

CS202

Section:03

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HW1

Question1

a) $f(n)=5n^3+4n^2+10$ is $O(n^4)$

There are two positive constants: c and n_0 such that:

$$0 \leq 5n^3 \leq cn^4 \quad \text{for all } n \geq n_0$$

Choose $c = 2$ and $n_0 = 1$

Then, $5n^3 \leq 2n^4$ for all $n \geq 1$

Or, choose $c = 1$ and $n_0 = 2$

Then, $5n^3 \leq n^4$ for all $n \geq 2$

b) Insertion Sort

- [24, 8, 51, 28, 20, 29, 21, 17, 38, 27]

Step1- 24 | 8 51 28 20 29 21 17 38 27. key:8

Step2- 8 24 | 51 28 20 29 21 17 38 27. key:51

Step3- 8 24 51 | 28 20 29 21 17 38 27. key:28

Step4- 8 24 28 51 | 20 29 21 17 38 27. key:20

Step5- 8 20 24 28 51 | 29 21 17 38 27. key:29

Step6- 8 20 24 28 29 51 | 21 17 38 27. key:21

Step7- 8 20 21 24 28 29 51 | 17 38 27. key:17

Step8- 8 17 20 21 24 28 29 51 | 38 27. key:38

Step9- 8 17 20 21 24 28 29 38 51 | 27. key:27

Step10- 8 17 20 21 24 27 28 29 38 51 | sorted.

Bubble Sort

- [24, 8, 51, 28, 20, 29, 21, 17, 38, 27]

First pass

Comparisons

24 8 51 28 20 29 21 17 38 27 -	24 and 8
8 24 51 28 20 29 21 17 38 27 -	24 and 51
8 24 51 28 20 29 21 17 38 27 -	51 and 28
8 24 28 51 20 29 21 17 38 27 -	51 and 20
8 24 28 20 51 29 21 17 38 27 -	51 and 29
8 24 28 20 29 51 21 17 38 27 -	51 and 21
8 24 28 20 29 21 51 17 38 27 -	51 and 17
8 24 28 20 29 21 17 51 38 27 -	51 and 38
8 24 28 20 29 21 17 38 51 27 -	51 and 27
8 24 28 20 29 21 17 38 27 - 51	pass 1 ends

Second pass

Comparisons

8 24 28 20 29 21 17 38 27 - 51	8 and 24
8 24 28 20 29 21 17 38 27 - 51	24 and 28
8 24 28 20 29 21 17 38 27 - 51	28 and 20
8 24 20 28 29 21 17 38 27 - 51	28 and 29
8 24 20 28 29 21 17 38 27 - 51	29 and 21
8 24 20 28 21 29 17 38 27 - 51	29 and 17
8 24 20 28 21 17 29 38 27 - 51	29 and 38
8 24 20 28 21 17 29 38 27 - 51	38 and 27
8 24 20 28 21 17 29 27 - 38 51	pass 2 ends

Third pass

Comparisons

8 24 20 28 21 17 29 27 - 38 51	8 and 24
8 24 20 28 21 17 29 27 - 38 51	24 and 20
8 20 24 28 21 17 29 27 - 38 51	24 and 28
8 20 24 28 21 17 29 27 - 38 51	28 and 21
8 20 24 21 28 17 29 27 - 38 51	28 and 17
8 20 24 21 17 28 29 27 - 38 51	28 and 29
8 20 24 21 17 28 29 27 - 38 51	29 and 27
8 20 24 21 17 28 27 29 38 51	pass 3 ends

Fourth pass

Comparisons

8 20 24 21 17 28 27 29 38 51	8 and 20
8 20 24 21 17 28 27 29 38 51	20 and 24
8 20 24 21 17 28 27 29 38 51	24 and 21

8 20 21 24 17 28 27 29 38 51	24 and 17
8 20 21 17 24 28 27 29 38 51	24 and 28
8 20 21 17 24 28 27 29 38 51	28 and 27
8 20 21 17 24 27 28 29 38 51	pass 4 ends

Fifth pass

Comparisons

8 20 21 17 24 27 28 29 38 51	8 and 20
8 20 21 17 24 27 28 29 38 51	20 and 21
8 20 21 17 24 27 28 29 38 51	21 and 17
8 20 17 21 24 27 28 29 38 51	21 and 24
8 20 17 21 24 27 28 29 38 51	24 and 27
8 20 17 21 24 27 28 29 38 51	pass 5 ends

Sixth pass

Comparisons

8 20 17 21 24 27 28 29 38 51	8 and 20
8 20 17 21 24 27 28 29 38 51	20 and 17
8 17 20 21 24 27 28 29 38 51	sorted

Question2

c)

```

busra.ziyagil@dijkstra:~/hw1cs202
login as: busra.ziyagil
busra.ziyagil@dijkstra.ug.bcc.bilkent.edu.tr's password:
Last login: Sun Feb 28 21:16:43 2021 from 10.201.182.249
[busra.ziyagil@dijkstra ~]$ ls
a.out  hw1cs202  main.o  sorting.cpp  sorting.h.gch  system
cs201  main.cpp  makefile  sorting.h  sorting.o
[busra.ziyagil@dijkstra ~]$ cd hw1cs202
[busra.ziyagil@dijkstra hw1cs202]$ ls
main.cpp  makefile  sorting.cpp  sorting.h
[busra.ziyagil@dijkstra hw1cs202]$ make
g++ -c -Wall sorting.cpp
g++ -c -Wall main.cpp
g++ sorting.o main.o -o hw1
[busra.ziyagil@dijkstra hw1cs202]$ ./hw1
Comparison count:120 Movement count:45
Selection Sorted:3 5 6 7 8 9 11 12 12 14 14 17 18 19 20 21
Comparison count:46 Movement count:128
Merge Sorted:3 5 6 7 8 9 11 12 12 14 14 17 18 19 20 21
Comparison count:45 Movement count:102
Quick Sorted:3 5 6 7 8 9 11 12 12 14 14 17 18 19 20 21
Radix Sorted:3 5 6 7 8 9 11 12 12 14 14 17 18 19 20 21
[busra.ziyagil@dijkstra hw1cs202]$ ~[23~

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Comparison count:120 Movement count:45
 Selection Sorted:3 5 6 7 8 9 11 12 12 14 14 17 18 19 20 21
 Comparison count:46 Movement count:128
 Merge Sorted:3 5 6 7 8 9 11 12 12 14 14 17 18 19 20 21
 Comparison count:45 Movement count:102
 Quick Sorted:3 5 6 7 8 9 11 12 12 14 14 17 18 19 20 21
 Radix Sorted:3 5 6 7 8 9 11 12 12 14 14 17 18 19 20 21

Analysis of Selection Sort

Random arrays

Array Size	Elapsed time	compCount	moveCount
6000	32978	17997000	17997
10000	87997	49995000	29997
14000	179042	97993000	41997
18000	282600	161991000	53997
22000	415647	241989000	65997
26000	603975	337987000	77997
30000	800349	449985000	89997

Ascending arrays

Array Size	Elapsed time	compCount	moveCount
6000	37322	17997000	17997
10000	104600	49995000	29997
14000	201183	97993000	41997
18000	334909	161991000	53997
22000	485268	241989000	65997
26000	691458	337987000	77997
30000	912888	449985000	89997

Descending arrays

Array Size	Elapsed time	compCount	moveCount
6000	34420	17997000	17997
10000	95802	49995000	29997
14000	188445	97993000	41997
18000	309508	161991000	53997
22000	465657	241989000	65997
26000	649860	337987000	77997
30000	854058	449985000	89997

d) Analysis of Merge Sort

22000	465657	241989000	65997
26000	649860	337987000	77997
30000	854058	449985000	89997

Analysis of Merge Sort

Random arrays

Array Size	Elapsed time	compCount	moveCount
6000	1010	67798	151616
10000	1778	120470	267232
14000	2339	175271	387232
18000	3363	231974	510464
22000	3892	290200	638464
26000	4938	348815	766464
30000	5292	408764	894464

Ascending arrays

Array Size	Elapsed time	compCount	moveCount
6000	693	39152	151616
10000	938	69008	267232
14000	1271	99360	387232
18000	1552	130592	510464
22000	1953	165024	638464
26000	2625	197072	766464
30000	2819	227728	894464

Descending arrays

Array Size	Elapsed time	compCount	moveCount
6000	538	36656	151616
10000	870	64608	267232
14000	1214	94256	387232
18000	1639	124640	510464
22000	2112	154208	638464
26000	2290	186160	766464
30000	2648	219504	894464

Analysis of Quick Sort

Random arrays

Array Size	Elapsed time	compCount	moveCount
6000	678	92744	140373
10000	1479	154772	268622

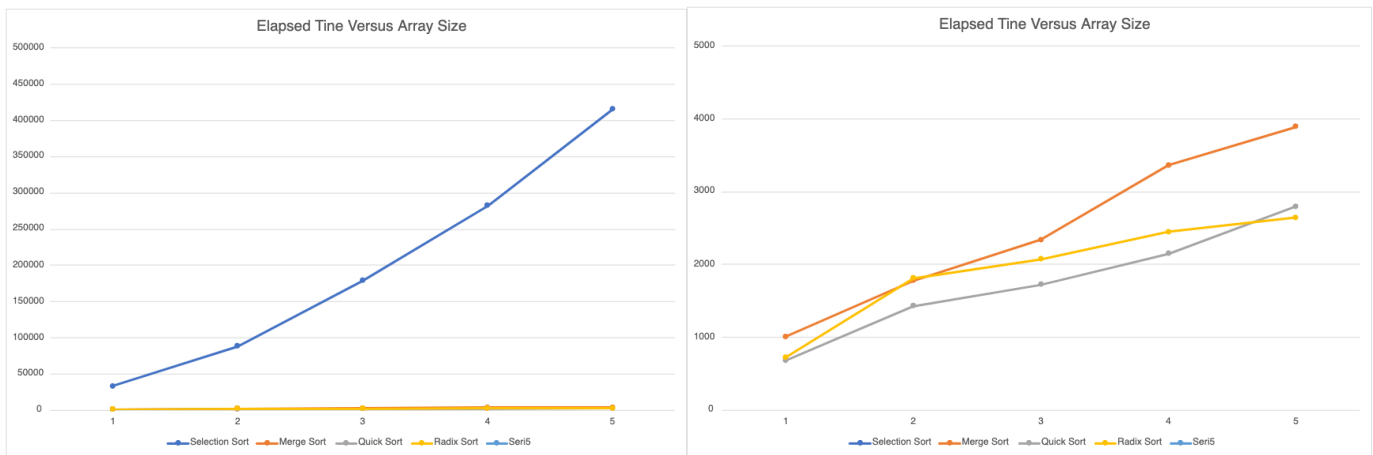
```

20000      2290      188100      788484
30000      2648      219504      894464
-----
Analysis of Quick Sort
Random arrays
    Array Size      Elapsed time      compCount      moveCount
        6000          678          92744          140373
       10000         1479         154772         268622
       14000         1723         222665         399328
       18000         2150         302320         458481
       22000         2800         364644         620521
       26000         3442         449474         731269
       30000         4101         518744         909868
Ascending arrays
    Array Size      Elapsed time      compCount      moveCount
        6000         26522         17997000         23996
       10000         76533         49995000         39996
       14000        147459         97993000         55996
       18000        238944        161991000         71996
       22000        353009        241989000         87996
       26000        484058        337987000        103996
       30000        655075        449985000        119996
Descending arrays
    Array Size      Elapsed time      compCount      moveCount
        6000         61605         17997000        27023996
       10000        174148         49995000        75039996
       14000        340361         97993000        147055996
       18000        515529        161991000        243071996
       22000        787857        241989000        363087996
       26000       1130880        337987000        507103996
       30000       1532988        449985000        675119996
-----
Analysis of Radix Sort
Random arrays
    Array Size      Elapsed time
        6000          725
       10000         1809
       14000         2072
       18000         2448
       22000         2646
       26000         4268
       30000         3637
-----
Analysis of Radix Sort
Random arrays
    Array Size      Elapsed time
        6000          725
       10000         1809
       14000         2072
       18000         2448
       22000         2646
       26000         4268
       30000         3637
Ascending arrays
    Array Size      Elapsed time
        6000          725
       10000         1636
       14000         1848
       18000         2387
       22000         2587
       26000         4104
       30000         3498
Descending arrays
    Array Size      Elapsed time
        6000          725
       10000         1599
       14000         1826
       18000         2342
       22000         2592
       26000         4012
       30000         3506
Program ended with exit code: 0
All Output ↕

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Question3

a)



Note: In order to see the comparison between sorting algorithms clearly I have added two graphs instead of one. Because difference between selection sort and other algorithms was vast.

Selection sort algorithm always uses quadratic time which is $O(n^2)$ to complete its work. As it can be observed from the graph it is obviously the least fast algorithm. It has taken the most time because it had made every data move and every comparison possible to complete running. The time algorithm had taken did not diverge that much because the moves stayed the same no matter how array is sorted before. Its empirical results are in harmony with theoretical ones.

Merge sort algorithm uses $O(n \log n)$ in average of cases. It is a recursive algorithm whose strategy is divide, conquer and combine. It is slightly slower than quick sort and radix sort algorithm and it is probably due to its double memory usage. The time algorithm had taken diverges slightly and the best case happens when the array is sorted descendingly according to the results and its best case is still $O(n \log n)$.

Quick sort algorithm uses $O(n \log n)$ in average of cases. It is a recursive algorithm whose worst case is $O(n^2)$. It is the fastest algorithm in most of the cases in the results. The time algorithm had taken diverges a lot and the best case happens when the array is not sorted so, random. According to the results and its best case is still $O(n \log n)$.

Radix sort algorithm uses $O(n)$ in average of cases which is linear time. The time taken do not change no matter how array is sorted. However, as it can be observed in results it is not the fastest algorithm. Actually, its graph is similar to $O(n \log n)$. The result is a consequence of having many parallel loops and using n as ten times. Its empirical results differs from theoretical values.