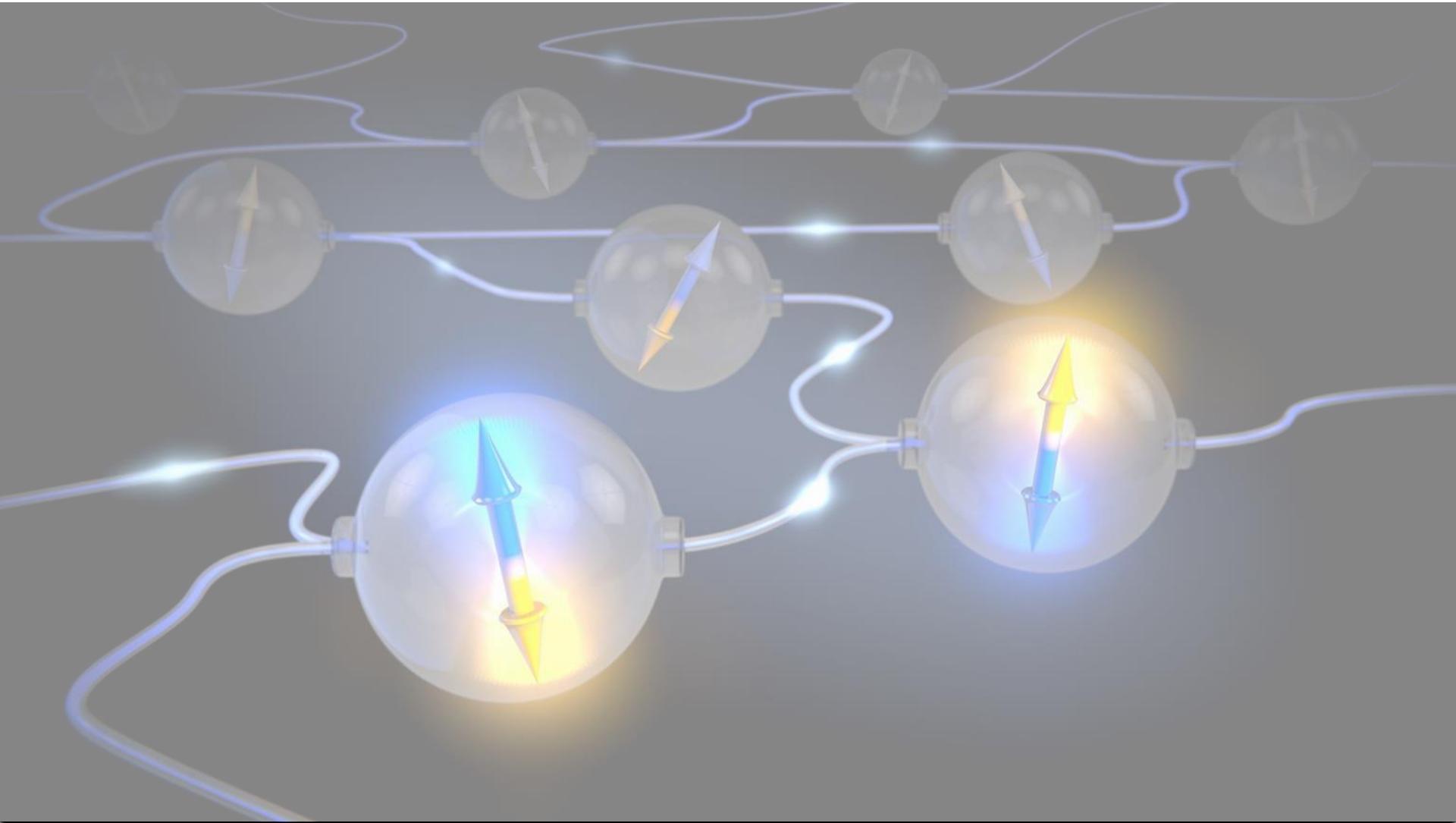


Introduction to SPIN QUBITS in SEMICONDUCTING QUANTUM DOTS



The electron SPIN as prototype of every 2-level system

Quantum State
Dirac Notation $|\Psi\rangle$

Contains all the information about the systems

- A particle localized at the position x, $|X\rangle$
- A particle localized at the position y, $|Y\rangle$



SUPERPOSITION: Quantum Mechanics is a linear theory: all the possible sum of the possible states is also a state allowed.

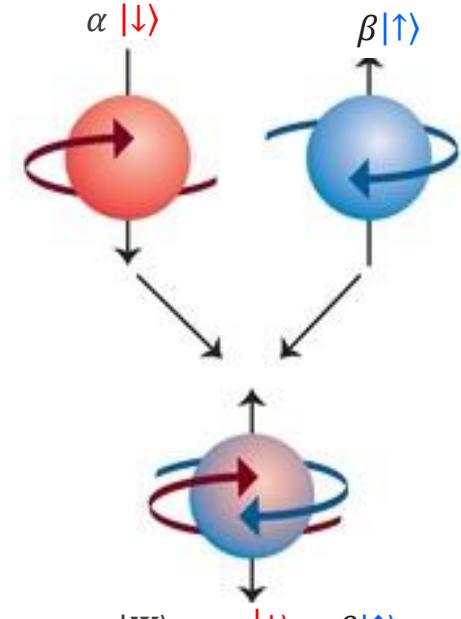
$\frac{1}{\sqrt{2}}(|X\rangle + |Y\rangle)$ is also an allowed state for our system

A particle in two places at once???
Convenient, but shocking!

The possibility of superposing states even in multiple-particle systems naturally results in the concept of ENTANGLEMENT.

A prototype for every artificial 2-level systems (qubits) is the **real spin of an electron**

- An electron can have a spin \downarrow , $|\downarrow\rangle$
- An electron can have a spin \uparrow , $|\uparrow\rangle$

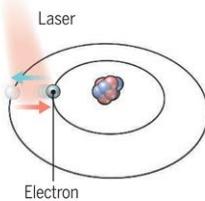


$$|\alpha|^2 + |\beta|^2 = 1$$

Multiple Quantum Platforms

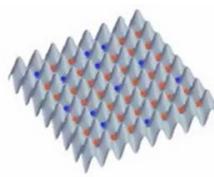
In the race to build a quantum computer, researchers are pursuing many types of quantum bits, each with its own strengths and weaknesses

Natural Qubits



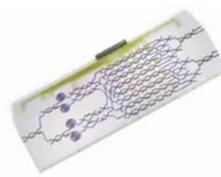
Trapped ions

Electrically charged atoms, or ions, have quantum energies that depend on the location of electrons. Tuned lasers cool and trap the ions, and put them in superposition states.



Neutral atoms

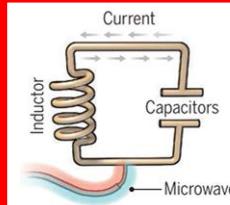
Neutral atoms, like ions, store qubits within electronic states. Interactions through excitation to Rydberg states



Photonics

Photonic qubits interact via linear elements

Syntetic Qubits



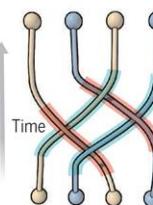
Superconducting loops

A resistance-free current oscillates back and forth around a circuit loop. An injected microwave signal excites the current into super-position states.



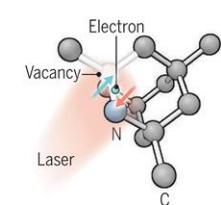
Silicon quantum dots

These "artificial atoms" are made by adding an electron to a small piece of pure silicon. Microwaves control the electron's quantum state.



Topological qubits

Quasiparticles can be seen in the behavior of electrons channeled through semiconductor structures. Their braided paths can encode quantum information.



Diamond vacancies

A nitrogen atom and a vacancy add an electron to a diamond lattice. Its quantum spin state, along with those of nearby carbon nuclei, can be controlled with light.

Define, control and readout the quantum states of single particles and photons gives insights into new quantum technology

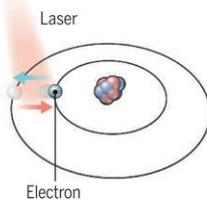
Make use of the quantum properties to enhance sensing, security in communication and boost computing and simulation.

Popkin, G.. "Quest for qubits." (2016): 1090-1093.

Multiple Quantum Platforms

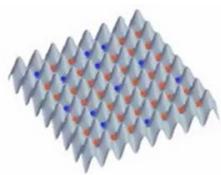
In the race to build a quantum computer, researchers are pursuing many types of quantum bits, each with its own strengths and weaknesses

Natural Qubits



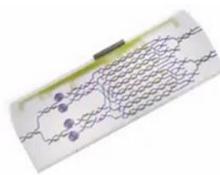
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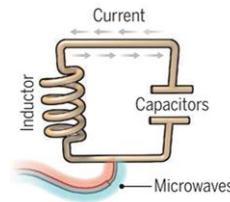
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Photonics

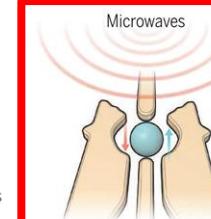
Photonic qubits interact via linear elements



Superconducting loops

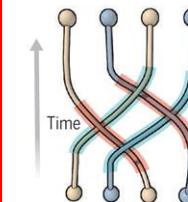
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Syntetic Qubits



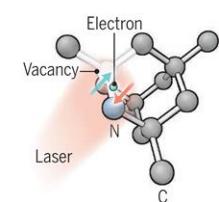
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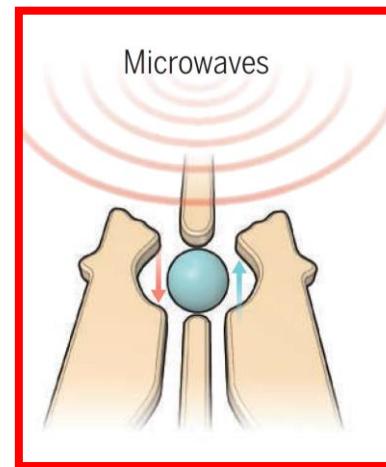
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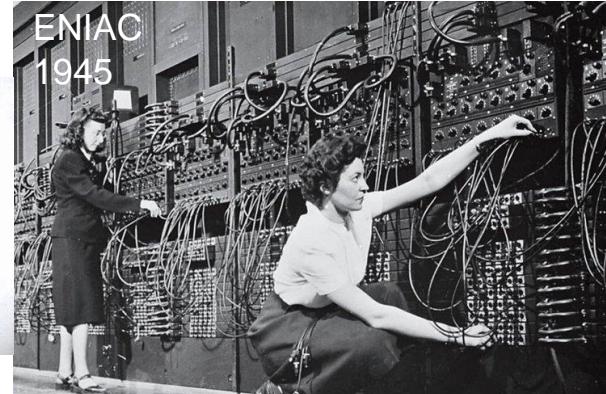
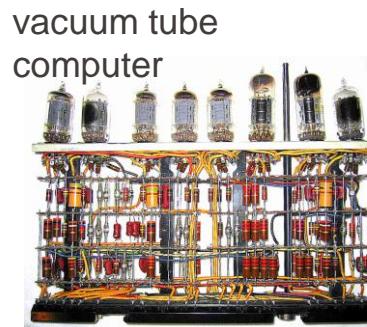
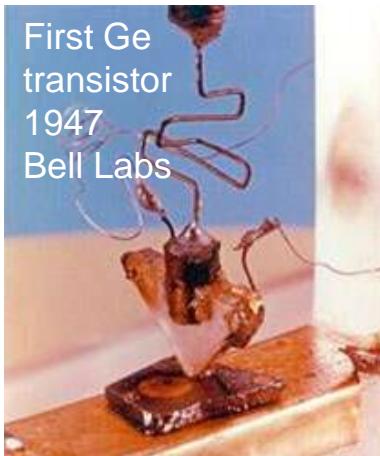
Semiconducting Spin Qubits



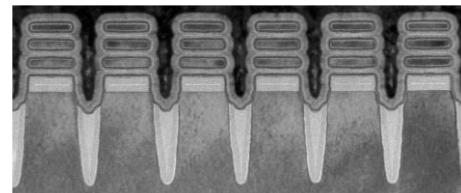
Semiconductor
QDs platform

First Quantum Revolution in Information Technology was based on semiconductors

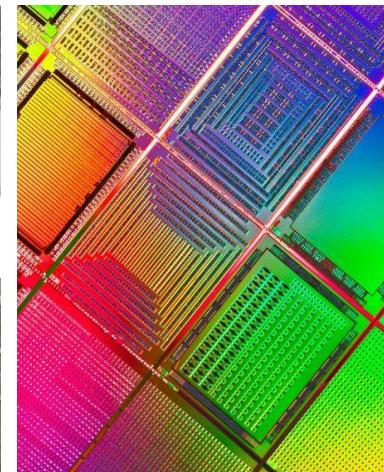
- Unprecedented series of successes which provided us with novel extraordinary experimental tools.
- A revolutionary societal and economic impact:
 - large part of GDP results from quantum technology;
 - no information society without lasers;
 - longer life expectation thanks to NMR;



IBM 2-nanometer (nm) node 2021

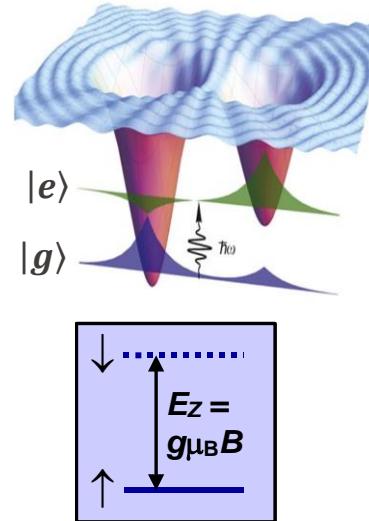
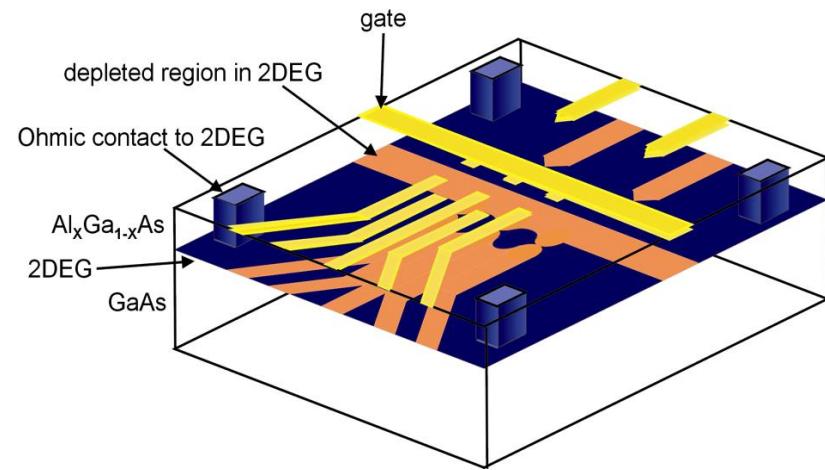


50 billion transistors in a space roughly the size of a fingernail



All-electrical semiconductor quantum dots

How to define Quantum Dots islands?



Confinement

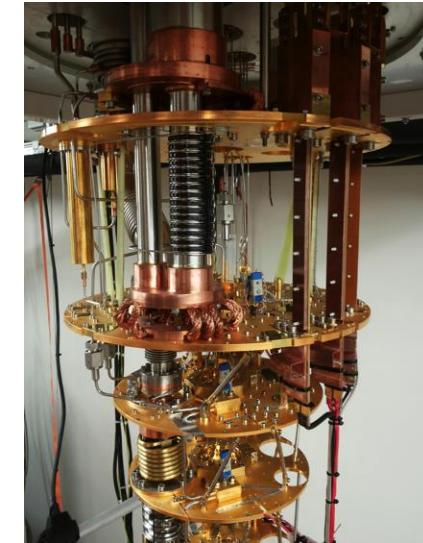
- Discrete # charges
- Discrete orbitals

Electrical control and detection

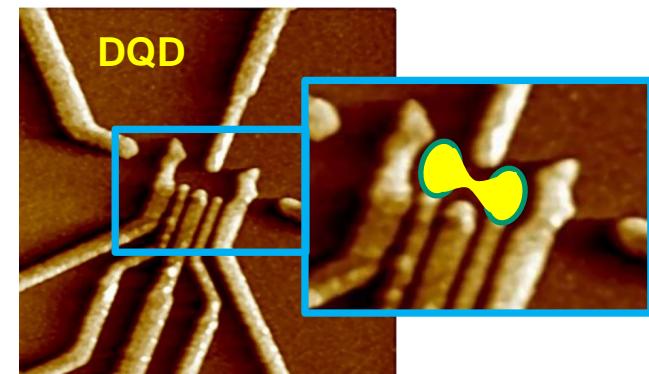
- Tunable # of electrons
- Tunable tunnel barriers

W. G. van der Wiel, et al., *Rev. Mod. Phys.* **75**, 1 (2002)

R. Hanson et al., *Rev. Mod. Phys.* **79**, 1217 (2007)



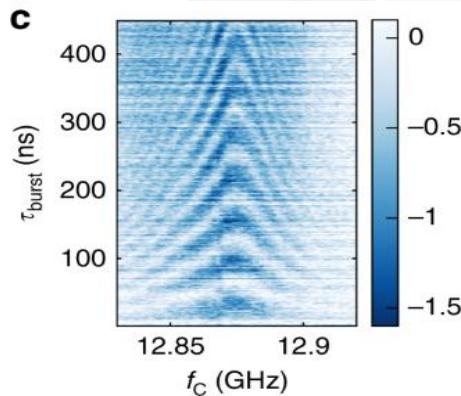
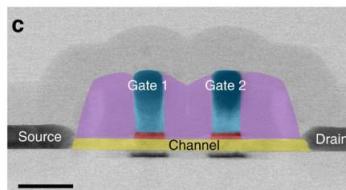
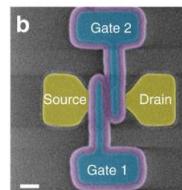
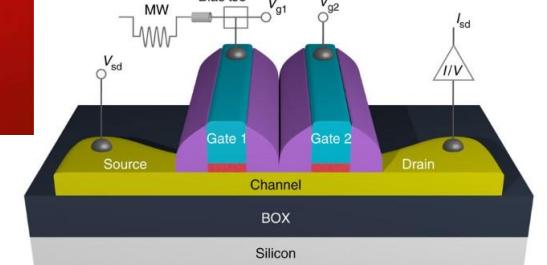
Dilution refrigerator



Leverage CMOS platform to design quantum bits

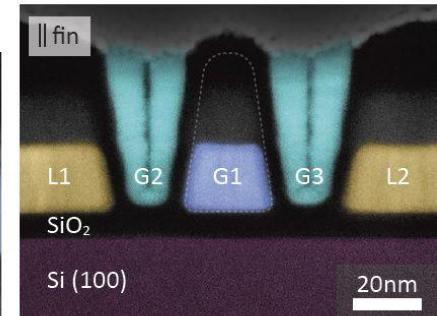
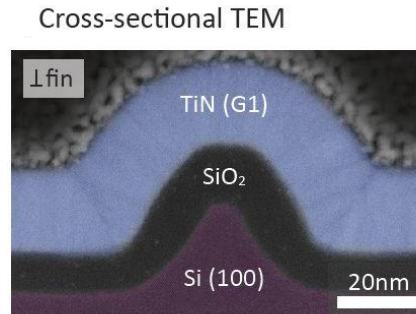


Silicon quantum bit (qubit) devices made with an industry-standard fabrication process

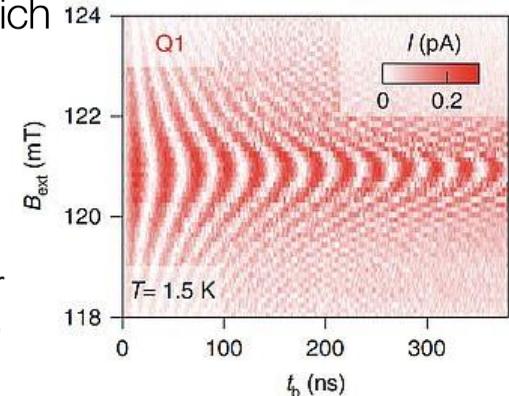


Leveraging the well-established complementary metal–oxide–semiconductor (CMOS) technology would be a clear asset to the development of scalable quantum computing architectures and to their co-integration with classical control hardware.

