# One Tissue Compartment Model for Radioligand Kinetics

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## 1 Model setup

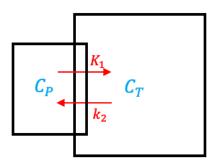


Figure 1: One-tissue compartment model. P: plasma (including free plus protein bound). T: tissue (including free, specific bound, and non-specific bound.)

This document is based on [2] Appendix B.

The differential equation for the radioligand kinetics is

$$\frac{\mathrm{d}C_T(t)}{\mathrm{d}t} = K_1 C_P(t) - k_2 C_T(t), \qquad (1)$$

where

- $C_P$ : metabolite-corrected plasma concentration (kBq/ml).
- $C_T$ : concentration of radioligand in the tissue (i.e. free plus specifically bound plus non-specifically bound) (kBq/ml).
- $K_1$ : rate constant for transfer from arterial plasma to tissue (ml·ml<sup>-1</sup>·min<sup>-1</sup>).
- $k_2$ : rate constant for transfer from ND compartment to plasma compartment (min<sup>-1</sup>).

### 2 Solution

Take Laplace transform on both side, along with the initial conditions  $C_T(0) = 0$ , we get

$$s\bar{C}_T(s) = K_1\bar{C}_P(s) - k_2\bar{C}_T(s).$$

That give us

$$\bar{C}_T(s) = \frac{K_1}{s + k_2} \bar{C}_P(s) .$$

The solution is

$$C_T(t) = K_1 C_P(t) \otimes e^{-k_2 t}.$$

### 3 Volume of distribution

The volume of distribution  $V_D$  of the tracer can be calculated as

$$V_D = \frac{K_1}{k_2} \,.$$

If we are more interested in estimating  $V_D$  instead of  $k_2$ , we can replace  $k_2$  by  $K_1/V_D$ , the solution then becomes

$$C_T(t) = K_1 C_P(t) \otimes e^{-(K_1/V_D)t}.$$

Then we do curve fitting with respect to  $K_1$  and  $V_D$ .

### References

- [1] Robert B Innis, Vincent J Cunningham, Jacques Delforge, Masahiro Fujita, Albert Gjedde, Roger N Gunn, James Holden, Sylvain Houle, Sung-Cheng Huang, Masanori Ichise, et al. Consensus nomenclature for in vivo imaging of reversibly binding radioligands. *Journal of Cerebral Blood Flow & Metabolism*, 27(9):1533–1539, 2007.
- [2] AA Lammertsma, CJ Bench, SP Hume, S Osman, K Gunn, DJ Brooks, and RSJ Frackowiak. Comparison of methods for analysis of clinical [11c] raclopride studies. *Journal of Cerebral Blood Flow & Metabolism*, 16(1):42–52, 1996.