# Model Output Statistics (MOS) - Objective Interpretation of NWP Model Output

Millersville U. @ NCEP - December 9, 2005

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#### OUTLINE

- 1. Why objective statistical guidance?
- 2. What is MOS?

  Definition and characteristics

  The "traditional" MOS product suite

  (NGM, eta, GFS)

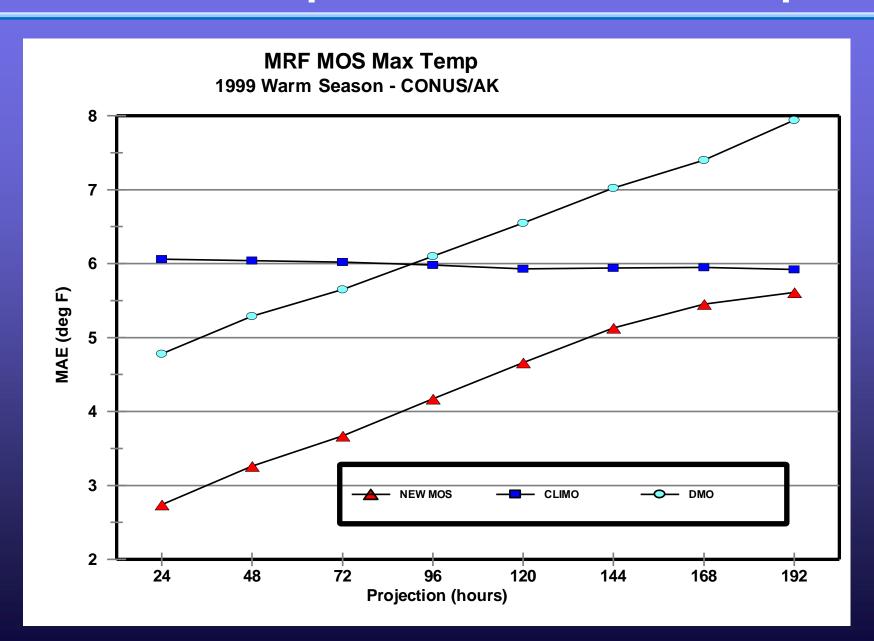
  Recent additions to the lineup
- 3. Simple regression examples / Probability
- 4. Development strategy MOS in the "real world"
- 5. Verification
- 6. Where we're going The future of MOS

#### WHY STATISTICAL GUIDANCE?

- Add value to direct NWP model output
   Objectively interpret model
  - remove systematic biases
  - quantify uncertainty
    Predict what the model does not
    Produce site-specific forecasts
    (i.e. a "downscaling" technique)

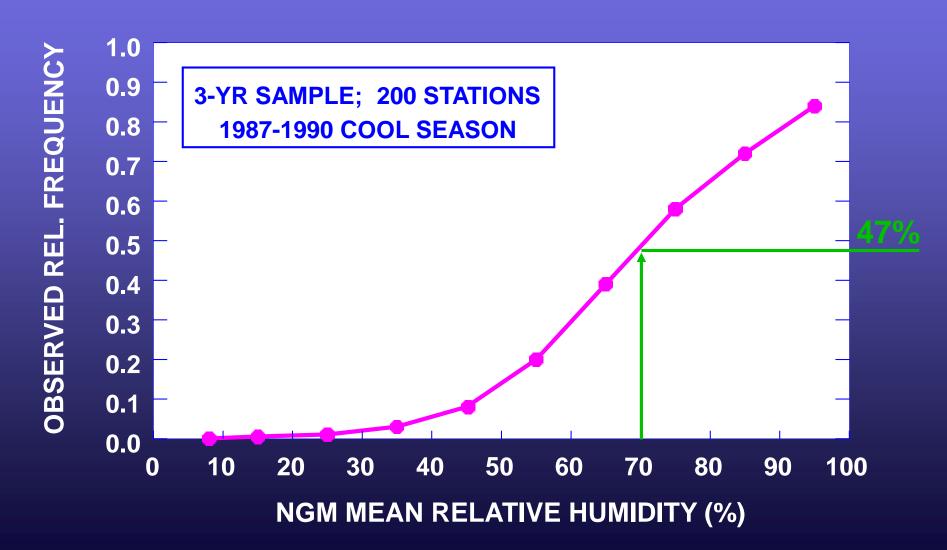
Assist forecasters
 "First Guess" for expected local conditions
 "Built-in" model/climo memory for new staff

#### MOS Max Temp vs. Direct Model Output



#### A SIMPLE STATISTICAL MODEL

Relative Frequency of Precipitation as a Function of 12-24 Hour NGM Model-Forecast Mean RH



# What is MOS?

Relates observed weather elements (PREDICTANDS) to appropriate variables (PREDICTORS) via a statistical approach.

#### **Predictors are obtained from:**

- 1. Numerical Weather Prediction (NWP) Model Forecasts
- 2. Prior Surface Weather Observations
- 3. Geoclimatic Information

Current Statistical Method:

MULTIPLE LINEAR REGRESSION

(Forward Selection)

#### **Properties**

- Mathematically simple, yet powerful
- Need historical record of observations at forecast points (Hopefully a long, stable one!)
- Equations are applied to future run of similar forecast model

#### **Properties (cont.)**

- Non-linearity can be modeled by using NWP variables and transformations
- Probability forecasts possible from a single run of NWP model
- Other statistical methods can be used e.g. Polynomial or logistic regression; Neural networks

#### ADVANTAGES

Recognition of model predictability
Removal of some systematic model bias
Optimal predictor selection
Reliable probabilities
Specific element and site forecasts

#### DISADVANTAGES

Short samples
Changing NWP models
Availability & quality of obs

# "Traditional" MOS text products

# GFS MOS GUIDANCE MESSAGE FOUS21-26 (MAV)

KLNS GFS MOS GUIDANCE							11/29/2004 1200 UTC														
DT /NOV 29/NOV					30			/D				EC 1							/DE	EC	2
HR	18	21	00	03	06	09	12	15	18	21	00	03	06	09	12	15	18	21	00	06	12
N/X							28				48				35				49		33
TMP	43	44	39	36	33	32	31	39	46	45	41	38	37	39	41	44	45	44	40	40	35
DPT	27	27	28	29	29	29	29	33	35	35	36	35	36	39	41	42	37	34	30	30	28
CLD	CL	BK	ВK	вĸ	ov	ov	ov	ov	ov	ov	ov	ov	ov	ov	ov	ov	ov	BK	CL	CL	CL
WDR	34	36	00	00	00	00	00	00	00	14	12	12	10	11	12	19	28	29	29	29	28
WSP	06	02	00	00	00	00	00	00	00	01	02	04	04	06	07	08	15	17	18	09	05
P06			0		0		4		3		11		65		94		96		7	0	0
P12							6				19				94				96		0
Q06			0		0		0		0		0		3		4		4		0	0	0
Q12							0				0				4				2		0
<b>T</b> 06		0/	0	0,	/18	0/	3	0/	0	0/	0	0,	18	2,	/ 1	10,	4	0/	3	1,	/ 0
<b>T12</b>				0,	0/26			0/17				0/27					/25		1/38		
POZ	2	0	0	1	2	4	4	0	1	1	2	3	3	1	1	0	2	1	2	3	1
POS	13	2	1	2	1	0	0	0	0	0	0	0	0	2	0	0	0	3	0	9	28
TYP	R	R	R	R	R	R	R	R	R	R	R	R	R	R	R	R	R	R	R	R	R
SNW							0								0						0
CIG	8	8	8	8	7	7	7	8	8	7	7	7	4	2	3	3	6	7	8	8	8
VIS	7	7	7	7	7	7	7	7	7	7	7	7	5	5	4	2	6	7	7	7	7
OBV	N	N	N	N	N	N	N	N	N	N	N	N	BR	BR	BR	BR	N	N	N	N	N

# Eta MOS GUIDANCE MESSAGE FOUS44-49 (MET)

KTHV ETA MOS GUIDANCE							11/28/2005				120	00 τ	JTC								
DT /NOV 28/NOV 29							/N				OV	30							/DEC		
HR	18	21	00	03	06	09	12	15	18	21	00	03	06	09	12	15	18	21	00	06	12
N/X	6						60				65				52				54		28
TMP	58	60	58	61	65	66	66	60	62	61	62	61	59	57	54	52	53	50	41	35	32
DPT	50	52	52	54	57	58	58	55	58	59	57	56	54	52	49	43	39	36	34	29	27
CLD	ov	ov	ov	ov	ov	ov	ov	ov	ov	ov	ov	ov	ov	ov	ov	ov	ov	sc	CL	sc	BK
WDR	15	13	12	14	16	15	13	17	16	15	15	16	18	24	29	29	31	32	30	27	32
WSP	05	07	07	10	12	12	10	10	10	09	08	80	07	07	05	10	09	06	03	01	03
P06			14		62		87		94		91		90		71		21		6	6	0
P12							88			1	L00				93				28		7
Q06			0		1		2		3		4		4		2		0		0	0	0
Q12							1				4				4				0		0
т06		2,	/ 0	7,	/ 0	8,	/ 4	13/	/ 2	25,	/ 3	28,	/ 2	21,	/ 2	9/	1	3,	/ 39	999,	/99
T12	7/ 0						22/	4			41/ 4				24/3			999/99			
SNW							0								0						0
CIG	3	5	3	3	2	2	2	3	5	4	3	3	3	4	5	6	6	8	8	8	8
VIS	5	6	6	5	5	3	3	3	5	5	4	2	3	3	7	7	7	7	7	7	7
OBV	BR	N	BR	BR	BR	BR	BR	BR	HZ	BR	BR	BR	BR	BR	N	N	N	N	N	N	N

