## 02-750

# Assignment 3

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### HW3q1

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```
[1]: import numpy as np
     import random
     import matplotlib.pyplot as plt
     from sklearn.model_selection import train_test_split
     from sklearn import preprocessing
     from sklearn.utils import shuffle
     from sklearn.gaussian_process import GaussianProcessRegressor
     from sklearn.ensemble import RandomForestRegressor
     from sklearn.gaussian_process.kernels import Matern,RBF,WhiteKernel,DotProduct
     from sklearn.metrics import r2_score
     from warnings import simplefilter
     from sklearn.exceptions import ConvergenceWarning
     from modAL.uncertainty import uncertainty_sampling
     from modAL.models import BayesianOptimizer, ActiveLearner, CommitteeRegressor
     from modAL.acquisition import max_EI
     from modAL.disagreement import max_std_sampling, max_disagreement_sampling
     import seqlogo
     import copy
     ### Set random seed
     seed = 5
     random.seed(seed)
     np.random.seed(seed)
[2]: data = np.loadtxt('hw3_data.csv', dtype = str, delimiter = ',')[1:]
     peptide = data[:,2]
     def create_ohe_dictionary(peptide):
```

ohe\_dict = {}
encoding = 0

for i in range(len(peptide)):

for j in range(len(peptide[i])):

```
if peptide[i][j] not in ohe_dict.keys():
                ohe_dict[peptide[i][j]] = encoding
                encoding += 1
    return ohe_dict
ohe_dict = create_ohe_dictionary(peptide)
def ohe_row(peptide_string, ohe_dict):
    idx = 0
    row = np.zeros(shape=9*len(ohe_dict))
    for aa in peptide string:
        row[idx + ohe_dict[aa]] = 1
        idx += len(ohe dict)
    return row
def one_hot_encoding(peptide, ohe_dict):
    ohe_encoding_peptide = np.zeros(shape=(len(peptide), 9 * len(ohe_dict)))
    for i in range(len(peptide)):
        ohe_encoding_peptide[i] = ohe_row(peptide[i], ohe_dict)
    return ohe_encoding_peptide
X = one_hot_encoding(peptide, ohe_dict)
y = data[:,3].astype('float64')
```

#### [6]: X\_train, X\_test, y\_train, y\_test = train\_test\_split(X, y, test\_size=0.33)

```
[7]: # RandomForestRegressor with random query
     X_train_random = copy.deepcopy(X_train)
     y_train_random = copy.deepcopy(y_train)
     regressor = ActiveLearner(
         estimator=RandomForestRegressor(),
         query_strategy=uncertainty_sampling,
         X_training=X_train_random[0].reshape(1, -1),
         y_training=y_train_random[np.array(0)].reshape(1),
     n_queries = 2000
     for idx in range(n_queries):
         query_idx = np.random.randint(len(X_train_random))
         regressor.teach(X_train_random[query_idx].reshape(1, -1), y_train_random[np.
     →array(query_idx)].reshape(1))
         X_train_random, y_train_random = (np.delete(X_train_random, query_idx,__
     →axis=0), np.delete(y_train_random, query_idx))
         if idx % 100 == 0:
             y_pred_final = regressor.predict(X_test)
             y_train_pred = regressor.predict(X_train)
```

