## Towards Semi-Supervised Subspace Learning for Outlier Detection in Big Data

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Background: Outlier detection in big data is vital for applications [1]. It is concerned with different challenges, such as the curse of dimensionality and massive amounts of data, which raise the need for scalable and efficient algorithms.

Many attempts have been made in order to address challenges of outlier detection in big data. Several methods are based on approximate nearest neighbor (ANN) search methods [2]. Distributed approaches are also used in order to conduct outlier detection in large-scale data by leveraging multiple computing nodes to process large-scale, high-dimensional datasets in parallel.

## **Proposed Method:**

- ☐ We propose a semi-supervised subspace learning method to learn a low-dimensional subspace for outlier detection.
- ☐ We construct a novel linear Deep Neural Network (DNN), namely Hybrid Deep Support Vector Data Description (HDSVDD). HDSVDD is trained only on inliers to learn a mapping to a lower-dimensional representation of the data points.
- ☐ Inspired From Deep SVDD [3], The training procedure involves training connected linear DNNs specialized in mapping the inliers into lower-dimensional compact hyperspheres. The distance of the lower-dimensional representation of the data point to the center of the hyperspheres constructs the coordinates of the data points in the lower-dimensional subspace. The one-class training procedure of the neural network learns the representation of the inliers. Hence, when dealing the unseen data points (e.g., test set), it is expected to map the inliers closer to the center of the hyperspheres and the outliers further apart. This process allows the discrimination between inliers and outliers in the lower-dimensional subspace.



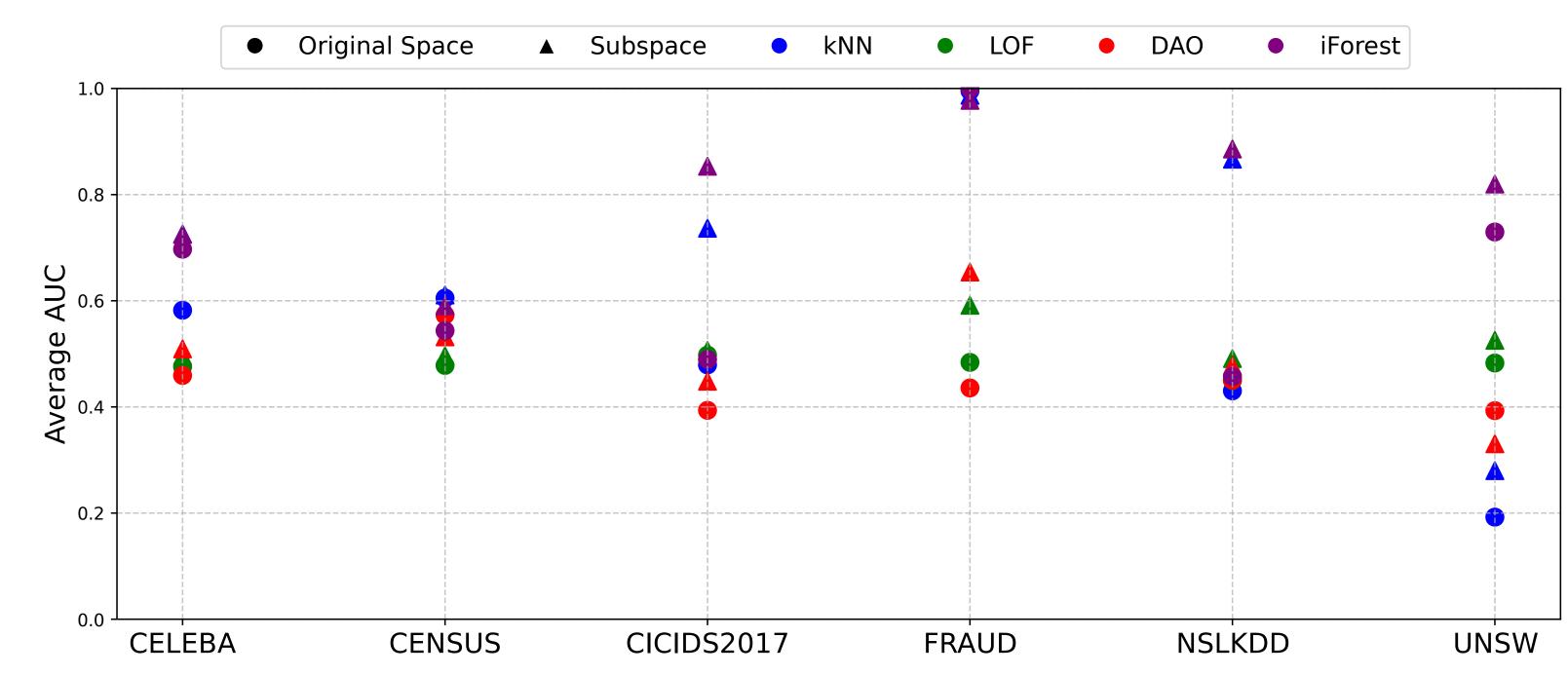
**Input:** Dataset D (only inliers), subspace dimensionality d'

