Static Program Analysis For Security

Cambridge IB Tech Talks

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Overview

- 1. Introduction to Static Program Analysis
- 2. Lattices and Fixed Points
- 3. Data Flow Analysis
- 4. CodeQL

How to find bugs in code?

Dynamic Analysis (e.g. Unit Testing, Fuzzing)

- Done on a limited number of different inputs
- Often reveals the presence of errors but cannot guarantee their absence
- 100% test coverage != bug-free code
- Many tests are regressive and only added after a bug is found

Static Analysis: analyze code without executing it

- Can check all possible executions and provide guarantees about its behavior
- With the right tools, can catch bugs early in the development process
- Particularly useful for testing the absence of security vulnerabilities

How to find bugs in code?



Brenan Keller @brenankeller

A QA engineer walks into a bar. Orders a beer. Orders 0 beers. Orders 9999999999 beers. Orders a lizard. Orders -1 beers. Orders a ueicbksjdhd.

First real customer walks in and asks where the bathroom is. The bar bursts into flames, killing everyone.

1:21 PM · 30 Nov 18

Data Flow Analysis

A particular form of static analysis that examines how data moves through a program to answer questions such as:

- What values can reach this point in the code?
- Is this variable always initialized before it is used?
- Does untrusted data ever reach an unsafe function?

Partial Orders

Definition

A partial order (S, \sqsubseteq) is a set S equipped with a binary relation \sqsubseteq that is:

- Reflexive: $\forall x \in S, x \sqsubseteq x$
- Transitive: $\forall x, y, z \in S, x \sqsubseteq y \land y \sqsubseteq z \Rightarrow x \sqsubseteq z$
- Antisymmetric: $\forall x, y \in S, x \sqsubseteq y \land y \sqsubseteq x \Rightarrow x = y$
- $y \in S$ is an upper bound for X ($X \sqsubseteq y$) if $\forall x \in X, x \sqsubseteq y$
- $y \in S$ is the least upper bound for X ($X \coprod y$) if y is an upper bound for X and $\forall z \in S, X \sqsubseteq z \Rightarrow y \sqsubseteq z$
- $y \in S$ is a lower bound for X ($y \sqsubseteq X$) if $\forall x \in X, y \sqsubseteq x$
- $y \in S$ is the greatest lower bound for X ($y \sqcap X$) if y is a lower bound for X and $\forall z \in S, z \sqsubseteq X \Rightarrow z \sqsubseteq y$

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Lattices

Definition

A **lattice** (L, \sqsubseteq) is a partial order (L, \sqsubseteq) in which every pair of elements $x, y \in L$ has a least upper bound $x \sqcup y$ (join) and a greatest lower bound $x \sqcap y$ (meet).

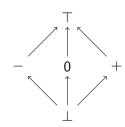
A **complete lattice** is a lattice in which every subset has a least upper bound and a greatest lower bound.

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Sign Analysis

As an example, we want to find the possible signs of integer variables and expressions. Consider the following abstract values for the sign of an integer:

- ⊤: unknown sign
- +: positive
- -: negative
- 0: zero
- \(\peraction\): not an integer, or unreachable code



This partial order, with edges for \sqsubseteq , forms a complete lattice. e.g. $+ \sqsubseteq \top$ means + is at least as precise as \top

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Sign Analysis

Let's create a **map lattice** $State = Var \rightarrow Sign$ that describes the sign of each variable. Derive a system of equations, one per line, using values from the lattice.

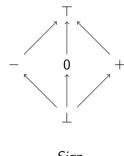
var a, b; // 1
a = 42; // 2
b = a + input(); // 3
a = a - b; // 4

$$x_1 = [a \mapsto \top, b \mapsto \top]$$

$$x_2 = x_1[a \mapsto +]$$

$$x_3 = x_2[b \mapsto x_2(a) + \top]$$

$$x_4 = x_3[a \mapsto x_3(a) - x_3(b)]$$



Sign

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Sign Analysis

$$x_1 = [a \mapsto \top, b \mapsto \top]$$
 $f_1(x_1, \dots, x_n) = [a \mapsto \top, b \mapsto \top]$
 $x_2 = x_1[a \mapsto +]$ $f_2(x_1, \dots, x_n) = x_1[a \mapsto +]$
 $x_3 = x_2[b \mapsto x_2(a) + \top]$ $f_3(x_1, \dots, x_n) = x_2[b \mapsto x_2(a) + \top]$
 $x_4 = x_3[a \mapsto x_3(a) - x_3(b)]$ $f_4(x_1, \dots, x_n) = x_3[a \mapsto x_3(a) - x_3(b)]$

Generalised equation system over a lattice L, with functions $f_i: L^n \to L$:

$$x_1 = f_1(x_1, \dots, x_n)$$

$$x_2 = f_2(x_1, \dots, x_n)$$

$$\vdots$$

$$x_n = f_n(x_1, \dots, x_n)$$

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Monotonicity and Fixed Points

Generalised equation system over a lattice L, with functions $f_i: L^n \to L$:

$$x_1 = f_1(x_1, \dots, x_n)$$

$$x_2 = f_2(x_1, \dots, x_n)$$

$$\vdots$$

$$x_n = f_n(x_1, \dots, x_n)$$

Combine the *n* functions into $F: L^n \to L^n$:

$$F(x_1,...,x_n) = (f_1(x_1,...,x_n),...,f_n(x_1,...,x_n))$$

= $(x_1,...,x_n)$

Then we are looking for x = F(x), i.e. a fixed point of F.

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Monotonicity and Fixed Points

Definition

A function $f: L_1 \to L_2$ is **monotone** if $\forall x, y \in L_1, x \sqsubseteq y \Rightarrow f(x) \sqsubseteq f(y)$

More precise input leads to more precise output

Theorem

Kleene's Fixed Point Theorem: In a complete lattice L with finite height, every monotone function $f: L \to L$ has a unique least fixed point $\bigsqcup_{i=0}^{\infty} f^i(\bot)$

These results generalise to functions that take multiple arguments $f: L^n \to L$ that are monotone in each argument – such as the ones we derived for sign analysis.

Corollary

For an equation system over complete lattices of finite height with monotone constraint functions, a unique, most precise solution always exists

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Computing the Least Fixed Point

Algorithm 1 Naive Fixed Point Algorithm

```
1: procedure NAIVEFIXEDPOINT(F)
2: x := \bot
3: while x \neq F(x) do
4: x := F(x)
5: end while
6: return x
```

7: end procedure

In each iteraction, all of f_1, \ldots, f_4 are applied. But f_2 depends only on x_1 , and the value of x_1 is unchanged in most iterations. We'll see a more efficient way later.

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Data Flow Analysis

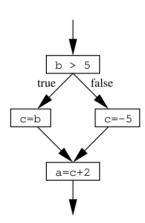
Main idea: we want to find the possible values of variables at each point in the program.

- In compilers: used for optimisations (e.g. constant propagation)
- In security: used to find vulnerabilities (e.g. untrusted data reaching a sink)

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Control Flow Graph

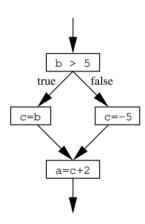
- In our previous example, we had a sequence of statements with no branches
- In general, we have a control flow graph (CFG) with basic blocks and edges



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Abstract States

- Recall: each element of the lattice State = Var → Sign is an abstract state that maps variables to signs
- For each CFG node v, let the constraint variable [[v]] be the abstract state at the program point immediately after v
- We have a lattice Stateⁿ of abstract states, where n is the number of CFG nodes

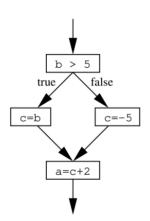


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Constraint Rules

We need to combine the abstract states of the predecessors of a node to get the abstract state of the node itself.

$$\mathsf{JOIN}(v) = \bigsqcup_{u \in \mathsf{pred}(v)} [[u]]$$



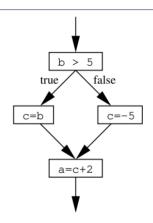
$$\mathsf{JOIN}([[a = c + 2]]) = [[c = b]] \sqcup [[c = -5]]$$

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Constraint Rules

$$[[c = b]] = [b \mapsto +, c \mapsto +]$$
$$[[c = -5]] = [b \mapsto \top, c \mapsto -]$$

JOIN([[
$$a = c + 2$$
]]) = [[$c = b$]] \sqcup [[$c = -5$]]
= [$b \mapsto \top, c \mapsto \top$]



$$[[a = c + 2]] = \mathsf{JOIN}([[a = c + 2]])[a \mapsto eval(\mathsf{JOIN}([[a = c + 2]]), c + 2)]$$
$$= [a \mapsto \top, b \mapsto \top, c \mapsto \top]$$

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Solving Data Flow Equations

Generalised equation system over a lattice L, with functions $f_i: L^n \to L$:

$$\begin{aligned} [[v_1]] &= f_{v_1}([[v_1]], \dots, [[v_n]]) \\ [[v_2]] &= f_{v_2}([[v_1]], \dots, [[v_n]]) \\ &\vdots \\ [[v_n]] &= f_{v_n}([[v_1]], \dots, [[v_n]]) \end{aligned}$$

Combine the *n* functions into $F: L^n \to L^n$:

$$F([[v_1]], \ldots, [[v_n]]) = (f_{v_1}([[v_1]], \ldots, [[v_n]]), \ldots, f_{v_n}([[v_1]], \ldots, [[v_n]])$$

$$= ([[v_1]], \ldots, [[v_n]])$$

Then we are looking for x = F(x), i.e. a fixed point of F.

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A More Efficient Algorithm

Algorithm 2 Simple Worklist Algorithm

```
1: procedure SIMPLEWORKLIST(F)
      (x_1,\ldots,x_n):=(\perp,\ldots,\perp)
     W := \{v_1, \dots, v_n\}
      while W \neq \emptyset do
 5:
      v_i := W.pop()
      y:=f_{v_i}(x_1,\ldots,x_n)
      if y \neq x_i then
               x_i := v
               for v_i \in dep(v_i) do
                    W.add(v_i)
10.
11:
               end for
12.
           end if
13:
        end while
        return (x_1, \ldots, x_n)
14:
15: end procedure
```

```
Insight: most f_{v_i} will only read the
values from a few other variables.
instead of all [[v_1]], \ldots, [[v_n]].
dep(v_i) is the set of nodes that depend
on v_i (i.e. the successors of v_i)
```

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Taint Tracking

- Can we tell which computations may involve "tainted" data?
- i.e. data that comes from an untrusted source
- e.g. user input, HTTP responses, environment variables

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Taint Tracking

The approach is similar! We just define different abstract values and equations.

- Abstract taint values:
 - T: Unknown taint status.
 - T: Tainted.
 - U: Untainted.
 - ⊥: Unreachable.
- Ordering: $\bot \sqsubseteq U \sqsubseteq T \sqsubseteq \top$
- **Abstract state:** A mapping $\sigma : Var \rightarrow \{\bot, U, T, \top\}$.
- Transfer functions: e.g. for an assignment x := y op z, define

$$f(\sigma) = \sigma[x \mapsto \sigma(y) \sqcup \sigma(z)]$$

i.e. if either operand is tainted, the result is tainted

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In Practice: CodeQL

A tool developed by Semmle (a spin-out company from Oxf*rd), now acquired by GitHub. Used with CLI or GitHub integration (free for all public repos!)

- The source code is compiled into a relational database, which includes information about the control flow graph, data flow, and other properties of the code.
- The user writes queries in a high-level language called QL, which is executed by the CodeQL engine.
- The engine uses fixed-point algorithms to perform data flow analysis.
- Results are exported into the SARIF format which can be consumed by CI tools or custom integrations.

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Let's Go On A Little Adventure

- Next.js, the most popular React framework, has some weird, poorly documented URL parsing semantics that does not conform to the widely accepted WHATWG URL standard
- This is unexpected behaviour, and often results in wrong URL validation
- ullet Made a responsible disclosure pprox 1 year ago, still not fixed

Let's query open-source GitHub projects to find instances of this bug!

- Common design pattern: unauthenticated user visits /admin, gets redirected to /login?next=/admin, logs in, and gets redirected back to /admin
- Use Next.js URL parsing trickery to turn a "normal" URL into javascript:sendToAttacker(authToken) at the final step

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Taint Tracking in CodeQL

We want to find all instances where untrusted user input (source) reaches a sensitive function (sink) without being sanitized.

```
import javascript
3 class UnsafeRouterPushConfiguration extends TaintTracking::Configuration {
    UnsafeRouterPushConfiguration() { this = "UnsafeRouterPushConfiguration" }
    override predicate isSource(DataFlow::Node source) {}
    override predicate isSink(DataFlow::Node sink) {}
9 }
  from DataFlow::PathNode source, DataFlow::PathNode sink, UnsafeRouterPushConfiguration config
  where config.hasFlowPath(source, sink)
  select sink.getNode(). "Potentially unsafe router.push with $0.". source.getNode().
    "untrusted input"
```

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Defining Sources

You can also extend this with custom logic, to incorporate codebase-specific patterns e.g. RPC calls, deserialization, etc.

