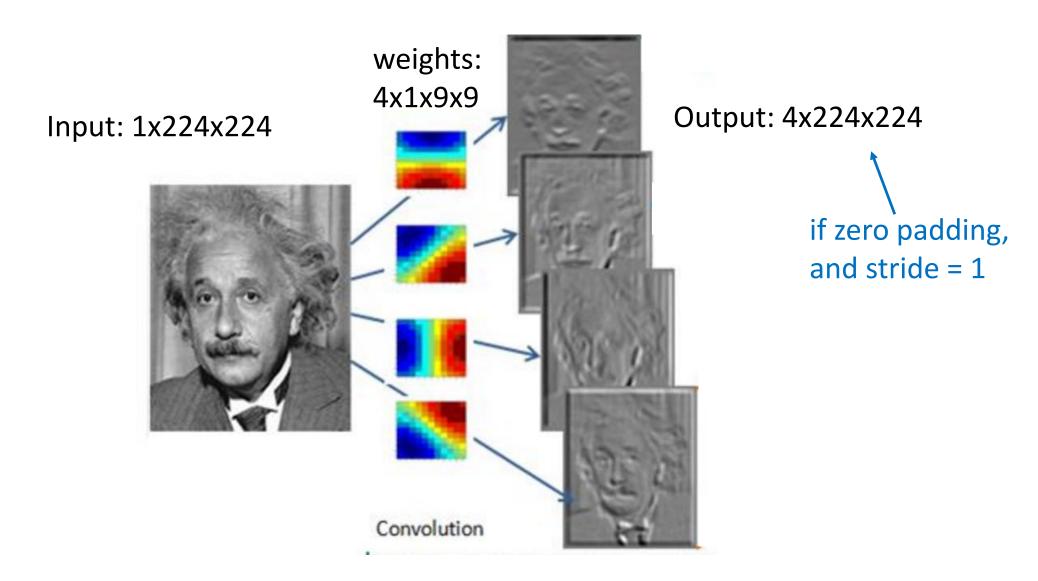
# Convolution v.s. Fully Connected



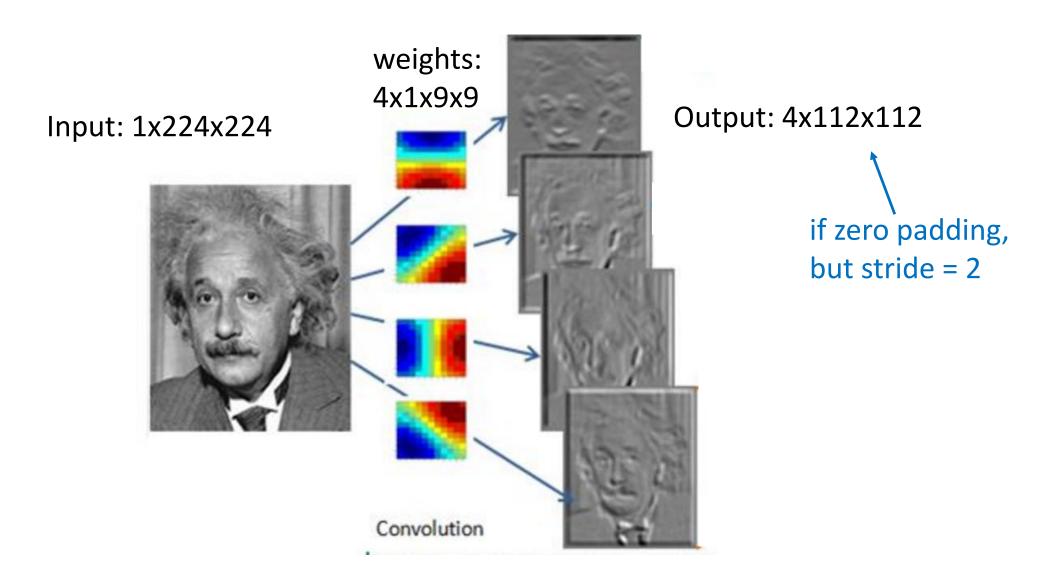
Fully-connected



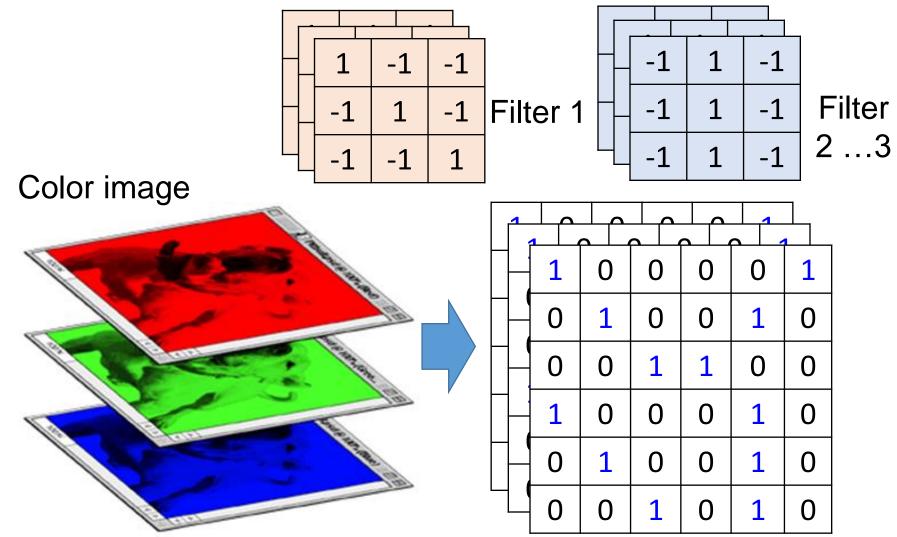
# Convolutional Layer (with 4 filters)



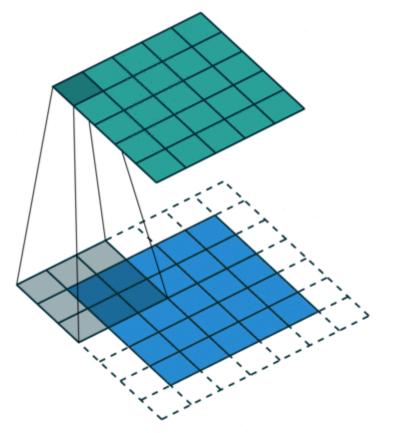
# Convolutional Layer (with 4 filters)



