

```
using System;
using System.Collections.Generic;
using System.ComponentModel;
using System.Data;
using System.Drawing;
using System.Linq;
using System.Text;
using System.Threading.Tasks;
using System.Windows.Forms;

namespace _2DTransformation
{
    public partial class Form1 : Form
    {
        private PointF[] points; // Polygon points

        public Form1()
        {
            InitializeComponent();
            this.points = new PointF[] {
                new PointF(0, 0),
                new PointF(110, 40),
                new PointF(140, 100),
                new PointF(200, 150)
            };
        }

        // This Pain method is called everytime where the Form loads or, this.Invalidate() or this.Refresh() is called. So, redraw the polygon on the Paint method and
        // call this.Refresh() on button clicks after points are adjusted using various Transformation functions.
        private void Form1_Paint(object sender, PaintEventArgs e)
        {
            Graphics grapics = e.Graphics;
            grapics.DrawPolygon(new Pen(Color.Red), this.points);
            grapics.Dispose();
        }

        private void btn_rotate_Click(object sender, EventArgs e)
        {
            int angle = int.Parse(this.txt_rotate_in.Text); // Get the input angle
            for (int j = 1; j <= angle; j++)
            {
                /* Rotate each point of the polygon by 1 degree around the point 'this.point[3]' */
                for (int i = 0; i < this.points.Length; i++)
                {
                    rotate_point(ref this.points[i], this.points[3], 1);
                }
                this.Refresh(); // This will call the paint method (Form1_Paint())
                System.Threading.Thread.Sleep(10);
            }
        }

        /* This function rotates a point around a given point.
        * A point that rotates around the origin will have the matrix ((Cos(t) -sin(t)), (Sin(t) Cos(t))).
        * In order to rotate around a given point, first we must bring the pivot to the origin along with the point (bring the line to the origin so that pivot lies with the origin)
        * Then apply the rotation matrix, then move it back to where it was.
        * In order to bring it the origin,
        *     Move the point so that pivot lies on origin -> To do that, Apply the translation matrix T(x)
        *     Rotate around the pivot/origin -> To do that, Apply the rotation matrix R(x)
        *     Move the point back to where it was -> To do that, Apply the translation matrix.
        *
        *     So, if point P is (x, y) then, resulting point after above operations will be, (Remember that the Transformation matrices are applied in reverse order)
        *
        *         | x |   =   | 1  0  tx | | cos(a)  sin(a)  0 | | 1  0  -tx |
        *         | y |       | 0  1  ty | * | -sin(a) cos(a)  0 | * | 0  1  -ty |
        *         | 1 |       | 0  0  1 | | 0      0      1 | | 0  0  1 |
        *
        * Then, apply the 2D matrix. Then move the resulting cordinate back to original place by adding the Xp, Yp.
        */

        // 'ref' is to pass the pointer of the 'point'. pivot is the rotation point. 'angle' is the angle to rotate in degrees.
        private void rotate_point(ref PointF point, PointF pivot, int angle)
        {
            double angle_rad = (Math.PI / 180)*angle;    // Convert degree -> radians
            point.X = (float)((Math.Cos(angle_rad) * (point.X - pivot.X)) - (Math.Sin(angle_rad) * (point.Y - pivot.Y)) + pivot.X);
            point.Y = (float)((Math.Sin(angle_rad) * (point.X - pivot.X)) + (Math.Cos(angle_rad) * (point.Y - pivot.Y)) + pivot.Y);
        }

        private void scale_point(ref PointF point, float scale)
        {
            point.X = scale * point.X;
            point.Y = scale * point.Y;
        }

        private void btn_scale_Click(object sender, EventArgs e)
        {
            float scale = float.Parse(txt_scale_in.Text);

            // Scale each point of polygon by a 'scale'
            for (int i = 0; i < this.points.Length; i++)
            {
                scale_point(ref points[i], scale);
            }
            this.Refresh(); // This will call the paint method (Form1_Paint())
        }

        private void btn_translate_Click(object sender, EventArgs e)
        {
            float tx = float.Parse(txt_translate_x_in.Text);
            float ty = float.Parse(txt_translate_y_in.Text);

            // Translate each point of the polygon
            for (int i = 0; i < this.points.Length; i++)
            {
                translate_point(ref points[i], tx, ty);
            }
            this.Refresh(); // This will call the paint method (Form1_Paint())
        }

        private void translate_point(ref PointF point, float tx, float ty)
        {
            point.X += tx;
            point.Y += ty;
        }
    }
}
```