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Defining Sinks

```
override predicate isSink(DataFlow::Node sink) {
   exists(DataFlow::MethodCallNode call, DataFlow::Node receiver |
     call.getMethodName() = "push" and
     call.getReceiver() = receiver and
     receiver.getALocalSource().(DataFlow::InvokeNode).getCalleeName() = "useRouter" and
     sink = call.getArgument(0)
   )
}
```

```
isSink(node) \triangleq \exists call, receiver . call invokes the .push method on receiver \land \exists invocation . invocation is useRouter() \land invocation \rightarrow^* receiver\land node = args(call)[0]
```

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Changing the Transfer Function

```
override predicate isAdditionalTaintStep(DataFlow::Node pred, DataFlow::Node succ) {
  exists(DataFlow::ArrayCreationNode array |
    pred = array.getAnElement() and
    succ = array
  exists(DataFlow::MethodCallNode call |
    call.getMethodName().regexpMatch("find|filter|some|every|map") and
    pred = call.getReceiver() and
    succ = call.getABoundCallbackParameter(1, 0)
```

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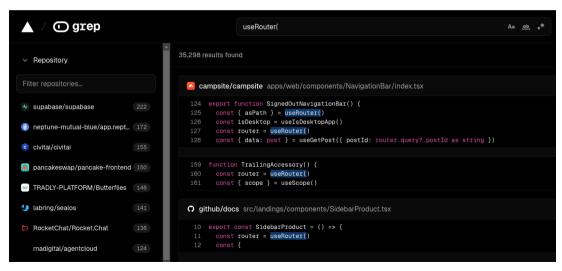
Changing the Transfer Function

```
override predicate isSanitizer(DataFlow::Node node) {
   node = DataFlow::moduleImport("dompurify").getAMemberCall("sanitize")
}
```

Any results from DOMPurify.sanitize are treated as untainted. Know your assumptions!

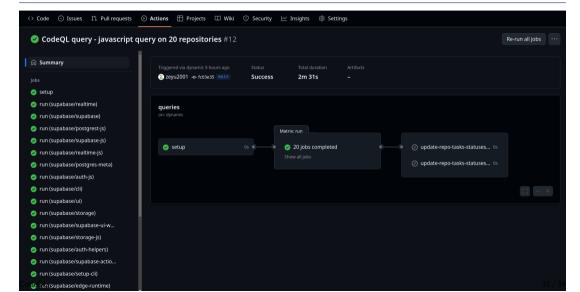
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Let's Go Hunting



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Let's Go Hunting



Limitations

CodeQL is very useful as a CI integration to catch security issues early in the development process, and provide guarantees about your code. But it's really hard to get right . . .

- We need to create custom taint specifications for third-party library APIs.
- False positives: even if tainted data reaches a sink, it may not always be exploitable

 some other conditions may need to be met
- Requires a good understanding of the codebase and the problem domain, and lots of fine-tuning to get good results – only as good as the queries you write

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Alternative Approaches

- **Symbolic execution**: represent the program inputs symbolically and explore all possible paths through the program, generating constraints on the inputs such that a certain path is taken
- Ziyang Li, Saikat Dutta, and Mayur Naik. LLM-assisted static analysis for detecting security vulnerabilities, 2024

IRIS leverages LLMs to infer taint specifications and perform contextual analysis, alleviating needs for human specifications and inspection . . .

A state-of-the-art static analysis tool CodeQL detects only 27 of these vulnerabilities whereas IRIS with GPT-4 detects 55 (+28) and improves upon CodeQL's average false discovery rate by 5% points.

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References

- [1] Anders Møller and Michael I. Schwartzbach. *Static Program Analysis*. November 2020.
- [2] Oege de Moor, Mathieu Verbaere, Elnar Hajiyev, Pavel Avgustinov, Torbjorn Ekman, Neil Ongkingco, Damien Sereni, and Julian Tibble. Keynote address: .ql for source code analysis. In Seventh IEEE International Working Conference on Source Code Analysis and Manipulation (SCAM 2007), pages 3–16, 2007.
- [3] Ziyang Li, Saikat Dutta, and Mayur Naik. LLM-assisted static analysis for detecting security vulnerabilities, 2024.

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