Color image: RGB 3 channels – conv. over depth

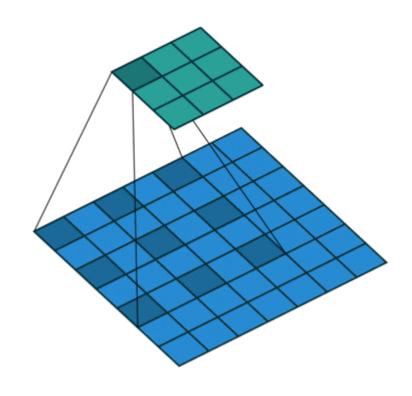


# Different types of convolution



### Parameters:

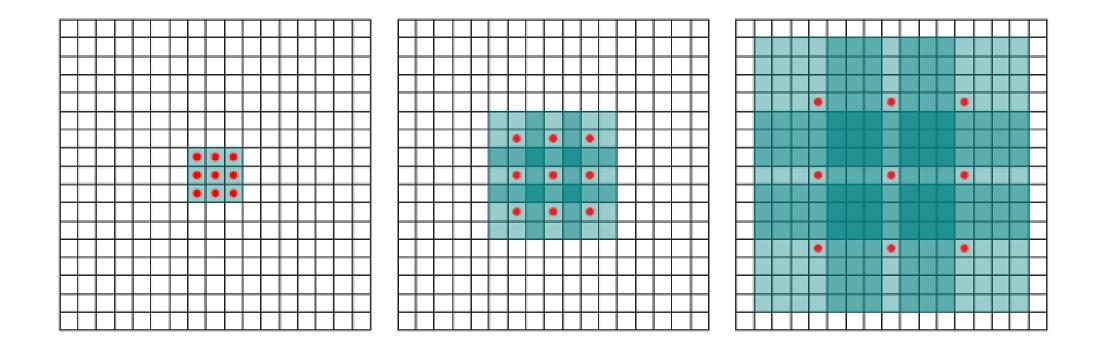
- ✓ Kernel stride
- ✓ Size
- ✓ Padding



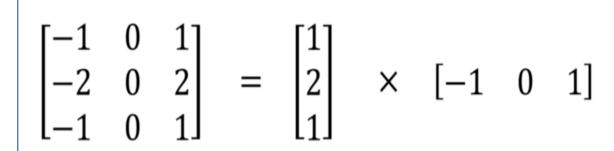
**Normal vs dialated** 

Dialation width = 2

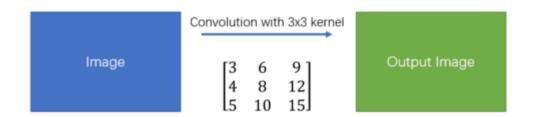
# Dialated convolution



# Spatially Separable convolution



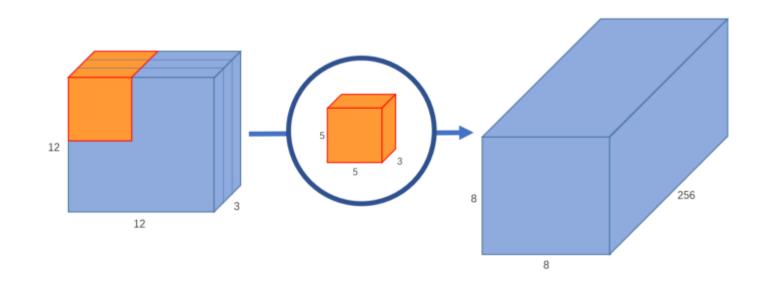