#### GFS / Eta MOS vs. NGM MOS

#### MORE STATIONS:

Now at approx. 1650 Forecast Sites (CONUS, HI, PR)

#### MORE FORECASTS:

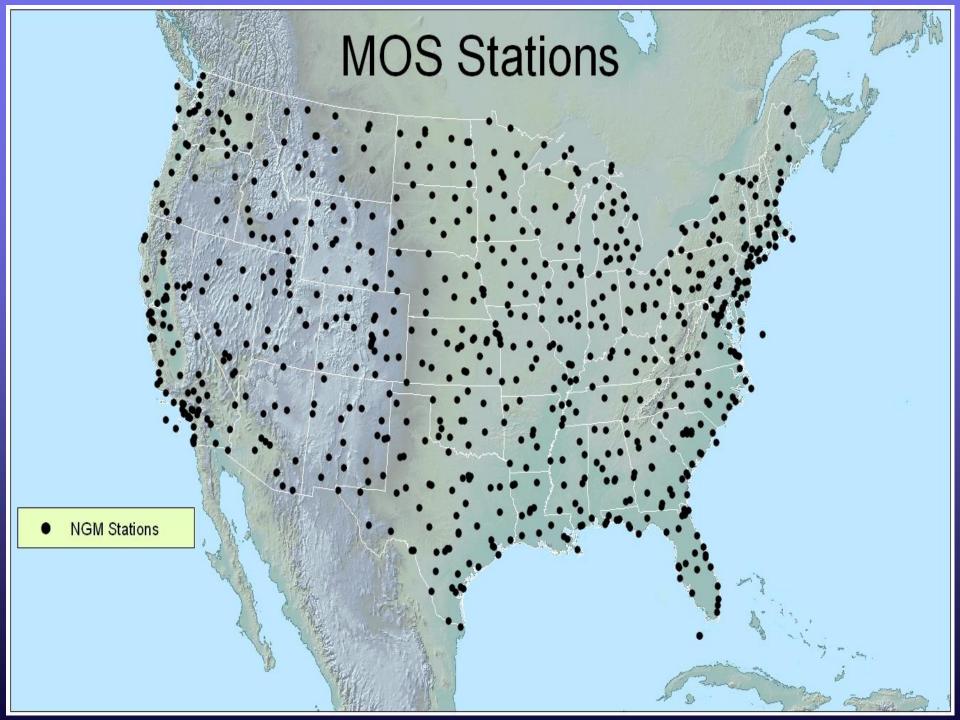
Available at projections of 12-84 hours GFS available for 0600 and 1800 UTC cycles

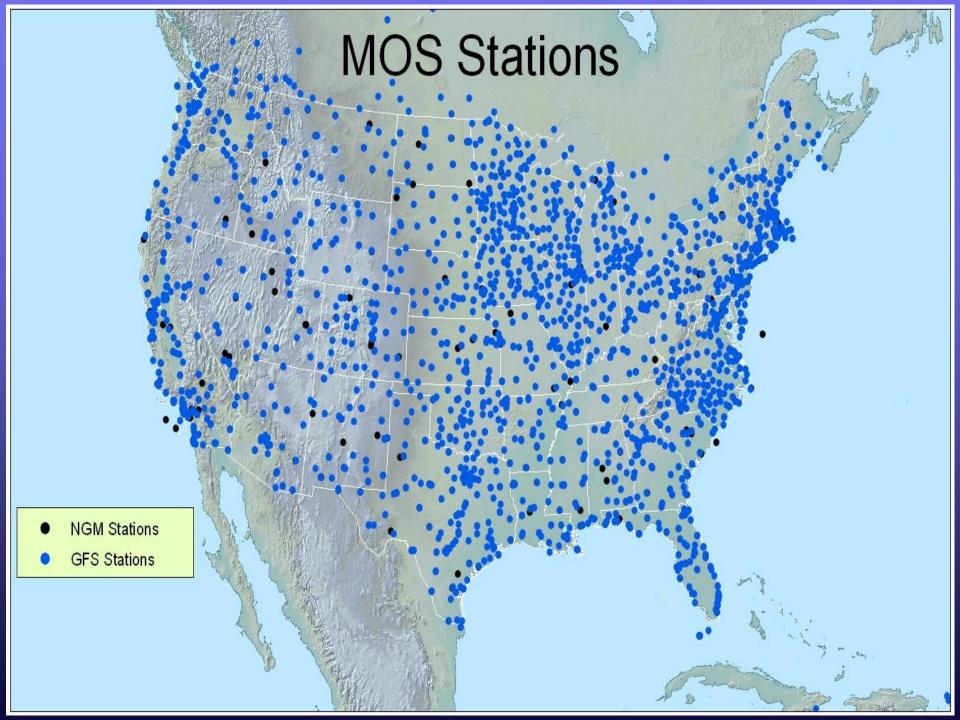
#### BETTER RESOLUTION:

GFS predictors on 95.25 km grid; Eta on 32 km Predictor fields available at 3-h timesteps Predictors available beyond 48-h projection \* No extrapolative forecasts

#### DEPENDENT SAMPLE NOT "IDEAL":

Fewer Seasons
Non-static underlying NWP model





#### GFS / Eta MOS vs. NGM MOS

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# GFSX MOS GUIDANCE MESSAGE FEUS21-26 (MEX)

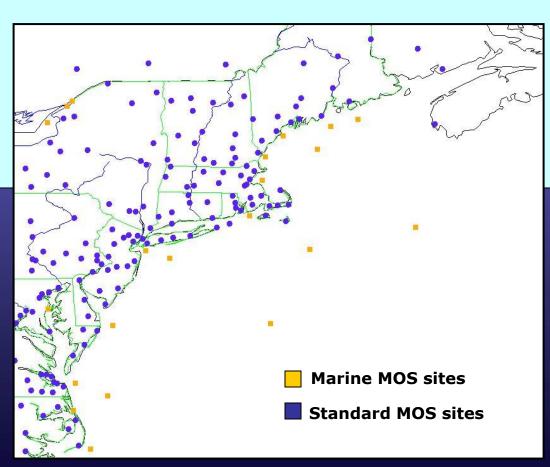
```
KCXY
         GFSX MOS GUIDANCE
                                11/26/2004
                                               0000 UTC
      241 36
FHR
                481 60
                           721
                                84
                                     96 | 108 | 120 | 132 | 144 | 156 | 168 | 180 | 192
FRI
                           281
                                     29| TUE
                     SUN
                                MON
                                               30| WED
                                                         011
                                                              THU
                                                                    021
                                                                              03 CLIMO
X/N
                471
                     40
                           551
                                35
                                     51 I
                                          29
                                               45 I
                                                    32
                                                          40 I
                                                              36
                                                                    421
                                                                         30
                                                                              45
                                                                                 31 46
           32
                     43
                               37
                                          32
                                               391 35
                                                              38
                                                                         33
                                                                              37
TMP
                431
                           461
                                     41|
                                                         361
                                                                    37 I
      37 I
DPT
           27
                                28
                                     281
                                          26
                                               311
                                                    32
                                                              32
                                                                         24
                                                                              25
      241
                37 I
                     40
                          321
                                                         301
                                                                    27 I
CLD
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WND
      101
                11 | 11
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                                           5
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                                                                         12
                                                                              12
P12
                131
                     91
                          131
                                3
                                      91
                                          14
                                               241
                                                    52
                                                         541
                                                              48
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                                                                              25 20
       01
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                                                                                      18
P24
                161
                         1001
                                               261
                                                          621
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012
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                            31
                                      01
                                                01
                                                           4 |
T12
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                  01
                            01
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                       3
                                      01
                                                4 |
                                                           4 |
                                                                3
                                                                     11
                                 0
                                           0
                                                      6
                       3
T24
            0
                                 0
                                           0
                                                      6
                                                                4
                                      61
                                                81
                                                           31
PZP
      121
             9
                121
                       4
                            31
                                 5
                                          10
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                                                                    101
                                                                               8
PSN
      62 I
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                                                                    321
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                                                                              18
PRS
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                           17 I
                                18
                                     201 13
                                               15I
                                                           21
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                       R
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                                                           RI
                                                                R
                                                                         RS
                                                                               \mathbf{R}
                  01
                            01
                                      01
                                                01
SNW
```

# Recent additions to the MOS product lineup

#### **Marine MOS**

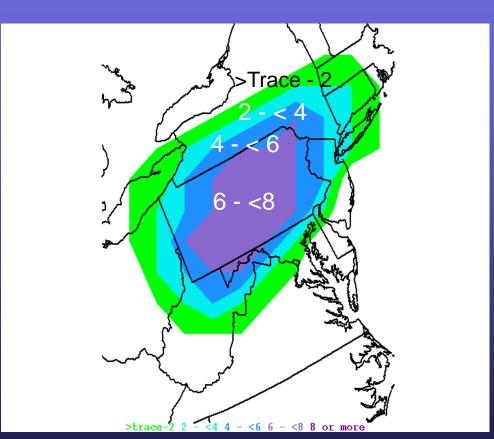
DT /NOV 25 /
HR 09 12 15 18 21 00
TMP 45 45 45 47 47 47
WD 29 29 28 30 29 34
WS 18 15 10 10 13 12
WS10 20 16 11 11 14 13