```
r2_test = r2_score(y_test, y_pred_final)
             r2_train = r2_score(y_train, y_train_pred)
             print("[%d/%d]\tR2 train:\t%.4f\tR2 test:\t%.4f" %(idx, n_queries,__
      →r2_train, r2_test))
     y pred final = regressor.predict(X test)
     y_train_pred = regressor.predict(X_train)
     r2_test = r2_score(y_test,y_pred_final)
     r2_train = r2_score(y_train,y_train_pred)
     # print(y_test,y_pred_final,y_train_pred)
     print("R2 train:\t %.4f" %(r2_train))
     print("R2 test:\t %.4f" %(r2_test))
    [0/2000]
                    R2 train:
                                     -0.8543 R2 test:
                                                             -0.8299
                                     0.2774 R2 test:
    [100/2000]
                    R2 train:
                                                             0.2764
    [200/2000]
                                     0.4214 R2 test:
                                                             0.4013
                    R2 train:
    [300/2000]
                    R2 train:
                                     0.4382 R2 test:
                                                             0.4211
                                     0.4588 R2 test:
    [400/2000]
                    R2 train:
                                                             0.4219
    [500/2000]
                    R2 train:
                                     0.4977 R2 test:
                                                             0.4487
                    R2 train:
                                     0.5131 R2 test:
    [600/2000]
                                                             0.4607
    [700/2000]
                    R2 train:
                                     0.5428 R2 test:
                                                             0.4846
                    R2 train:
                                     0.5514 R2 test:
    [800/2000]
                                                             0.4857
    [900/2000]
                    R2 train:
                                     0.5723 R2 test:
                                                             0.5055
    [1000/2000]
                    R2 train:
                                     0.5999 R2 test:
                                                             0.5242
    [1100/2000]
                    R2 train:
                                     0.6053 R2 test:
                                                             0.5190
    [1200/2000]
                    R2 train:
                                     0.6048 R2 test:
                                                             0.5210
    [1300/2000]
                    R2 train:
                                     0.6174 R2 test:
                                                             0.5301
    [1400/2000]
                    R2 train:
                                     0.6215 R2 test:
                                                             0.5293
    [1500/2000]
                    R2 train:
                                     0.6275 R2 test:
                                                             0.5224
                                     0.6378 R2 test:
    [1600/2000]
                    R2 train:
                                                             0.5215
    [1700/2000]
                    R2 train:
                                     0.6502 R2 test:
                                                             0.5275
                                     0.6631 R2 test:
    [1800/2000]
                    R2 train:
                                                             0.5336
    [1900/2000]
                                     0.6703 R2 test:
                    R2 train:
                                                             0.5337
    R2 train:
                     0.6786
    R2 test:
                     0.5397
[8]: simplefilter("ignore", category=ConvergenceWarning)
     # activeGaussianProcessRegressor with active sampling
     X_train_active = X_train.copy()
     y_train_active = y_train.copy()
     kernel = DotProduct(sigma_0=1.5)+WhiteKernel()
     learners = [
         ActiveLearner(
             estimator=GaussianProcessRegressor(kernel = kernel),
```

```
X_training=X_train_active[idx].reshape(1, -1),
        y_training=y_train_active[np.array(idx)].reshape(1),
    ) for idx in range(4)
committee = CommitteeRegressor(
    learner_list = learners,
    query_strategy = max_std_sampling,
)
n_queries = 2000
for idx in range(n_queries):
    query_idx,_ = committee.query(X_train_active)
    committee.teach(X_train_active[query_idx].reshape(1, -1), y_train_active[np.
 →array(query_idx)].reshape(1))
    X_train_active, y_train_active = (np.delete(X_train_active, query_idx,__
 →axis=0), np.delete(y_train_active, query_idx))
    if idx % 100 == 0:
        y_pred_final = committee.predict(X_test, return_std = False)
        y_train_pred = committee.predict(X_train, return_std = False)
        r2_test = r2_score(y_test, y_pred_final)
        r2_train = r2_score(y_train, y_train_pred)
        print("[%d/%d]\tR2 train:\t%.4f\tR2 test:\t%.4f" %(idx, n_queries,_
 →r2_train, r2_test))
y_pred_final = committee.predict(X_test, return_std = False)
y_train_pred = committee.predict(X_train, return_std = False)
r2_test = r2_score(y_test, y_pred_final)
r2_train = r2_score(y_train, y_train_pred)
# print(y_test,y_pred_final,y_train_pred)
print("R2 train:\t %.4f" %(r2_train))
print("R2 test:\t %.4f" %(r2_test))
[0/2000]
                R2 train:
                                -1.6069 R2 test:
                                                        -1.5795
[100/2000]
                R2 train:
                                0.1704 R2 test:
                                                        0.1232
[200/2000]
                R2 train:
                                0.1088 R2 test:
                                                        0.0704
                                0.3947 R2 test:
                R2 train:
[300/2000]
                                                        0.3574
[400/2000]
               R2 train:
                                0.4907 R2 test:
                                                        0.4531
                                0.5065 R2 test:
                                                        0.4732
[500/2000]
                R2 train:
[600/2000]
                R2 train:
                                0.5356 R2 test:
                                                        0.5005
[700/2000]
               R2 train:
                                0.5474 R2 test:
                                                        0.5137
                R2 train:
                                0.5790 R2 test:
[800/2000]
                                                        0.5485
[900/2000]
               R2 train:
                                0.5865 R2 test:
                                                        0.5541
[1000/2000]
               R2 train:
                                0.5934 R2 test:
                                                        0.5636
[1100/2000]
               R2 train:
                                0.6058 R2 test:
                                                        0.5766
[1200/2000]
               R2 train:
                                0.6131 R2 test:
                                                        0.5811
```