## Simple Convolution



## Spatial Separable Convolution

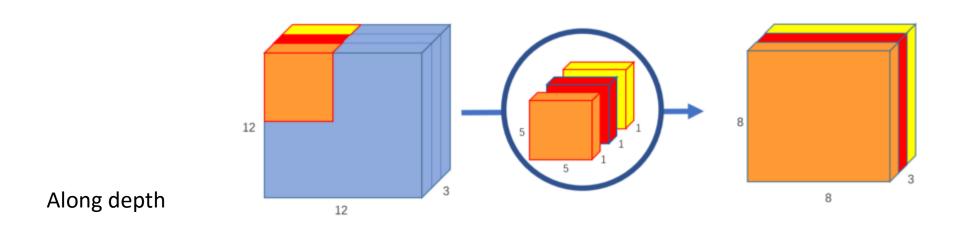


# Depthwise separable convolution



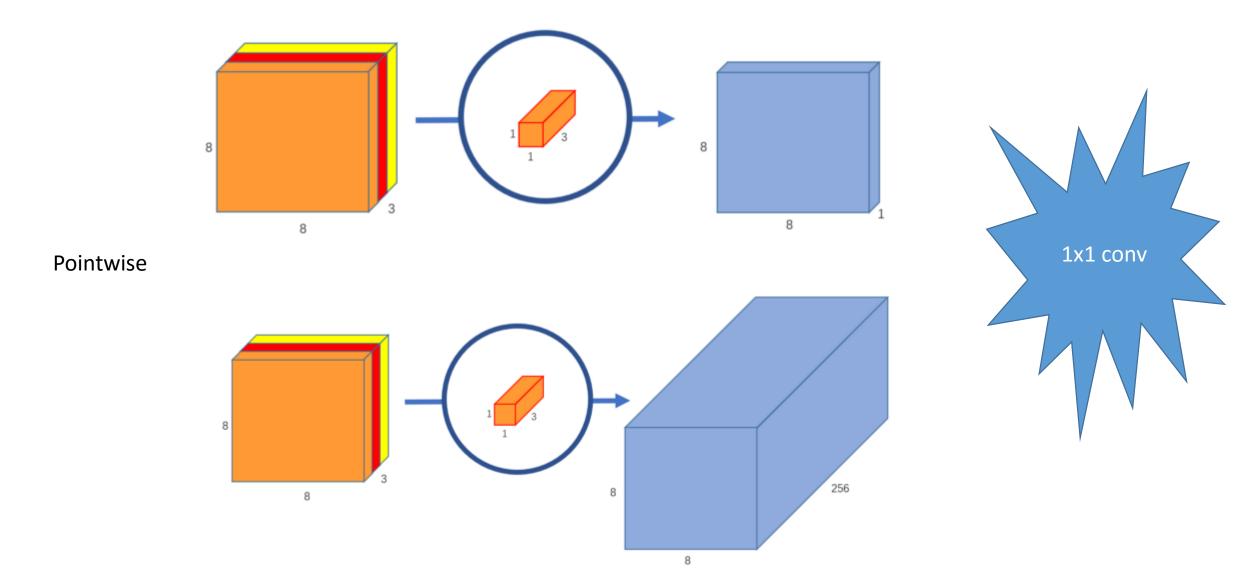
Convolving by 256 5x5 kernels over the input volume

# Depthwise separable convolution – step1



Each 5x5x1 kernel iterates 1 channel of the image (note: **1 channel**, not all channels), getting the scalar products of every 25 pixel group, giving out a 8x8x1 image. Stacking these images together creates a 8x8x3 image.