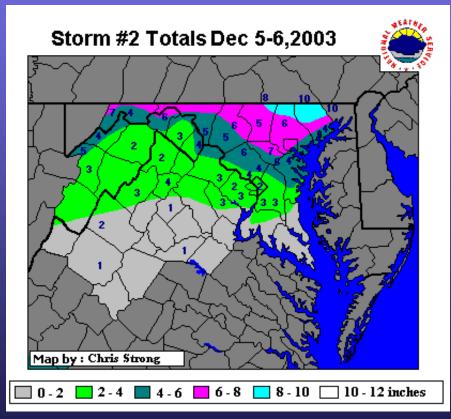




## **MOS Snowfall Guidance**

#### **Uses Observations from Cooperative Observer Network**





36-hr forecast 12Z 12/05/03 – 12Z 12/06/03

Verification

### Max/Min Guidance for Co-op Sites

```
GFS-BASED MOS COOP MAX/MIN GUIDANCE 12/01/04
                                                    1200 UTC
                   FRI
                       031
                            SAT 04
                   29
GYLP1
          30
               411
                        411
                            28
                                 46
HAWP1
          28
                       391
                                 38
               421
                   24
                            20
HBGP1
          34
              47 I
                   28
                        45 I
                            27
                                 43
HRBP1
          35
              451
                   29
                        44|
                            29
                                 43
INDP1
          28
                                 46
               44|
                   27
                        441
                            28
JMSP1
          26
              391
                   24
                        401
                            28
                                 42
                                 36
          24
              341
KANP1
                   22
                       331
                            22
                                 36
LAPP1
          27
              371
                   25
                       351
                            22
LBGP1
          33
               451
                   28
                        42|
                            25
                                 42
                                              Lancaster 2 NE
LCRP1
          33
               461
                   27
                        461
                            27
                                 46
LDVP1
          29
              491 25
                       45 | 23
                                 42
                                              Landisville, PA
LEBP1
          30
               461
                   26
                        431
                            24
                                 45
LHGP1
          30
               451
                   24
                        44|
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                                 41
          26
                            26
                                 41
LMPP1
              361
                   25
                        37 I
LNVP1
               381
                   27
                            27
          28
                        381
                                 41
          32
               431
                            27
                                 41
LOKP1
                   27
                        431
LRLP1
          29
                        431
                            23
                                 40
               471
                   24
               461
                            29
                                 42
LSTP1
          34
                   29
                        451
                                 38
MATP1
          29
               451
                   24
                        42|
                            22
MCKP1
          27
               40|
                   27
                        41|
                            26
                                 45
          22
               401
                   22
                        41|
                            24
                                 43
MERP1
```

#### **Western Pacific MOS Guidance**



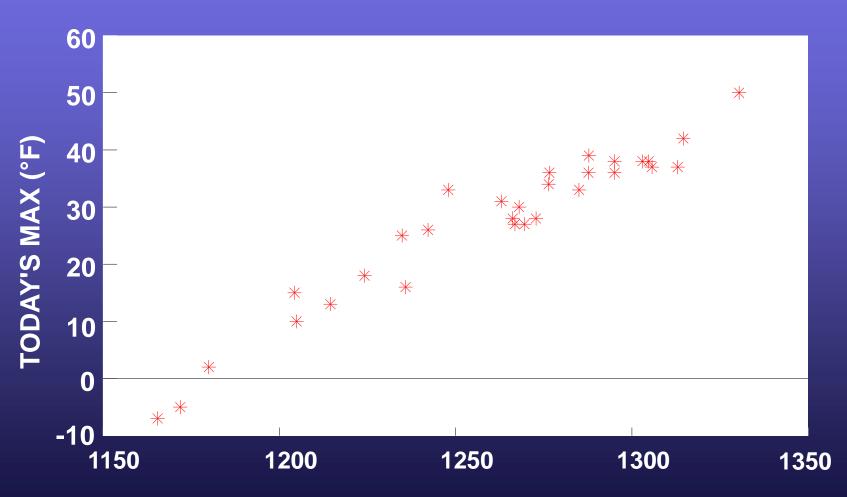
## Very recent additions

New within the past year...

- GFSX MOS:
  New 1200 UTC package (no clds, wind, ptype)
- Eta MOS: Visibility and obstruction to vision forecasts
- Marine MOS: Temperature forecasts
- Western Pacific MOS wind guidance

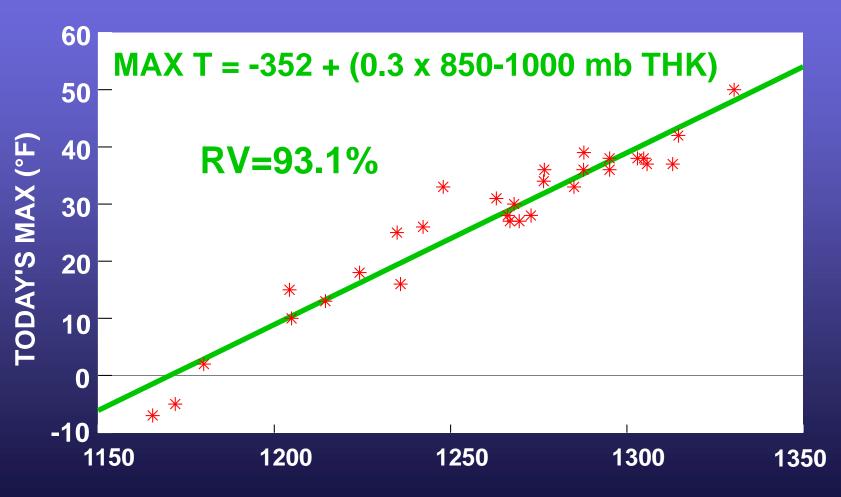
# Application of Linear Regression to MOS Development

JANUARY 1 - JANUARY 30, 1994 0000 UTC KCMH



18-H NGM 850-1000 MB THICKNESS (M)

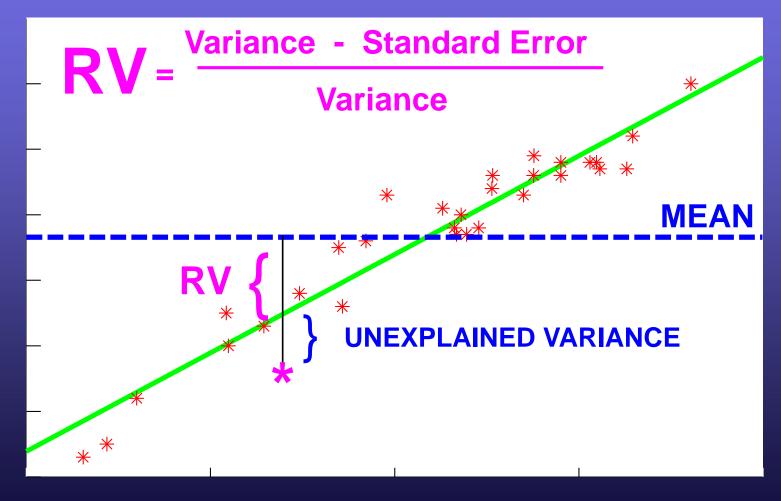
JANUARY 1 - JANUARY 30, 1994 0000 UTC KCMH



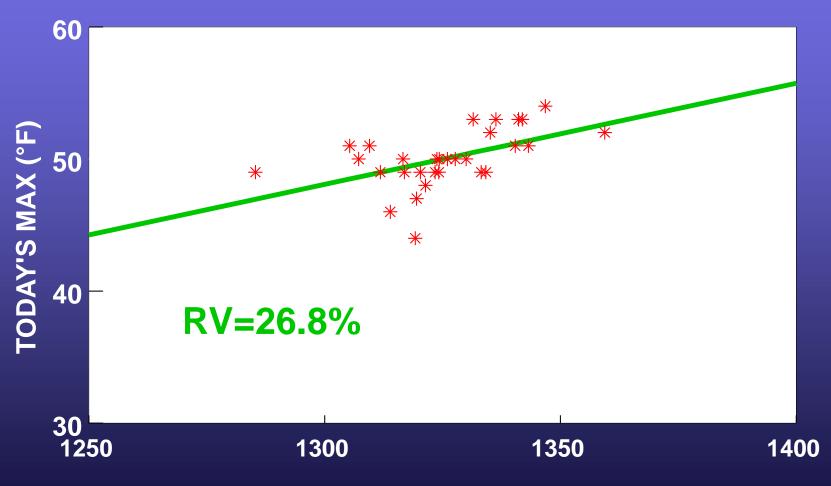
18-H NGM 850-1000 MB THICKNESS (M)

#### REDUCTION OF VARIANCE

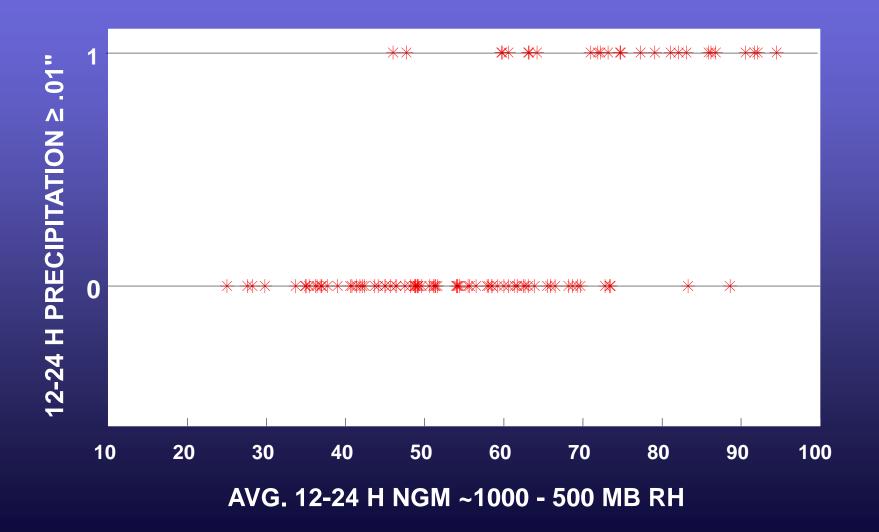
A measure of the "goodness" of fit and Predictor / Predictand correlation