- **Output:** Trained neural networks for subspace representation  $\{NN_1, NN_2, \dots, NN_{d'}\}$ 1: Initialize d' autoencoders  $\{AE_1, AE_2, \ldots, AE_{d'}\}$ , each with a different number of
- layers. 2: Set pre-training epochs  $E_{\text{pre-train}}$  and joint training epochs  $E_{\text{joint}}$ .
- 3: Ensure a layer with m units in the encoder part for all autoencoders.
- 4: **for** i = 1 to d' **do**
- Train  $AE_i$  on D for  $E_{pre-train}$  epochs.
- 6: end for
- 7: Select a subset of encoders' architectures from all autoencoders up to the point it reaches the layer with m units.
- 8: for each  $NN_j$  in  $\{NN_1, NN_2, \dots, NN_{d'}\}$  do
- Project D to output space using NN<sub>j</sub> to obtain  $Z_j = \{z_{j1}, z_{j2}, \ldots, z_{jn}\}.$  $\triangleright z_{ji} \in \mathbb{R}^m$
- Compute center  $c_j = \frac{1}{n} \sum_{i=1}^n z_{ji}$ .
- 11: end for
- 12: for e = 1 to  $E_{joint}$  do
- Compute loss  $L = \sum_{j=1}^{d'} \sum_{x_i \in D} \| NN_j(x_i) c_j \|_2^2$ .
- Update parameters of  $\{NN_1, NN_2, \dots, NN_{d'}\}$  to minimize L.
- 15: end for
- 16: **return** Trained Neural networks  $\{NN_1, NN_2, \dots, NN_{d'}\}$

## Algorithm 2 Projecting Data into the Subspace Using HDSVDD

**Input:** Dataset D, trained neural networks  $\{NN_1, NN_2, \dots, NN_{d'}\}$ 

- **Output:** The coordinates of the data in the subspace  $D_s$ 1: for each data point  $x_i \in D$  do
- Compute coordinates  $[d_{i1}, d_{i2}, \ldots, d_{id'}]$ , where  $d_{ij} = \| NN_j(x_i) c_j \|_2$ .
- Assign  $D_s = [d_{i1}, d_{i2}, \dots, d_{id'}]$  as the subspace coordinates of  $x_i$ .
- 4: end for
- 5: **return** Subspace coordinates  $D_s$ .