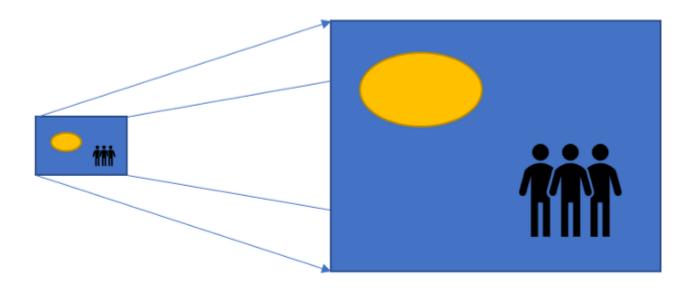
# Depthwise separable convolution – step2



Let's calculate the number of multiplications the computer has to do in the original convolution. There are  $256\ 5x5x3$  kernels that move 8x8 times. That's 256x3x5x5x8x8=1,228,800 multiplications.

What about the separable convolution? In the depthwise convolution, we have  $3\,5x5x1$  kernels that move 8x8 times. That's 3x5x5x8x8 = 4,800 multiplications. In the pointwise convolution, we have  $256\,1x1x3$  kernels that move 8x8 times. That's 256x1x1x3x8x8 = 49,152 multiplications. Adding them up together, that's 53,952 multiplications.

# Transpose convolution



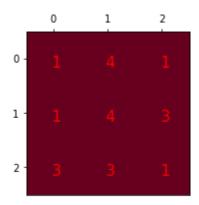
- Nearest neighbor interpolation
- Bi-linear interpolation
- Bi-cubic interpolation

$$\begin{pmatrix} x1 & x2 & x3 \\ x4 & x5 & x6 \\ x7 & x8 & x9 \end{pmatrix} * \begin{pmatrix} k1 & k2 \\ k3 & k4 \end{pmatrix}$$

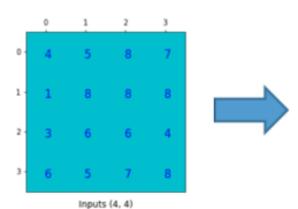
Here is a constructed matrix with a vector:

which is equal to

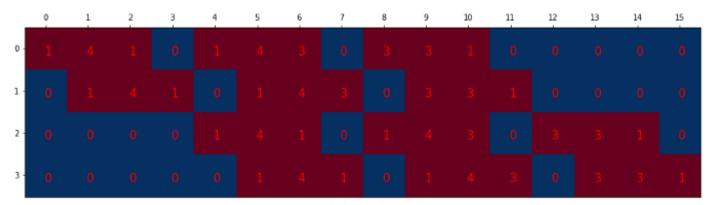
Suppose we have a 4x4 matrix and apply a convolution operation on it with a 3x3 kernel, with no padding, and with a stride of 1. As shown further below, the output is a 2x2 matrix.



### Convolution as a matrix multiplication







Convolution Matrix (4, 16)