```
[1300/2000]
                 R2 train:
                                   0.6164
                                                             0.5841
                                            R2 test:
                 R2 train:
                                   0.6243
[1400/2000]
                                            R2 test:
                                                             0.5906
[1500/2000]
                                   0.6280
                                            R2 test:
                                                             0.5961
                 R2 train:
[1600/2000]
                                   0.6325
                                                             0.6007
                 R2 train:
                                            R2 test:
[1700/2000]
                 R2 train:
                                   0.6329
                                            R2 test:
                                                             0.5994
[1800/2000]
                                   0.6367
                                                             0.6031
                 R2 train:
                                            R2 test:
[1900/2000]
                 R2 train:
                                   0.6390
                                            R2 test:
                                                             0.6038
R2 train:
                  0.6404
```

R2 train: 0.6404 R2 test: 0.6048

#### 0.1 Questions:

- 1. Done (see code)
- 2. Done (see code)
- 3. We use committee regressor. It contains three guassian process regressor using a combination of DotProduct and WhiteKernel. Each regressor intializes with different training samples.
- 4. Active Learner:  $R^2 = 0.6048$ . Number of n gueries = 2000
- 5. Random Forest regressor with random query:  $R^2 = 0.5337$ . Number of n\_queries = 2000
- 6. Comparison: With same amount of training data (2000 queries), committee regressor achieves higher  $R^2$  score than random forest regressor with random query. Random forest regressor has a higher  $R^2$  score than committee regressor. However, when number of queries increase, committee regressor outperforms random forest regressor.

Within the first 1000 queries, random forest regressor achieves  $R^2 = 0.5999$  in training set and  $R^2 = 0.5242$  in test set. However, the final  $R^2 = 0.6703$  in training set and  $R^2 = 0.5337$  in test set. It implies that in 1000-2000 queries, random forest regressor begins the overfit the training data and there is no large improvement of  $R^2$  in test set.

Within the first 1000 queries, committee regressor achieves  $R^2 = 0.5934$  in training set and  $R^2 = 0.5636$  in test set. It behaves better than random forest regressor in test set. It finally achieves is  $R^2 = 0.6390$  in training set and  $R^2 = 0.6038$  in test set. We notice that compared to random forest regressor, committee regressor has a higher  $R^2$  in test set and a lower  $R^2$  in training set. During queries 1000-2000, committee regressor continues to achieves higher  $R^2$  in test set which means that it does learn something.

Therefore, from comparison above, committee regressor with active learning achieves higher  $R^2$  in the same amount of queries than random forest regressor with random query. It also reduces overfitting of the model.

[]:

### HW3q2

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### 1 Question 2 (50 points)

In this question, you will simulate a peptide design experiment, trying to find peptides with high binding affinity to MHC class I using a bayesian optimization approach. Notice the goal here is not trying to find a peptide sequence that maximize the binding affinity to MHC, Since a sizable proportion of the sequence data we are using contains maximum binding affinity out of the data (9.0). Using the same feature encoding as question 1, we will examine several techniques to maximize the percentage of sequence with affinity of 9.0 for stringent querying.

```
[1]: import numpy as np
     import random
     import matplotlib.pyplot as plt
     from sklearn.model selection import train test split
     from sklearn import preprocessing
     from sklearn.utils import shuffle
     from sklearn.gaussian_process import GaussianProcessRegressor
     from sklearn.gaussian process.kernels import Matern
     from sklearn.ensemble import RandomForestRegressor
     from modAL.models import BayesianOptimizer
     from modAL.acquisition import max_EI
     import seqlogo
     import copy
     ### Set randome seed
     seed = 5
     random.seed(seed)
     np.random.seed(seed)
```

#### 2 Reading and Processing the Data¶