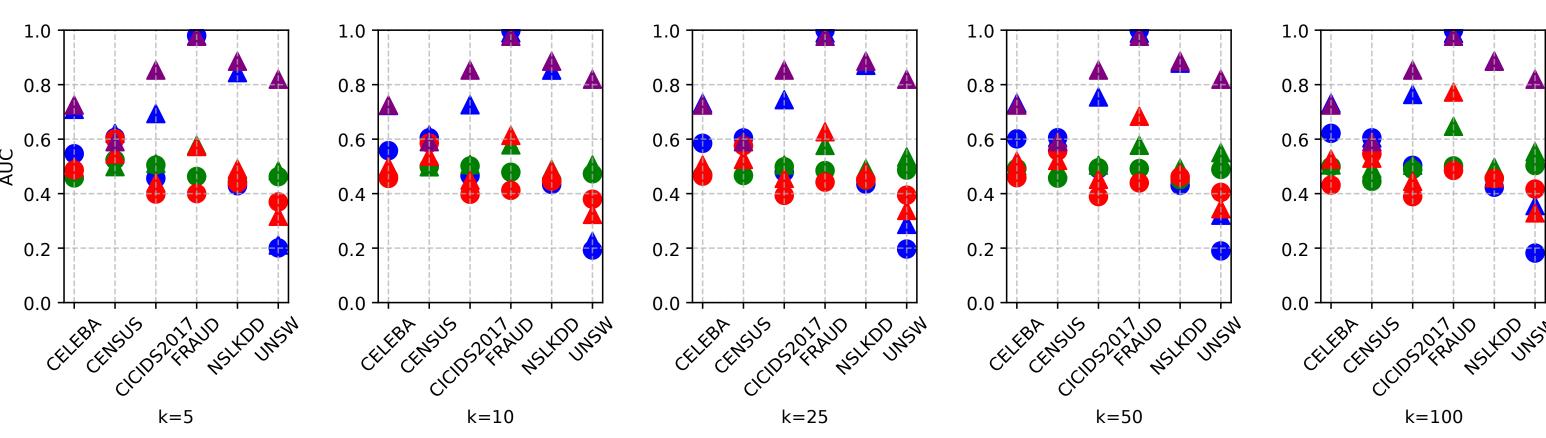
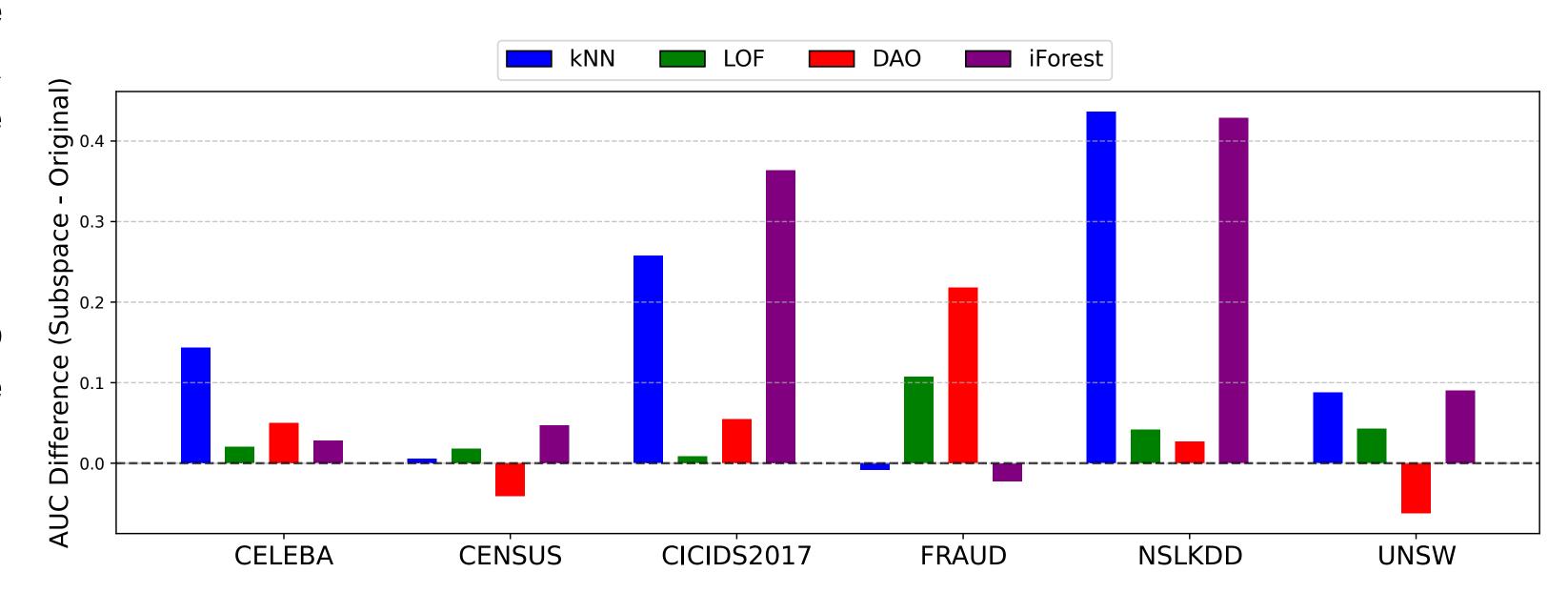


Figure 1 – The comparison of the different outlier detection methods on the original feature space and the subspace learned by HDSVDD. The experiments are done using 5-fold cross-validation. The top plot shows the average results over all values of k. The results for specific values of k are presented in the subplots below.



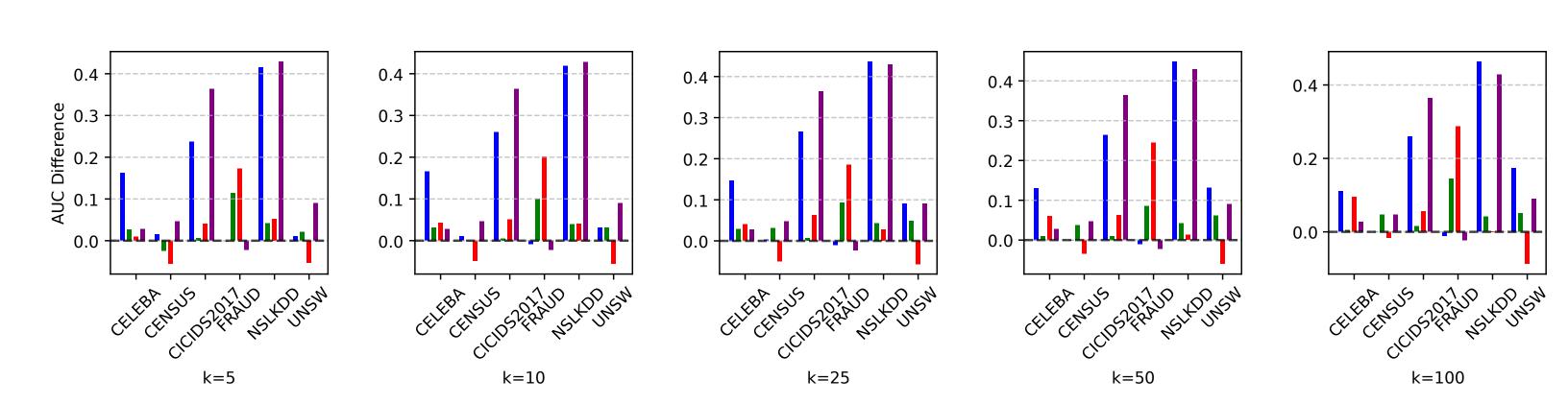
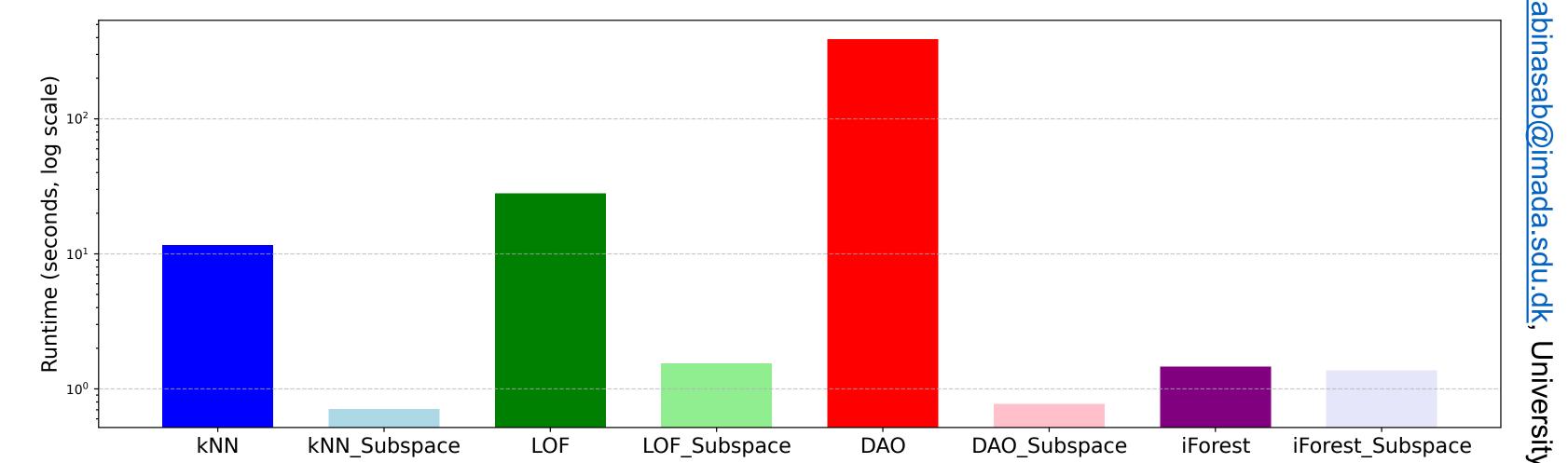


Figure 2 – The difference in the AUC values of different outlier detection algorithms on the subspace learned by HDSVDD compared to the original feature space. The experiments are done using 5-fold cross-validation. The top plot shows the average results over all values of k. The results for specific values of k are presented in the subplots below.



**Figure 3** – Runtime comparison on the original feature space and the subspace for different methods on CELEBA dataset. The y-axis is represented on a logarithmic scale.

## References



[1] Li, W., Zhang, H., Wang, L.: Anomaly detection in industrial iot with machine learning: A survey. IEEE Internet Things J. 9(15), 12345–12360 (2022).