$$CE(\gamma, \hat{\gamma}) = -\sum_{w} \gamma_{w} \log (\hat{\gamma}_{w})$$

$$= -1 \cdot \log (\hat{\gamma}_{o}) - \sum_{w \neq o} O \cdot \log (\hat{\gamma}_{w})$$

$$= -\log (\hat{\gamma}_{o})$$

yw= [0,-, 1,-, 0]

b.
$$\frac{JJ}{Jv_c} = \int_{Jv_c}^{J} \left[-\log(\hat{y}_0) \right] = -\int_{Jv_c}^{J} \left[\log(\exp(u_0^T v_c)) - \log(\sum_{v} \exp(u_v^T v_c)) \right]$$

$$= -u_0 + \int_{Jv_c}^{J} \log(\sum_{v} \exp(u_v^T v_c))$$

$$= -u_0 + \sum_{x} \frac{e^{x} p(u_x^T v_c)}{\sum_{w} e^{x} p(u_w^T v_c)} u_x$$

$$= \left[-u_0 + \sum_{w}^{\vee} \hat{Y}_w u_w \right]$$

Jun: dxl Jun Un VC = VC JUN Vc = UW

 $\frac{2J}{2u_{n}} = -\frac{2}{2u_{n}} \left[\log \left(\exp \left(u_{o}^{T} v_{c} \right) \right) - \log \left(\sum \exp \left(u_{i}^{T} v_{c}^{T} \right) \right) \right]$ exp(uwvc) Vc = Ŷw Vc

=
$$\begin{cases} v_c(\hat{y}_w - 1) & \text{if } w = 0 \\ v_c(\hat{y}_w) & \text{otherwise} \end{cases}$$

$$\sigma(\alpha) = \frac{1}{1+e^{-\alpha}} = (1+e^{-\alpha})^{-1}$$

$$\frac{\partial\sigma(\alpha)}{\partial\alpha} = -(1+e^{-\alpha})^{-2}(-e^{-\alpha})$$

$$= \frac{e^{-\alpha}}{(1+e^{-\alpha})^{2}} = \frac{1+e^{-\alpha}}{(1+e^{-\alpha})^{2}} - \frac{1}{(1+e^{-\alpha})^{2}}$$

$$= \sigma(\alpha) - \sigma^{2}(\alpha) = \sigma(\alpha)(1-\sigma(\alpha))$$

$$J = -\log(\sigma(u_0^T v_c)) - \sum_{k=1}^{K} \log(\sigma(-u_k^T v_c)) \qquad = 1 - \sigma(x)$$

$$\frac{\partial J}{\partial v_c} = -\frac{\sigma(u_0^T v_c)(1 - \sigma(u_0^T v_c))(u_0)}{\sigma(u_0^T v_c)} - \sum_{k=1}^{K} \frac{\sigma(-u_k^T v_c)(1 - \sigma(-u_k^T v_c))(-u_k)}{\sigma(-u_k^T v_c)}$$

$$= -(1-\sigma(u_0^T v_c)) u_0 + \sum_{k=1}^{K} (1-\sigma(-u_k^T v_c) u_k)$$

$$= -\sigma(-u_0^T v_c) u_0 + \sum_{k=1}^{K} \sigma(u_k^T v_c) u_k$$

$$\frac{JJ}{Ju_k} = 0 - \left(1 - \sigma(-u_k^T v_c)\right)(-v_c)$$

$$= \sigma(u_k^T v_c) v_c$$

$$\frac{\partial J}{\partial u_0} = -\left(1 - \sigma\left(u_0^T v_c\right)\right) v_c$$

$$= \left(\sigma\left(u_0^T v_c\right) - 1\right) v_c$$

Looping over K << V much faster than over entire vocabulary

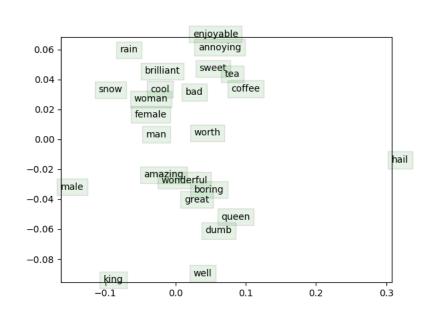
i)
$$\frac{2J_{skip}(v_{c}, w_{t-m}, \dots, w_{t+m}, U)}{2U} = \sum_{\substack{-m \leq j \leq m \\ j \neq 0}} \frac{2J(v_{c}, w_{t+j}, U)}{2U}$$

ii)
$$\frac{\partial J_{skip}}{\partial v_c} = \sum_{j} \frac{\partial J(v_{e}, w_{taj}, U)}{\partial v_c}$$

$$\frac{111}{\sqrt{3}} \frac{\partial J_{skip}}{\partial V_w} = 0$$

$$w \neq C$$

2



- Interchangeable words are grouped [amozing, wonderful]
- · Grouped words do not necessarily have similar meaning:

[boring, great] [enjoyable, annoying]

· Consistent vector from good to bad:

bad-brilliant & boring-amazing & dumb-great

~ annoying - enjoyable