10 -

11 -

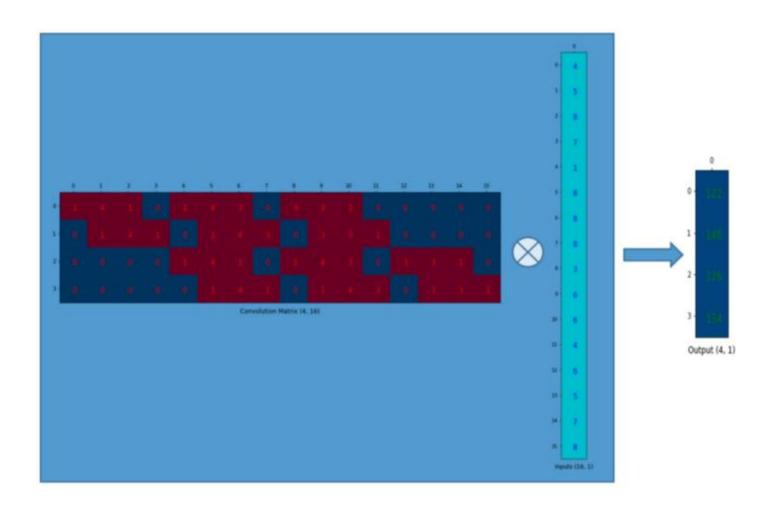
12 -

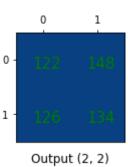
13 -

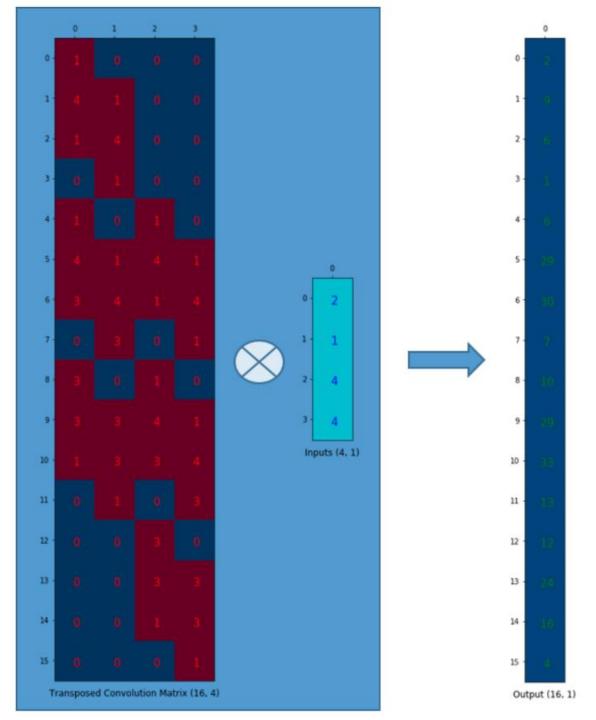
14 -

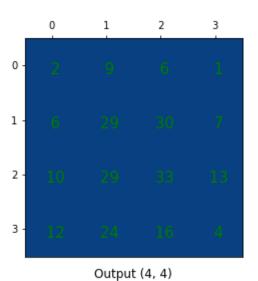
15 -

## Many to one mapping – 9 values to 1 value







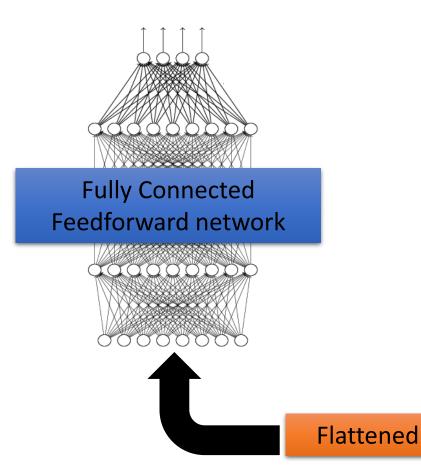


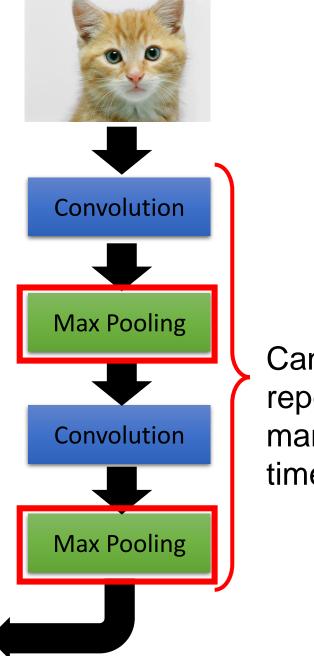
- Fractionally-strided convolution
- Deconvolution

One to many mapping

## The whole CNN

cat dog .....

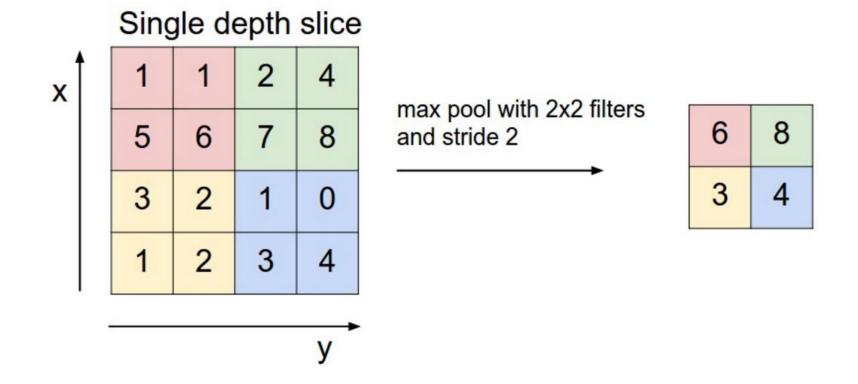




Can repeat many times

# Pooling

• Down-sample the image – controls the parameters of the CNN model



# Why Pooling

Subsampling pixels will not change the object

bird



- ✓ We can subsample the pixels to make image smaller
- √ fewer parameters to characterize the image

# Pooling or strided convolution?

# STRIVING FOR SIMPLICITY: THE ALL CONVOLUTIONAL NET

Jost Tobias Springenberg\*, Alexey Dosovitskiy\*, Thomas Brox, Martin Riedmiller Department of Computer Science University of Freiburg Freiburg, 79110, Germany {springj, dosovits, brox, riedmiller}@cs.uni-freiburg.de

