

# Example\_Assignment\_2\_Layout

October 16, 2018

## 1 Assignment 2

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Due Wednesday, Oct. 17 at 11:30 AM

```
In [1]: # Import packages
import numpy as np
import pandas as pd
import statsmodels.api as sm
import matplotlib.pyplot as plt
```

```
C:\ProgramData\Anaconda3\lib\site-packages\statsmodels\compat\pandas.py:56: FutureWarning: The
from pandas.core import datetools
```

### 1.0.3 1. Imputing age and gender

(a) Here is where I will describe my proposed strategy ... and so on and so forth. Regress 'age' and 'female' on 'weight' and 'total income' using the data from SurveyIncome.txt. Using linear model for 'age' and logit model for 'female'. That is:

$$age = \beta_1 * tot\_inc + \beta_2 * wgt + cons$$

$$female = \frac{e^{\alpha_1 * tot\_inc + \alpha_2 * wgt + cons}}{1 + e^{\alpha_1 * tot\_inc + \alpha_2 * wgt + cons}}$$

Then use regression functions to predict 'age' and 'female' variable in BestIncome.txt.

(b) Here is where I'll use my proposed method from part (a) to impute variables.

```
In [2]: df = pd.read_csv("SurvIncome.txt", index_col=0, header = None).reset_index()
df.columns = ['tot_inc', 'wgt', 'age', 'female']
df['const'] = 1
reg1 = sm.OLS(endog=df['age'], exog=df[['tot_inc', 'wgt', 'const']], missing='drop')
result1 = reg1.fit()
reg2 = sm.Logit(endog=df['female'], exog=df[['tot_inc', 'wgt', 'const']], missing='drop')
```

```

result2 = reg2.fit()
df2 = pd.read_csv("BestIncome.txt", index_col=0, header = None).reset_index()
df2.columns = ['lab_inc', 'cap_inc', 'hgt', 'wgt']
df2['const'] = 1
df2['tot_inc'] = df2['lab_inc'] + df2['cap_inc']
df2['age'] = result1.predict(exog=df2[['tot_inc', 'wgt', 'const']])
df2['female'] = result2.predict(exog=df2[['tot_inc', 'wgt', 'const']])
df2['female'][df2['female'] >= 0.5] = 1
df2['female'][df2['female'] < 0.5] = 0

```

Optimization terminated successfully.

Current function value: 0.036050

Iterations 11

C:\ProgramData\Anaconda3\lib\site-packages\ipykernel\_launcher.py:14: SettingWithCopyWarning:  
A value is trying to be set on a copy of a slice from a DataFrame

See the caveats in the documentation: <http://pandas.pydata.org/pandas-docs/stable/indexing.html>

C:\ProgramData\Anaconda3\lib\site-packages\ipykernel\_launcher.py:15: SettingWithCopyWarning:  
A value is trying to be set on a copy of a slice from a DataFrame

See the caveats in the documentation: <http://pandas.pydata.org/pandas-docs/stable/indexing.html>  
from ipykernel import kernelapp as app

**(c) Here is where I'll report the descriptive statistics for my new imputed variables.**

```

In [3]: print(df2['age'].describe())
        print(df2['female'].describe())

```

```

count      10000.000000
mean         44.890828
std           0.219150
min          43.976495
25%          44.743776
50%          44.886944
75%          45.038991
max          45.703819
Name: age, dtype: float64
count      10000.000000
mean         0.454600
std           0.497959
min           0.000000
25%           0.000000
50%           0.000000
75%           1.000000

```

```
max          1.000000
Name: female, dtype: float64
```

#### (d) Correlation matrix for the now six variables

```
In [4]: ols_df = df2[['lab_inc', 'cap_inc', 'hgt', 'wgt', 'age', 'female']]
        corr = ols_df.corr()
        corr.style.background_gradient()
```

```
Out[4]: <pandas.io.formats.style.Styler at 0x28737763208>
```

### 1.0.4 2. Stationarity and data drift

#### (a) Estimate by OLS and report coefficients

```
In [5]: df3 = pd.read_csv("IncomeIntel.txt", index_col=0, header = None).reset_index()
        df3.columns = ['grad_year', 'gre_qnt', 'salary_p4']
        df3['const'] = 1
        reg3 = sm.OLS(endog=df3['salary_p4'], exog=df3[['gre_qnt', 'const']], missing='drop')
        result3 = reg3.fit()
        print(result3.summary())
```

```

                                OLS Regression Results
=====
Dep. Variable:                  salary_p4      R-squared:                0.263
Model:                            OLS      Adj. R-squared:            0.262
Method:                 Least Squares      F-statistic:                 356.3
Date:                Tue, 16 Oct 2018      Prob (F-statistic):        3.43e-68
Time:                  18:24:24      Log-Likelihood:            -10673.
No. Observations:                1000      AIC:                       2.135e+04
Df Residuals:                     998      BIC:                       2.136e+04
Df Model:                           1
Covariance Type:                nonrobust
=====