```
[2]: data = np.loadtxt('hw3_data.csv', dtype = str, delimiter = ',')[1:]
     ### TO DO
     peptide = data[:,2]
     encode_order = 'ACDEFGHIKLMNPQRSTVWY'
     def create ohe dictionary(encode order):
         ohe_dict = {}
         encoding = 0
         for i in range(len(encode_order)):
             ohe_dict[encode_order[i]] = encoding
             encoding += 1
         return ohe_dict
     ohe_dict = create_ohe_dictionary(encode_order)
     def ohe_row(peptide_string, ohe_dict):
         idx = 0
         row = np.zeros(shape=9*len(ohe_dict))
         for aa in peptide string:
             row[idx + ohe_dict[aa]] = 1
             idx += len(ohe dict)
         return row
     def one_hot_encoding(peptide, ohe_dict):
         ohe encoding peptide = np.zeros(shape=(len(peptide), 9 * len(ohe dict)))
         for i in range(len(peptide)):
             ohe_encoding_peptide[i] = ohe_row(peptide[i], ohe_dict)
         return ohe_encoding_peptide
    X = one_hot_encoding(peptide, ohe_dict)
     y = data[:,3].astype('float64')
```

#### 3 2.1: Random Sampling (5 pts. total)

Create a random query strategy for randomly selecting a sample to query from the data. If the data selected is a new sequence with binding affnity of 9.0, append it to a list. After each query selection, measure the percentage of sequence with binding affnity 9.0 found by the strategy. Do this for 200 sampling steps. This will serve as the baseline to compare with optimizator performance in section 2.2 and 2.3.

```
[3]: X_cp = copy.deepcopy(X)
y_cp = copy.deepcopy(y)
optimal_idx_rand = []
history_rand = []
cnt = 0
### TO DO
```

```
n_query = 200
for i in range(n_query):
    idx = np.random.randint(0, len(y_cp))
    if y_cp[idx] == 9.0:
        cnt += 1
        optimal_idx_rand.append(X_cp[idx])
    history_rand.append(cnt / (i+1))
    X_cp, y_cp = np.delete(X_cp, idx, axis=0), np.delete(y_cp, idx)
```

#### 4 2.2: Baysian Optimization with Gaussian Process (15 pts. total)

Create a Baysian optimizer with Gaussian process as regressor and Max Expected improvement as the queuing strategy. If the data selected is a new sequence with binding affinity of 9.0, append it to a list. After each query selection, measure the percentage of sequence with binding affinity 9.0 found by the strategy. Do this for 200 sampling steps.

Hint: Check the modAL documentation for how to set up a Baysian optimizer.

```
[4]: X_cp = copy.deepcopy(X)
     y_{cp} = copy.deepcopy(y)
     optimal_idx_gp = []
     history_gp = []
     arr = np.arange(len(X_cp))
     np.random.shuffle(arr)
     ### TO DO
     # initializing the optimizer
     optimizer = BayesianOptimizer(
         estimator=GaussianProcessRegressor(),
         X_training=X_cp[arr[:10]],
         y training=y cp[arr[:10]],
         query_strategy=max_EI
     # Bayesian optimization
     cnt = 0
     for i in range(n_query):
         query_idx, query_inst = optimizer.query(X_cp)
         optimizer.teach(X_cp[query_idx].reshape(1, -1), y_cp[np.array(query_idx)].
      \rightarrowreshape(1))
         if y_cp[query_idx] == 9.0:
             cnt += 1
             optimal_idx_gp.append(X_cp[query_idx])
         history_gp.append(cnt / (i+1))
         X_cp, y_cp = np.delete(X_cp, query_idx, axis=0), np.delete(y_cp, query_idx)
```

#### 5 2.3: Bayesian Optimizer with Random Forest (10 pts. total)

Although Baysian optimization often uses the Gaussian process, Baysian optimizer in ModAL can take any other regressor that has a predict function with a return\_std input parameter. If return\_std is set to True, the function returns the predicted values and standard deviation in the prediction. Create a Baysian optimizer with random forest regressor and Max Expected improvement as the queuing strategy. If the data selected is a new sequence with binding affinity of 9.0, append it to a list. After each query selection, measure the percentage of sequences with binding affinity 9.0 found by the strategy. Do this for 200 sampling steps.

**Hint**: You might find the following class wrapper for random forest helpful.