"when pooling is replaced by an additional convolution layer with stride r=2 performance stabilizes and even improves on the base model"

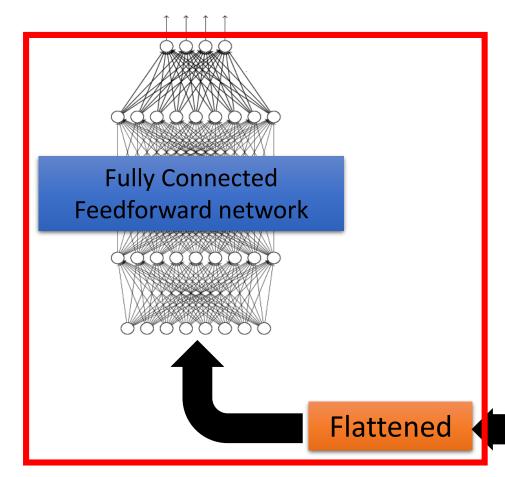
# Unpool

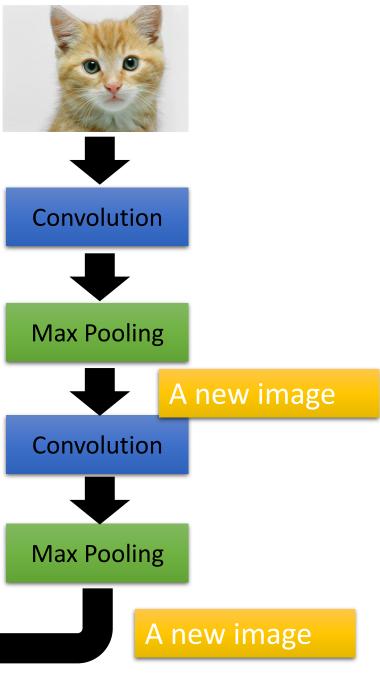


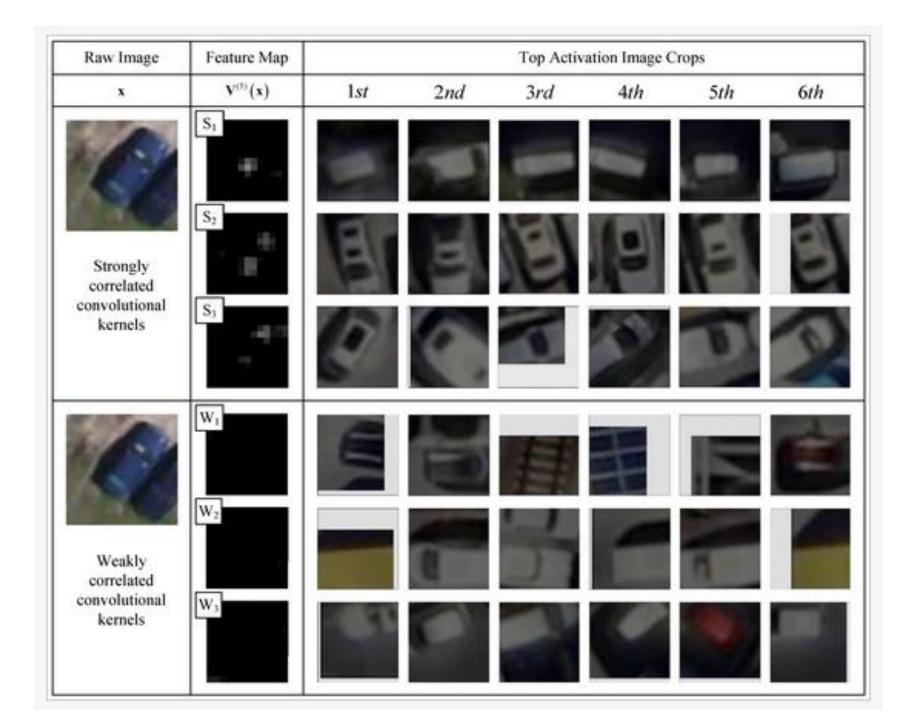
Unpooling: In the convnet, the max pooling operation is non-invertible, however we can obtain an approximate inverse by recording the locations of the maxima within each pooling region in a set of switch variables. In the deconvnet, the unpooling operation uses these switches to place the reconstructions from the layer above into appropriate locations, preserving the structure of the stimulus. See Fig. 1(bottom) for an illustration of the procedure.