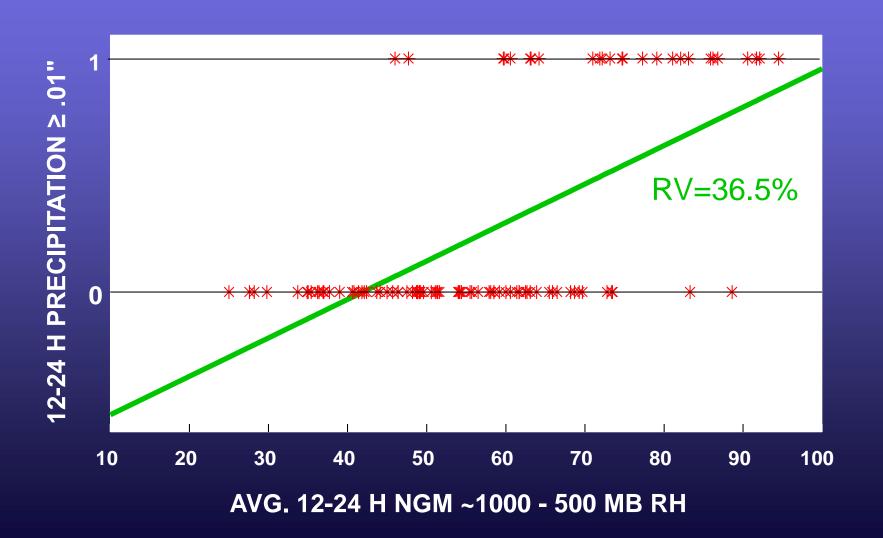


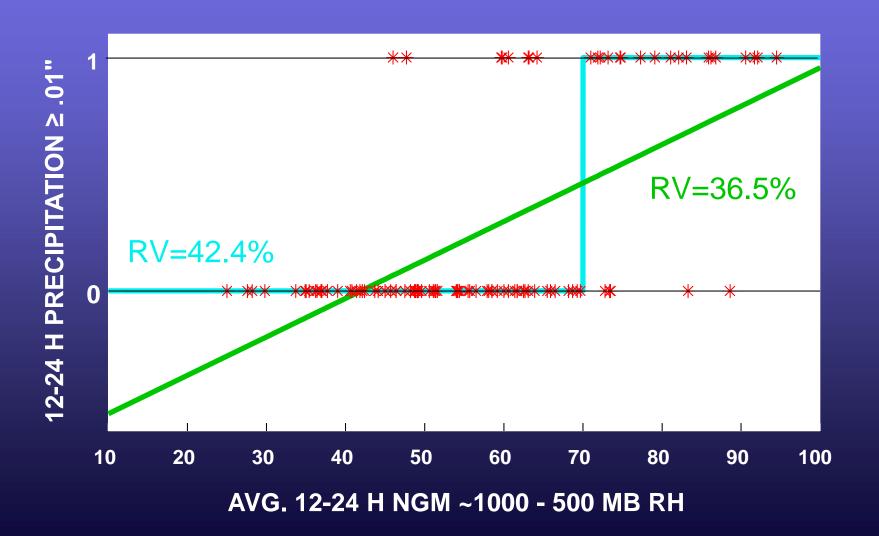
JANUARY 1 - JANUARY 30, 1994 0000 UTC

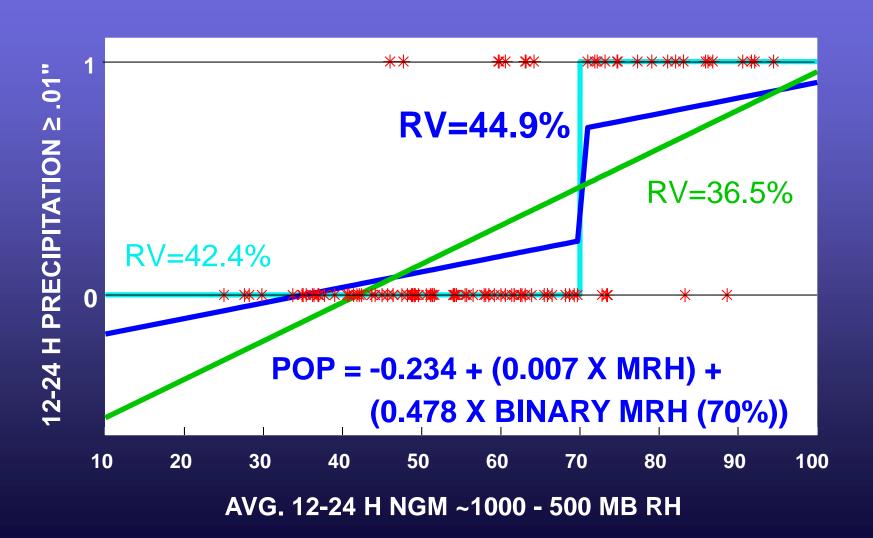


18-H NGM 850-1000 MB THICKNESS (M)









#### **EXAMPLE REGRESSION EQUATIONS**

$$Y = a + bX$$

#### CMH MAX TEMPERATURE EQUATION

 $MAXT = -352 + (0.3 \times 850 - 1000 \text{ mb THICKNESS})$ 

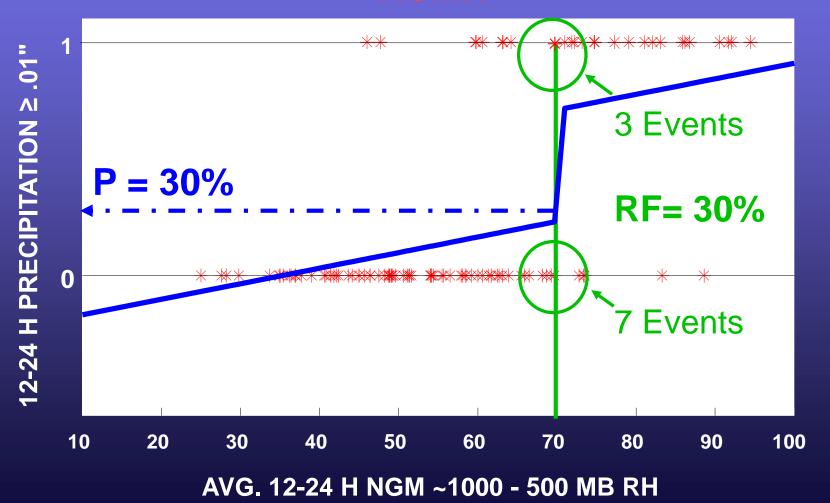
#### CMH PROBABILITY OF PRECIPITATION EQUATION

POP = -0.234 + (0.007 x MEAN RH) + (0.478 x BINARY MEAN RH CUTOFF AT 70%)\*

\*(IF MRH ≥ 70% BINARY MRH = 1; else BINARY MRH = 0)

# If the predictand is BINARY, MOS regression equations produce estimates of event PROBABILITIES...

#### **KCMH**



# Making a PROBABILISTIC statement...



Quantifies the uncertainty!

## **DEFINITION of PROBABILITY**

(Wilks, 1994)

- LONG TERM RELATIVE FREQUENCY OF AN EVENT
- DEGREE OF BELIEF OR QUANTIFIED JUDGMENT ABOUT THE OCCURRENCE OF AN UNCERTAIN EVENT

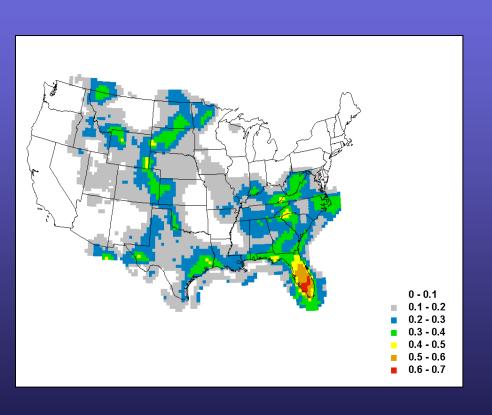
#### **KEEP IN MIND:**

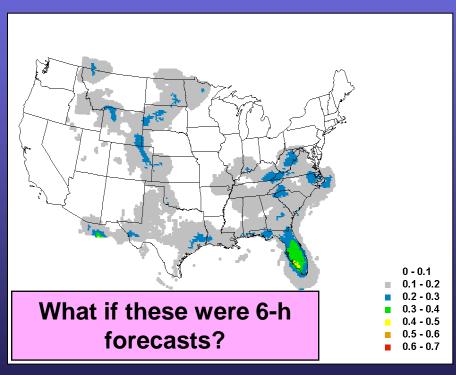
Assessment of probability is **EXTREMELY** dependent upon how predictand "event" is defined:

- Time period of consideration
- Area of occurrence
- Dependent upon another event?
  - POINT PROBABILITY
  - AREAL PROBABILITY
  - CONDITIONAL PROBABILITY

#### **AREAL PROBABILITIES**

## 3H Eta MOS thunderstorm probability forecasts valid 0000 UTC 8/27/2002 (21-24h proj)





40-km gridbox 10% contour interval

20-km gridbox 10% contour interval

# Designing an Operational MOS System:

Putting theory into practice...

#### **DEVELOPMENTAL CONSIDERATIONS**

#### MOS in the real world

Selection (and QC!) of Suitable
 Observational Datasets
 ASOS? Remote sensor? Which mesonet?

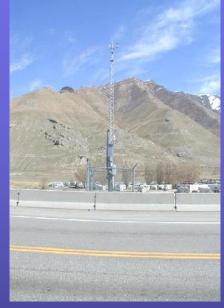
## Suitable observations?