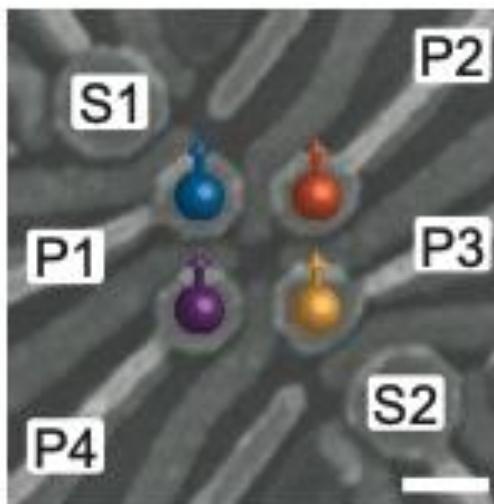
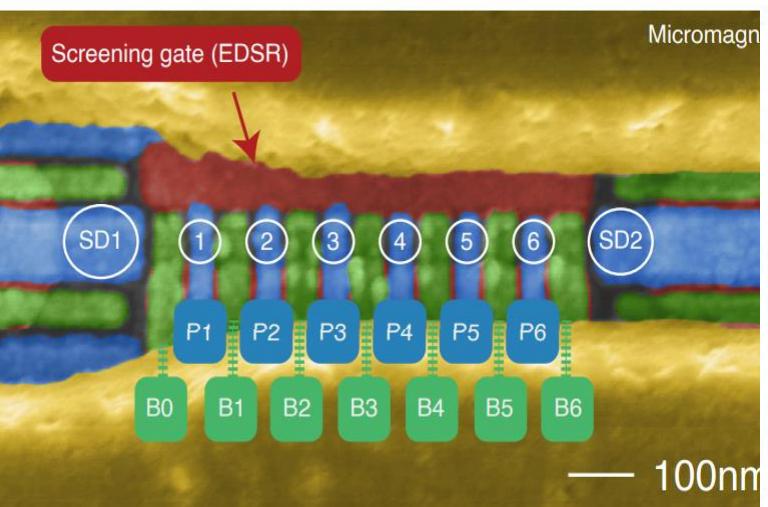
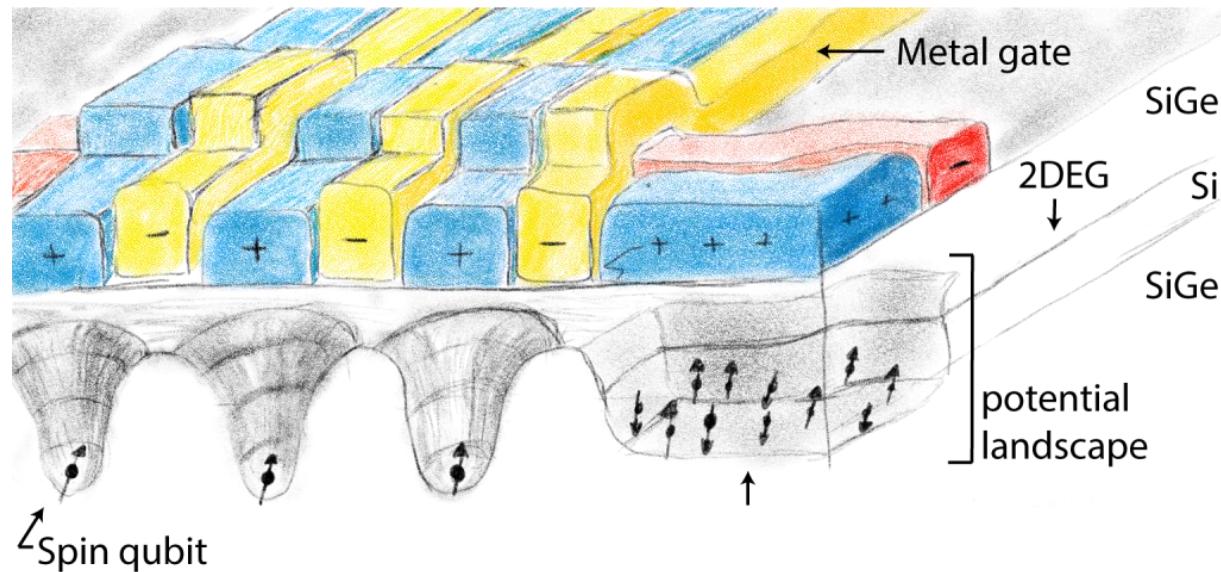
Cross-sectional TEM



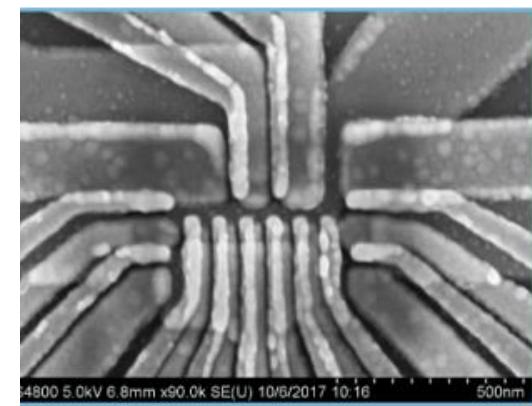
IBM Research | Zurich



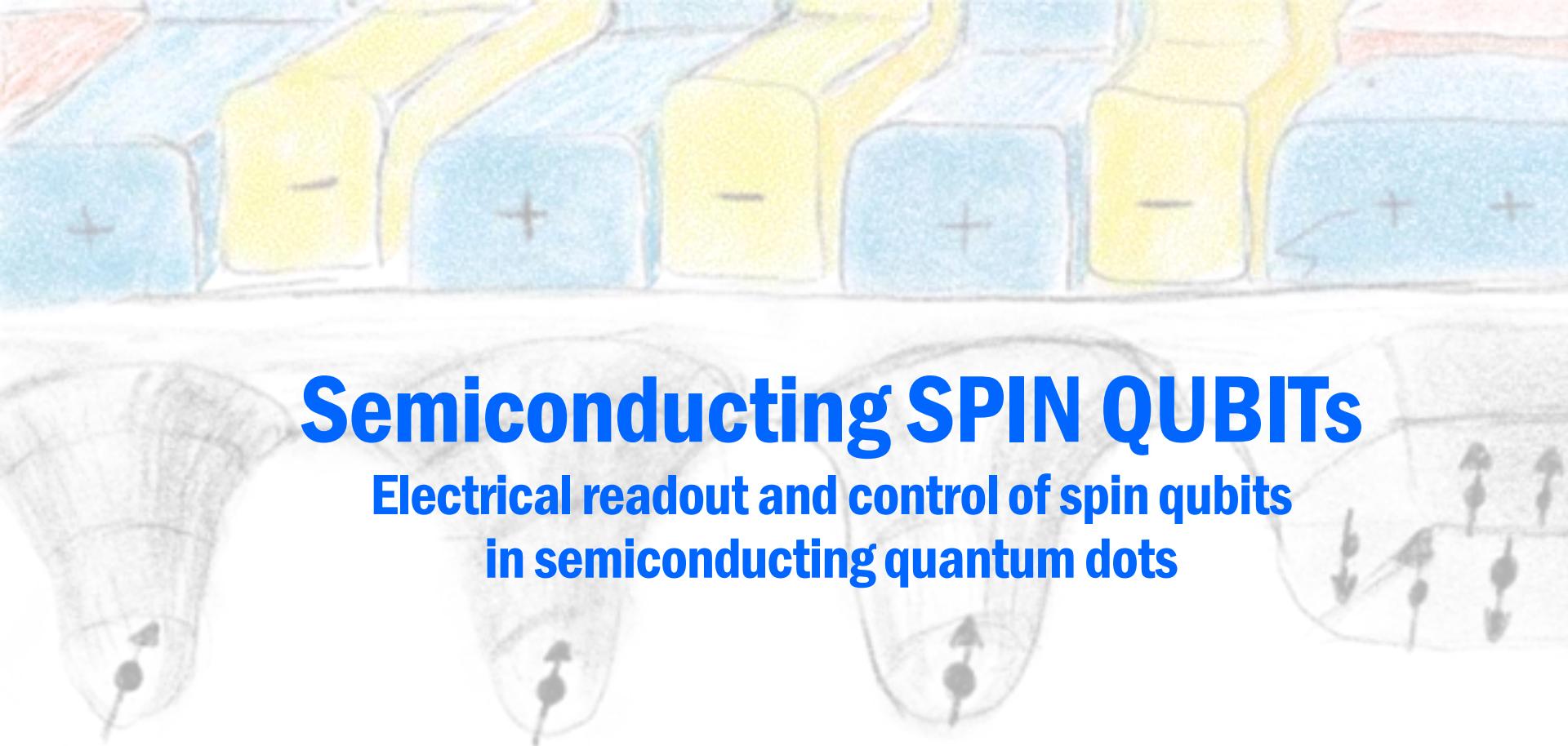
Rabi oscillations of a single spin qubit implemented in a transistor!!!



SEM picture of the metal gates on top of the qubits



<https://blog.qutech.nl/2018/04/20/making-quantum-computers-with-spin-qubits/>



Semiconducting SPIN QUBITS

**Electrical readout and control of spin qubits
in semiconducting quantum dots**

Spin qubit

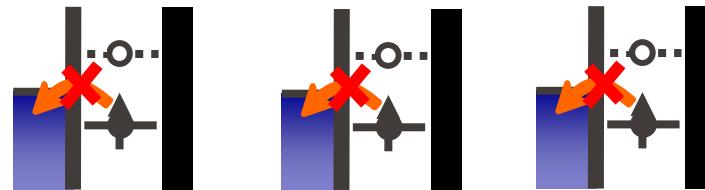
<https://blog.qutech.nl/2018/04/20/making-quantum-computers-with-spin-qubits/>

All-electrical semiconductor quantum dots

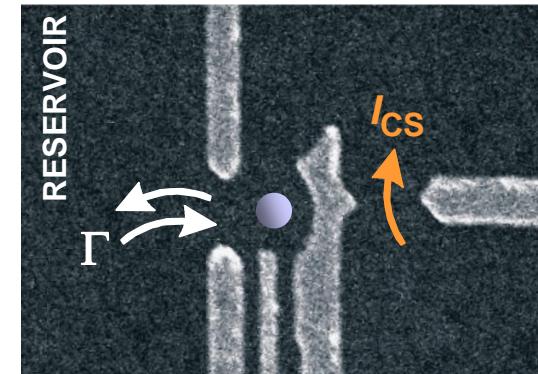
Spin Readout spin-selective tunnelling + charge detection

Spin to charge conversion mechanism

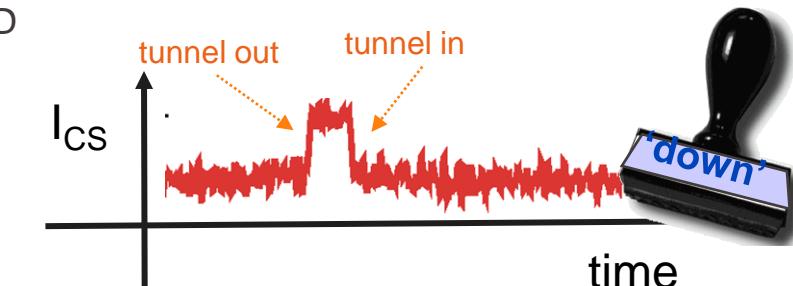
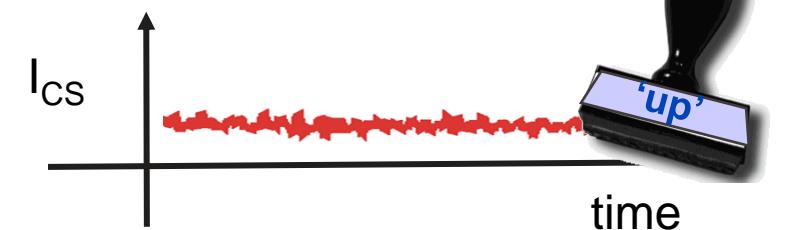
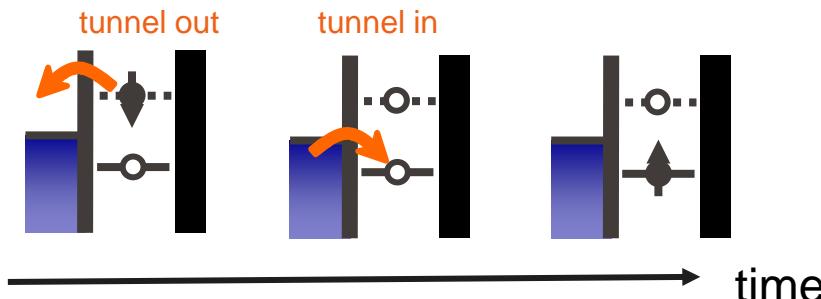
Spin ground state – Electron stays in the QD



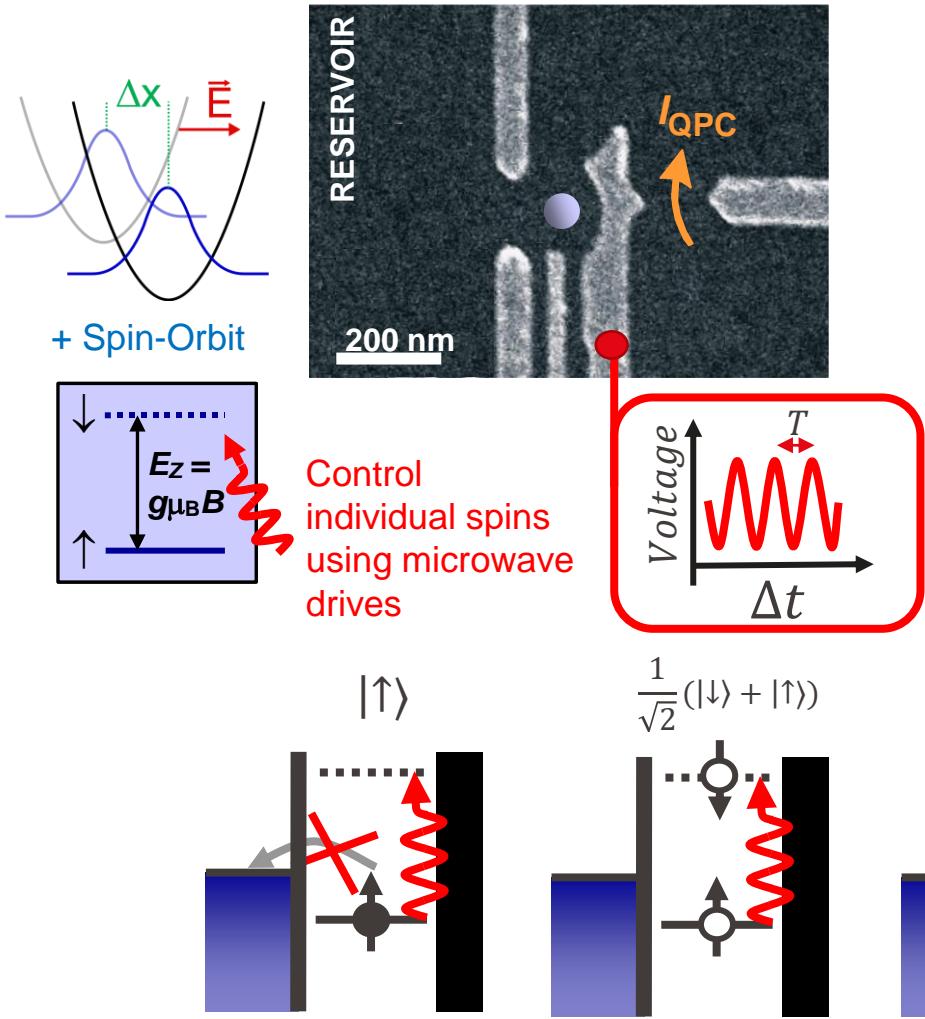
Charge Sensor (CS) responds to changes of charges stored in the QD



Spin excited state – Electron moves out from the QD

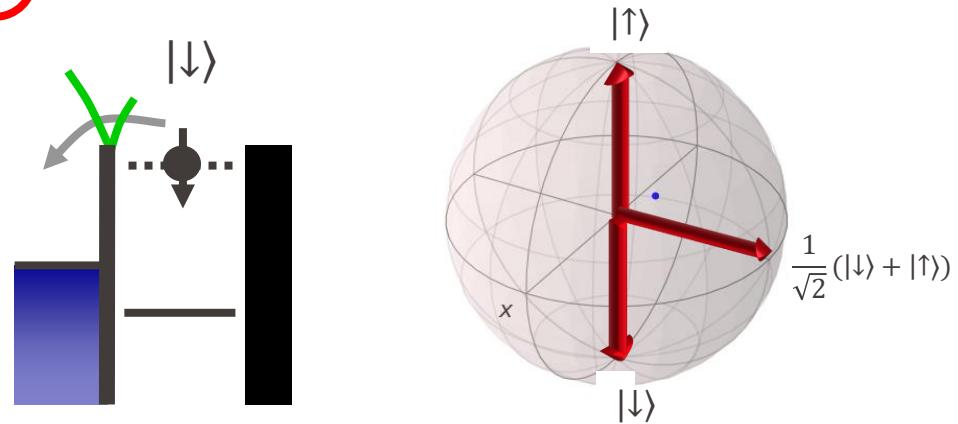
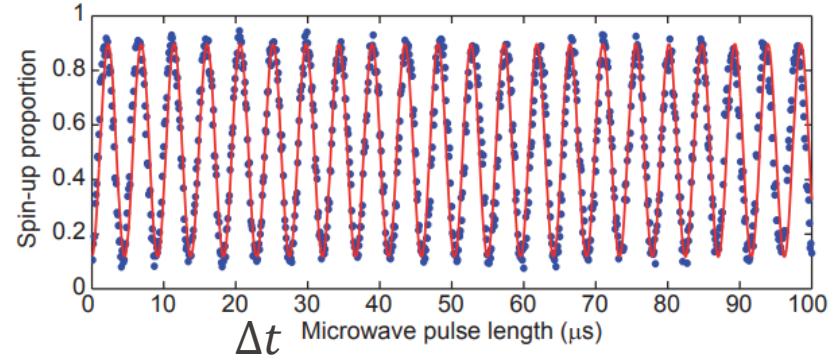


All-electrical semiconductor quantum dots



Single spin operations

EDSR pulsed microwave magnetic field
 $H_{RF} \sim \sum A_i(t) \cos(\omega_i t) \sigma_{xi}$

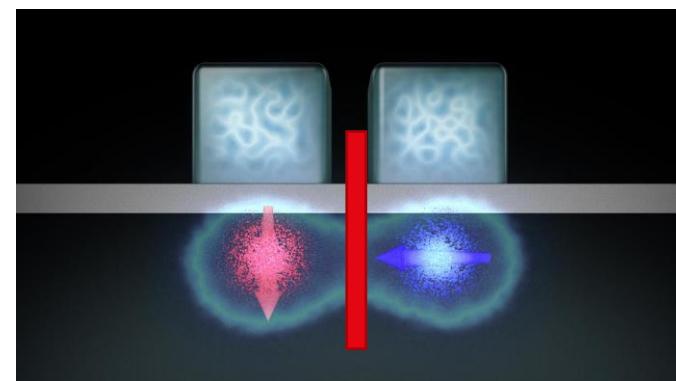
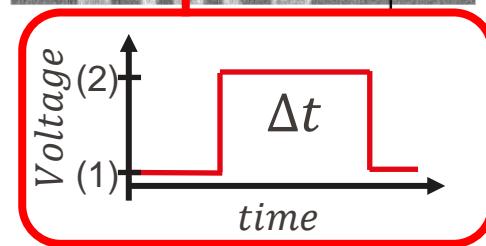
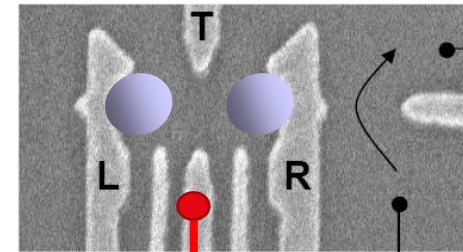
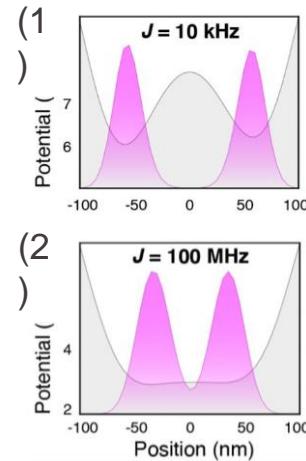
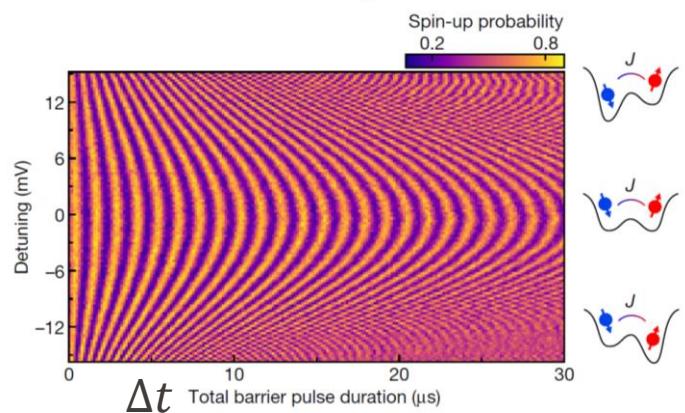
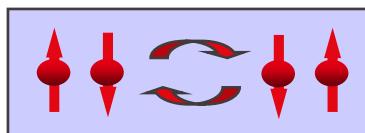


All-electrical semiconductor quantum dots

Two-spins operations

Electrical control of the coupling between neighbouring spins

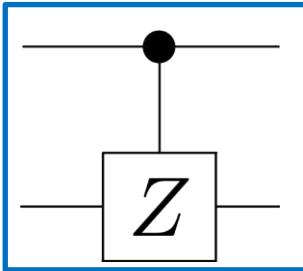
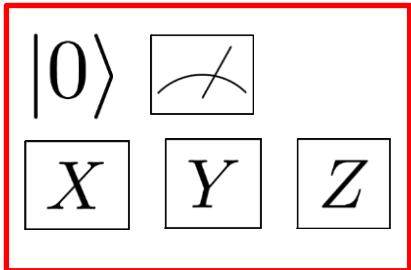
SWAP exchange interaction
 $H_J \sim \sum J_{ij}(t) \sigma_i \cdot \sigma_j$



SPIN-SPIN interaction is SHORT RANGE !
(potential issues for scalability)

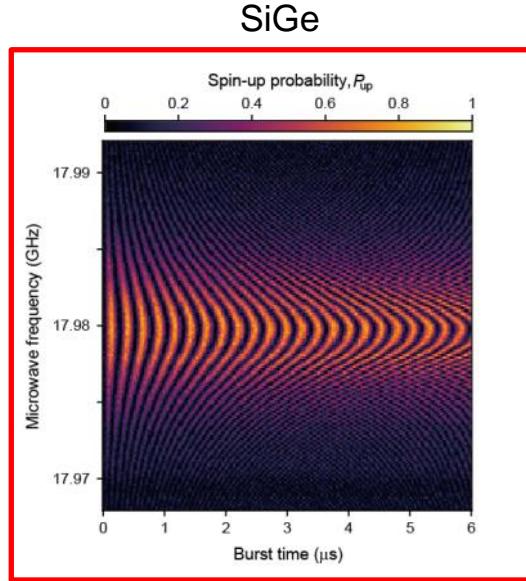
Long Coherence spins in silicon

Single Qubit Gates

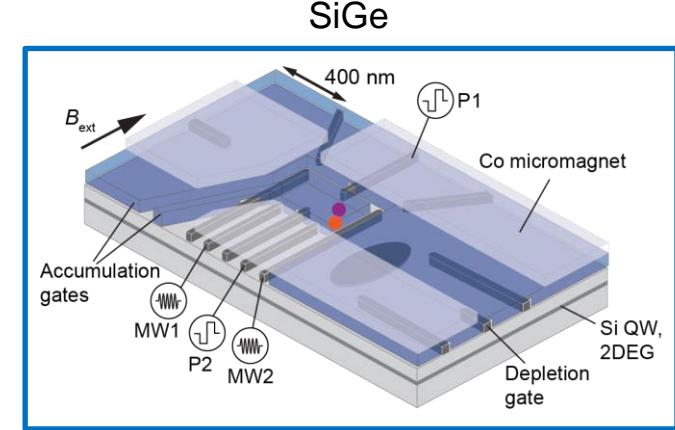


Two Qubits Gates

For electron spin:
 $T_2^* = 200\text{ }\mu\text{s}$
 $T_2 = 28\text{ ms}$
 $T_1 = 100\text{ ms}$ to s
 $F_C = 99.9\%$



Yoneda, et al. *Nat. Nanotech* **13**, 102 (2018)



Watson et al., *Nature* **555**, 633 (2018)

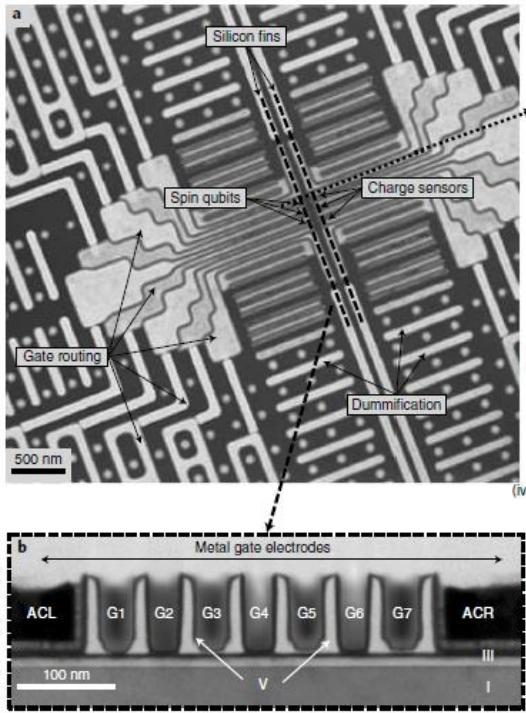
Xiao Xue, et al., *Nature* **601**, 343 (2022)
Computing with spin qubits at the surface code error threshold

'Now that the **99% barrier** for the two-qubit gate fidelity has been surpassed, semiconductor qubits have gained credibility as a leading platform, not only for scaling but also for high-fidelity control.'