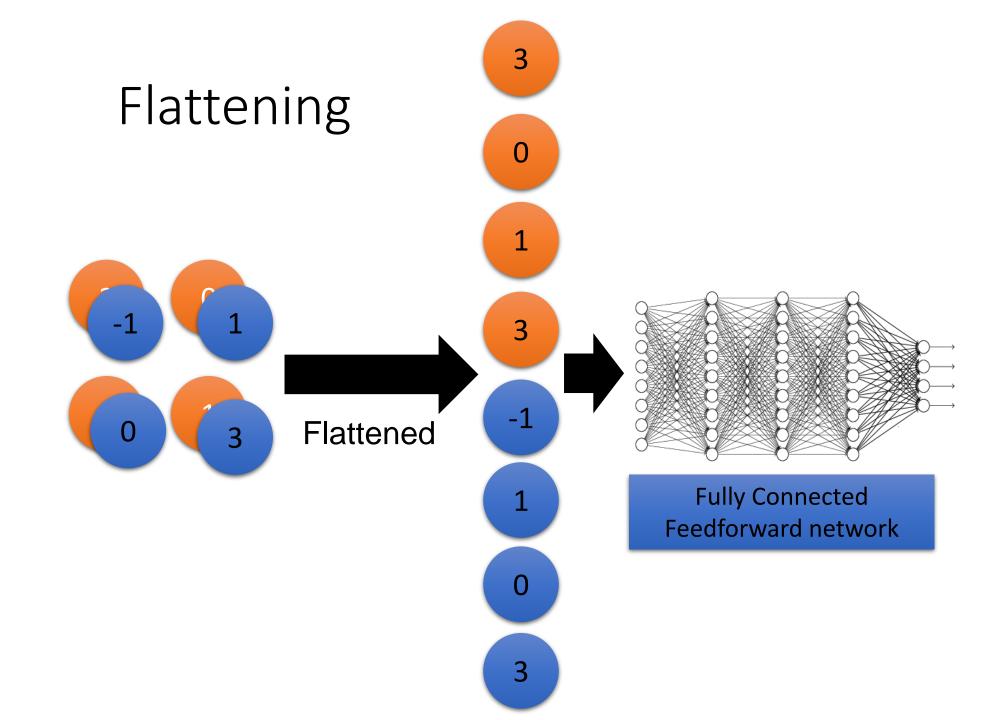
## The whole CNN

cat dog .....









# Conv Net Topology

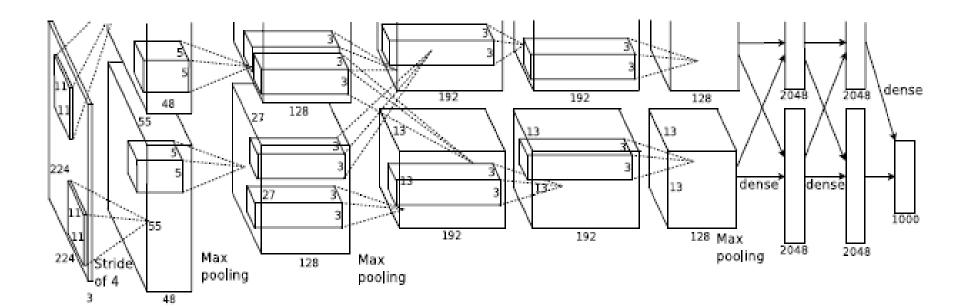
- 5 convolutional layers
- 3 fully connected layers + soft-max
- 650K neurons , 60 Mln weights

#### **ImageNet Classification with Deep Convolutional Neural Networks**

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Ilya Sutskever University of Toronto

Geoffrey E. Hinton University of Toronto ilya@cs.utoronto.ca hinton@cs.utoronto.ca





track cycling

ultramarathon

marathon

road bicycle racing





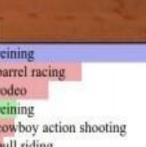
heptathlon











longboarding

longboarding

sandboarding

aggressive inline skating

freestyle scootering

freeboard (skateboard)



hurling flag football association football rugby sevens



blackball (pool)

