# An optimization of threshold scan of $e^+e^- \rightarrow ZH$ for Higgs spin determinatin and ISR correction at Higgs factories \*

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- Abstract: The cross section determination of  $\sigma(e^+e^- \to ZH)$  will reach unprecedented precision at furture Higgs
- <sup>7</sup> factories. This makes the theoretical correction an important uncertainty in the measurement, such as initial state
- 8 radiation correction and other high order electroweak corrections. Initial state radiation correction needs the exper-
- 9 iment measurements below the present center of mass energy as input. This work study the optimal scan scheme
- for ISR correction to match the requirement of experimental precision. The effect of scan scheme on Higgs spin
- determination is discussed as well.
- Key words: Higgs Factory, Initial state radiation, Higgs spin
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## 1 Introduction: $e^+e^-$ collider as a Higgs factory

The discovery of the Higgs boson [1, 2] is a great milestone for the particle physics. Precision measurements of properties of the Higgs boson are critical for the SM physics; any deviation away from the SM expectation will improve our knowledge of the elementary particles and their interactions. Based on this consideration, an  $e^+e^-$  collider with high luminosity and energy is best suited for the Higgs research and several  $e^+e^-$  experiments have been proposed [3–8] by high energy physics community.

At Higgs factories, usually the observables of Higgs can be measured to unprecedented precision. For example,

the Born cross section,  $\sigma_B(e^+e^- \to ZH)$  ( abbreviated to  $\sigma_B(ZH)$  ), can be measured to 0.8% at ILC, 0.5% at CEPC, and 0.4% at FCC-ee, respectively. Therefore the high order correction, including initial state radiation (ISR) and other virtual corrections, has significant contribution to the observed cross section compared with the expected precision. Recent calculations shows that the NLO EW correction has significant contribution [9, 10]. But from the view point of experiment, ISR correction is more important, since it depends on the theoretical calculation, but the experiment itself.

The line shape of  $\sigma_B(ZH)$ 

This article is organized as the following. After the introduction, the ISR procedure of  $e^+e^-$  experiment will be described in detail. Then the optimization of  $e^+e^- \to ZH$  threshold scan scheme will be performed in order to meet the requirement of the cross section measurement and spin determination of Higgs boson. In the end, there will be a conclusive discussion.

# $\sigma$ 2 $\sigma(ZH)$ , ISR correction, and the Higgs spin

In Higgs factories, such as CEPC, ILC, FCC-ee, and CLIC,  $\sigma(ZH)$  is one of the key measurands. It is solely determined by the  $C_{HZZ}$  coupling at tree level and also depends on the Higgs self-coupling at loop level, which may be altered by such couplings. Vise versa, precise measurement of  $\sigma(ZH)$  can constrain  $C_{HZZ}$  and Higgs self-coupling.

In experiment, the Born cross section is calculated with formula

$$\sigma_B = \frac{N^{\text{obs.}}}{\mathcal{L} \cdot \epsilon \cdot (1+\delta)^{\gamma} (1+\delta)^{V}} , \qquad (1)$$

where  $\mathcal{L}$  is integrated luminosity,  $\epsilon$  detection efficiency, and  $(1+\delta)^{\gamma}$  and  $(1+\delta)^{V}$  the correction factors of the ISR and other virtual correction, respectively. The ISR correction factor is calculated by the Monte Carlo (MC) generator

- being used to determine the detection efficiency. The measurement requires precise calculation of ISR correction.
- 40 This is done by the structure function approach, which yields the accuracy of 0.1% [11–15]. In this scheme, the
- observed cross section reads

$$\sigma(s) = \int_0^{1-s_{th}/s} dx \tilde{\sigma}[s(1-x)]F(x,s), \qquad (2)$$

- where  $\sqrt{s}$  is the center of mass energy (CM) of the colliding beam,  $\sqrt{s_{th}}$  is the kinematic threshold of  $e^+e^- \to ZH$ ,
- and the dressed cross section

$$\tilde{\sigma}(s) = \frac{\sigma_B(s)}{(1+\delta)^V},\tag{3}$$

- with  $\sigma_B(s)$  the Born order cross-section. Through this work,  $\sigma_B$  is used instead of  $\tilde{\sigma}$ , i.e. assuming that  $(1+\delta)^V = 1$ ,
- because that the virtual correction does not depend on experiments.
- According to the Eq. 2, it is apparent that  $\sigma(ZH)$  depends not only on F(x,s) but also on the line shape of
- $\sigma(s)$  of the region from the threshold to CM energy. The line shape has to be determined by experiment and its
- uncertainty contributes to the systematic uncertainty of  $\sigma(ZH)$ .
- In Eq. 2, the radiator F(x,s)

$$F(x,s) = \beta x^{\beta-1} \delta^{V+S} + \delta^H , \qquad (4)$$

50 with

$$\beta = \frac{2\alpha}{\pi} \left( \ln \frac{s}{m_e^2} - 1 \right) , \tag{5}$$

$$\delta^{V+S} = 1 + \frac{3}{4}\beta + \frac{\alpha}{\pi} \left(\frac{\pi^2}{3} - \frac{1}{2}\right) + \beta^2 \left(\frac{9}{32} - \frac{\pi^2}{12}\right) , \qquad (6)$$

$$\delta^{H} = -\beta \left(1 - \frac{x}{2}\right) + \frac{1}{8}\beta^{2} \left[4(2 - x)\ln\frac{1}{x} - \frac{1 + 3(1 - x)^{2}}{x}\ln(1 - x) - 6 - x\right] . \tag{7}$$

### 51 3 Optimization of threshold scan

### 52 4 Summary and Conclusion

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