State of the art of spin qubits

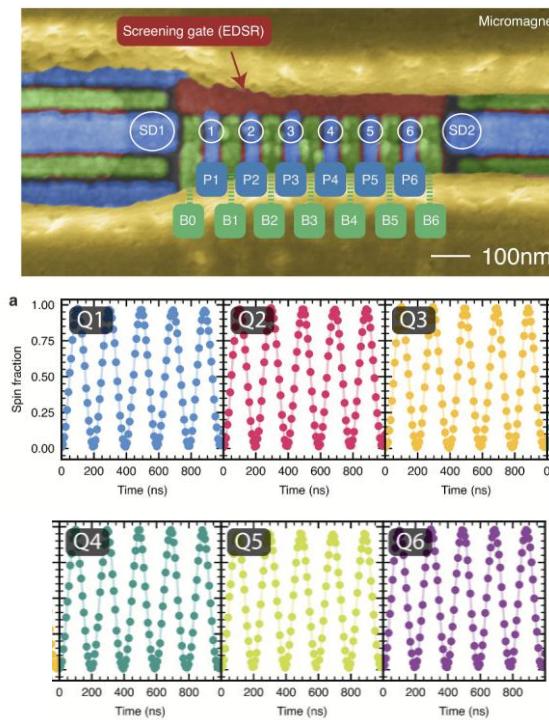
INTEL- TU Delft Qubits made by advanced semiconductor manufacturing

A. M. J. Zwerver, et al., *Nat. Electronics* 5, 184 (2022)



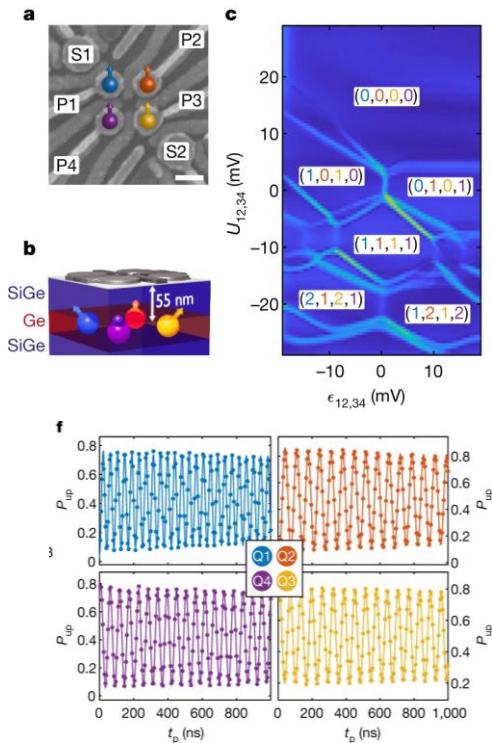
TU Delft Universal control of a six-qubit quantum processor in silicon

S. G.J. Philips, et al., *Nature* 609, 919–924 (2022)



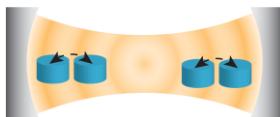
TU Delft A four-qubit germanium quantum processor

N.W. Hendrickx et al., *Nature* 591, 580–585 (2021)



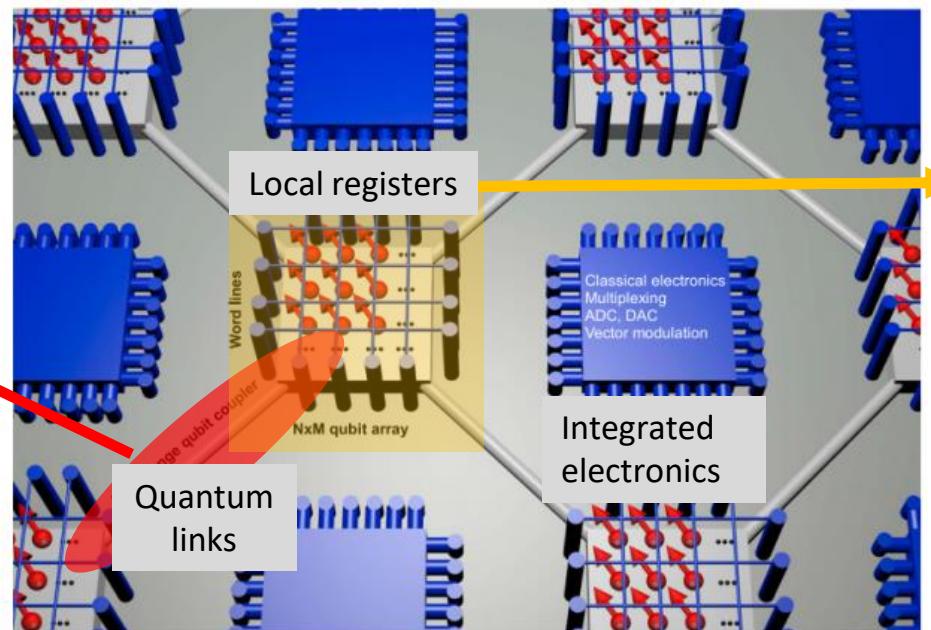
Vision of a scalable spin qubit architecture

**Circuit-QED
approach**



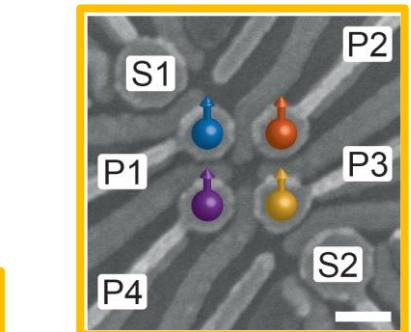
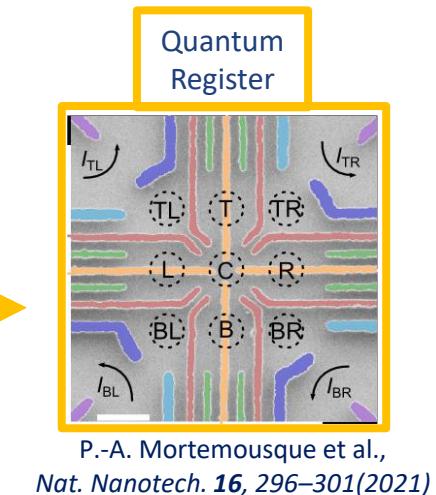
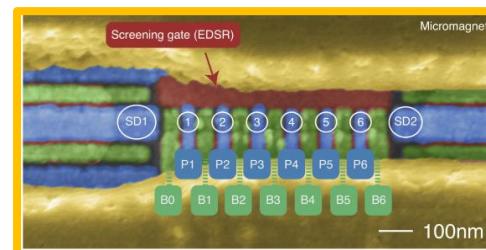
Coherent link ?

To couple distant
spin qubits



Using the strengths of spin qubits:
“Hot, dense and coherent”

L. M. K. Vandersypen et al., *npj Quantum Information* **3**, 34 (2017)

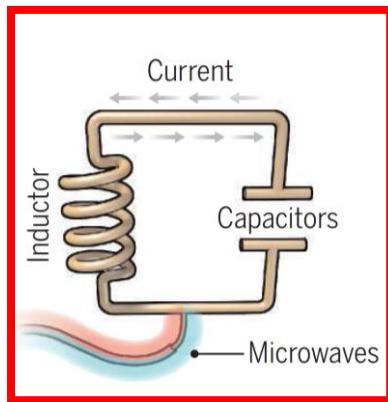


N.W. Hendrickx et al.,
Nature **591** (7851), 580-585

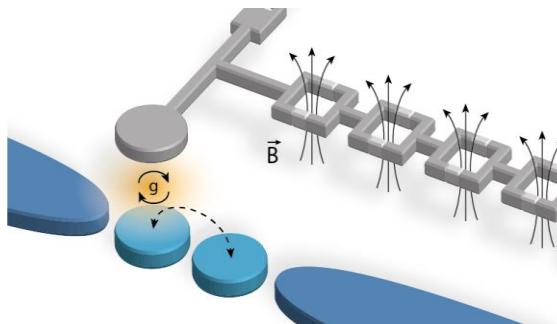
S. G.J. Philips, et al., *Nature* **609**, 919–924 (2022)

Quantum Dot - Cavity Hybrid Technology

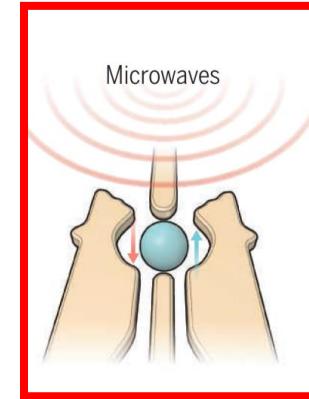
**Building a coherent interface for hybrid technology
via high impedance resonators**



**Superconducting circuits
platform**



Hybrid QD-resonator devices



**Semiconductor
QDs platform**

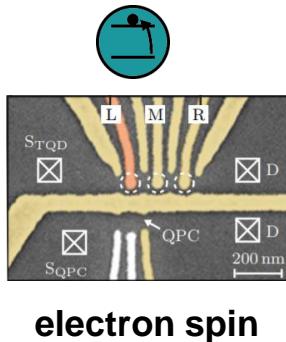
While both superconducting and semiconducting platforms have strong potential for **quantum technology** on their own, we will explore novel opportunities emerging at the interface between the two hardware.

For investigating light-matter interaction **at the fundamental level** and
implementing a rich set of novel applications in **quantum information technology**

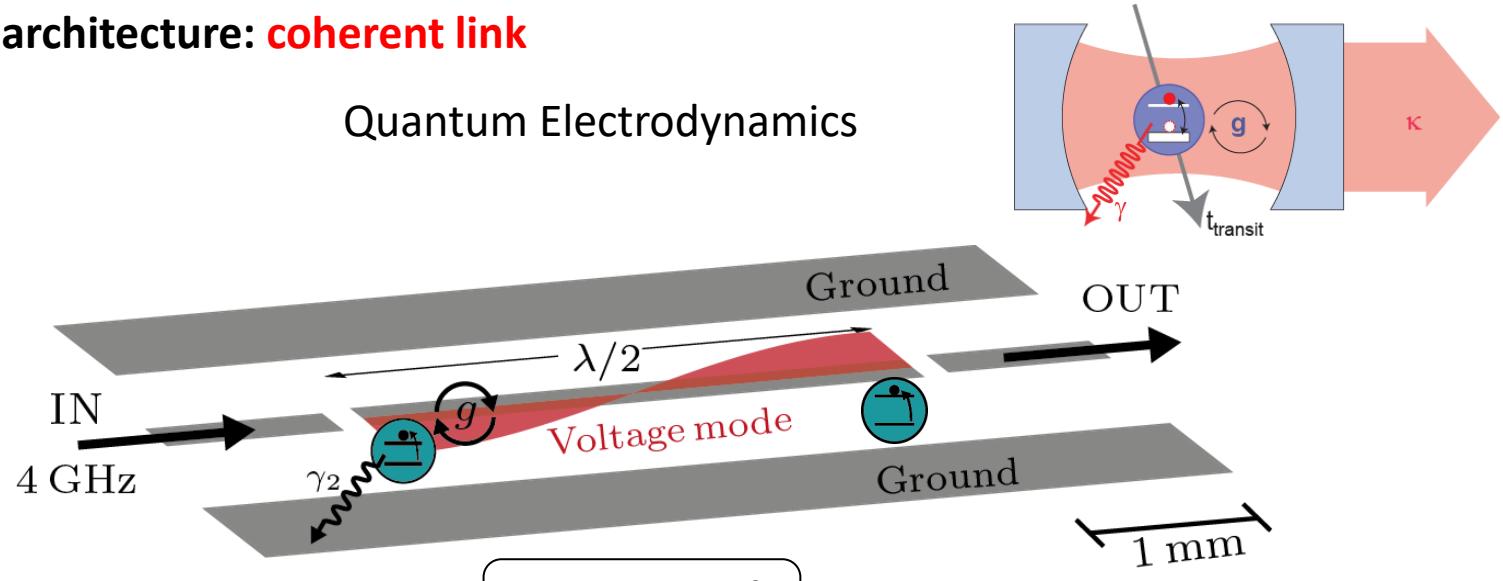
Quantum Dot - Cavity Hybrid Technology

Circuit QED architecture: **coherent link**

Quantum Electrodynamics



electron spin



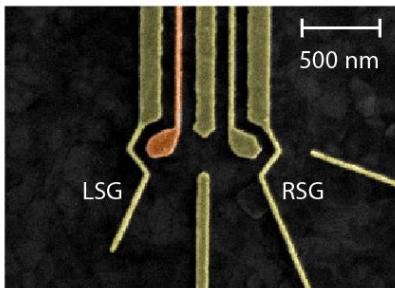
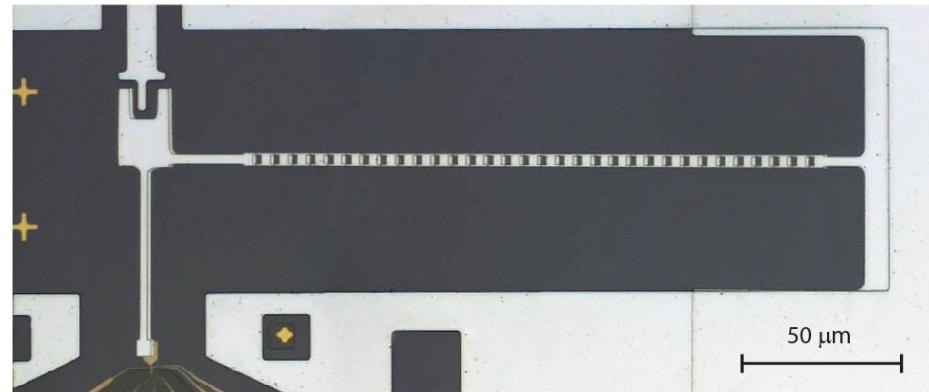
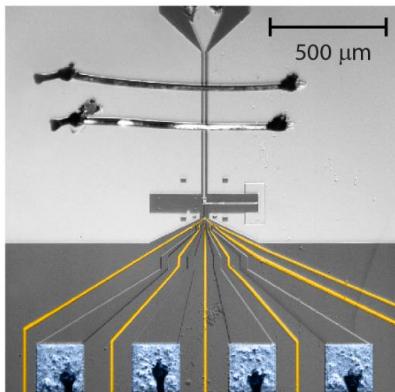
Blais *et al.*, Phys Rev A **69**, 062320 (2004)
Wallraff *et al.*, Nature **431**, 162 (2004)
Schoelkopf & Girvin, Nature **451**, 664 (2008)

Raimond *et al.*, Rev Mod Phys **73**, 565 (2001)
Haroche & Raimond, OUP Oxford (2006)
Ye *et al.*, Science **320**, 1734 (2008)

Interaction of distant qubits
Strong coupling of the qubit to a quantum information mediator (photon)

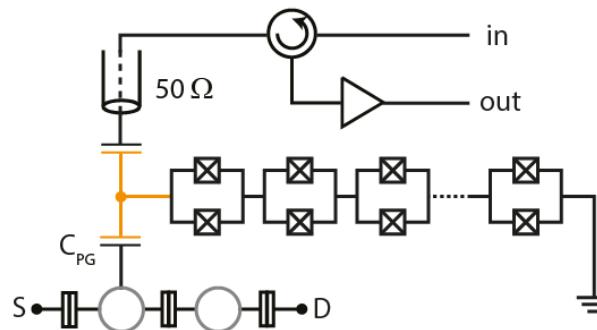
Quantum Dot - Cavity Hybrid Technology

Integrated GaAs DQD with SQUID Array Resonator in Hybrid Device



Gate defined GaAs DQD

- On small mesa
- Resonator coupling gate not DC biased



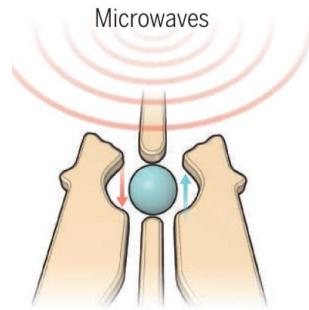
- 32 SQUID array resonator**
- 200 μm long
 - Al based
 - Dolan bridge technique

$$\begin{aligned}L_r &\sim 40 \text{ nH} \\C_r &\sim 15 \text{ fF} \\Z_r &\sim 1.5 \text{ k}\Omega \\f_r &\sim 6 \text{ GHz}\end{aligned}$$

Microwave reflectometry measurement

- Josephson parametric amplifier
- Custom FPGA electronics

Stockklauser*, Scarlino* et al., PRX 7, 011030 (2017)



SPIN Qubits in Quantum dots

Covering: basic concepts, measurement techniques,
implementations, qubit approaches, current trends

With figures and slides borrowed from
L. Vandersypen, J. Elzerman, R. Hanson, L. Kouwenhoven, M. Veldhorst (TU Delft)

Quantum dot

- A small semiconducting island where electrons are confined
 - discrete number of electrons
 - discrete energy level spacing
- Behavior in many ways similar to that of atoms
 - “artificial atoms”, with properties that can be engineered and controlled

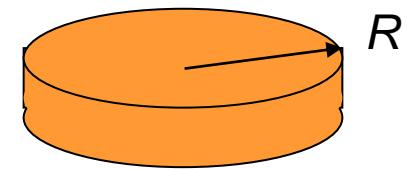
Energy scales

single electron charging energy: $E_C = e^2/C$

$$(C=8\epsilon_r\epsilon_0 R, \text{ disk})$$

$$R = 1 \text{ nm} \quad E_C = 0.3 \text{ eV} \Rightarrow \text{room temp.}$$

$$R = 100 \text{ nm} \quad E_C = 3 \text{ meV} \Rightarrow \text{low temp.}$$



confinement energy level spacing ΔE :

$$R = 1 \text{ nm} \quad E_j = 10 \text{ eV}$$

$$R = 100 \text{ nm} \quad E_j = 1 \text{ meV}$$

a particle trapped in
a cavity of radius R

$$E_j = h^2/8mR^2$$

thermal energy

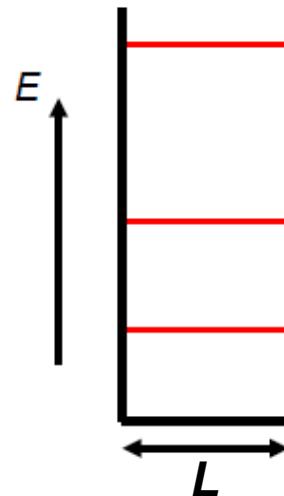
$$T = 300 \text{ K} \quad kT \sim 26 \text{ meV}$$

$$T = 4.2 \text{ K} \quad kT \sim 0.35 \text{ meV}$$

$$T = 30 \text{ mK} \quad kT \sim 2.6 \mu\text{eV}$$

Atoms vs. Quantum Dots

Schrödinger:
electrons in confined systems occupy quantized energy levels



Particle in a box:

$$E_n = \frac{\hbar^2}{2m} \left(\frac{\pi n}{L} \right)^2, \quad n = 1, 2, 3 \dots$$

QDs: 0.1 meV
Atoms: 10 eV

Pauli:
each level can be occupied with one spin-up electron and one spin-down electron

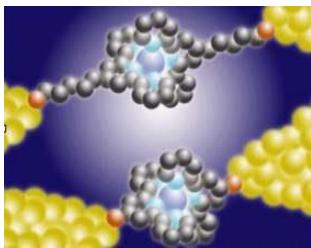
	Atom	Quantum dot
Confinement	r^1 , strong, rigid, hard to tune	r^2 , soft, parabolic, tunable
Symmetry	perfect, given by nature	never perfect, hard to achieve
Electrical addressing	hard to achieve	well suitable tunable coupling
Optical addressing	well suitable	well suitable
Coupling to	thermal photons, ...	photons, phonons, other electrons

Both systems give access to single electron/spin manipulation

Examples of quantum dots

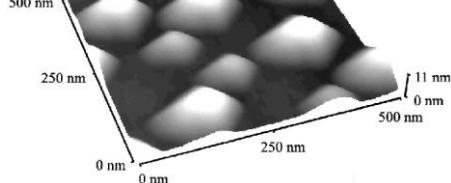
Electrostatically
defined QD in
semiconductors

single molecule



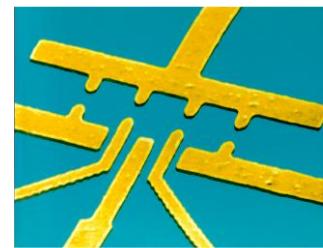
1 nm

self-assembled
QD



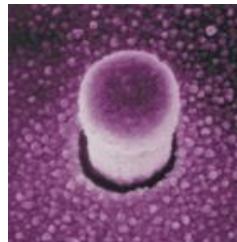
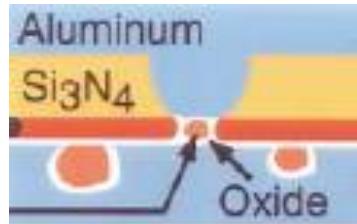
10 nm

lateral QD

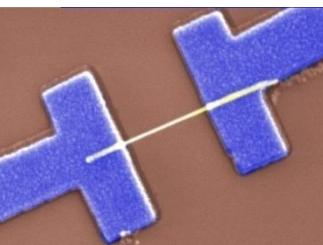


1 μm

metallic
nanoparticle

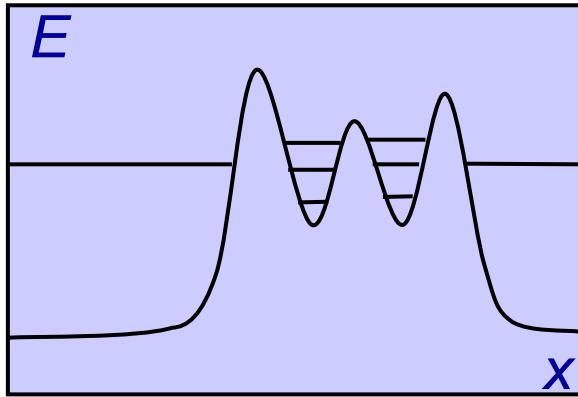


vertical QD

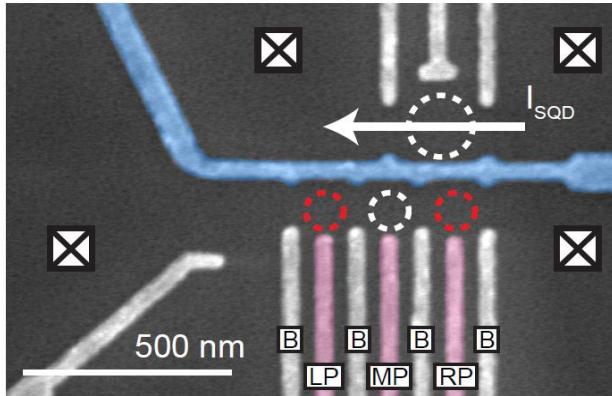


nanowire

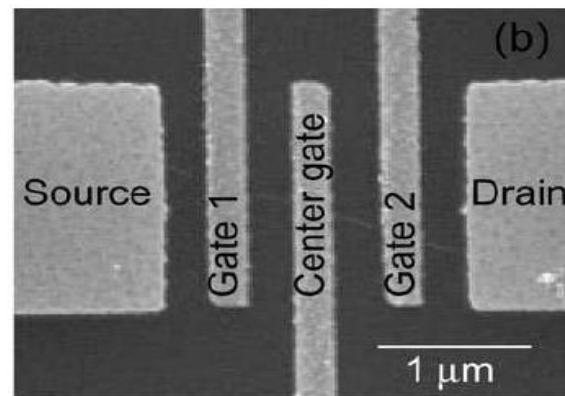
Quantum dots – electrostatically defined