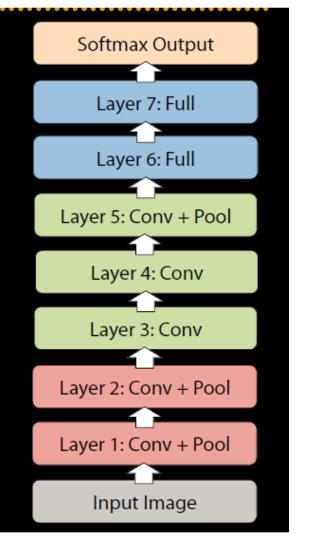
trick shot

eight-ball

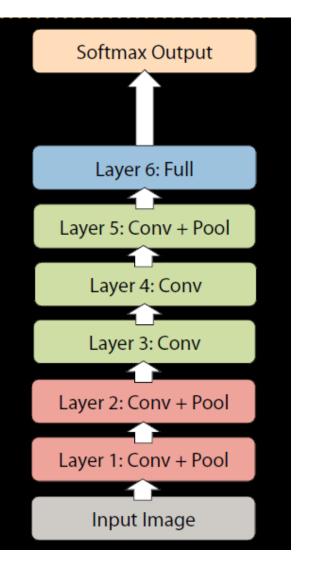
straight pool

demolition derby telemark skiing whitewater kayaking arena football reining demolition derby indoor american football barrel racing snowboarding whitewater kayaking monster truck telemark skiing rafting arena football rodeo mud bogging nordic skiing kayaking canadian football reining motocross ski touring canocing american football cowboy action shooting grand prix motorcycle racing skijoring women's lacrosse bull riding adventure racing

- 8 layers total
- Trained on Imagenet dataset [Deng et al. CVPR'09]
- 18.2% top-5 error
- Our reimplementation: 18.1% top-5 error



- Remove top fully connected layer
  - Layer 7
- Drop 16 million parameters
- Only 1.1% drop in performance!

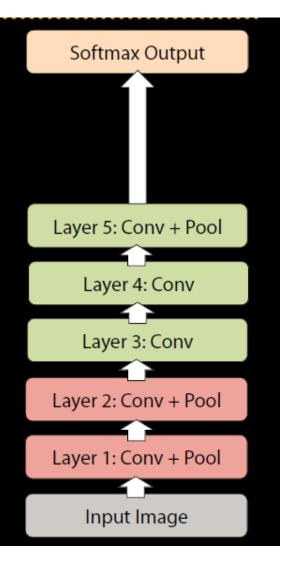


• Remove both fully connected layers

– Layer 6 & 7

Drop ~50 million parameters

• 5.7% drop in performance

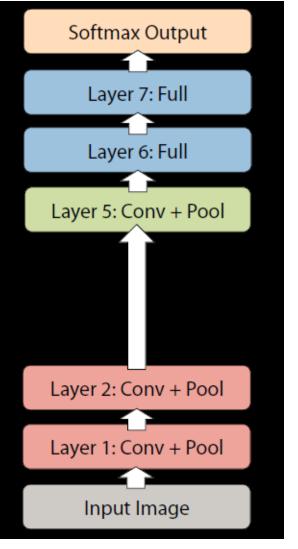


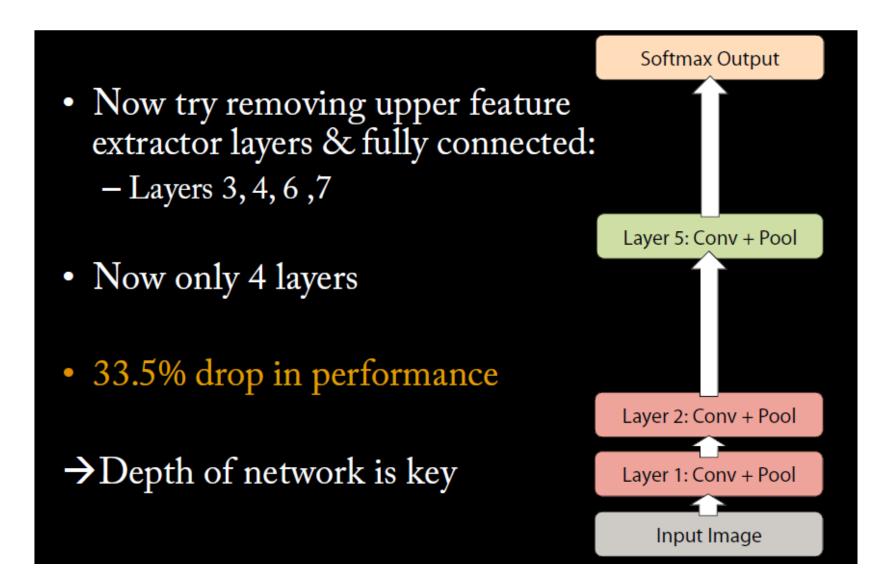
• Now try removing upper feature extractor layers:

– Layers 3 & 4

Drop ~1 million parameters

• 3.0% drop in performance





# Suggested reading

A guide to convolution arithmetic for deep learning

Vincent Dumoulin<sup>1★</sup> and Francesco Visin<sup>2★†</sup>

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January 12, 2018