```

	coef	std err	t	P> t	[0.025	0.975]
gre_qnt	-25.7632	1.365	-18.875	0.000	-28.442	-23.085
const	8.954e+04	878.764	101.895	0.000	8.78e+04	9.13e+04

```

=====
Omnibus:                        9.118      Durbin-Watson:                1.424
Prob(Omnibus):                  0.010      Jarque-Bera (JB):              9.100
Skew:                           0.230      Prob(JB):                      0.0106
Kurtosis:                       3.077      Cond. No.                      1.71e+03
=====

```

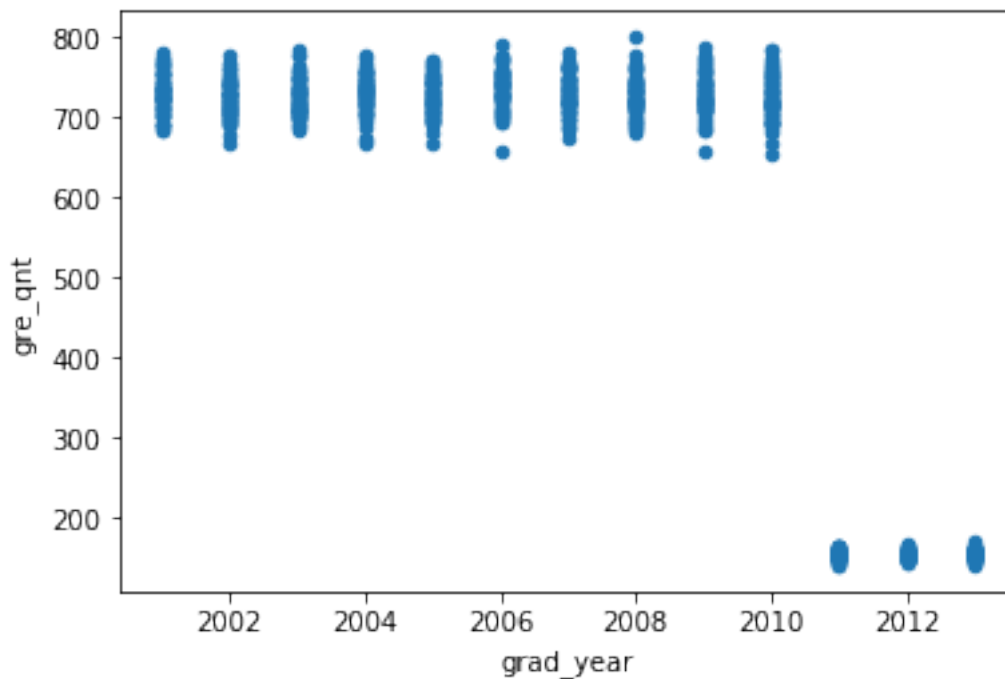
#### Warnings:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 1.71e+03. This might indicate that there are

strong multicollinearity or other numerical problems.

**(b) Create a scatterplot of GRE score and graduation year.**

```
In [6]: df3.plot(x='grad_year', y='gre_qnt', kind='scatter')  
plt.show()
```

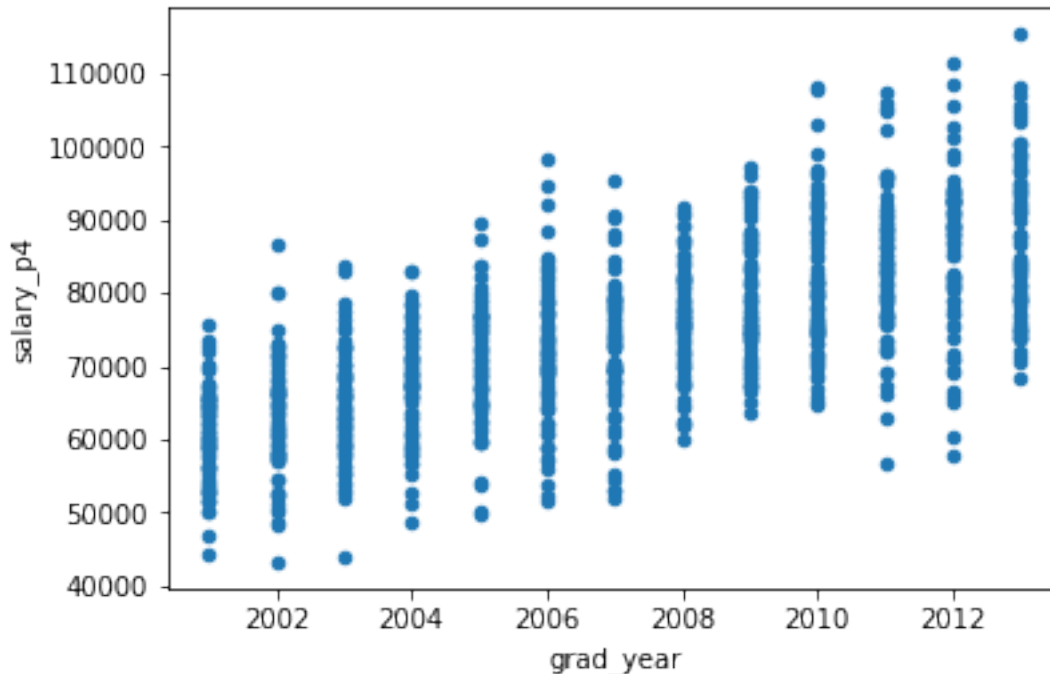


Here is where I'll discuss any problems that jump out. I'll propose a solution here as well.

It shows there might be a system drift on "gre\_qnt" on 2012, for all points of that year jumped from above 600 to less than 200. One solution is to find the official mapping function from grade of old version to that of new version on ETS homepage and use that to transform the grade of old version to that of new version. Then use new data for regression.

**(c) Create a scatterplot of income and graduation year**

```
In [7]: df3.plot(x='grad_year', y='salary_p4', kind='scatter')  
plt.show()
```



Here is where I'll discuss any problems again ... and propose another solution.

There seems to be a trend for income. One way to solve that is to use 2001 as the base year and divide each year by the average growth rate raised to the  $t$  power, where  $t = \text{grad\_year} - 2001$ .

**(d) Re-estimate coefficients with updated variables.**

```
In [8]: def transform(x):
    List1 = [800, 790, 780, 770, 760, 750, 740, 730, 720, 710, 690, 680, 670, 650, 630]
    List2 = [166, 164, 163, 161, 160, 159, 158, 157, 156, 155, 154, 153, 152, 151, 150]
    if x < 200:
        return x
    if x == 200:
        return 130
    for i in range(len(List2)):
        if x <= List1[i] and x > List1[i+1]:
            return List2[i]
    avg_inc_by_year = df3['salary_p4'].groupby(df3['grad_year']).mean().values
    avg_growth_rate = ((avg_inc_by_year[1:] - avg_inc_by_year[:-1]) / avg_inc_by_year[:-1])
    df3['new_salary'] = df3['salary_p4']
    df3['new_gre_qnt'] = 0
    for i in range(2002, 2014):
        df3['new_salary'][df3['grad_year']==i] = df3['salary_p4'] / ((1 + avg_growth_rate)
    for k in range(len(df3['new_gre_qnt'])):
        df3['new_gre_qnt'][k] = transform(df3['gre_qnt'][k])
    reg4 = sm.OLS(endog=df3['new_salary'], exog=df3[['new_gre_qnt', 'const']], missing='drop
```

```
result4 = reg4.fit()
print(result4.summary())
```

C:\ProgramData\Anaconda3\lib\site-packages\ipykernel\_launcher.py:16: SettingWithCopyWarning:  
A value is trying to be set on a copy of a slice from a DataFrame

See the caveats in the documentation: <http://pandas.pydata.org/pandas-docs/stable/indexing.html>  
app.launch\_new\_instance()

C:\ProgramData\Anaconda3\lib\site-packages\ipykernel\_launcher.py:18: SettingWithCopyWarning:  
A value is trying to be set on a copy of a slice from a DataFrame

See the caveats in the documentation: <http://pandas.pydata.org/pandas-docs/stable/indexing.html>

```

                                OLS Regression Results
=====
Dep. Variable:                  new_salary    R-squared:                0.001
Model:                            OLS        Adj. R-squared:           -0.000
Method:                 Least Squares    F-statistic:                0.5576
Date:                Tue, 16 Oct 2018    Prob (F-statistic):          0.455
Time:                  18:25:21    Log-Likelihood:            -10291.
No. Observations:                1000    AIC:                      2.059e+04
Df Residuals:                    998    BIC:                      2.060e+04
Df Model:                            1
Covariance Type:                nonrobust
=====
               coef      std err          t      P>|t|      [0.025      0.975]
-----
new_gre_qnt    -48.8918      65.474     -0.747     0.455    -177.374     79.591
const         6.909e+04    1.03e+04     6.728     0.000     4.89e+04     8.92e+04
=====
Omnibus:                 0.759    Durbin-Watson:           2.025
Prob(Omnibus):            0.684    Jarque-Bera (JB):         0.668
Skew:                    0.058    Prob(JB):                 0.716
Kurtosis:                3.051    Cond. No.                 7.14e+03
=====

```

Warnings:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 7.14e+03. This might indicate that there are strong multicollinearity or other numerical problems.

Here is where I'll discuss how the coefficients differ, where I'll interpret why the changes result in new coefficient changes, and where I'll discuss what this suggests about the answer to the question.

The coefficient of 'new\_gre\_qnt' represent for by how much student's income 4 years after graduation will increase for 1 more point of GRE quantative 170-scale grade. The coefficient becomes insignificant while still negative, which is better than the significant negative coefficients in

previous regression which is contradict to our common sense that a person getting higher quantitative grade in GRE is more intelligent and thus will have higher income. It suggests we have solve the problems mentioned before, and the previous uncommon results come from system drift and time trend.

### **1.0.5 3. Assessment of Kossinets and Watts.**

See attached PDF.