CORRECTION OF ENSEMBLE AVERAGED DENSITY- OPERATOR

$$H(+) = -\frac{1}{7} h \left[g(t) \left(g^{\epsilon}_{V} + g^{\epsilon}_{V}(t) \right) \right]$$

$$= \left(\frac{1}{2} \sum_{i=1}^{N_{c}} \frac{u_{i}}{(-i\epsilon)_{i}} \left(g^{\epsilon}_{V} \right)_{U} \right) \otimes I$$

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$$= \left(\frac{1$$

$$e^{-ik\sigma_{\xi}^{A}} \otimes I = \begin{bmatrix} \cos(k) I^{A} + i \sin(k) G_{\xi}^{A} \end{bmatrix} \otimes I^{B}$$

$$= \begin{bmatrix} e^{ik} \\ e^{ik} \\ 0 \end{bmatrix} \otimes \begin{bmatrix} e^{-ik} \\ e^{-ik} \end{bmatrix}$$

$$= \begin{bmatrix} e^{ik} \\ 0 \end{bmatrix} \otimes \begin{bmatrix} e^{-ik} \\ 0 \end{bmatrix} \otimes \begin{bmatrix} e^{-ik} \\ 0 \end{bmatrix}$$

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$$= \begin{bmatrix} e^{ik} \\ e^{-ik} \end{bmatrix} \otimes \begin{bmatrix} e^{-ik} \\ 0 \end{bmatrix} \otimes \begin{bmatrix} e^{-ik$$

$$U^{\dagger}(t) = \begin{cases} e^{-i(k+L)} \\ e^{-i(k-L)} \end{cases}$$

$$e^{+i(k+L)}$$

$$e$$

Characteristic Function of Gaussian Stochastic Process

+1 | p(s) C(s-s') P(s') disds'

E (e) = e

where
$$E(X(S)) = 0$$

 $E(X(S) X (S')) = C(S-S')$ (Autocorrelation)

L=
$$\left(-\frac{\mu}{2}\right)^{\frac{1}{2}} dt^{\frac{1}{2}} \left[\frac{\mu(t) + b_{0}(1)}{\mu(t)}\right]$$

= $\left(-\frac{\mu}{2}\right)^{\frac{1}{2}} \int_{\mu(t)}^{\mu(t)} \mu(t) dt^{\frac{1}{2}}$

= $\left(-\frac{\mu}{2}\right)^{\frac{1}{2}} \int_{\mu(t)}^{\mu(t)} \mu(t) dt^{\frac{1}{2}}$

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= $\left(-\frac{1}{2}\right)^{\frac{1}{2}} \int_{\mu(t)}^{\mu(t)} \mu(t) dt^{\frac{1}{2}} dt^{\frac{1}$

$$\int_{0}^{t} dt' \int_{0}^{t} dt'' \int_{0}^{t} (t''-t')$$

$$= \int_{0}^{t} dt' \left[\Theta(t''-t') - \Theta(0-t') \right] = \int_{0}^{t} dt' = t$$

$$= \int_{0}^{t} dt' \left[\Theta(t-t') - \Theta(0-t') \right] = \int_{0}^{t} dt' = t$$

$$= \int_{0}^{t} dt' = t$$

$$e^{i2l} = e^{-\frac{1}{2}i7t}$$
 $-\frac{1}{2}igt$ $-\frac{1}{2}(i7+i7e)t$

Using Characteristic function, the density operator can be obtained as below:

APPENDIX

Juhue does il come from?

-1 | P(s) C(s-s') P(s') dsds'

$$E\left(e^{i\int \varphi(s) \times (s) ds}\right) = e$$

Gaussian Random Process

Characteristic function of the Gaussian probability density:

probability
$$p(x) = \frac{1}{\sqrt{2\pi\sigma^2}}$$

characteristic
$$=\langle e^{ikx}\rangle = \frac{1}{\sqrt{2\pi\sigma^2}}\int_{-\infty}^{\infty} dxe^{-\frac{(x-\mu)^2}{2\sigma^2}}ikx$$

Gaussian probability density: Probability distribution of a random variable

Gaussian randon process: Any dinite number of randon variables was a Joint Gaussian distribution It's Ruly described by its mean function and covariance function.

Characteristic Function of Gaussian Randon Process:

Let X(t) be a Gaussian landou process with mean function m(t) and covariance function K(s,t) where sand t are in time abusin

ip(t)t - 1 SSK(s,t) dsdt

or \$(4) = e

Note: $C_{xx}(t_1,t_2) = C_{xx}(t_1,t_2) - \mu_x(t_1)\mu_x^*(t_2)$ covariance

autocorrelation

D(+)= E[exp(iwX(+))]