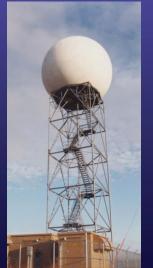




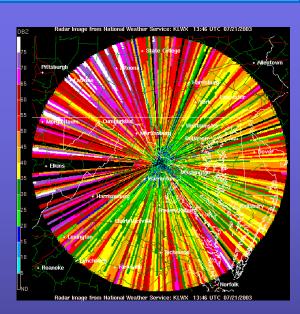


**Real or Memorex? Good siting?** 











#### **DEVELOPMENTAL CONSIDERATIONS**

#### MOS in the real world

- Selection (and QC!) of Suitable
   Observational Datasets
   ASOS? Remote sensor? Which mesonet?
- Predictand Definition Must be precise !!

## PREDICTAND DEFINITION

## Max/Min and PoP

Daytime Maximum Temperature "Daytime" is 0700 AM - 0700 PM LST

Nighttime Minimum Temperature "Nighttime" is 0700 PM - 0800 AM LST

Probability of Precipitation

Precipitation occurrence is accumulation

of ≥ 0.01 inches of liquid-equivalent at a

gauge location within a specified period

#### **DEVELOPMENTAL CONSIDERATIONS**

#### MOS in the real world

- Selection (and QC!) of Suitable
   Observational Datasets
   ASOS? Remote sensor? Which mesonet?
- Predictand Definition Must be precise !!
- Choice of Predictors
   "Appropriate" formulation
   Binary or other transform?

## "APPROPRIATE" PREDICTORS

DESCRIBE PHYSICAL PROCESSES ASSOCIATED WITH OCCURRENCE OF PREDICTAND

i.e. for POP:

PRECIPITABLE WATER
VERTICAL VELOCITY
MOISTURE DIVERGENCE
MODEL PRECIPITATION



"MIMIC" FORECASTER THOUGHT PROCESS (VERTICAL VELOCITY) X (MEAN RH)

## **DEVELOPMENTAL CONSIDERATIONS**

(cont.)

Terms in Equations; Selection Criteria

## "REAL" REGRESSION EQUATIONS

MOS regression equations are MULTIVARIATE, of form:

$$Y = a_0 + a_1 X_1 + a_2 X_2 + ... + a_N X_N$$

Where,

the "a's" represent COEFFICIENTS the "X's" represent PREDICTOR variables

The maximum number of terms, N, can be **QUITE** large:

For NGM QPF, N = 15 For NGM VIS, N = 20

The **FORWARD SELECTION** procedure determines the predictors and the order in which they appear.

## **DEVELOPMENTAL CONSIDERATIONS**

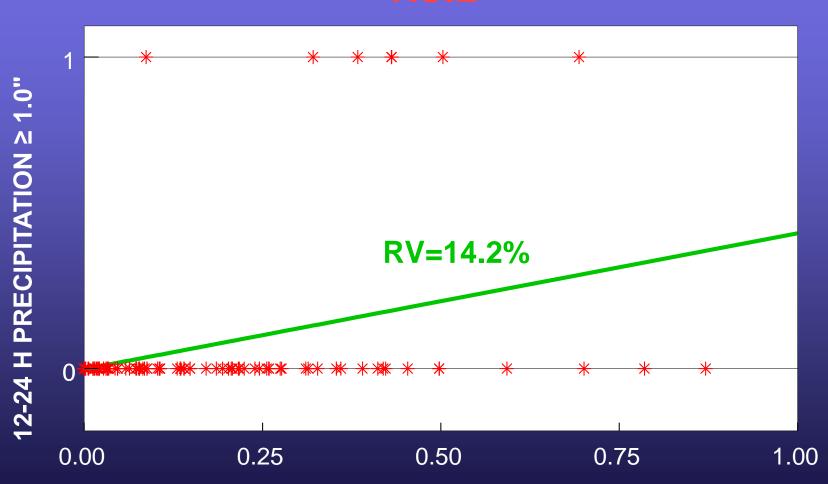
(cont.)

- Terms in Equations; Selection Criteria
- Dependent Data
   Sample Size, Stability, Representativeness
   AVOID OVERFIT!!

Stratification - Seasons
Pooling – Regions

## MOS LINEAR REGRESSION

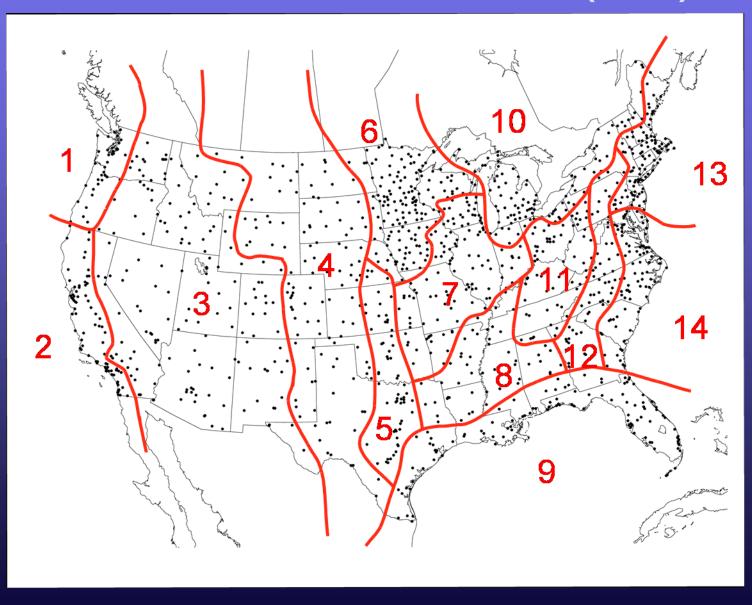
OCTOBER 1 1993 - MARCH 31 1994 0000 UTC KUIL



12-24 H NGM PRECIPITATION AMOUNT (IN.)

## **AVN/GFS Cool Season PoP/QPF Regions**

## With AVN MOS forecast sites (1406)



### **DEVELOPMENTAL CONSIDERATIONS**

(cont.)

- Terms in Equations; Selection Criteria
- Dependent Data
   Sample Size, Stability, Representativeness
   AVOID OVERFIT!!

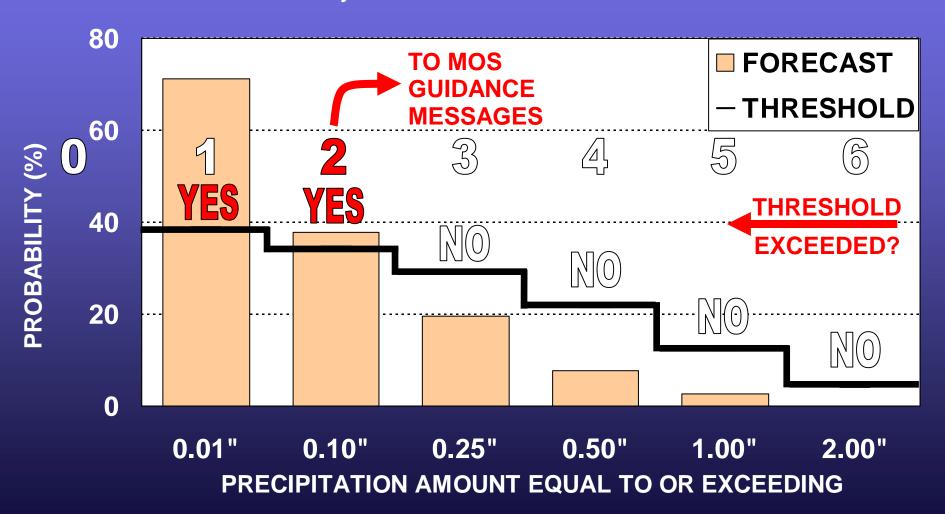
Stratification - Seasons
Pooling – Regions

Categorical Forecasts?

## MOS BEST CATEGORY SELECTION

#### **KDCA 12-Hour QPF Probabilities**

48-Hour Projection valid 1200 UTC 10/31/93

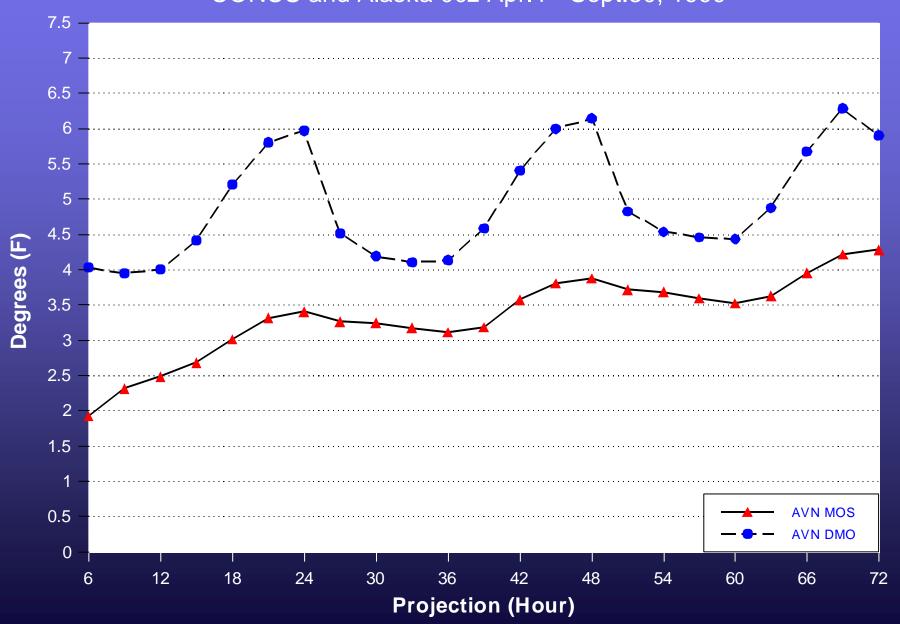


## How well do we do?

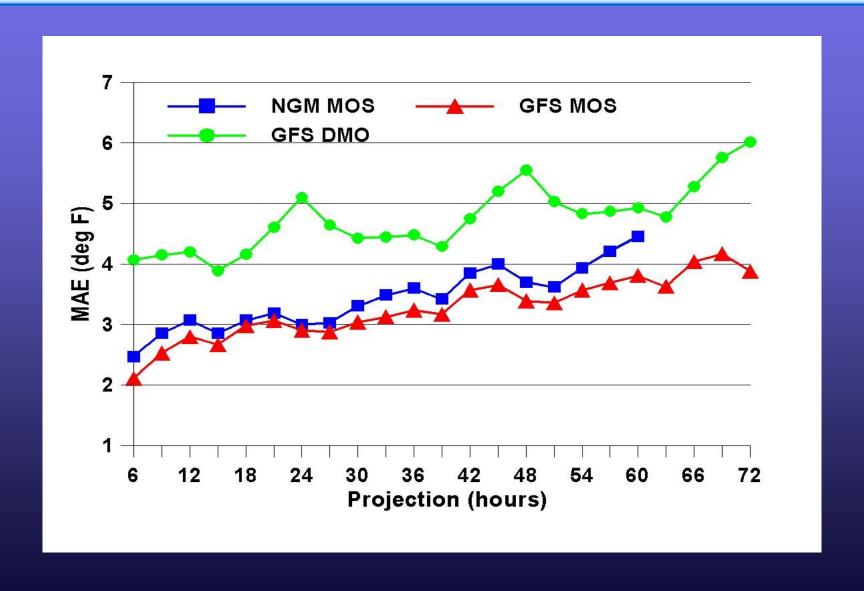
**MOS Verification** 

#### Dew Point Mean Absolute Error

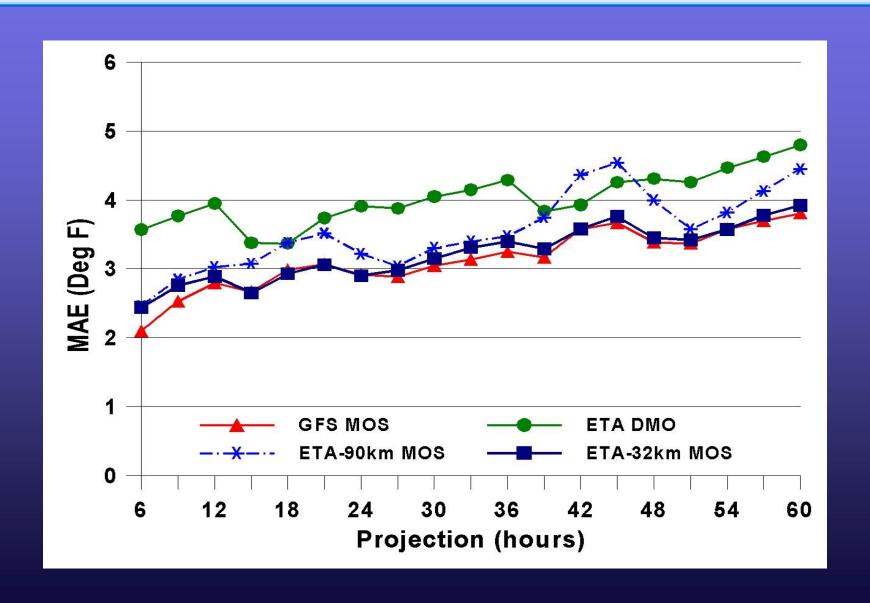
CONUS and Alaska 00z Apr.1 - Sept.30, 1999



## Temperature Verification - 0000 UTC Cool Season 2002 -2003

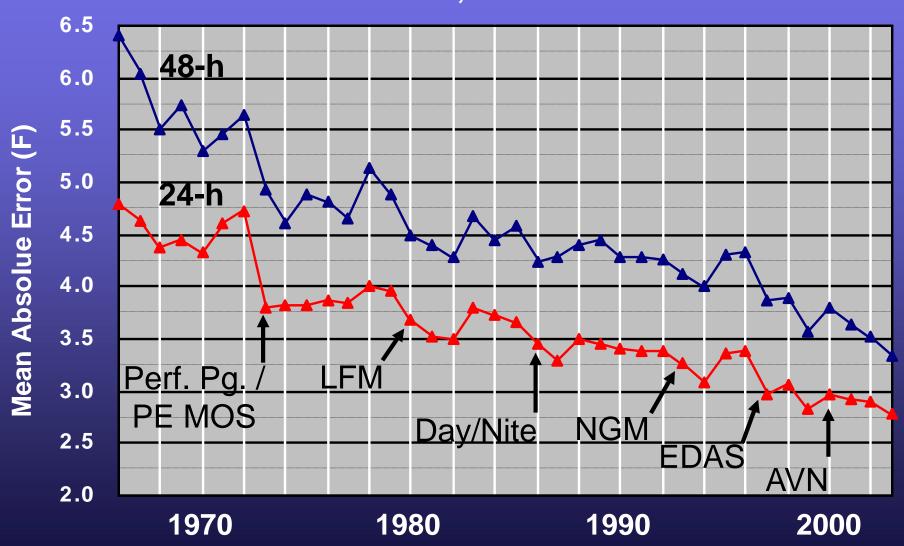


## Temperature Verification - 0000 UTC Cool Season 2002 -2003



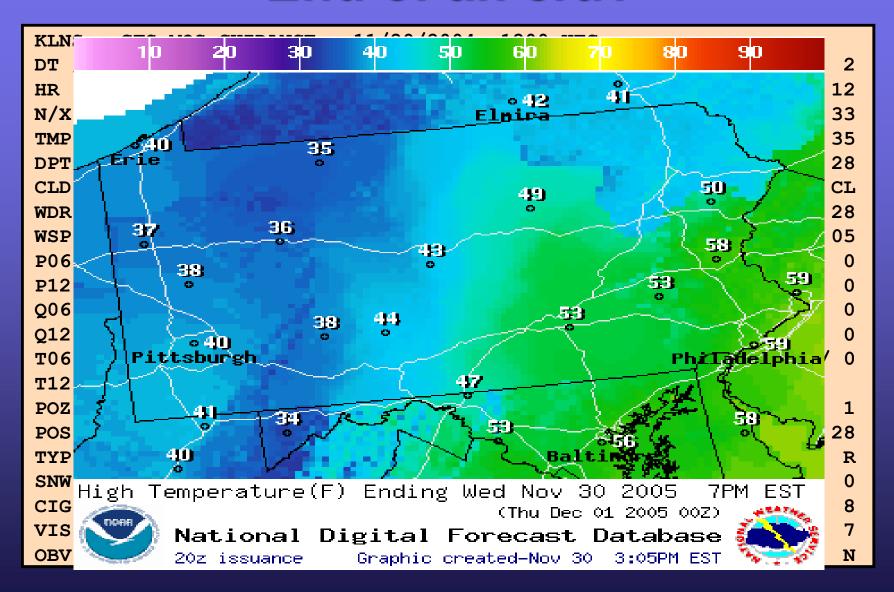
## Max Temperature Verification

Cool Season; 1966 - 2003



## MOS: Today and Beyond

## End of an era?



WANTED! High-resolution, gridded guidance for NDFD

## The Future of MOS

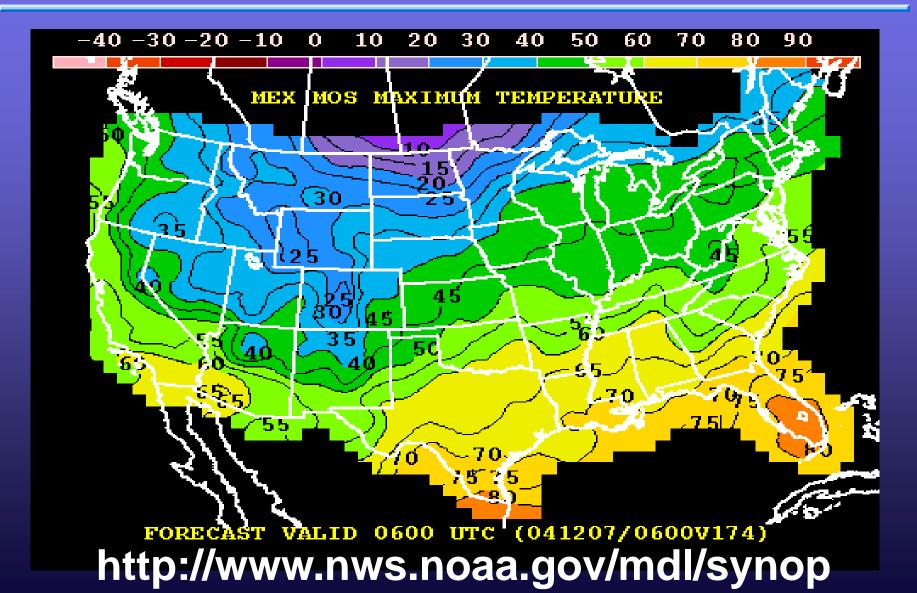
"Traditional" Station-oriented Products

- GFSX MOS:

  Changes to cloud and wind predictands

  (Instantaneous values, post-process to avg.)
- Eta MOS:
   Eta/WRF re-evaluation, possible phaseout
- Western Pacific MOS:
   Add new elements (PoP, T, T<sub>d</sub>, Max/Min, Cld)
- General:
   Periodic addition of new CONUS sites
   Gradual phaseout of station-oriented graphics

# GFSX MOS Day 7 Maximum Temperature

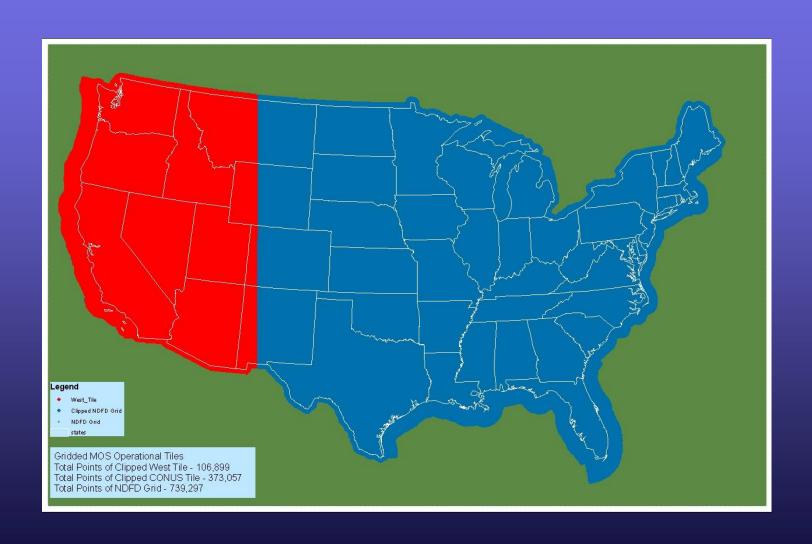


## The Future of MOS

## "Enhanced-Resolution" MOS Systems

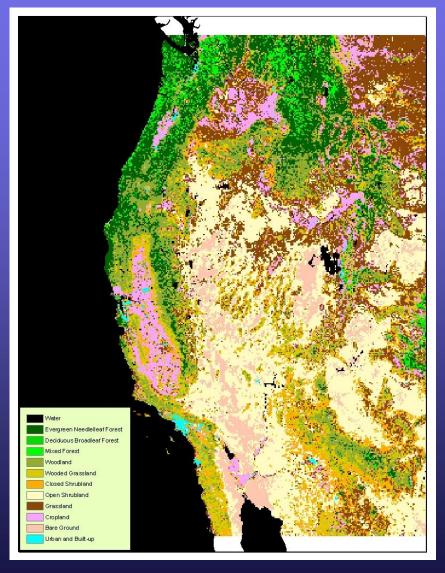
"MOS at any point"
 Support new NWS digital forecast database
 2.5 km - 5 km resolution
 Emphasis on high-density surface networks
 Co-Op, buoy, mesonet
 Equations valid away from observing sites
 Use high-resolution geophysical data

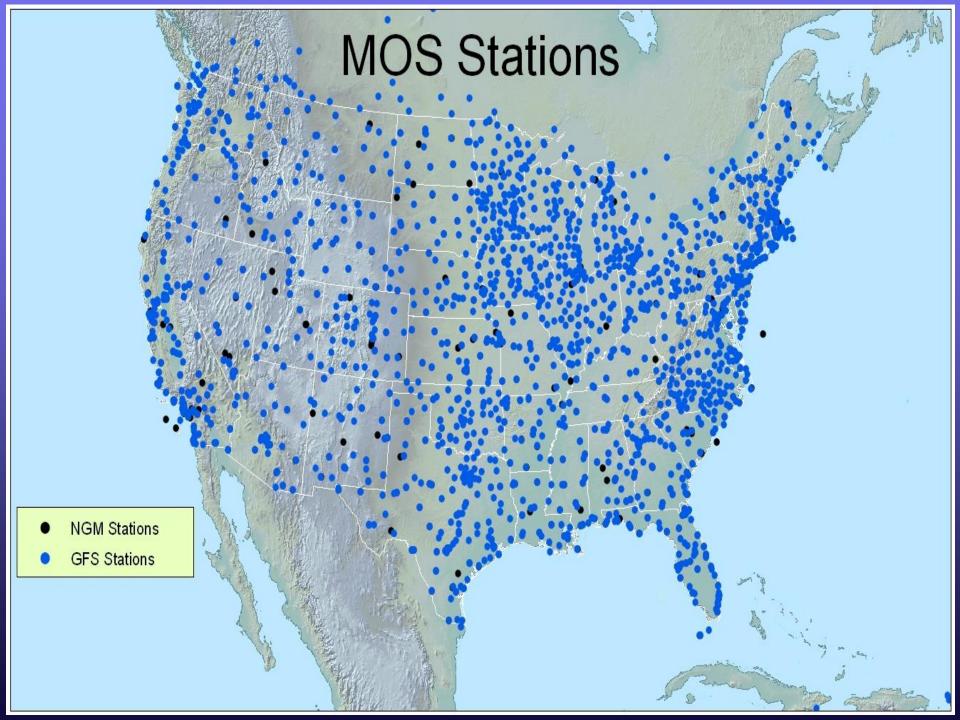
## **Gridded MOS Domains**

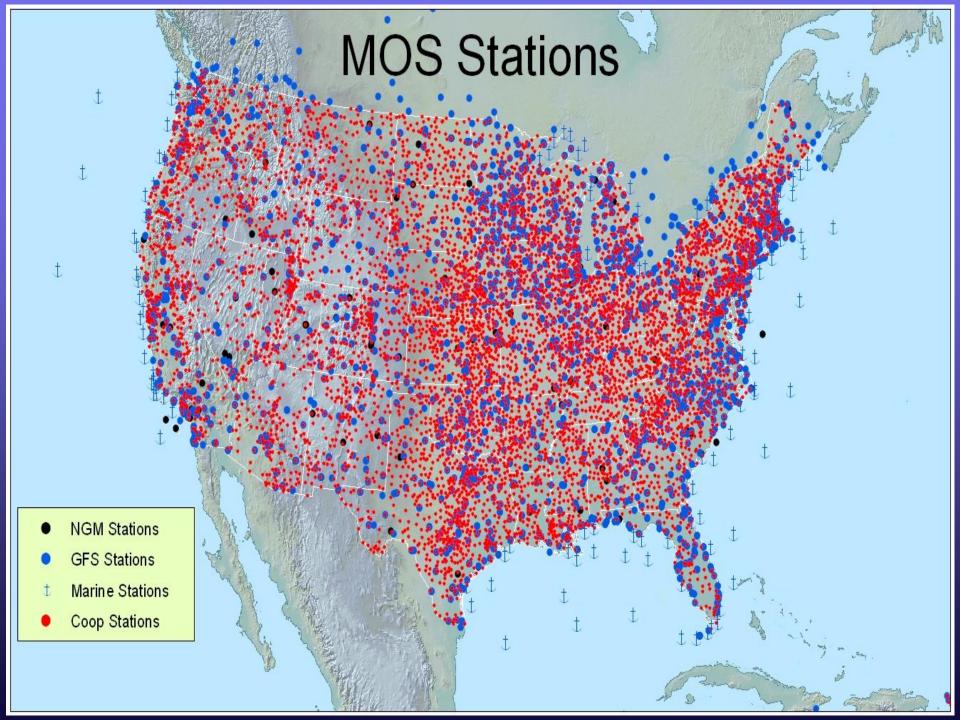


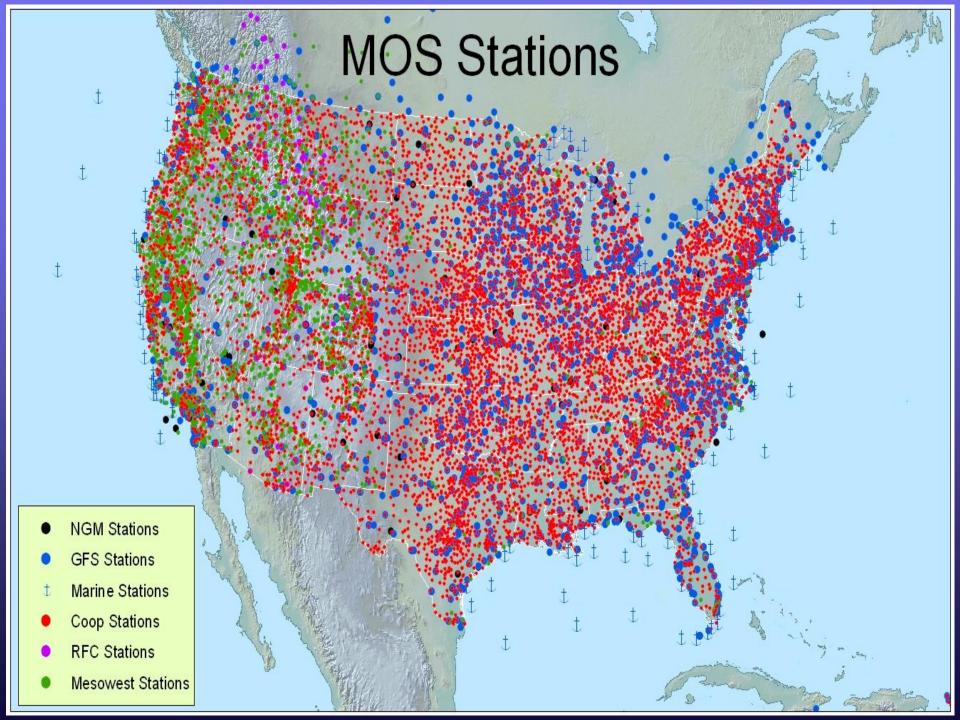
## **Geophysical Datasets**



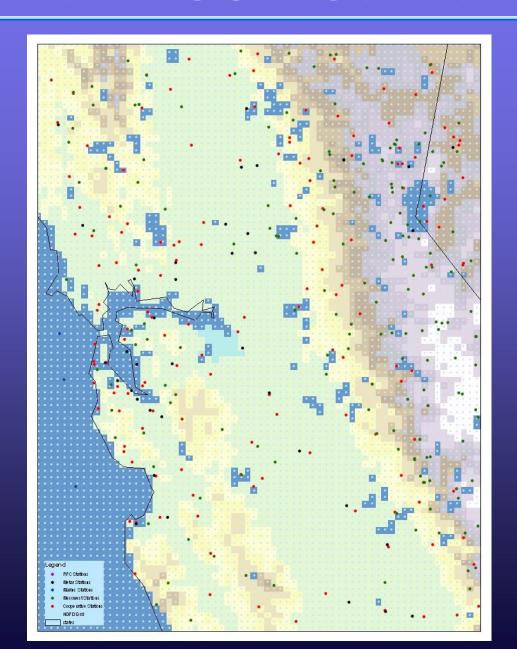






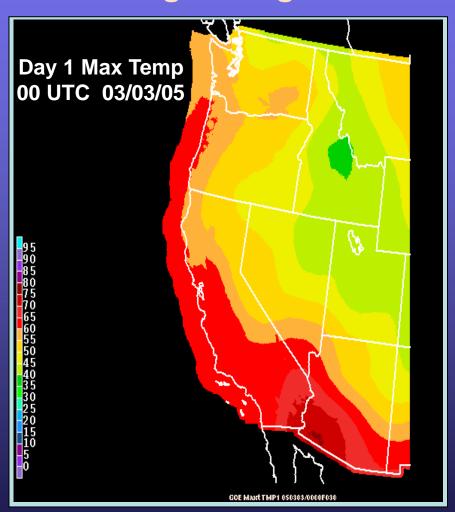


## **Gridded MOS – Central CA**

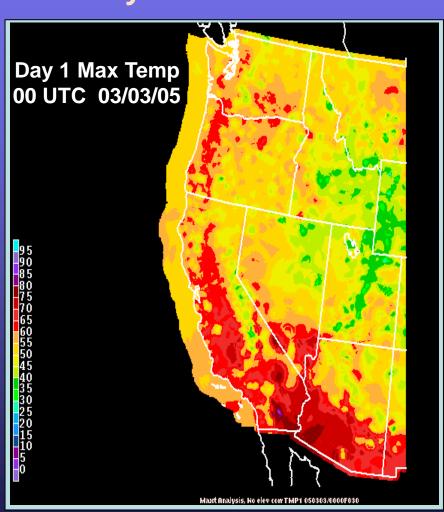


## **Gridded MOS Concept - Step 1**

"Blending" first guess and high-density station forecasts



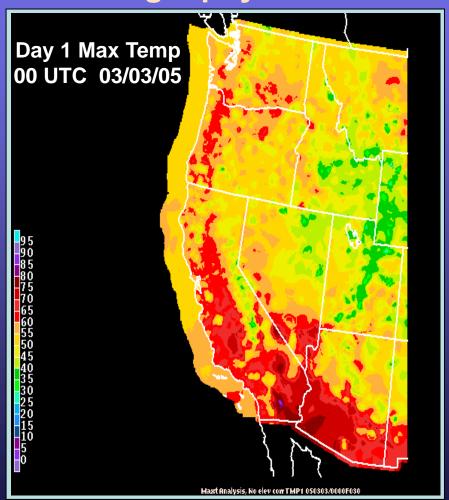
First guess field from Generalized Operator Equation or other source



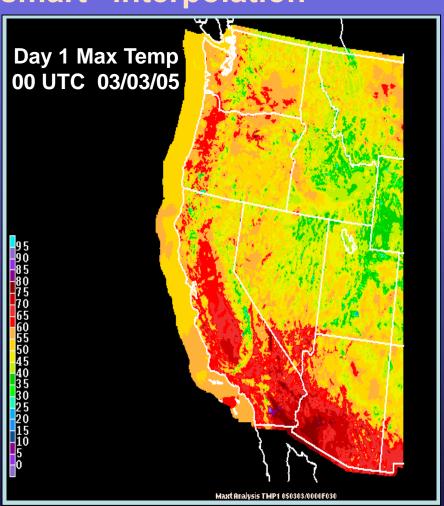
First guess + guidance at all available sites

## **Gridded MOS Concept - Step 2**

Add further detail to analysis with high-resolution geophysical data and "smart" interpolation



First guess + guidance at all available sites

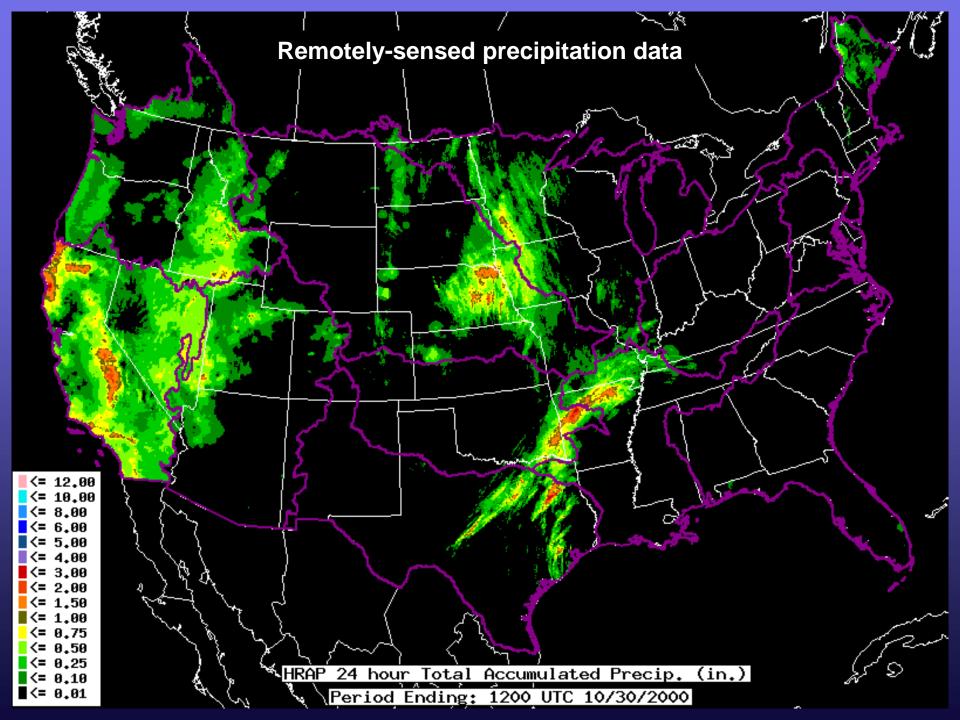


First guess + station forecasts + terrain

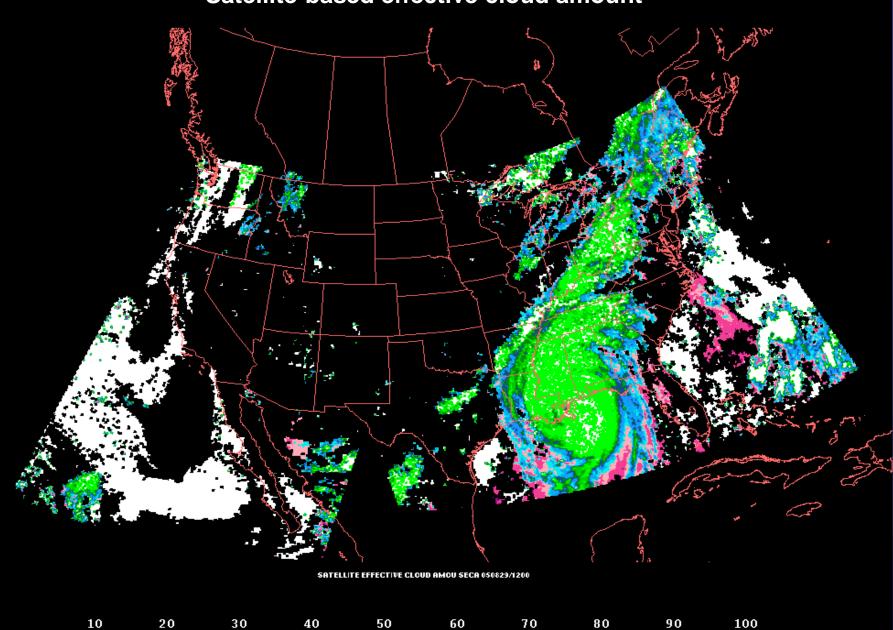
## The Future of MOS

## "Enhanced-Resolution" MOS Systems

- "MOS at any point"
   Support new NWS digital forecast database
   2.5 km 5 km resolution
   Emphasis on high-density surface networks
   Co-Op, buoy, mesonet
   Equations valid away from observing sites
   Use high-resolution geophysical data
- "True" gridded MOS
   Observations and forecasts valid on fine grid
   Use remotely-sensed predictand data
   e.g. PoP/QPF "Demonstration" System
   4-km HRAP grid; WSR-88D



#### **Satellite-based effective cloud amount**



## REFERENCES

Wilks, D.: Statistical Methods in the Atmospheric Sciences, Chap. 6, p. 159 - 210.

Draper, N.R., and H. Smith: Applied Regression Analysis, Chap. 6, p. 307 - 308.

Glahn, H.R., and D. Lowry, 1972: The use of model output statistics in objective weather forecasting, <u>JAM</u>, 11, 1203 - 1211.

Carter, G.M., et al., 1989: Statistical forecasts based on the NMC's NWP System, Wx. & Forecasting, p. 401 - 412.