

MICRO-435 HW6

Qualitative Questions

Question 1 Which are the 3 most important characteristics that a nanogap for Molecular Transistors should have?

- 1- They can be arranged small enough to place the molecule.
- 2- They should not lead a thermal runaway such as bowtie type.

Question 2 Identify 3 fundamental conditions that must be verified in order to generate nanogap based on electromigration without thermal runaway

- 1- Many electrons are present
- 2- High current density
- 3- Atoms are free to move

Question 3 Identify 3 critical points when using F.I.B. for nanogap creation

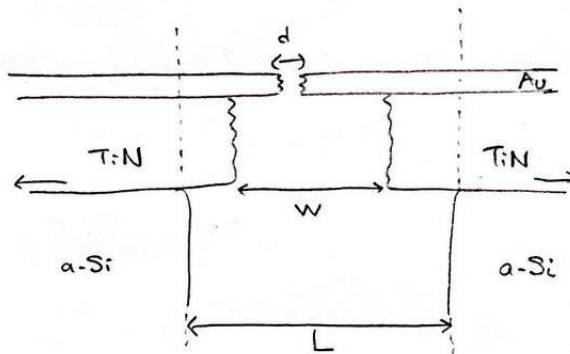
- 1- Energy of the coming ions should be sufficient to overcome the binding energy of the substrate's atom.
- 2- Requires a precise tuning of beam parameters.
- 3- Due to atom bounce backs, effective gap is exploited

Question 4 Identify 3 advantages in the case of CDBJ technology for the generation of nanogaps

- 1- CDBJs avoid the need for an external equipment to drive the breaking process; EBJs and MCBJs rely on sophisticated external apparatuses to achieve sufficient process control to obtain sub-5 nm gaps (feedback controlled current source and motorized bending stage, respectively). In place of this, crack defined break junctions rely on internal stress created in the brittle layer, which, without using any electronic devices, is a completely integrated method to cause the breaking of metal constrictions instantly and in a highly parallel manner [1]
- 2- Due to the self-generated nature of the cracking-pulling-breaking processes, CDBJs may be mass produced and integrated; all that is required are the hanging and notched bridge structures. Consequently, the lithography criteria are substantially eased. [1]
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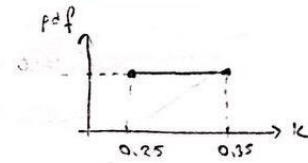
Quantitative Questions

Question 5



$$d = 0.8 \text{ nm}$$

$$d = k w$$



$$\text{Hence } k = 0.3 \leftarrow$$

$$d = k w = k L \epsilon \quad \text{elastic strain of TiN} \quad 0.25 \leq k \leq 0.35$$

$$0.8 = 0.25 \times L_{\max} \times (2.7) \frac{\text{nm}}{\mu\text{m}}$$

$$L_{\max} = \frac{0.8 \text{ nm}}{0.25 \times 2.7 \frac{\text{nm}}{\mu\text{m}}} \approx 1.185 \mu\text{m}$$

$$0.85 \mu\text{m} \leq L \leq 1.185 \mu\text{m}$$

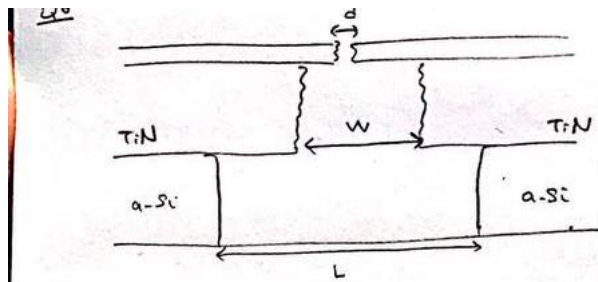
$$L_{\min} = \frac{0.8 \text{ nm}}{0.35 \times 2.7 \frac{\text{nm}}{\mu\text{m}}} \approx 0.85 \mu\text{m}$$

for $L < 1 \mu\text{m}$, no gaps can be created.

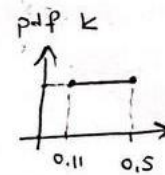
Thus, let choose $k = 0.25$ (min), $L = 1.185 \mu\text{m}$, $\epsilon = 2.7 \text{ nm}/\mu\text{m}$

$$\downarrow$$

$$w = 3.2 \text{ nm}$$



$$d = 1.8 \text{ nm}$$



$$d = k \sqrt{w}$$

$$1.8 \text{ nm} = (0.11)_{k_{\min}} \sqrt{L \cdot \epsilon_{\min}}$$

$$L \epsilon_{\min} = \left(\frac{1.8 \text{ nm}}{0.11} \right)^2$$

$$L_{\max} = \left(\frac{1.8}{0.11} \right)^2 \cdot \frac{1}{2.295} = 116 \text{ nm} \rightarrow \text{too big!}$$

ϵ can change around 15% wrt avg. value
 $2.7 \text{ nm} \mu\text{m}^{-1}$
 Bridge width is around 60 nm (?)
 $2.7 \times \frac{85}{100} \leq \epsilon \leq (2.7) \times \frac{115}{100}$

$$2.295 \leq \epsilon \leq 3.105$$

$$L_{\min} = \left(\frac{1.8 \text{ nm}}{0.5} \right)^2 \cdot \frac{1}{3.105} = 4.173 \text{ nm} \rightarrow \text{it is a very good approximation,}$$

Since $1 < L < 6 \text{ nm}$

Thus choose $k = 0.5$, $\epsilon = 3.105$; which yields $L_{\min} = 4.173 \rightarrow W = 32.96 \text{ nm}$

$$W \approx 60 \text{ nm}$$

? In that case, I ignored that
 W is around 60 nm

$$d = k \sqrt{w} = k \sqrt{L \epsilon}$$

$$k \approx \frac{1.8}{\sqrt{60}} \approx 0.232$$

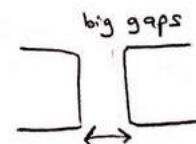
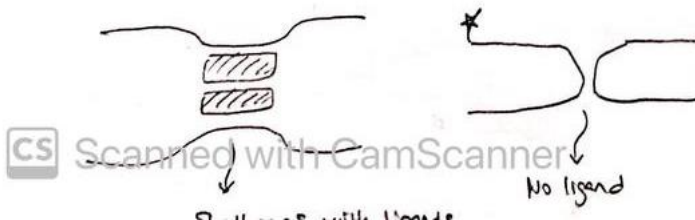
$$L \epsilon \approx 60$$

$$\epsilon_{\max} = 3.105$$

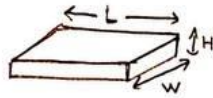
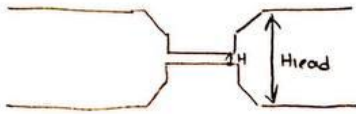
$$L_{\min} = 19.32 \text{ nm} \rightarrow \text{which is not good}$$

since $L > 6 \text{ nm}$

which yields a big gap



Question 7



$$H = 15 \text{ nm}$$

$$L = 250 \text{ nm}$$

$$W = 100 \text{ nm}$$

$$H_{\text{head}} = 150 \text{ nm}$$

$$R_{\text{tot}} = 86 \Omega \text{ @ } T = 77 \text{ K} \text{ just before E.M starts.}$$

$$T_{\text{crit}} = 345 \text{ K}$$

$$\text{Acc to Joule Heating} \rightarrow T = T_0 + \beta j^2$$

$$j_{\text{crit}} = 4 \times 10^8 \text{ A/cm}$$

a) Find P_{crit} and V_{crit}

$$P_{\text{crit}} = \rho \cdot j_{\text{crit}}^2 = 86 \Omega \times (4 \times 10^8 \text{ A/cm})^2$$

$$P_{\text{crit}} = 576 \times 10^{16} \frac{\text{A}^2 \Omega}{\text{cm}^2}$$

$$V_{\text{crit}} = \rho \cdot j_{\text{crit}} = 36 \times 4 \times 10^8 \text{ A/cm} = 144 \times 10^8 \frac{\text{A} \Omega}{\text{cm}}$$

b) Constraints for the device size in order to avoid thermal runaway.

As migration happens the wire gets narrower, which leads $R \uparrow \rightarrow P \uparrow \rightarrow T \uparrow$

$$R_{\text{u}} \leftarrow T_{\text{u}} \leftarrow P_{\text{u}} \leftarrow R_{\text{u}}$$

Thermal Runaway?

$$j(t) = j_{\text{critic}} \left(\frac{1 + \frac{R_S}{R_{\text{c}(0)}}}{1 + \frac{R_S}{R_{\text{c}(t)}}} \right)^2$$

$$j_{\text{critic}} = \frac{V_{\text{CRIT}}^2}{\rho e^2} \left(1 + \frac{R_S}{R_{\text{c}(0)}} \right)^2$$

$$\text{If } \frac{R_S}{R_{\text{c}(0)}} \ll 1 \rightarrow j(t) \approx j_{\text{critic}}$$

$$\text{If } \frac{R_S}{R_{\text{c}(0)}} \gg 1 \rightarrow j(t) \text{ increases rapidly, which yields ion accumulation and thermal runaway later on.}$$

$$c) J_m = \frac{\alpha}{T} (j - j_{\text{min}}) e^{\frac{-E_0}{kT}} \text{ where } \alpha = \frac{e D_0 2^* e \rho}{K}, j_{\text{min}} = \frac{\Omega \Delta \sigma_{\text{max}}}{2^* e g L}$$

$$J_{m, \text{crit}} = \frac{\alpha}{T} (j_{\text{crit}} - j_{\text{min}}) e^{\frac{-E_0}{kT}}$$

$\downarrow 1$
 $\downarrow 4 \times 10^8$

$$J_m = \frac{\alpha}{T} e^{\frac{-E_0}{kT}} + 4 \times 10^8 = j_{\text{min}}$$