2D electron gas

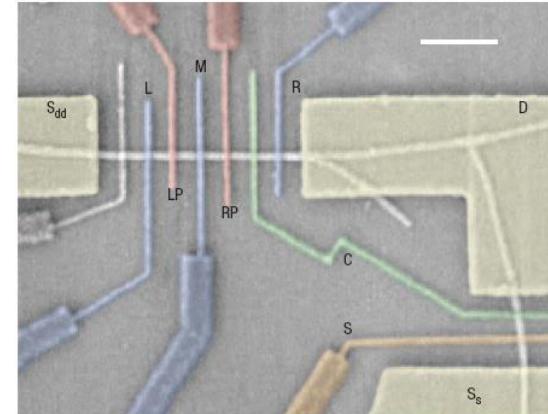


nanotube



© Schoenenberger

nanowire



© Marcus

Quantum computation with quantum dots

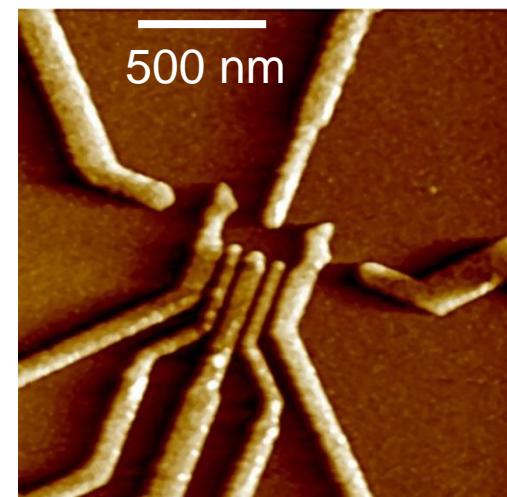
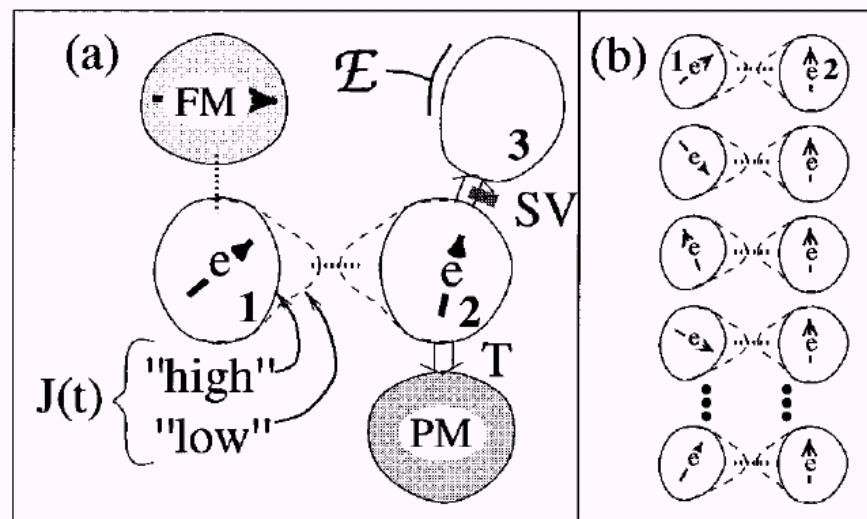
Daniel Loss^{1,2,*} and David P. DiVincenzo^{1,3,†}

¹*Institute for Theoretical Physics, University of California, Santa Barbara, Santa Barbara, California 93106-4030*

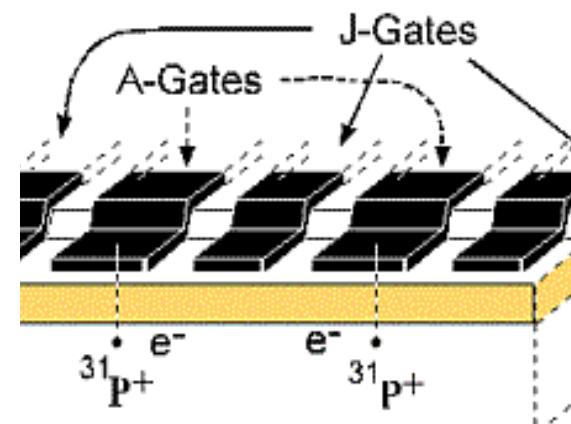
²*Department of Physics and Astronomy, University of Basel, Klingelbergstrasse 82, 4056 Basel, Switzerland*

³*IBM Research Division, T.J. Watson Research Center, P.O. Box 218, Yorktown Heights, New York 10598*

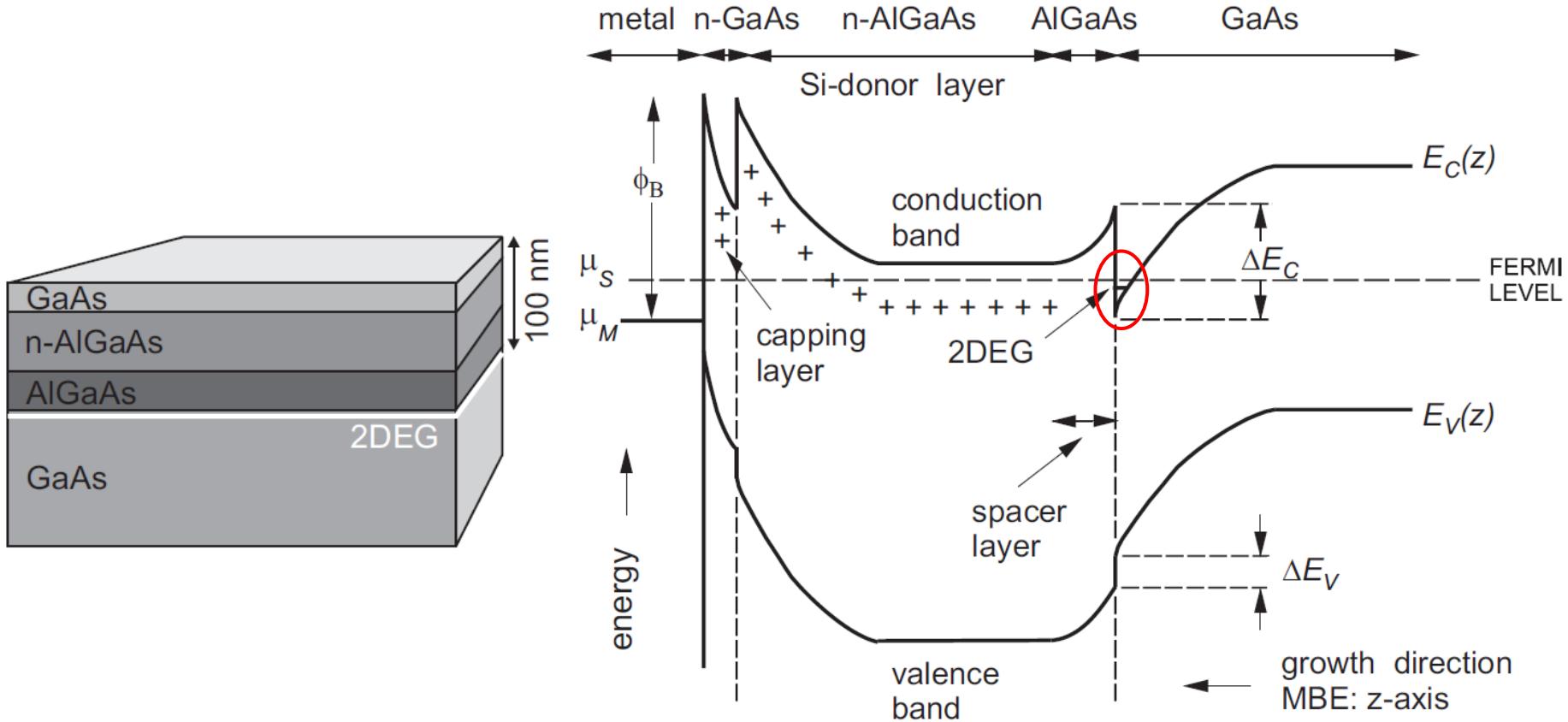
(Received 9 January 1997; revised manuscript received 22 July 1997)



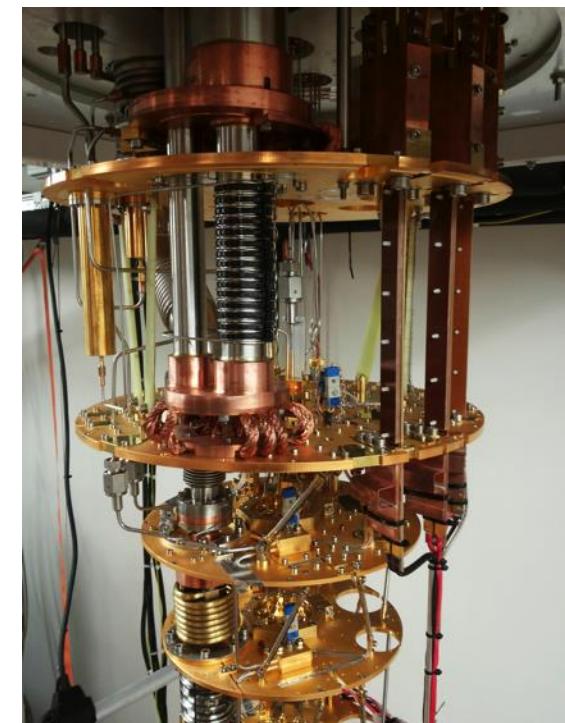
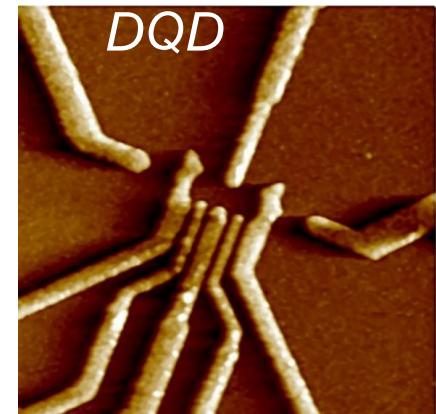
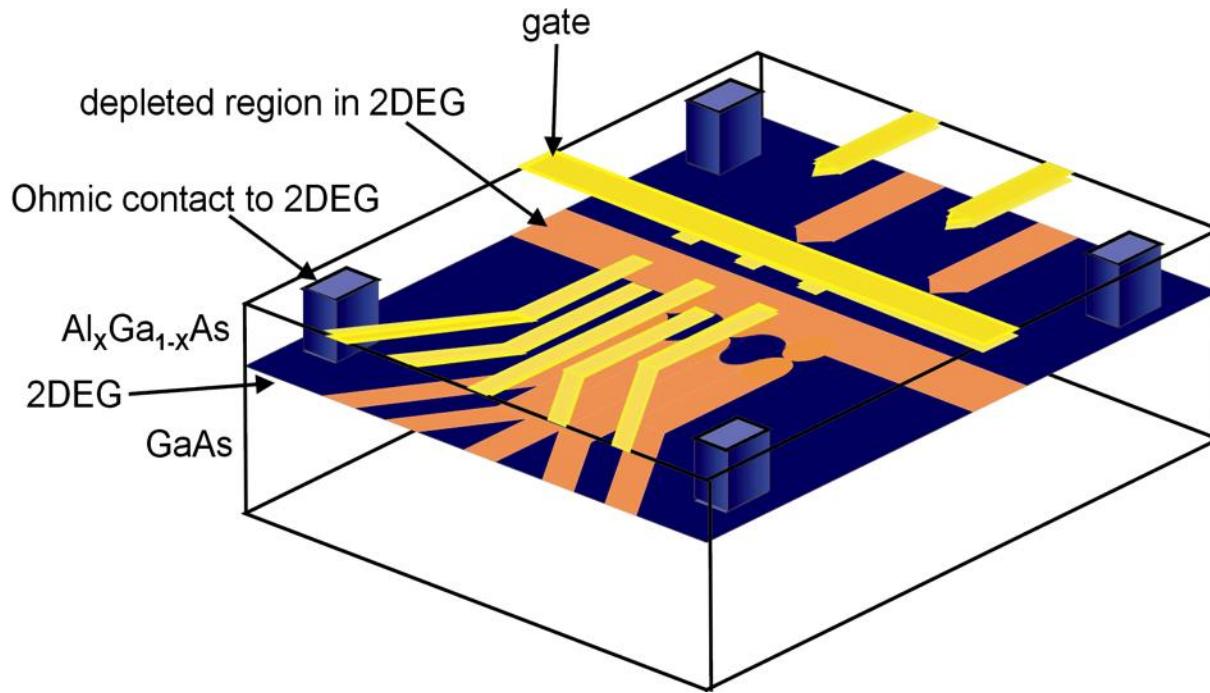
A Silicon-based Nuclear Spin Quantum Computer
B. E. Kane, Nature 393, 133 (1998).



Main implementations so far: Electrons in GaAs/AlGaAs or Si-based materials



Quantum dots: hosts for electron spin qubits

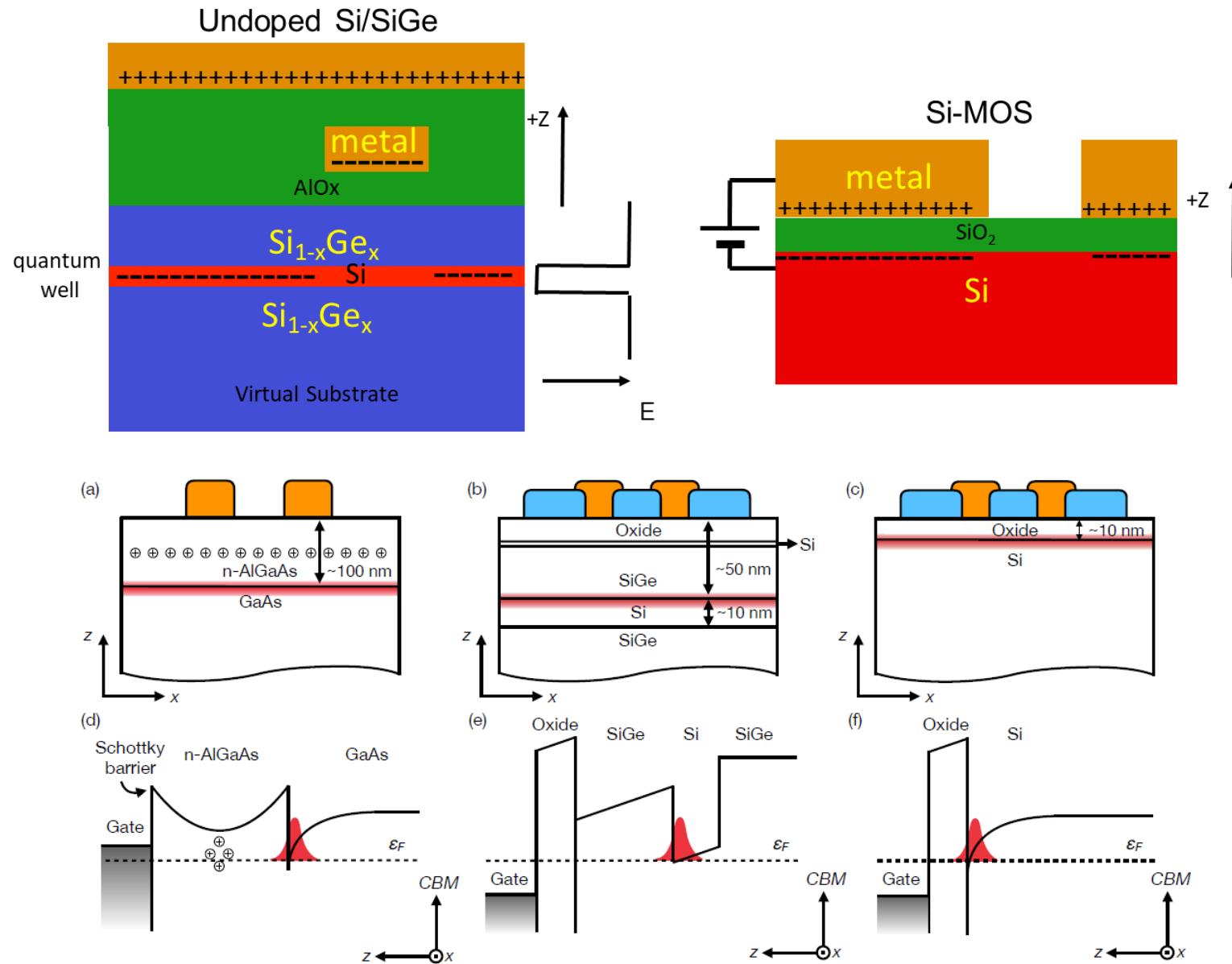


Discrete # charges, quantized orbitals

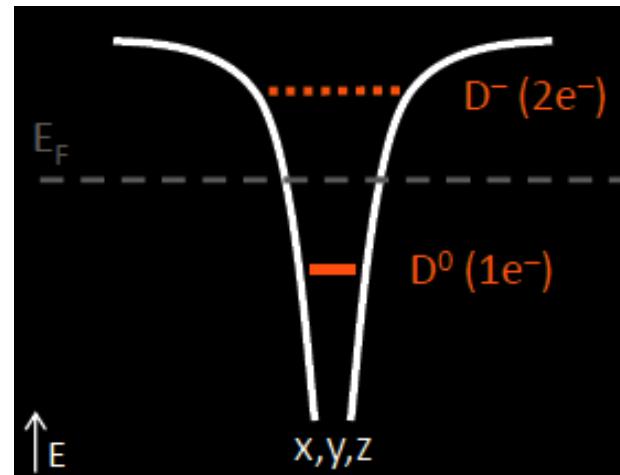
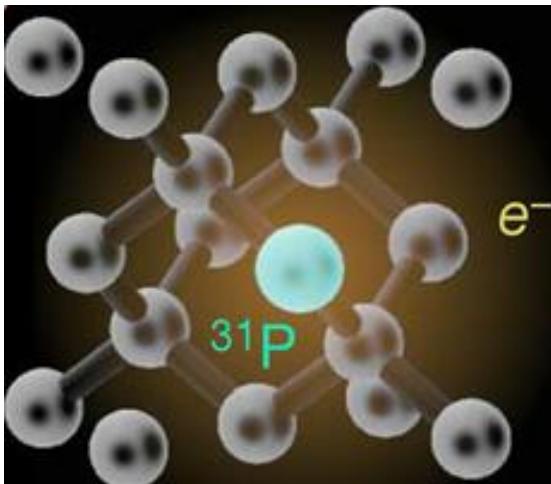
Electrical control and detection

- Tunable # of electrons
- Tunable tunnel barriers
- Electrical contacts

Accumulation versus depletion mode



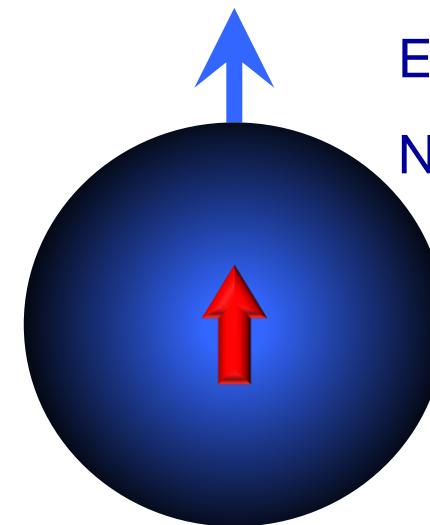
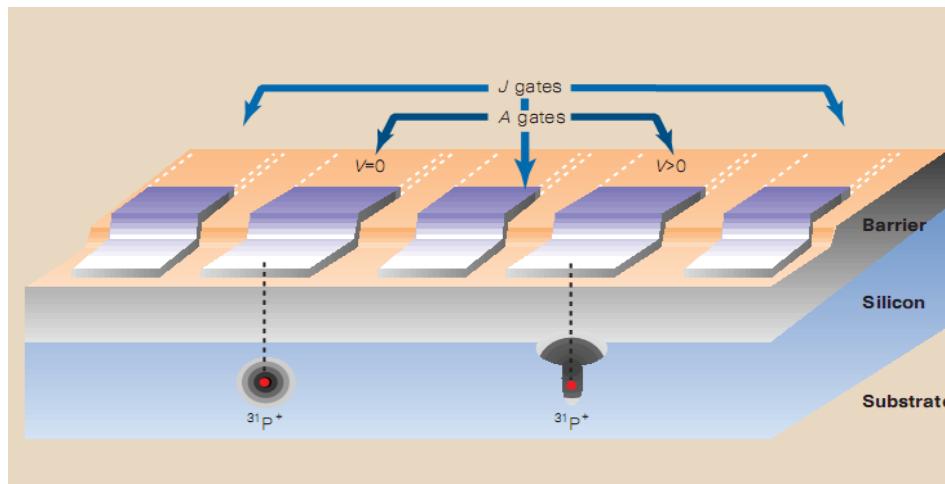
Donors – ^{31}P in Si



Loosely bound 15th electron of P

Bohr radius ~ 2.5 nm

Coulomb binding potential

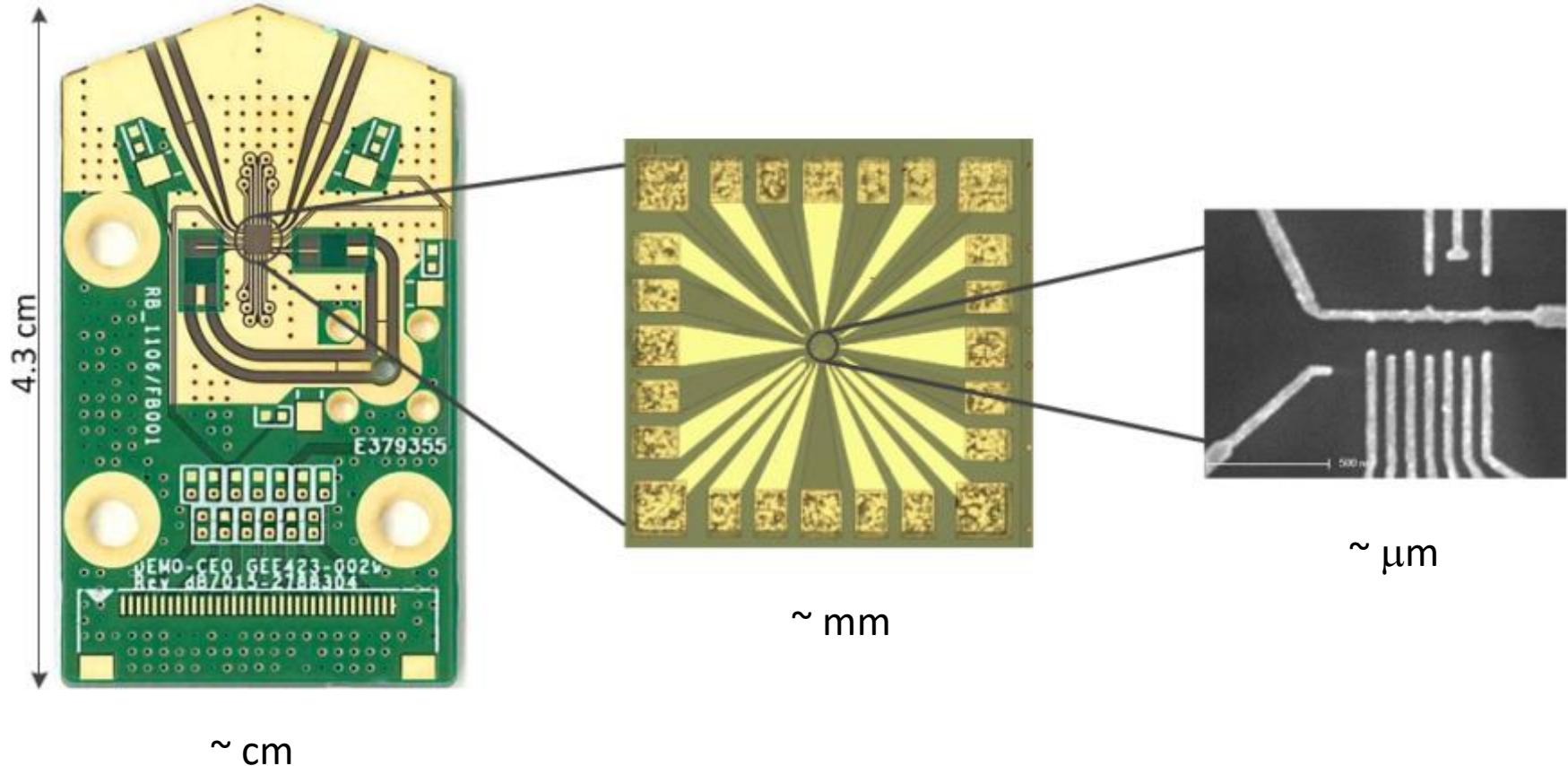


Electron spin $\frac{1}{2}$
Nuclear spin $1/2$

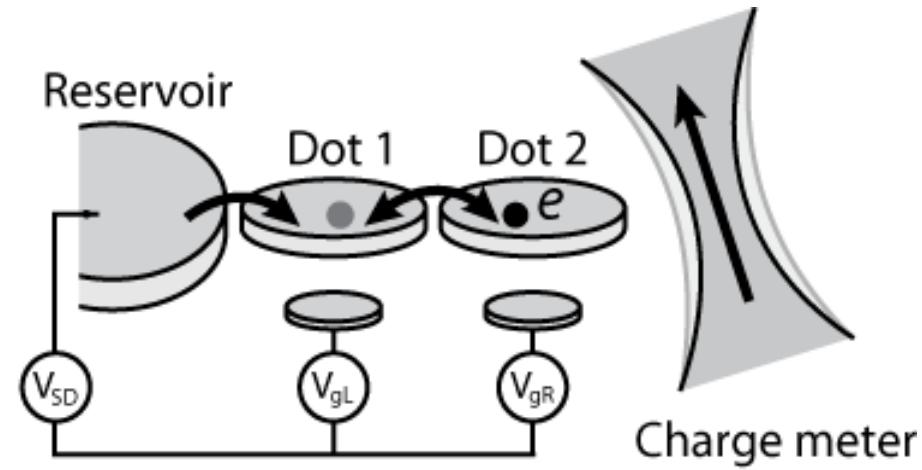
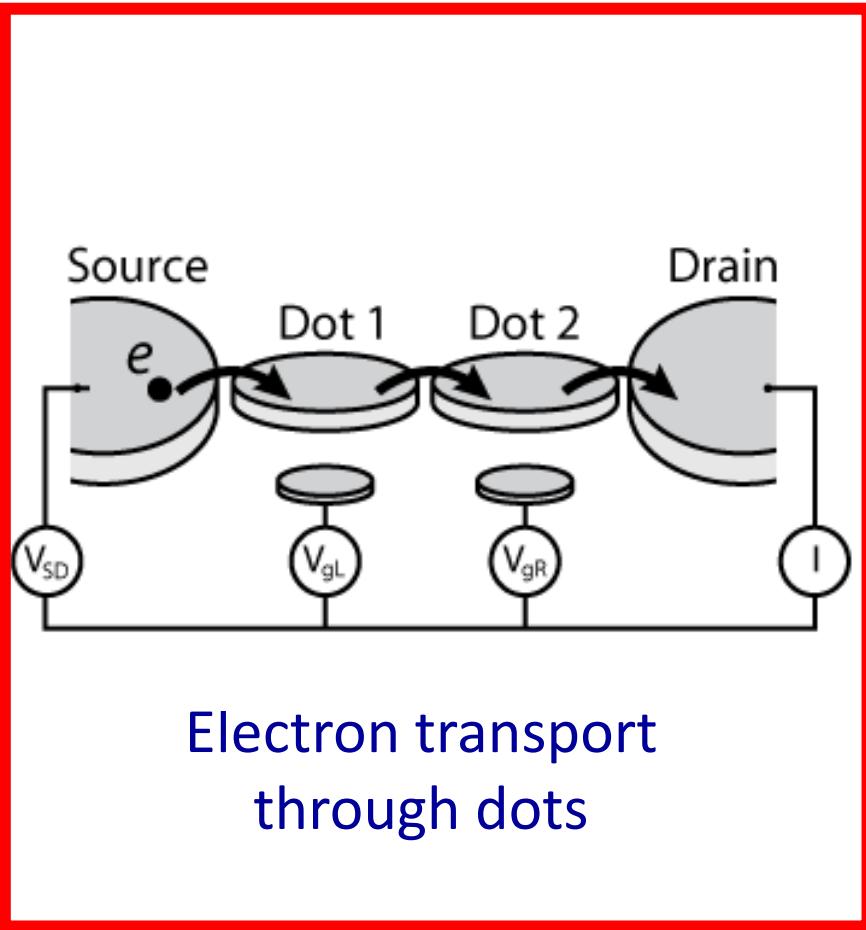
B. Kane, Nature 393, 133 (1998)

Images taken from A. Morello

Typical devices

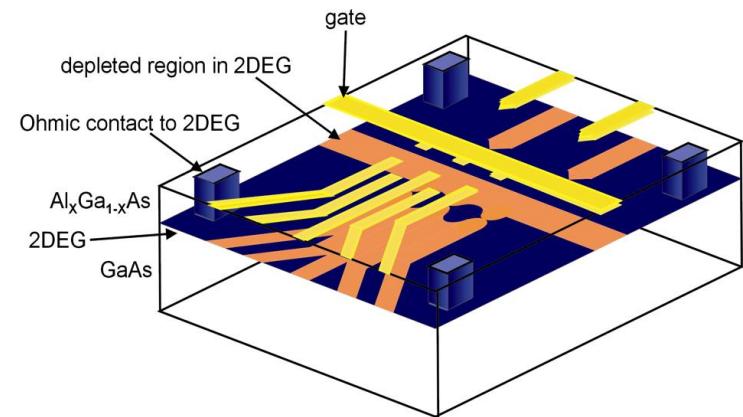
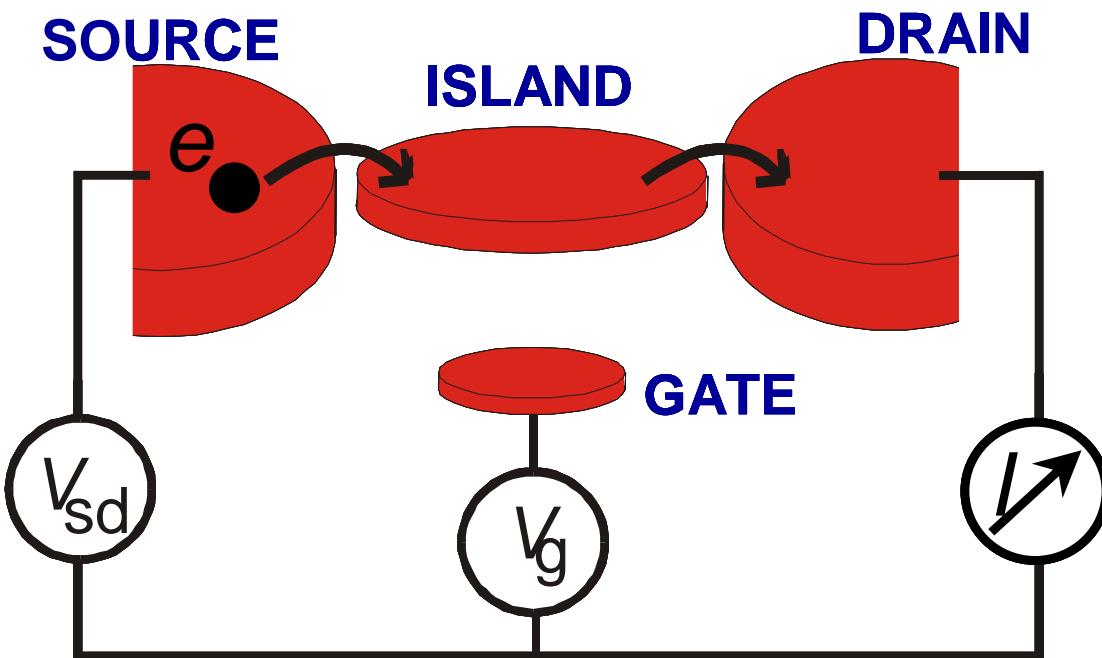


Electrical measurement of quantum dots



Electron transport
through QPC

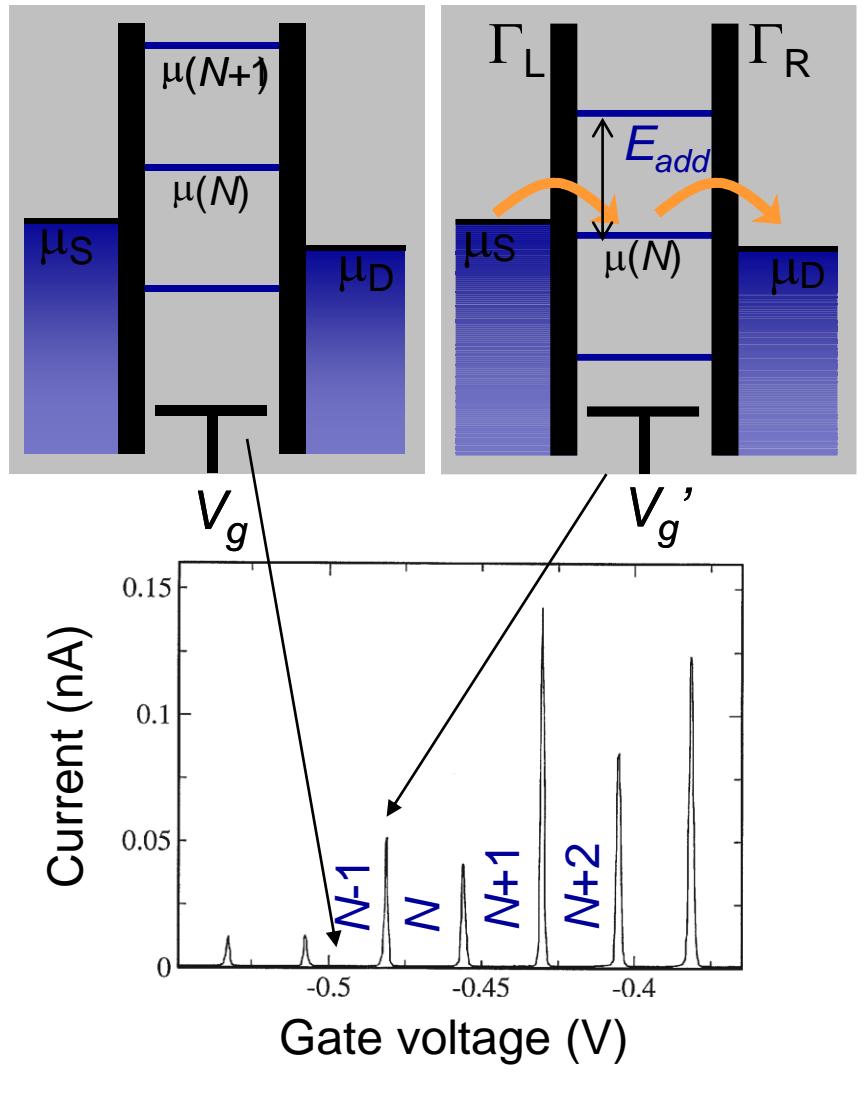
Electrically controlled quantum dots



- Coupled via tunnel barriers to source and drain reservoirs
- Coupled capacitively to gate electrode(s)

Single electron tunneling

Linear response



$\mu(N)$ electrochemical potential,

Energy an electron needs to have
in order to enter the dot

$$\mu(N) = U(N) - U(N-1)$$

with $U(N)$ total energy

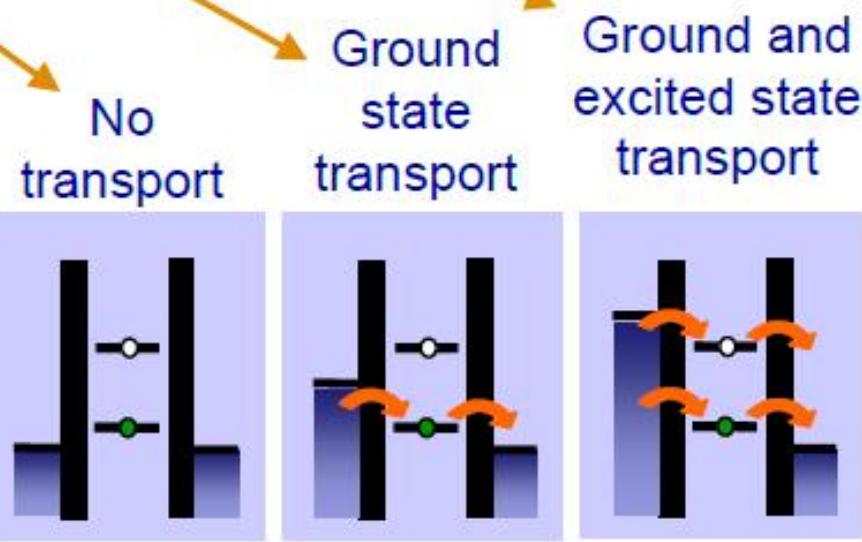
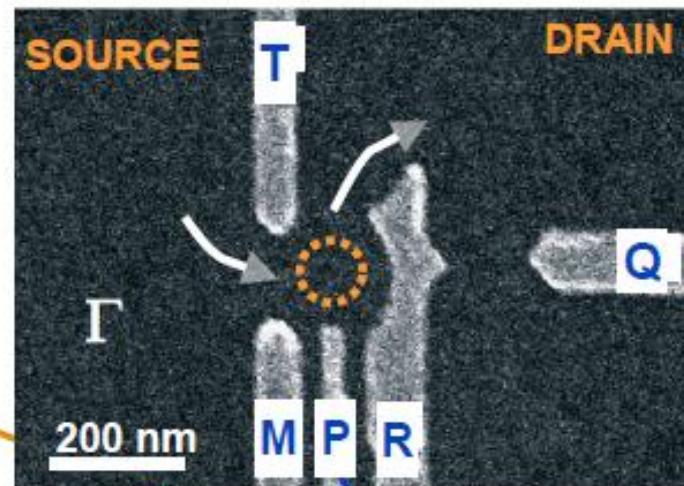
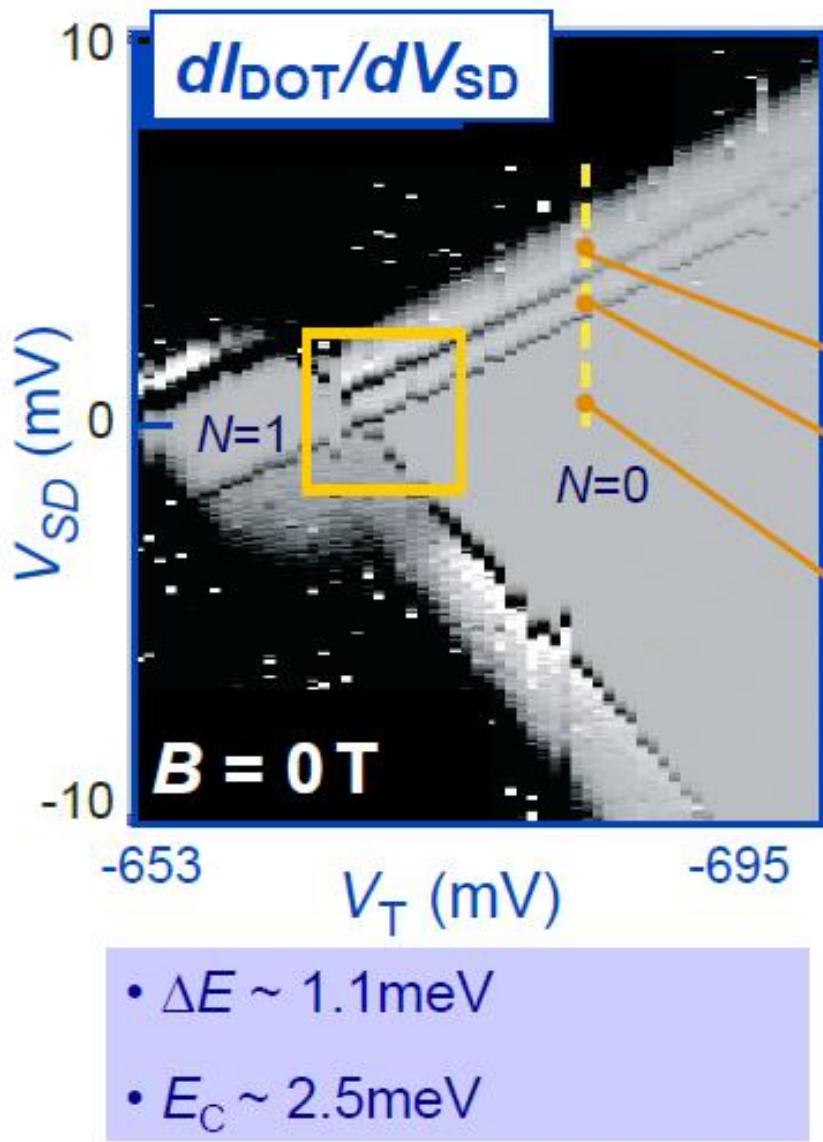
E_{add} extra energy needed to add
one electron

$$E_{add} = \mu(N+1) - \mu(N)$$

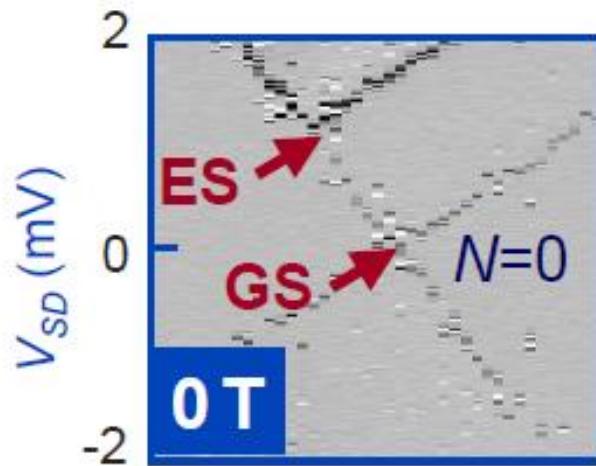
$$E_{add} = E_c + \Delta E$$

↑
Charging energy Confinement energy

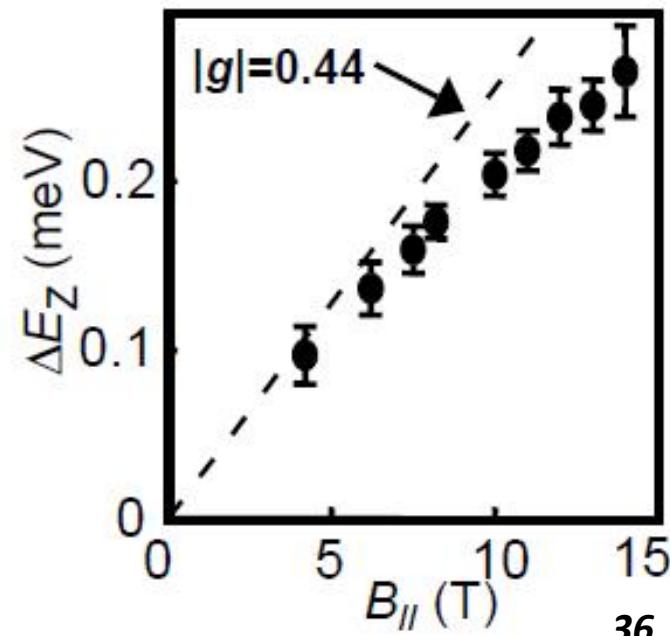
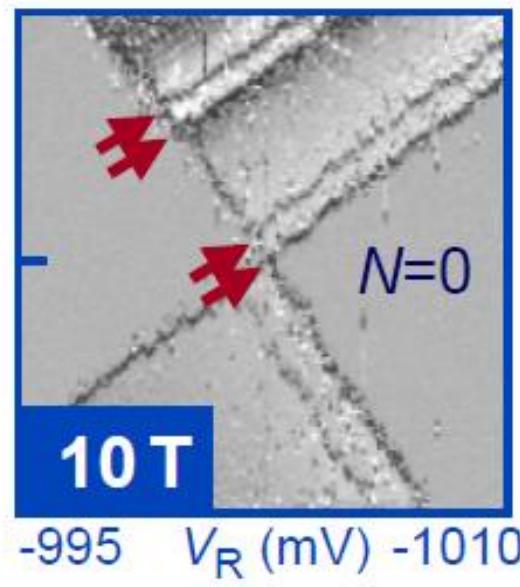
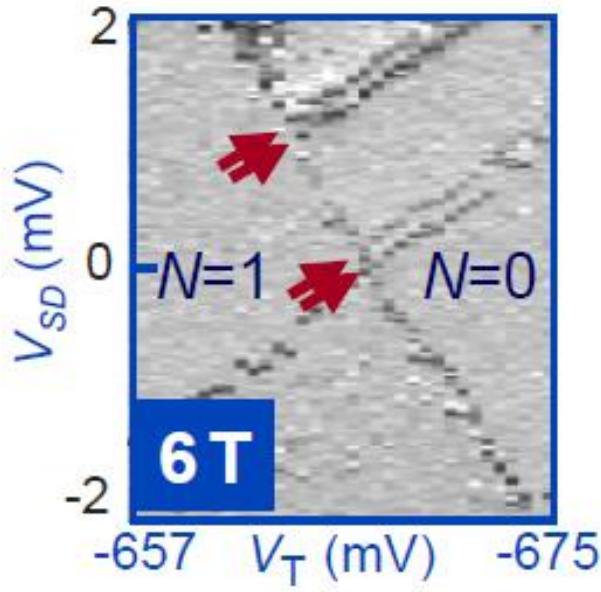
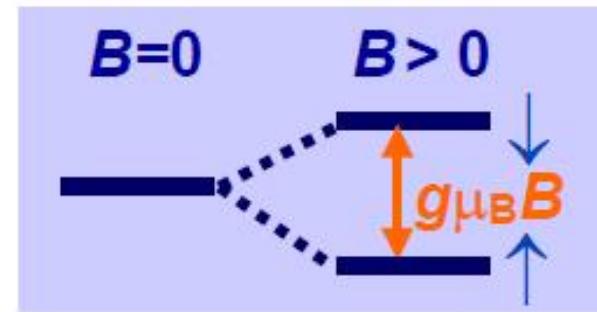
Energy level spectroscopy at $B=0$



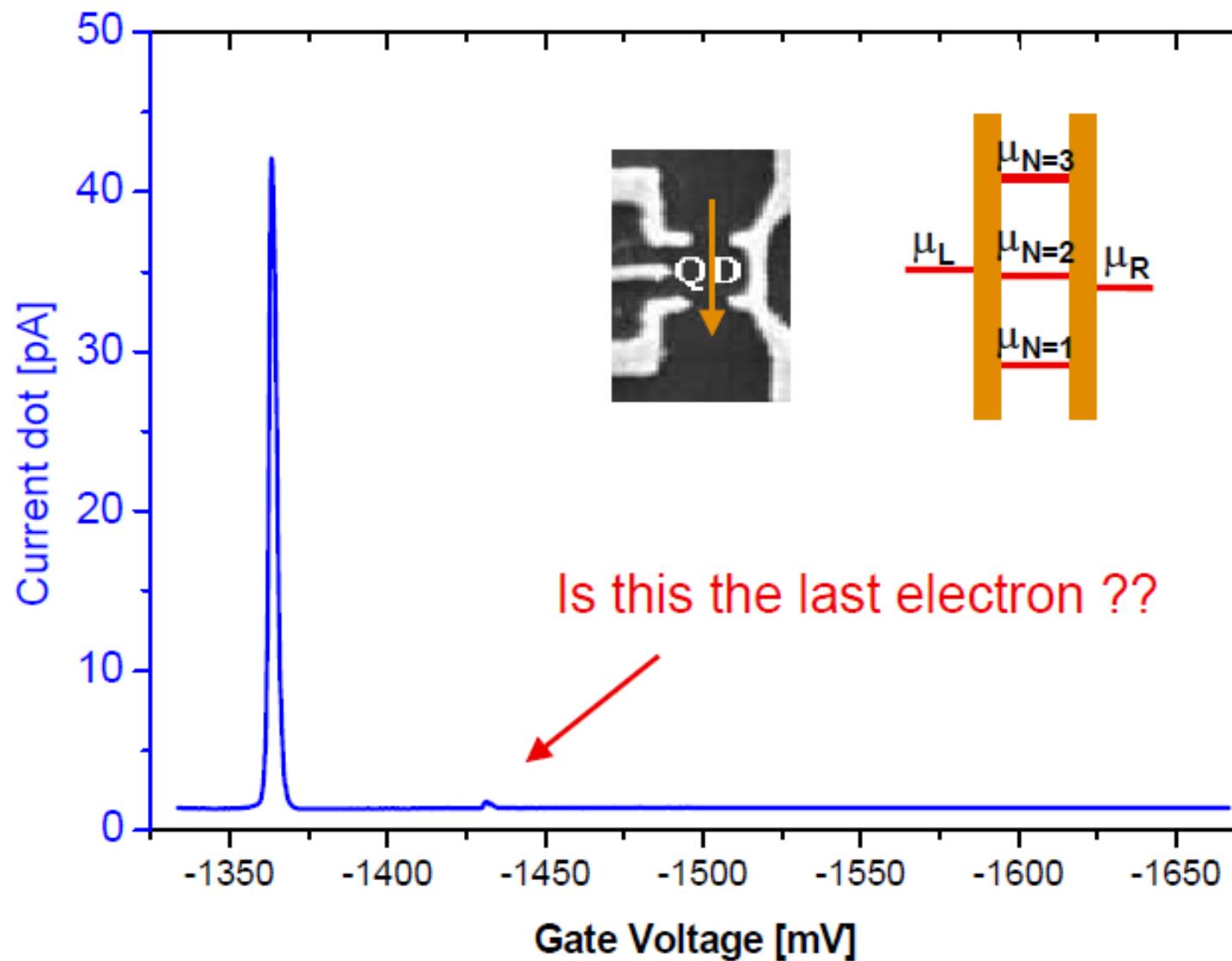
Single electron Zeeman splitting in $B//$



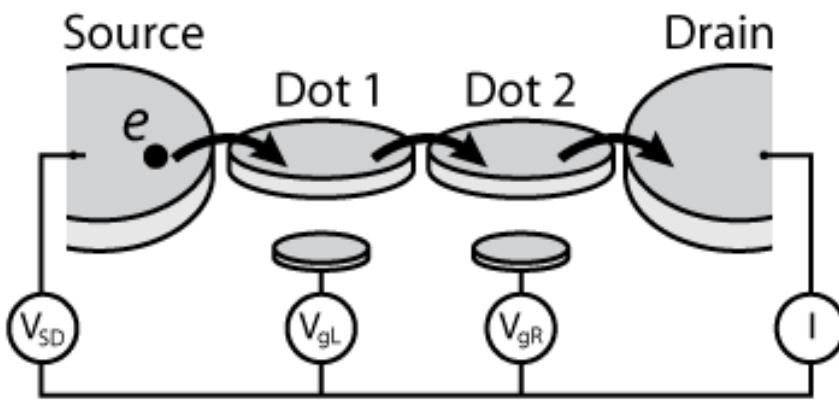
Hanson et al, PRL 91, 196802 (2003)
Also: Potok et al, PRL 91, 016802 (2003)



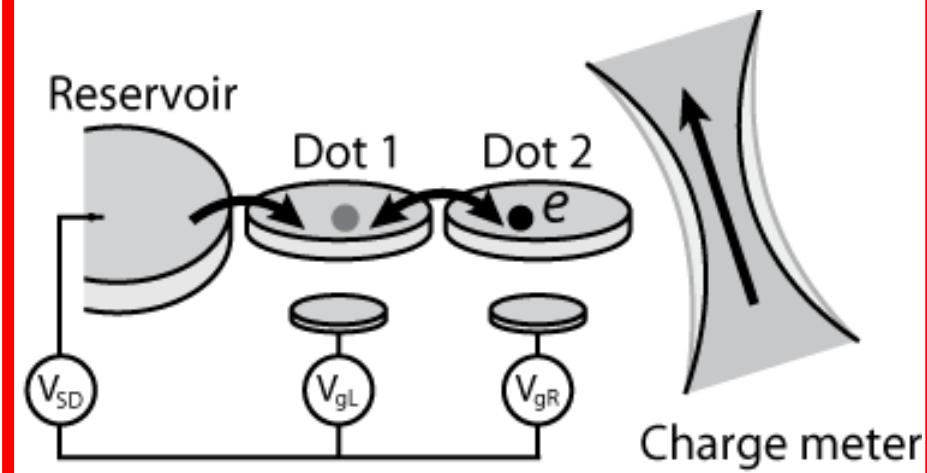
Toward the last electron



Electrical measurement of quantum dots



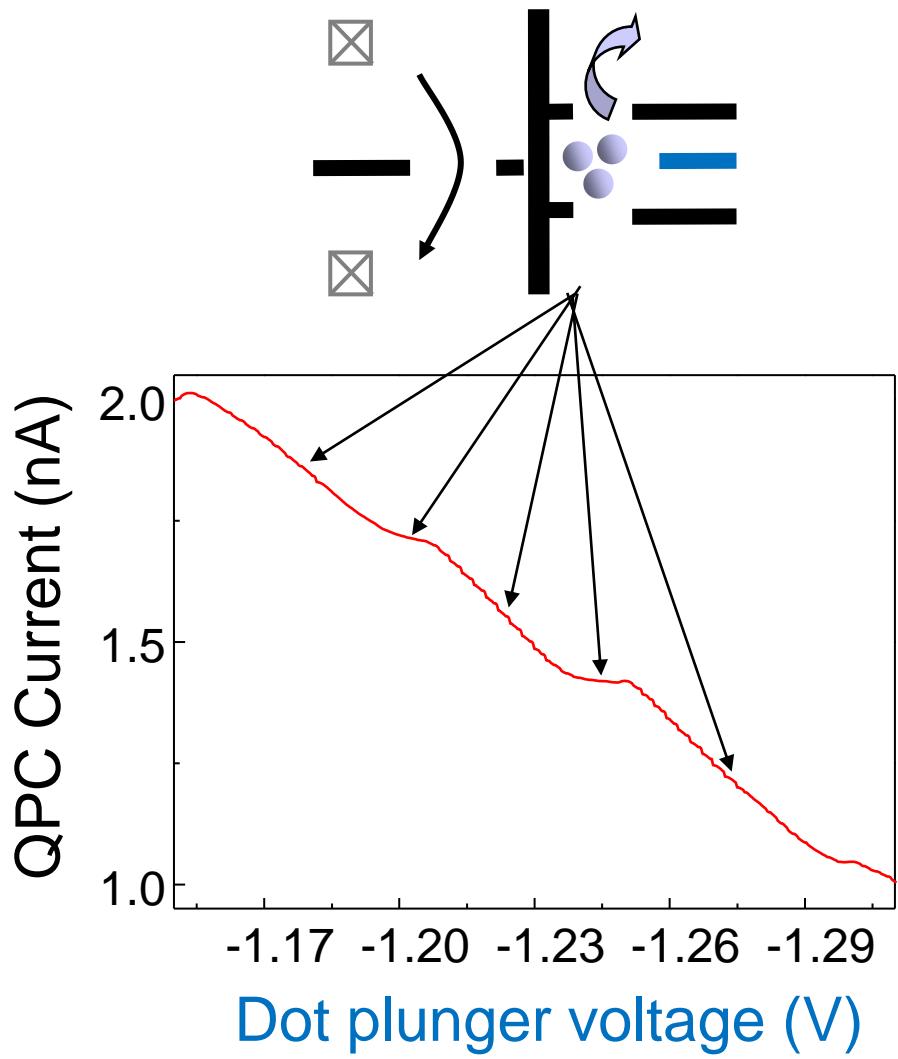
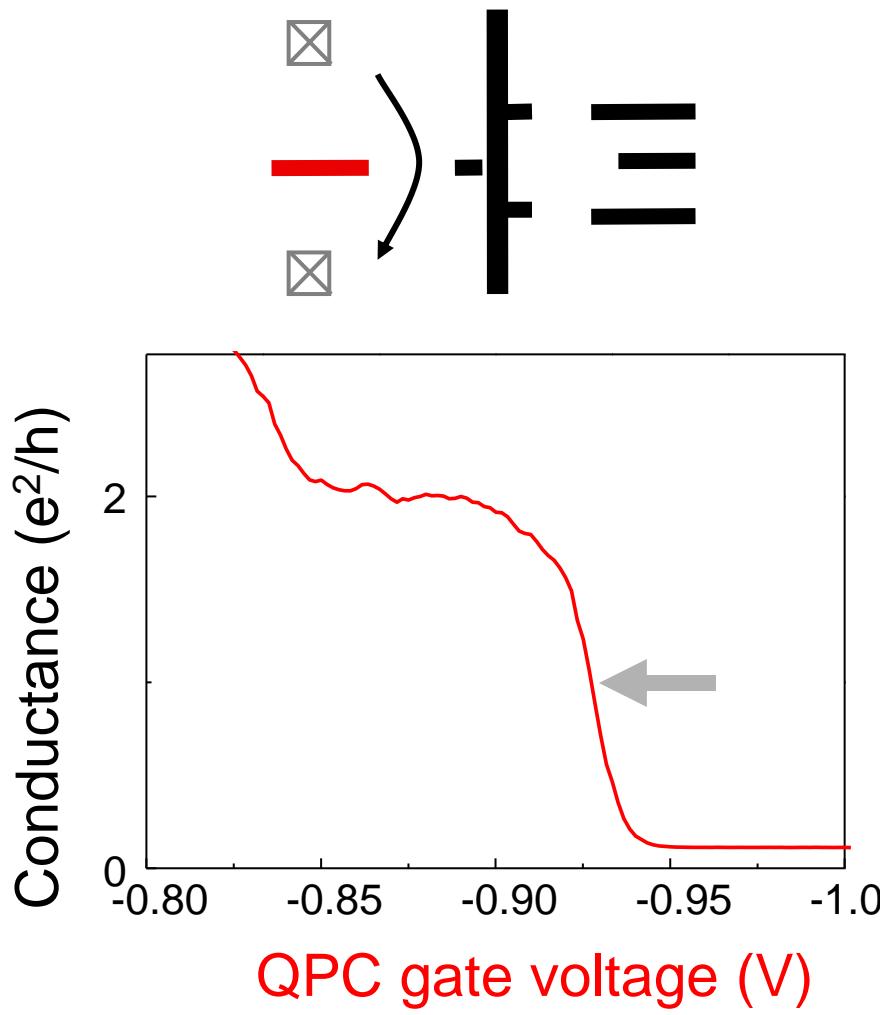
Electron transport
through dots



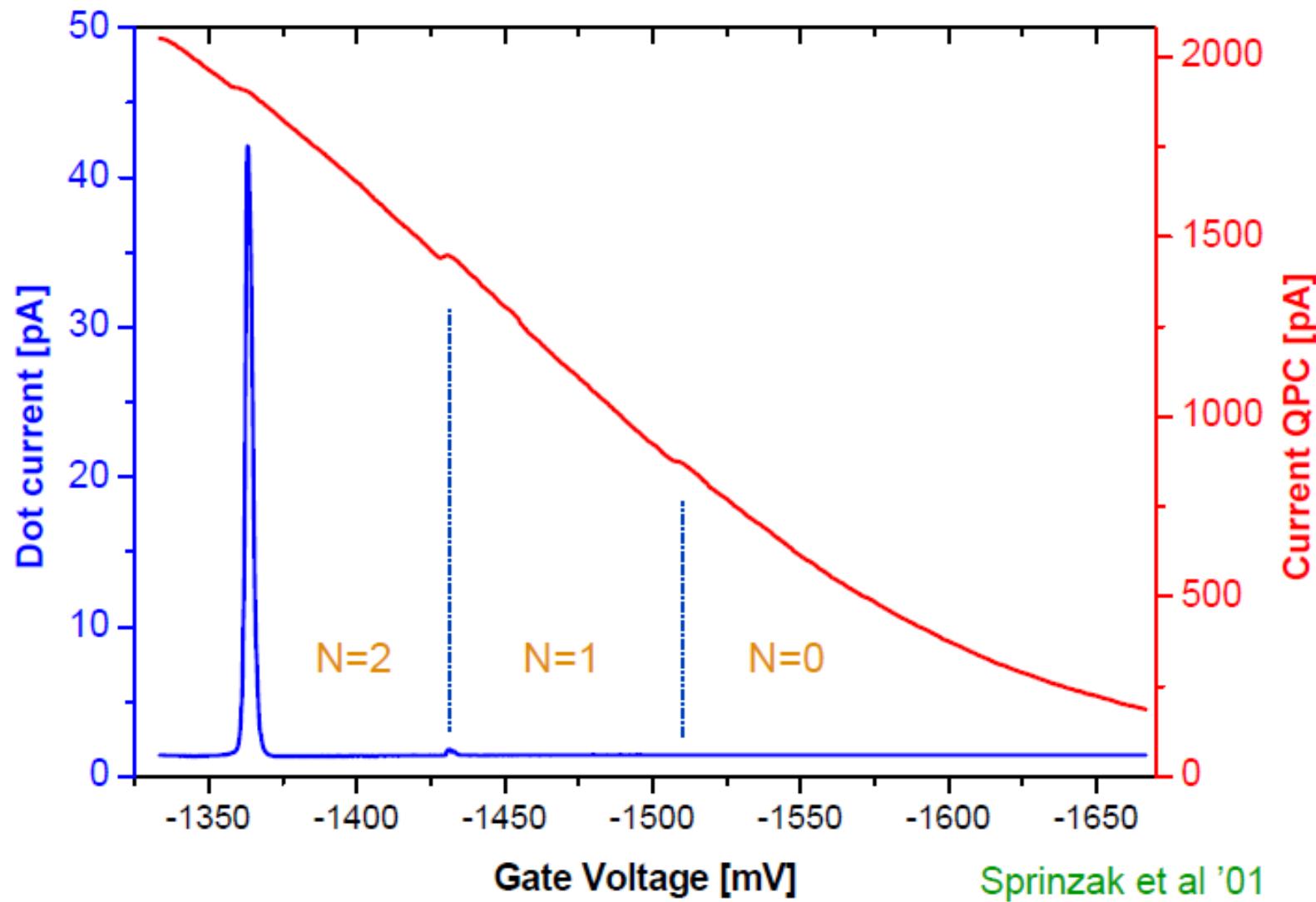
Electron transport
through QPC

A quantum point contact (QPC) as a charge detector

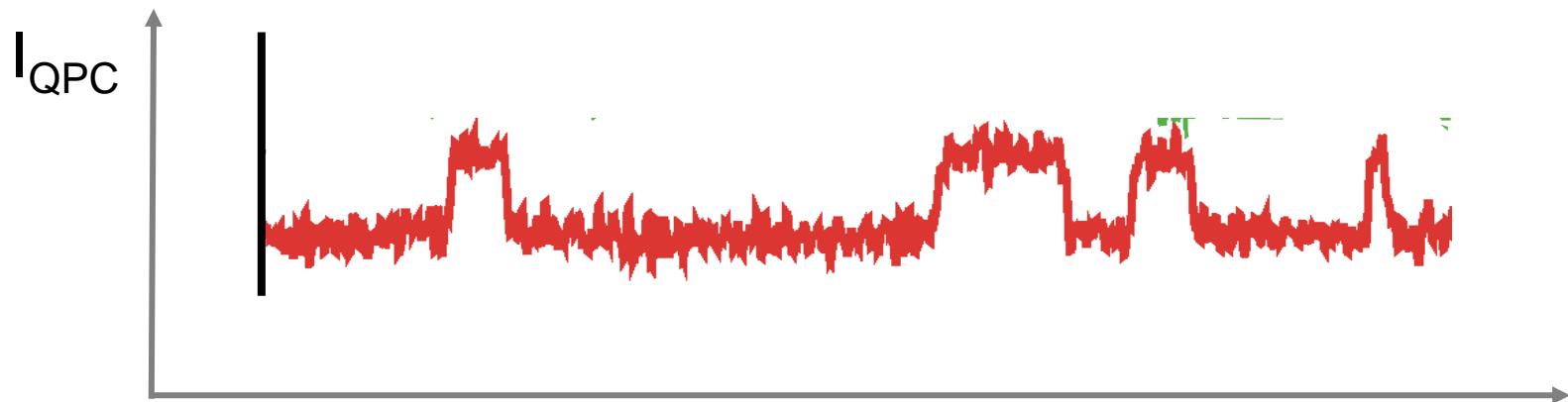
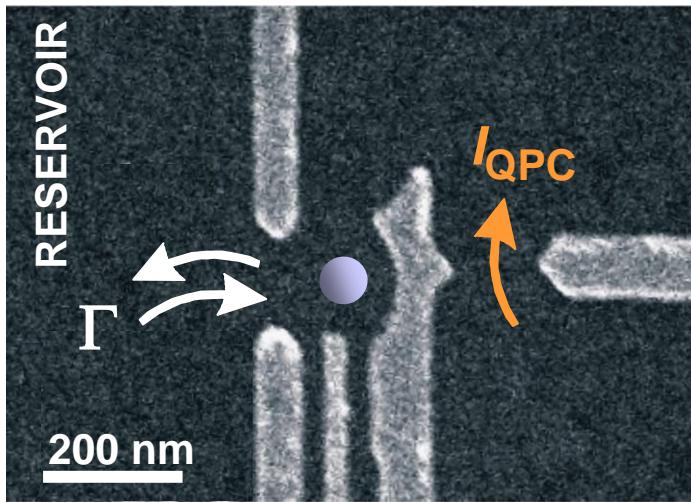
Field *et al*, PRL 1993



The last electron!



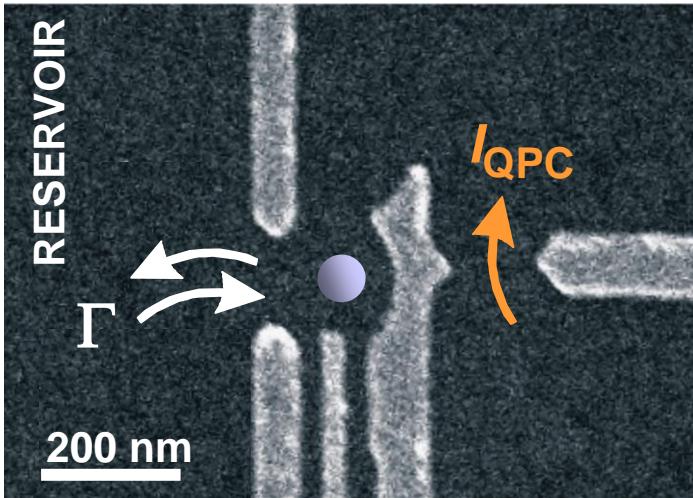
Real-time charge detection



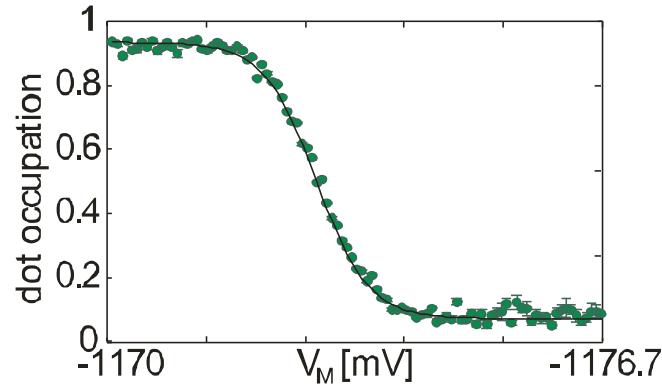
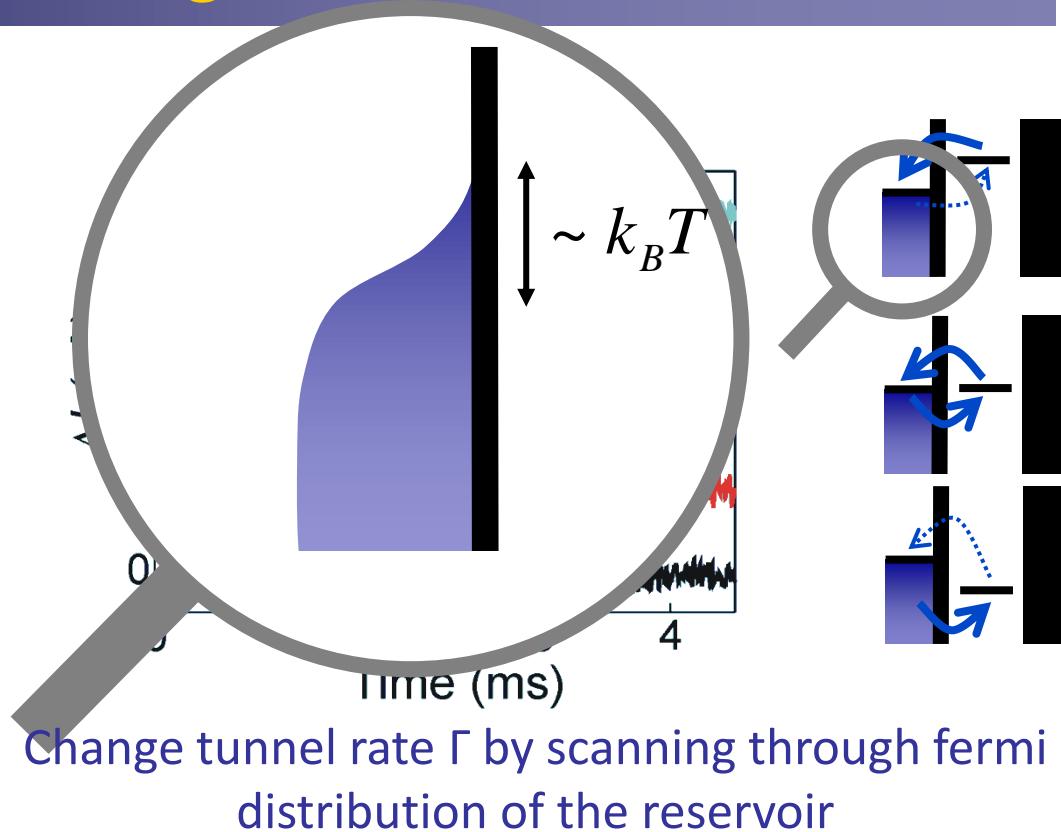
Vandersypen *et al*, APL 2004

time

Real-time charge detection

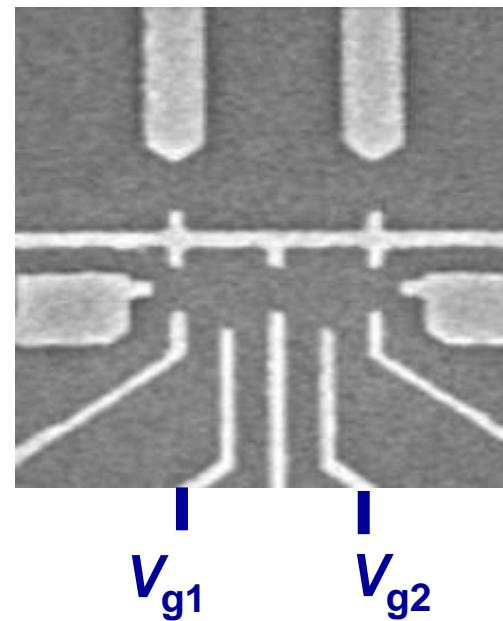
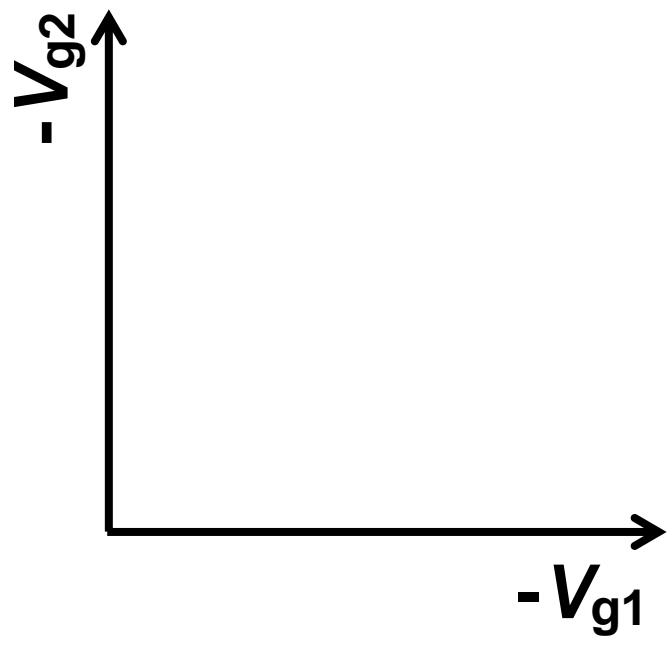


- $V_{SD} \sim 1$ mV
- $I_{QPC} \sim 30$ nA
- $\Delta I_{QPC} \sim 0.3$ nA
- Shortest steps ~ 8 μ s
- With cryogenic preamplifier (HEMT)
shortest steps ~ 300 ns



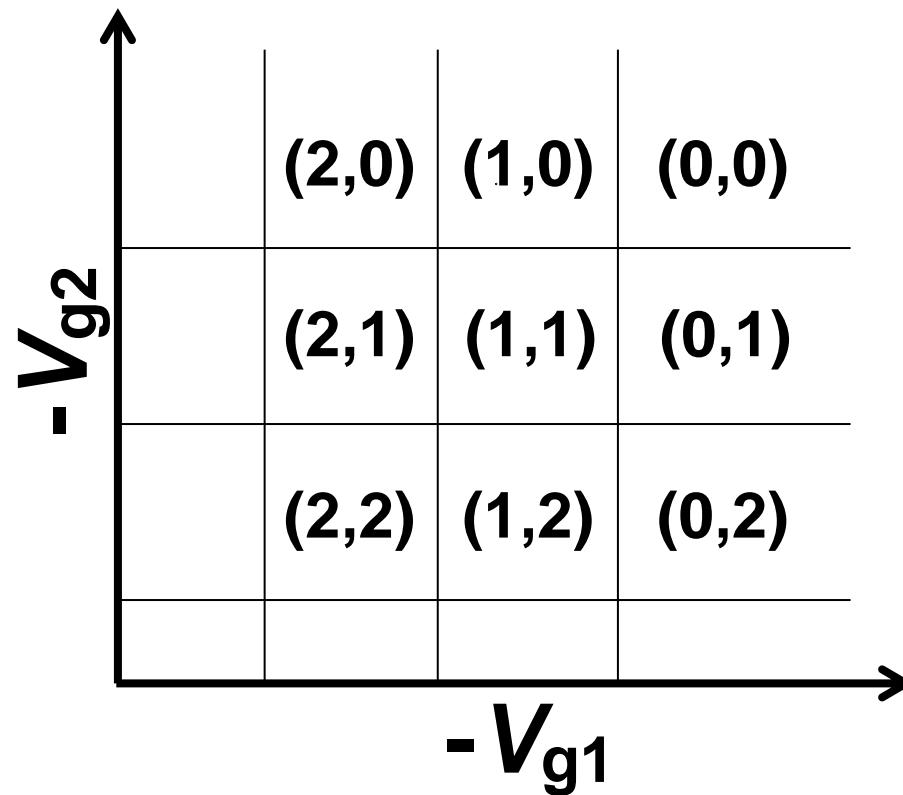
Vandersypen et al, *APL* ('04);
fast detection: Vink et al., *APL* ('07)

Two coupled quantum dots



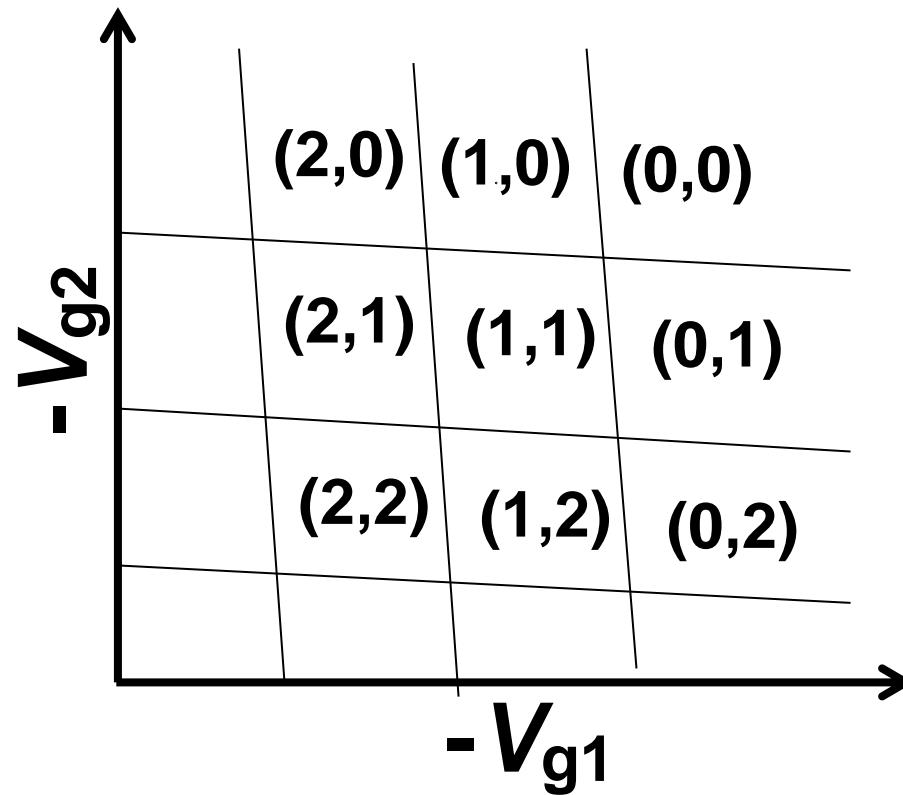
Two coupled quantum dots

Zero inter-dot capacitance, zero cross-talk

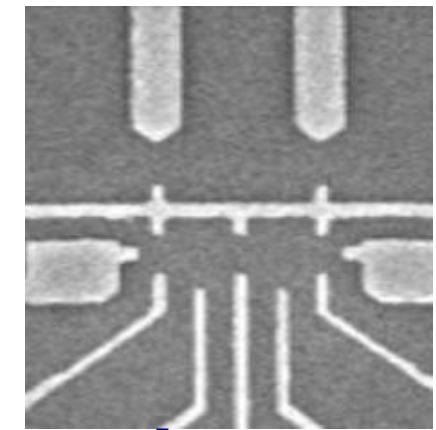


Two coupled quantum dots

Zero inter-dot capacitance, non-zero cross-talk

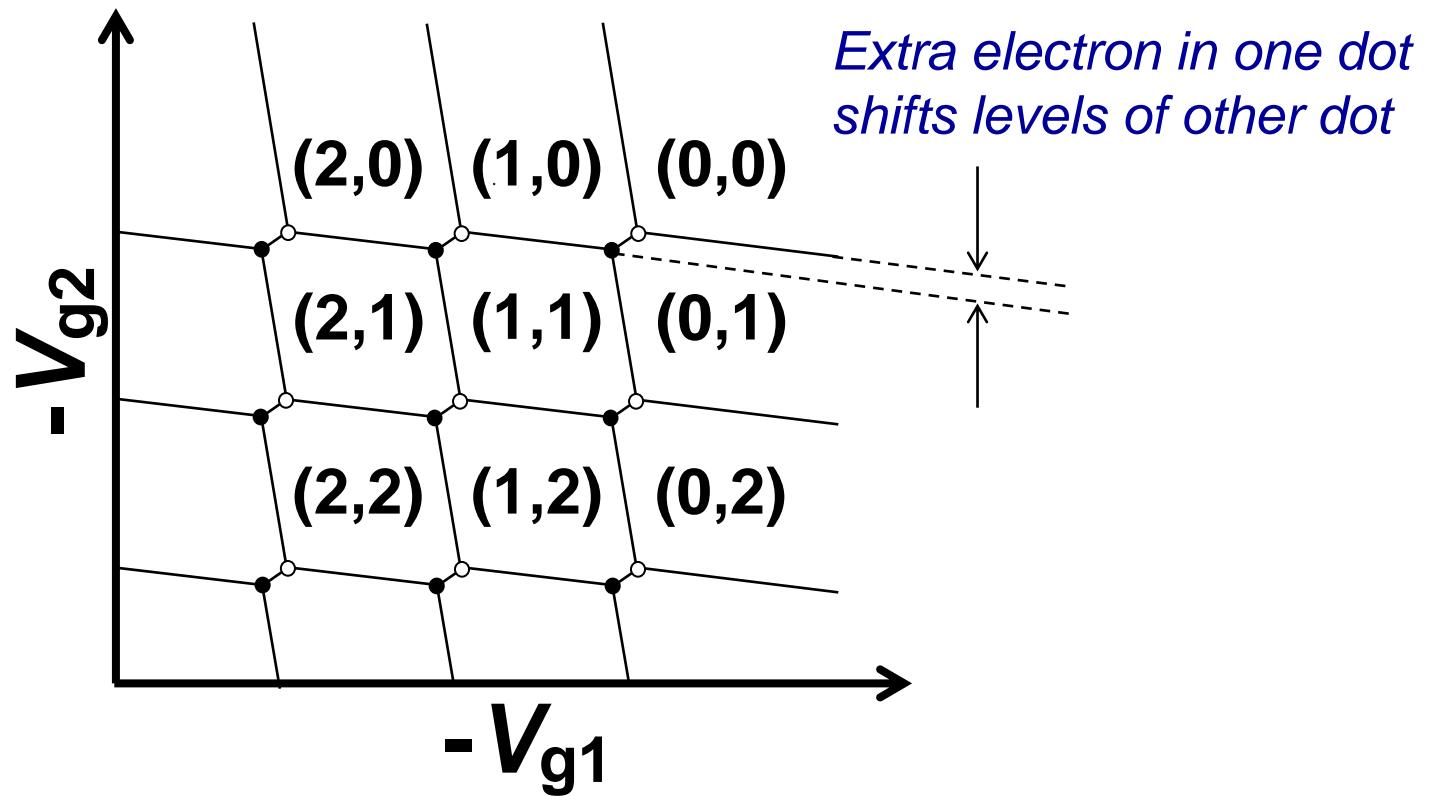


Left gate also affects right dot

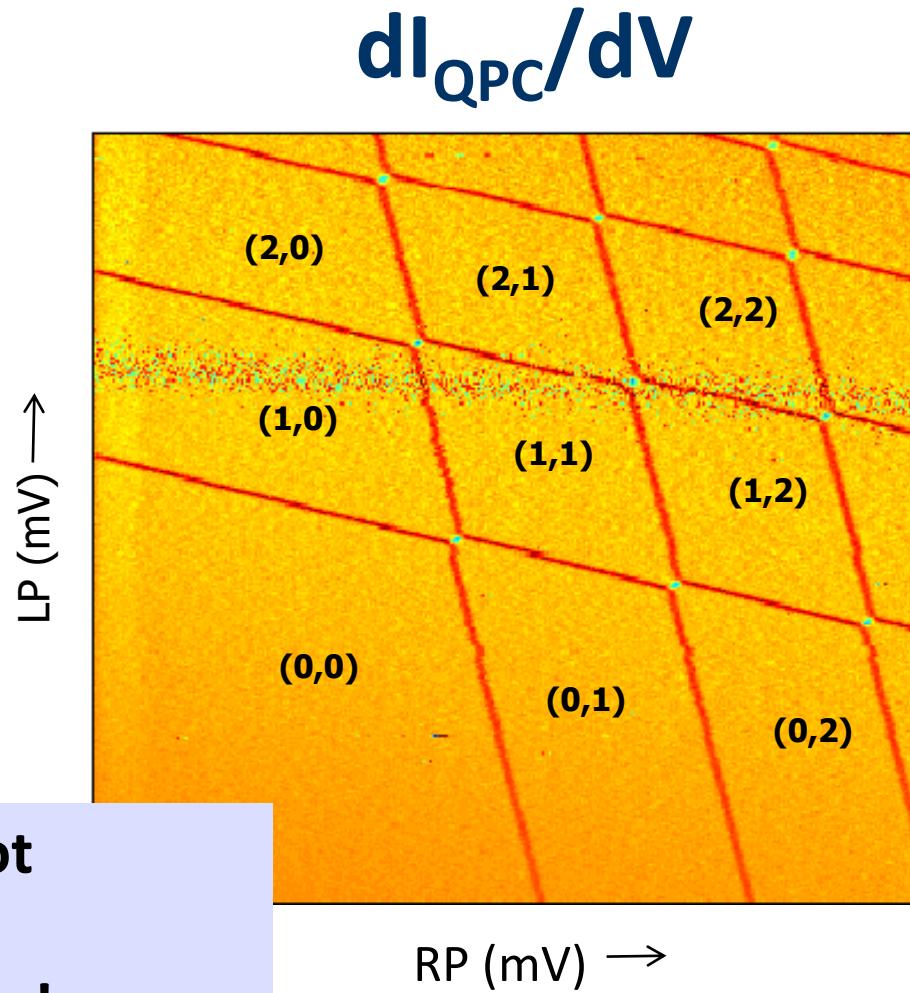
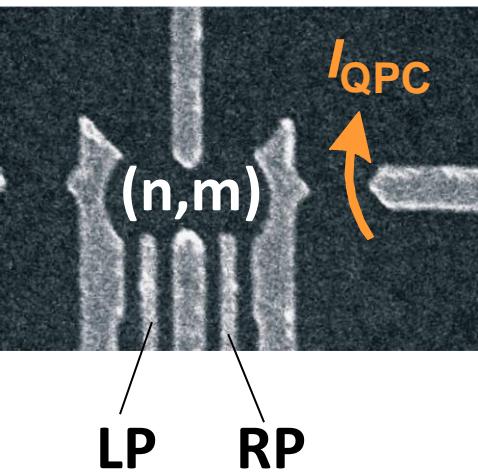


Two coupled quantum dots

Non-zero inter-dot capacitance and cross-talk



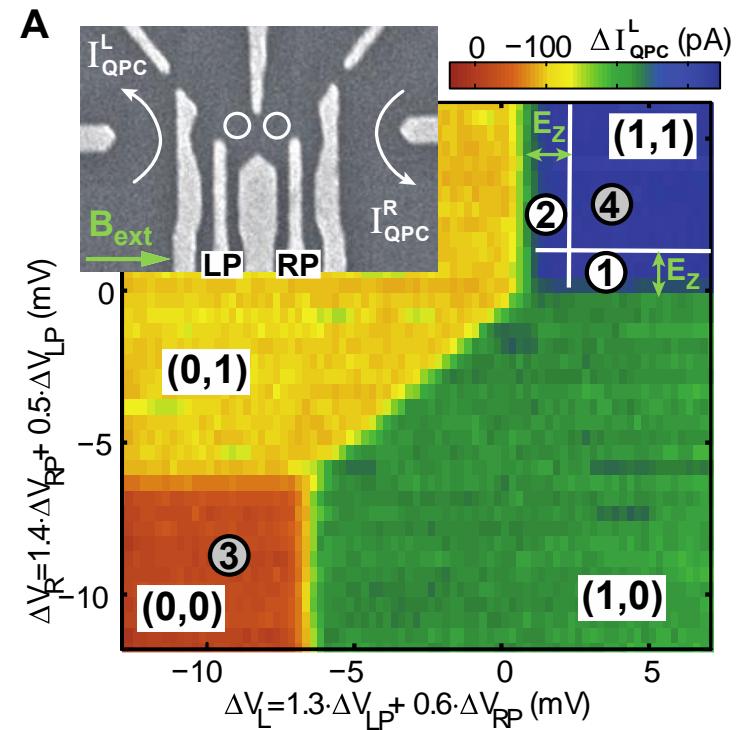
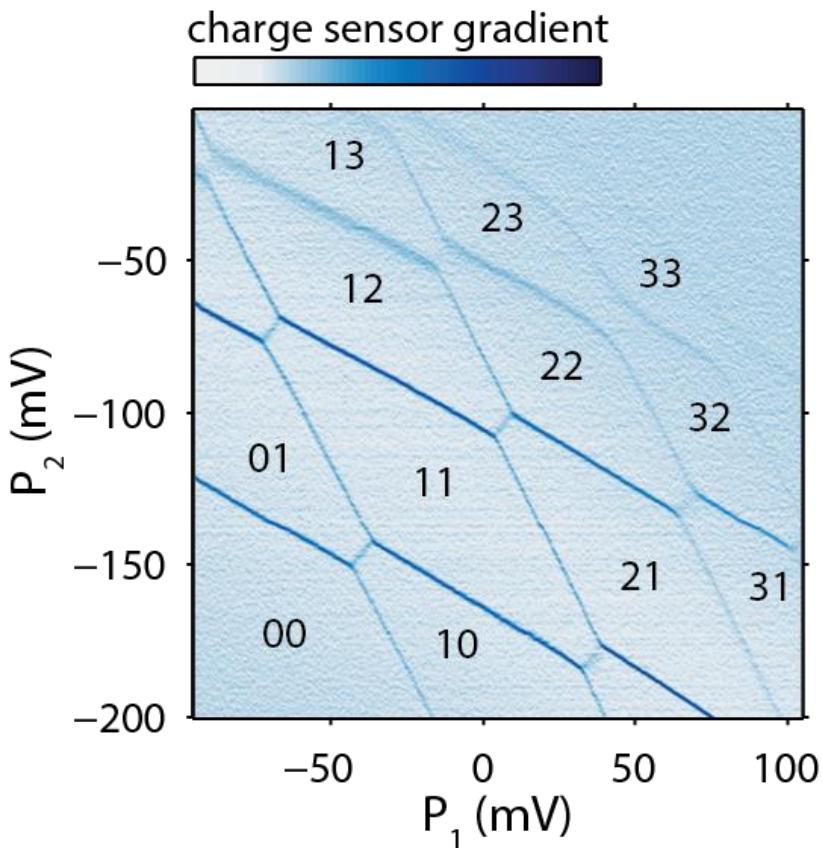
QPC – find the last electron



**Double dot
emptied
completely!**

**QPC detects
all charge
transitions,
also
between
dots**

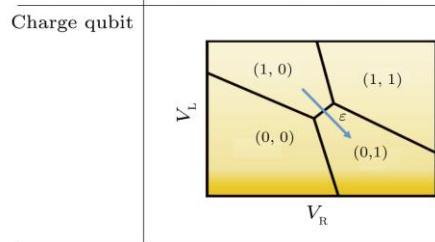
Charge detection in double dot



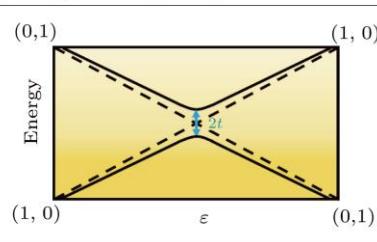
Number of charges on dot probed by external constriction/dot

Different types of QD-based qubits

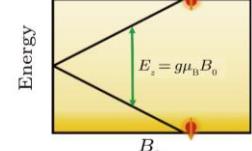
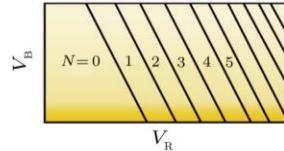
Qubit type Charge stability diagram



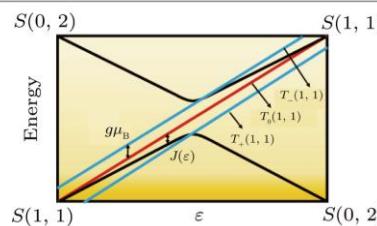
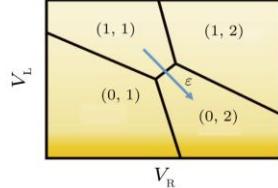
Energy level spectrum



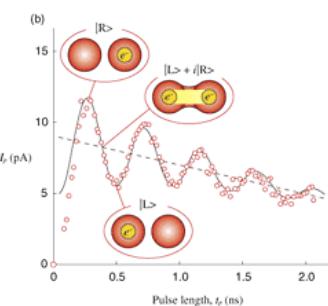
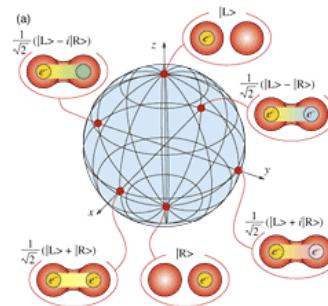
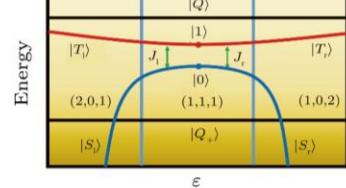
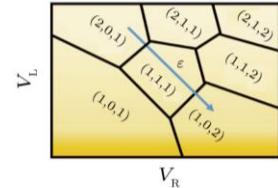
Spin qubit



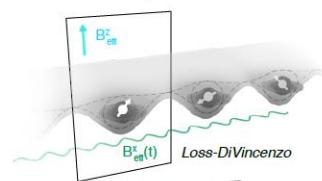
Singlet-triplet qubit



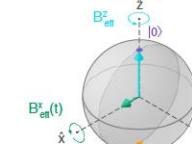
Exchange qubit



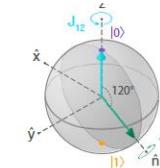
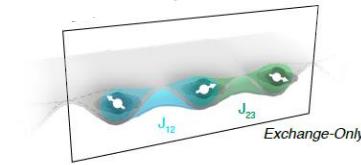
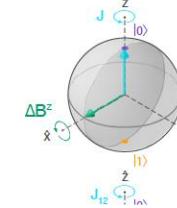
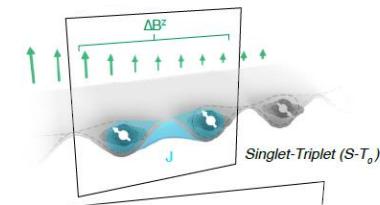
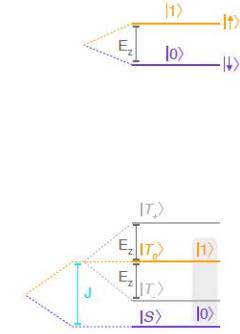
a) Spin Qubit



b) Bloch Sphere



c) Level Diagram

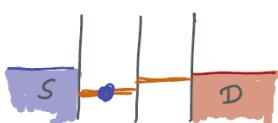


$$\begin{aligned} S_{123} &= \frac{\beta_2}{\beta_1} \\ S_{123} &= \frac{J_2}{J_1} |\psi\rangle \\ S_{123} &= J_2 |\psi\rangle \\ S_{12} &= 0 \end{aligned}$$

Charge qubit in a DQD

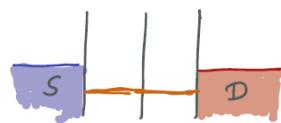
CHARGE QUBITS

$$V_{G1} > V_{G2}$$



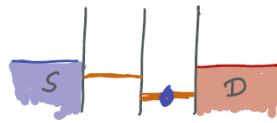
$|L\rangle$

$$V_{G1} = V_{G2}$$



WHERE IS
THE ELECTRON?

$$V_{G1} < V_{G2}$$



$|R\rangle$

$$\Delta E_{L-R} = \epsilon$$

$$\rightarrow H = \begin{bmatrix} -\epsilon/2 & 0 \\ 0 & \epsilon/2 \end{bmatrix} = \text{BASIS } \{|L\rangle, |R\rangle\}$$

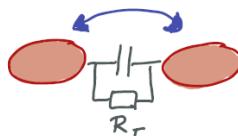
$$= -\frac{\epsilon}{2} |L\rangle\langle L| + \frac{\epsilon}{2} |R\rangle\langle R|$$

$$H|L\rangle = -\frac{\epsilon}{2}|L\rangle$$

$$H|R\rangle = \frac{\epsilon}{2}|R\rangle$$

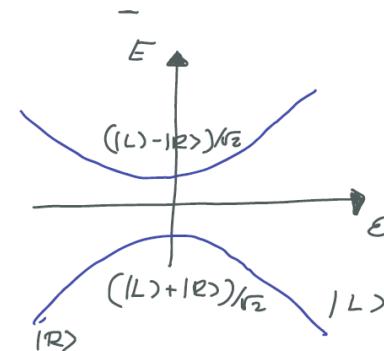
$$H = -\frac{\epsilon}{2} \sigma_z .$$

TUNNELING EVENTS



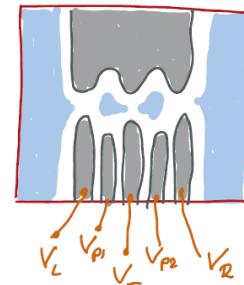
$$H_T = t \left[|L\rangle\langle R| + |R\rangle\langle L| \right] \underbrace{\sigma_x}_{\text{Gx}}$$

$$H = -\frac{\epsilon}{2} \sigma_z + \Delta \sigma_x$$



$$E_{1,2} = \pm \sqrt{(\epsilon/2)^2 + t^2}$$

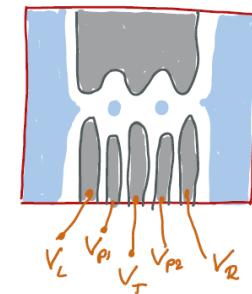
IF V_T NOT
TOO NEGATIVE



t IS LARGE

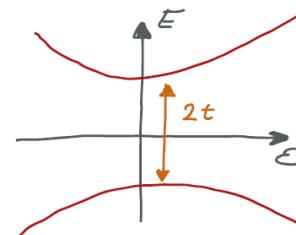
$$|\psi_L(r)|^2 / |\psi_R(r)|^2 \gg 0$$

IF V_T IS
VERY NEGATIVE

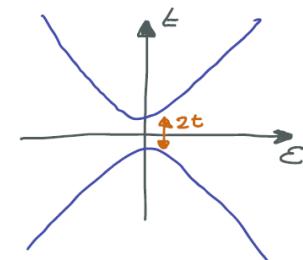


t IS SMALL

$$|\psi_L(r)|^2 / |\psi_R(r)|^2 \approx 0$$



t TUNES THE CROSSOVER FROM LOCALIZED
TO DELOCALIZED STATE

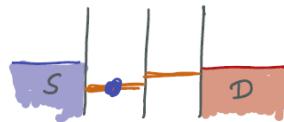


Charge qubit in a DQD

NON-ADIABATIC CONTROL

① INITIALIZATION

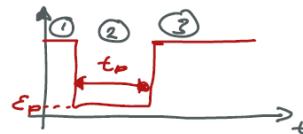
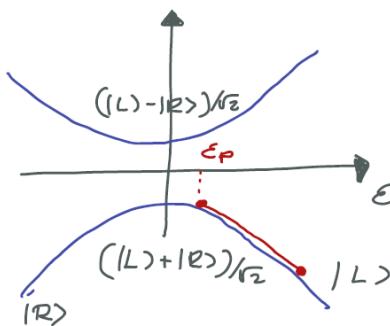
$$\epsilon \gg 0$$



$$|L\rangle = |R\rangle$$

$$|L\rangle$$

② FAST GATE:

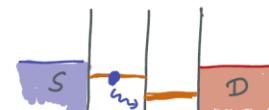


③ READ OUT

MEASURE THE POPULATION OF THE LEFT DOT

$$M_L = |L\rangle \langle L|$$

T_1 - MEASUREMENT



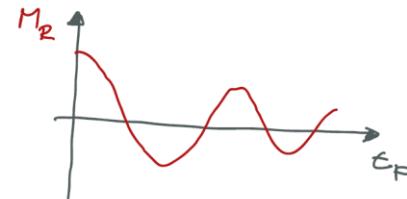
$$|R\rangle$$

WHERE DOES THE ENERGY GO?
→ PHONONS

$$T_1 \approx 30\text{ ns}$$

T_2 - MEASUREMENT

DECAY OF DRIVEN OSCILLATION



FOR EXAMPLE, $\epsilon_p = 0$. $\Rightarrow H = \Delta \sigma_x$
 $\Rightarrow U = e^{-iHt_p}$

$$R_x (\theta = 2\cdot\Delta t) = e^{-i\Delta t \sigma_x}$$

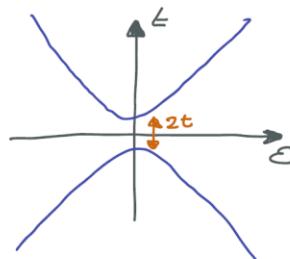
↳ X ROTATION

IF $\epsilon_p \neq 0$ $H = \Delta \sigma_x - \epsilon/2 \sigma_z$
 $U = e^{-i(\Delta \sigma_x - \epsilon/2 \sigma_z)t}$

↳ ROTATION AROUND DIFFERENT AXES

Charge qubit in a DQD

CHARGE NOISE : $H = -\frac{\epsilon(t)}{2}G_z + t(\epsilon)$



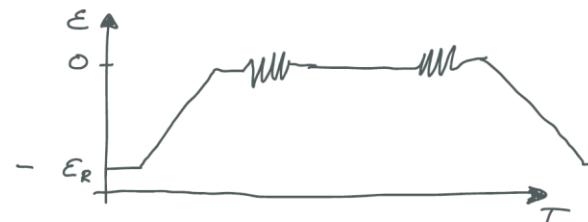
$$E(t) = \sqrt{[\epsilon(t)]^2 + 4t(\epsilon)^2}$$

QUBIT FREQUENCY
CHANGES

PURE DEPHASING

BEST $T_\phi \rightarrow @ \epsilon=0$ FIRST- ORDER INSENSITIVE
SWEET SPOT

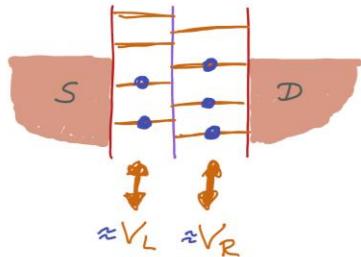
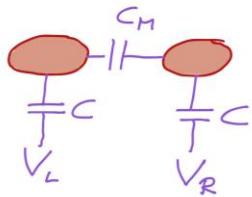
- ① ADIABATIC TRANSFER OF $|R\rangle \rightarrow (|R\rangle + |L\rangle)/\sqrt{2}$
- ② $X_{\pi/2}$ ROTATION
- ③ WAIT TIME ϵ
- ④ $X_{\pi/2}$ ROTATION
- ⑤ PROJECTING BACK TO $|R\rangle$



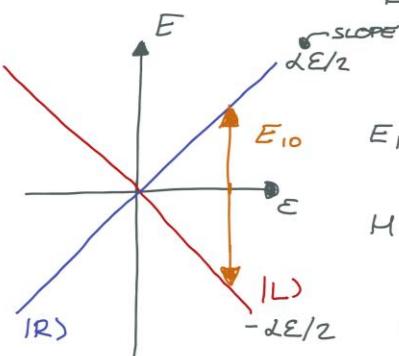
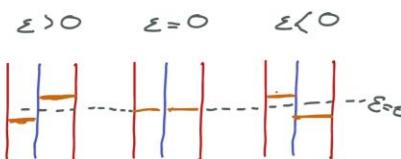
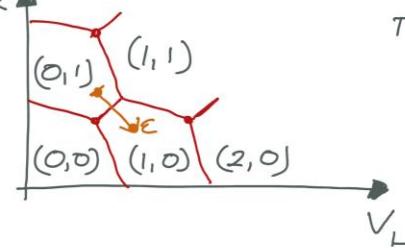
Charge qubit in a DQD

CHARGE QUBIT

DOUBLE QUANTUM DOT:



STABILITY DIAGRAM: (N_L, N_R) ELECTRONS ON THE DOT

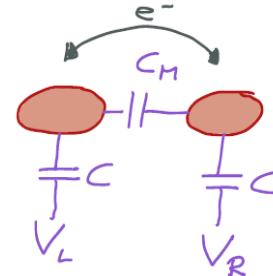


$$E_{10} = \frac{1}{2} \alpha \cdot \varepsilon - (-\alpha^{\dagger}_2) \varepsilon = \alpha \cdot \varepsilon$$

$$H = \frac{1}{2} [\alpha \cdot \varepsilon |R\rangle \langle R| + (-\alpha \cdot \varepsilon) |L\rangle \langle L|] =$$

IN $\begin{bmatrix} |L\rangle \\ |R\rangle \end{bmatrix}$ BASIS

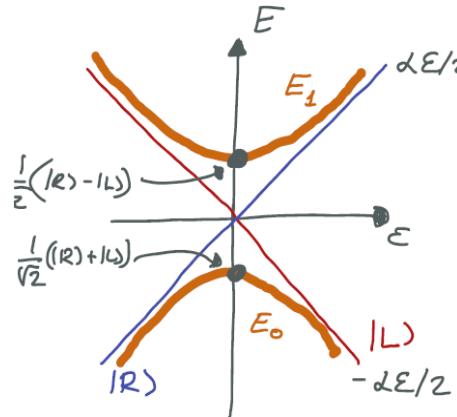
$$= -\frac{1}{2} \alpha \cdot \varepsilon \sigma_z$$



ELECTRONS JUMP:

$$H = -|t| [|L\rangle \langle R| + |R\rangle \langle L|] = -|t| \sigma_x$$

$$H = -\frac{1}{2} \alpha \cdot \varepsilon \sigma_z - |t| \sigma_x$$



CHARGE HYBRIDIZATION

$$E_{0,1} = \pm \sqrt{(\frac{1}{2} \alpha \cdot \varepsilon)^2 + (|t|)^2}$$

AT $\varepsilon = 0$

$$E_{0,1} = \mp t \quad \Delta E_\alpha = 2t$$

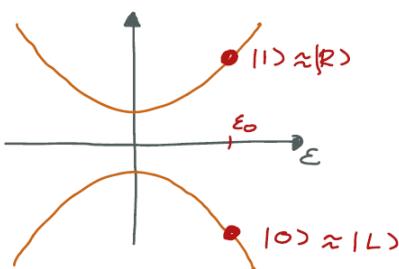
$$H = \begin{bmatrix} 0 & -t \\ -t & 0 \end{bmatrix}$$

$$|\psi_0\rangle = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix} \quad E_0 = -t$$

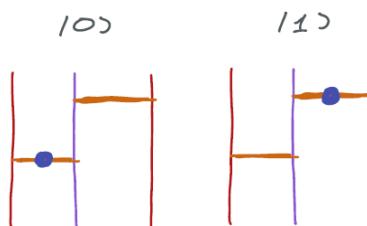
$$|\psi_1\rangle = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -1 \end{bmatrix} \quad E_1 = t$$

Charge qubit in a DQD

WE FIX $\epsilon = \epsilon_0 \gg 0$, AND DEFINE THE QUBIT THERE:



|10> |11>



③ MOVE ϵ FAST BACK TO ϵ_0

④ READ OUT: QPC - IS THE CHARGE IN THE LEFT OR RIGHT DOT?

NOTE IF WE MOVE TO A FINITE $\epsilon \neq 0$,

$$H = -|t|\sigma_x - \frac{1}{2}\epsilon\sigma_z$$

UNIVERSAL CONTROL OF THE QUBIT

HOW TO DO A GATE?

FOR EXAMPLE $R_x(\pi)$ [X GATE]

① $t=0 \quad \epsilon = \epsilon_0 \quad H \approx -\frac{1}{2}(\epsilon_0 \sigma_z) \quad |10\rangle$

② MOVE ϵ FAST (NON-ADIABATIC) TO $\epsilon = 0$
 $(\Delta/t < \epsilon_0)$

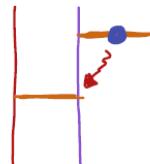
$$t=0.1ns \quad |\psi\rangle = |10\rangle \quad H = -|t|\sigma_x$$

$$U = e^{i(t)\sigma_x/\hbar \cdot t} \quad |\psi(t)\rangle = U(\epsilon)|10\rangle$$

$$|t|\sigma_x/\hbar \cdot t_{GATE} = \pi/2$$

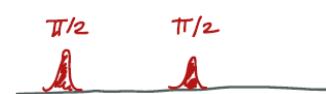
$$\Rightarrow |\psi(t_{GATE})\rangle = |11\rangle$$

|11>



DECAY OF THE EXCITED STATE
 $T_1 \approx 10ns$

THE ENERGY GOES INTO PHONONS



$$\frac{1}{2}(|10\rangle + |11\rangle) \rightarrow 50\% |10\rangle + 50\% |11\rangle$$

$$T_2 \approx 7ns$$

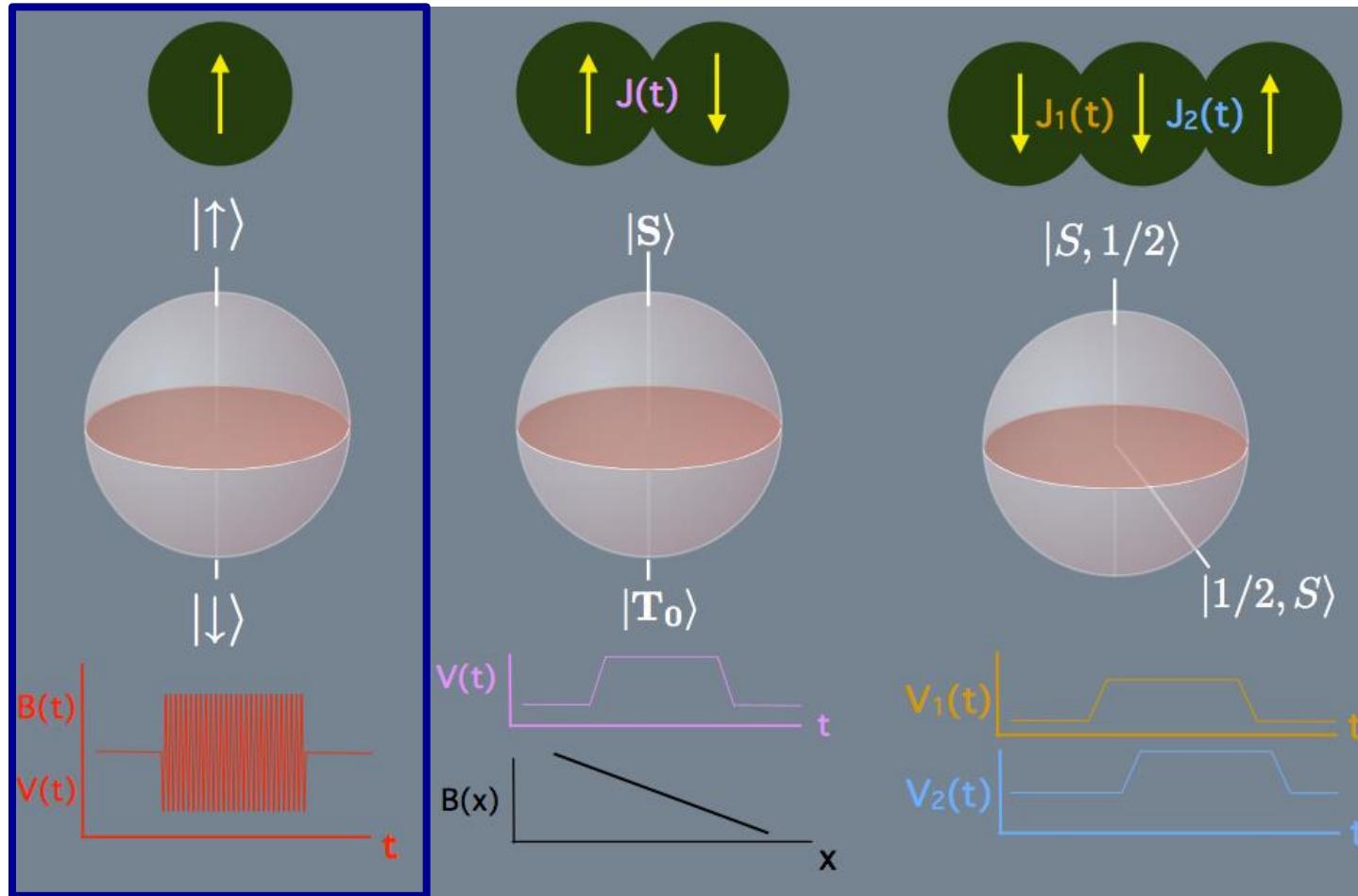
CHARGE NOISE CHANGES THE QUBIT FREQUENCY

$$H_0 = -\frac{1}{2}\epsilon_0\sigma_z$$

↳ $\epsilon_0 + \delta\epsilon$

GOOD STRATEGY FIND AN INSENSITIVE SPOT

Spin qubit flavors



*Our focus
(for illustration)*

Image: C. Marcus

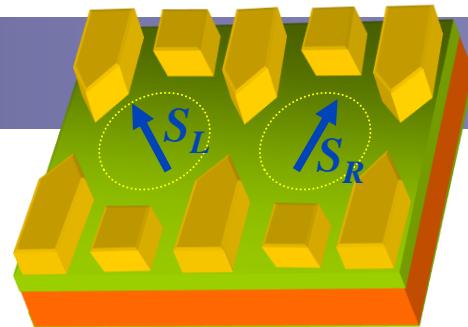
*Other options:
Hybrid qubit*

...

Spin qubits in quantum dots

Loss & DiVincenzo, PRA 1998

Vandersypen et al., Proc. MQC02 (quant-ph/0207059)



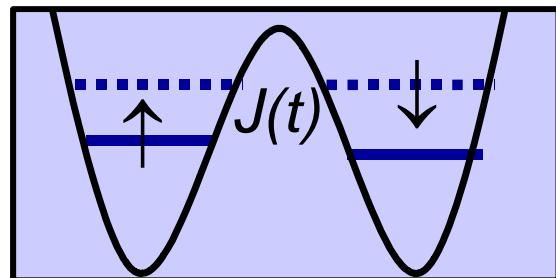
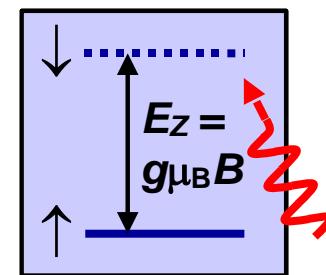
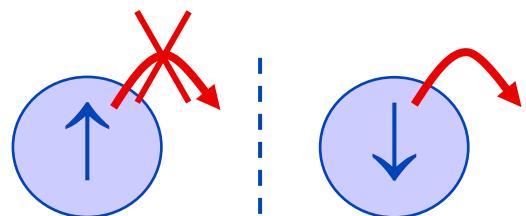
Initialization 1-electron, low T , high B_0
 $H_0 \sim \sum \omega_i \sigma_{zi}$

Read-out convert spin to charge
then measure charge

ESR pulsed microwave magnetic field
 $H_{RF} \sim \sum A_i(t) \cos(\omega_i t) \sigma_{xi}$

SWAP exchange interaction
 $H_J \sim \sum J_{ij}(t) \sigma_i \cdot \sigma_j$

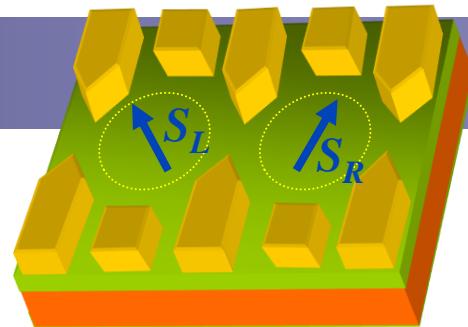
Coherence long relaxation time T_1
long coherence time T_2



Spin qubits in quantum dots

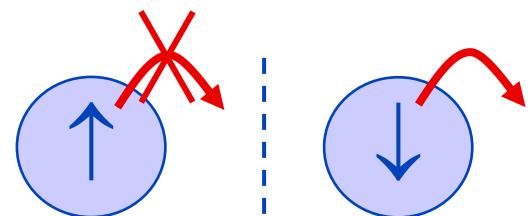
Loss & DiVincenzo, PRA 1998

Vandersypen et al., Proc. MQC02 (quant-ph/0207059)

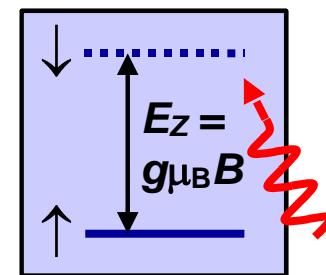


Initialization 1-electron, low T , high B_0
 $H_0 \sim \sum \omega_i \sigma_{zi}$

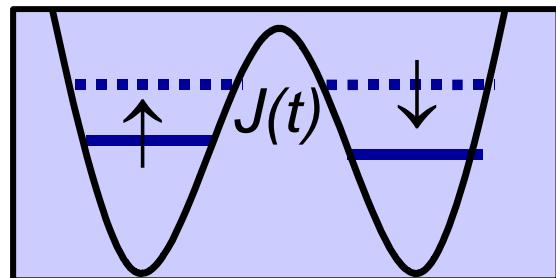
Read-out convert spin to charge
then measure charge



ESR pulsed microwave magnetic field
 $H_{RF} \sim \sum A_i(t) \cos(\omega_i t) \sigma_{xi}$



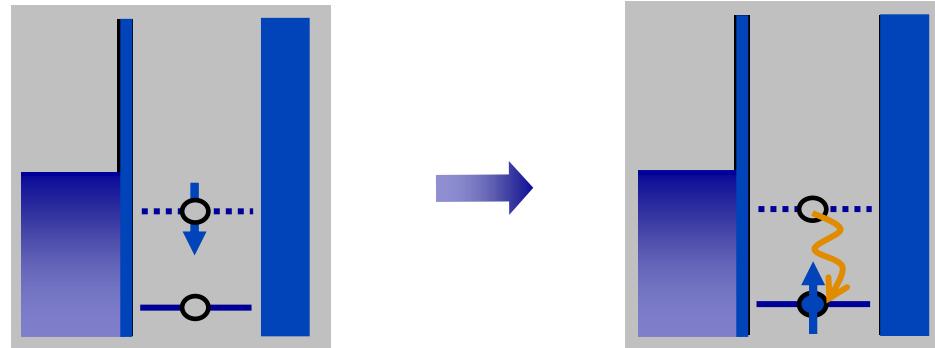
SWAP exchange interaction
 $H_J \sim \sum J_{ij}(t) \sigma_i \cdot \sigma_j$



Coherence long relaxation time T_1
long coherence time T_2

Initialization of a single electron spin

Method 1:
relaxation to
ground state



Method 2:
spin-selective
tunneling