```
[5]: class rfwapper(RandomForestRegressor):
    def predict(self, X, return_std = False):
        if return_std:
            ys = np.array([e.predict(X) for e in self.estimators_])
            return np.mean(ys, axis = 0).ravel(), (np.std(ys, axis = 0).ravel()_\(\subsetep \text{ \infty} + 1e-6)\)
        return super().predict(X).ravel()
```

```
[6]: X_cp = copy.deepcopy(X)
     y_cp = copy.deepcopy(y)
     optimal_idx_rf = []
     history_rf = []
     arr = np.arange(len(X_cp))
     np.random.shuffle(arr)
     ### TO DO
     # initializing the optimizer
     optimizer = BayesianOptimizer(
         estimator=rfwapper(),
         X_training=X_cp[arr[:10]],
         y_training=y_cp[arr[:10]],
         query_strategy=max_EI
     # Bayesian optimization
     cnt = 0
     n_query = 200
     for i in range(n_query):
         query_idx, query_inst = optimizer.query(X_cp)
         optimizer.teach(X_cp[query_idx].reshape(1, -1), y_cp[np.array(query_idx)].
      \rightarrowreshape(1))
         if y_cp[query_idx] == 9.0:
             cnt += 1
             optimal_idx_rf.append(X_cp[query_idx])
         history_rf.append(cnt / (i+1))
         X_cp, y_cp = np.delete(X_cp, query_idx, axis=0), np.delete(y_cp, query_idx)
```

6 2.4: Plot Percentage of sequence with maximum binding affinity with respect to number of sequence queried (10 pts. total)

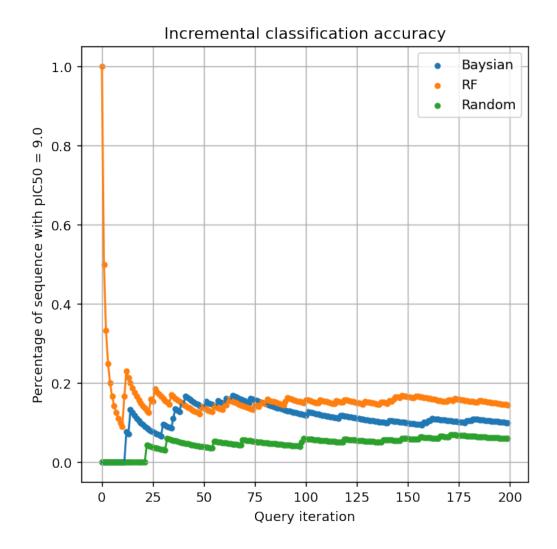
```
[7]: # Plot our performance over time.
fig, ax = plt.subplots(figsize=(6, 6), dpi=130)

ax.plot(history_gp)
ax.scatter(range(len(history_gp)), history_gp, s=13, label = 'Baysian')

ax.plot(history_rf)
ax.scatter(range(len(history_rf)), history_rf, s=13, label = 'RF')

ax.plot(history_rand)
ax.scatter(range(len(history_rand)), history_rand, s=13, label = 'Random')
ax.grid(True)

ax.set_title('Incremental classification accuracy')
ax.set_xlabel('Query iteration')
ax.set_ylabel('Percentage of sequence with pIC50 = 9.0')
ax.legend()
plt.show()
```



## 7 2.5: Create sequence logo based on sequences found with each querying strategies (5 pts. total)

A sequence logo is a graphical representation of the sequence conservation of amino acids in protein sequences), as amino acids that are important for functions are likely to be conserved. Hence, a sequence logo is a way to visualize such an importance. Convert the each sets of sequences obtained by one of your optimization strategies to a sequence logo. Below is an example using all of the sequence of affinity 9.0.

**Important**: We are using seqlogo to create sequence logo from our set of sequences. You can install seqlogo by entering the command

conda install -c bioconda seqlogo

in your conda terminal

```
[10]: X_rf = optimal_idx_rf
ppm = np.sum(X_rf, axis = 0).reshape(20,9)
ppm /= np.sum(ppm, axis = 0)
ppm = seqlogo.Ppm(ppm, alphabet_type="AA")
seqlogo.seqlogo(ppm, ic_scale = False, format = 'jpeg', size = 'medium')
```

[10]:

