

ECE 302H Hanson

Please answer ALL questions

100 points total.

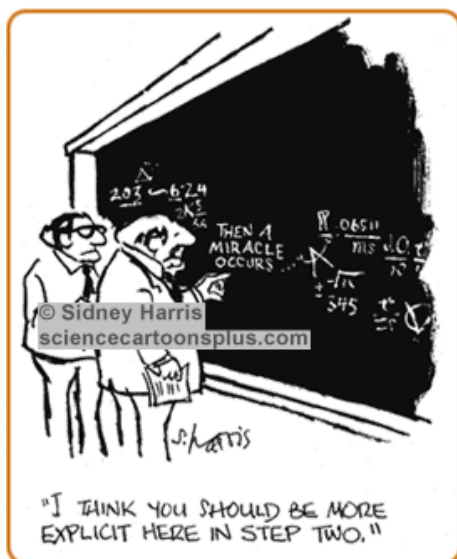
Fall 2022, Midterm Exam I

Time: 700-830 PM (90 minutes) + up to an additional 90 minutes, if required, with no penalty.

28 Sept. 2022



Kirchhoff's  
exams laws!



"I THINK YOU SHOULD BE MORE  
EXPLICIT HERE IN STEP TWO."

"Then a miracle occurs..."

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<u>Question</u>	<u>Points</u>
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Q1	
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Q2	
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Q3	
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Q4	
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Q5	
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Total:	
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**Q1. 30 Points total. This question has four parts (Part I-Part IV),**

**Part I: 6 Points.** Consider the following components (a)-(c). In each case, state if the component is linear or non-linear and briefly explain your answer:

(a) A voltage source of magnitude  $3I_0$ , where  $I_0$  is the current flowing through the source.

(b) A resistor whose value is given by  $R = 3I_0$ , where  $I_0$  is the current flowing through the resistor.

(c) A current source which provides a current of  $5V_0$  when the voltage applied across it is  $V_0$ .

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**Q1 Part II: 6 Points:** Provide examples of circuits with (i)  $V_{Th} = 0$  and  $R_{Th} \neq 0$ ; and (ii)  $V_{Th} \neq 0$ ;  $R_{Th} = 0$ . In each case, the circuit must have at least one source and two resistors.

**Q1 Part III: 8 Points:** The figure below, shows the ionic current (consisting of positive potassium ions) as a function of time flowing through a single biological component (called an ion channel) when a potential difference of 60 mV is applied across it. When the ion channel is open, the current is 4 pA ( $1 \text{ pA} = 10^{-12} \text{ A}$ ) and when the ion channel is closed, the current is zero.

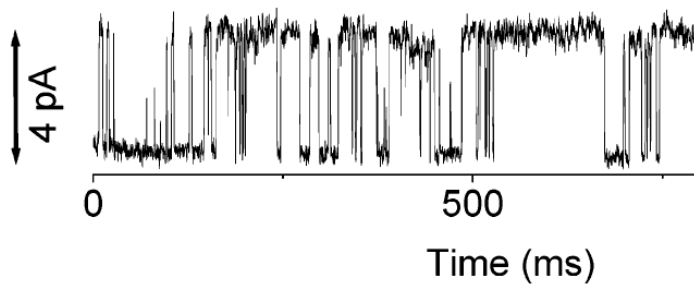


Figure for Q1 Part III

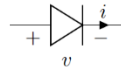
- (i) Draw a simple linear circuit model (or an equivalent circuit) for the ion channel. Make sure that your equivalent circuit captures all the electrical characteristics described above.
  
  
  
  
  
  
  
  
  
  
- (ii) For the time interval between  $t = 550 \text{ ms}$  and  $t = 650 \text{ ms}$ , calculate the total charge flowing through the ion channel, assuming it is open over the entire time interval.

- (iii) Scorpion venom blocks potassium ion channels and prevents any ions from flowing. Using your equivalent circuit proposed in (i), describe what a scorpion sting does to the ion channel.

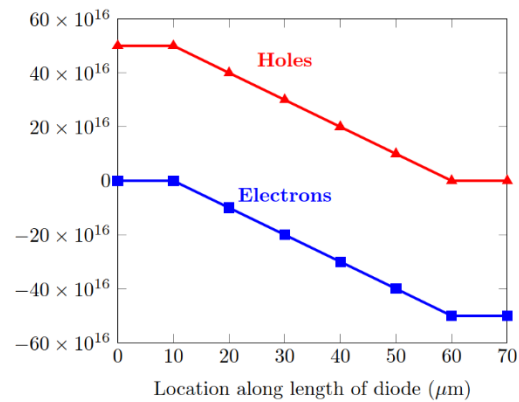
**Q1 Part IV: 10 Points** A diode is a circuit component with the following I-V characteristic:

$$i = I_0 \left( \exp^{\frac{q}{n k T} v} - 1 \right) \quad \text{where } i \text{ is the current}$$

through the diode,  $v$  is the voltage across the diode, and  $I_0$ ,  $n$ ,  $k$ , and  $T$  are all constants.



Number to pass location in 10 seconds (positive is to the right)



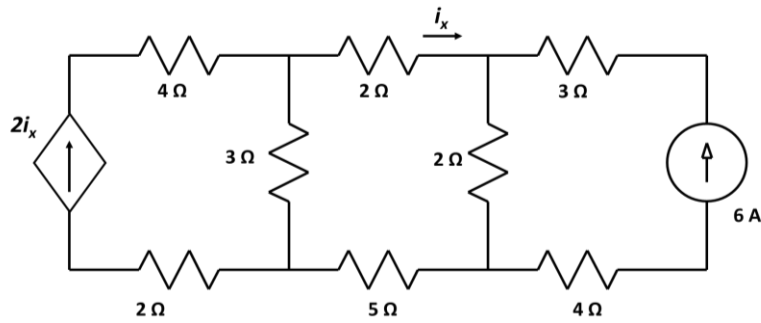
- a) Is the diode a linear component?
- b) Can the following techniques be used to analyze a circuit containing diodes?
- KVL
  - Node Voltage Analysis
  - Superposition
  - Norton Equivalent Circuits
- c) The charge flow in a diode is due to a combination of electrons and holes. Electrons have  $-1$  unit of charge ( $-1e^-$ ) and “holes” are positive charges which have  $+1$  unit of charge ( $+1e^-$ ). An experiment was performed on a diode which measured how many electrons and holes crossed certain locations along the diode’s length over a time of 10 seconds (see the Figure below). Explain how KCL is obeyed in the diode even though different numbers of charges pass each location in the diode.

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d) What is the current in the diode described above? Express your answer in Amperes with an appropriate SI prefix ( $\mu$ , m, k, M). Recall that 1 Coulomb has the same amount of charge as  $6.24 \times 10^{18}$  electrons.

**Q2. 15 Points.** Consider the circuit shown below.

- (i) Calculate  $i_x$
- (ii) Is the dependent source supplying or receiving power? Briefly justify your answer.
- (iii) Calculate the power received/supplied by the dependent source.

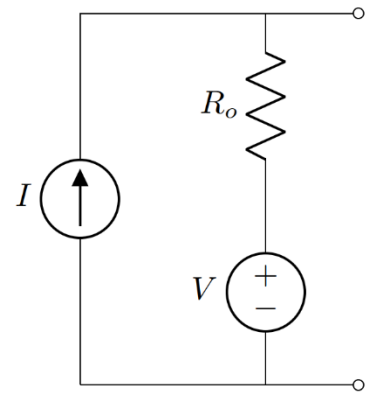




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**Q3. 15 Points.** A solar cell can be approximately modeled by the circuit in the Figure at right.

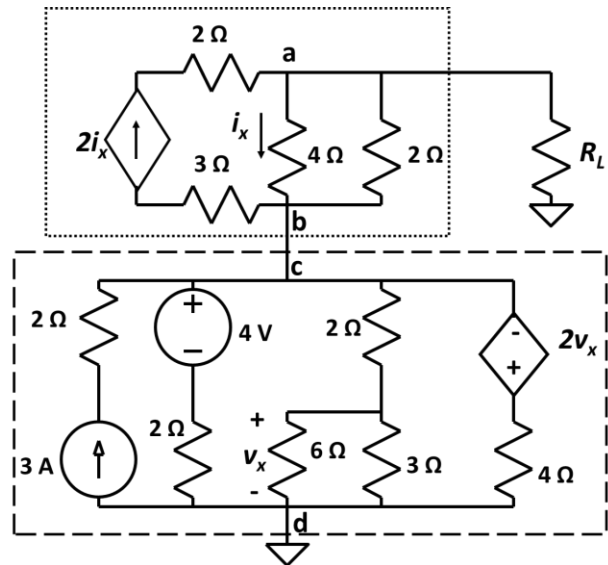
- a) Suppose that two identical solar cells are connected in series with each other and with a load resistor  $R_L$  (not shown in the figure). Calculate the voltage across  $R_L$ .
- b) Suppose that two identical solar cells are connected in parallel with each other and with a load resistor  $R_L$ . Calculate the current through  $R_L$ .



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**Q4. 20 Points.** Consider the figure in the circuit shown below:

- i) Calculate the Thevenin Equivalent circuit between a and b of the part of the whole circuit that is enclosed within the box with **dotted** lines.
- ii) Calculate the Thevenin Equivalent circuit between c and d of the part of the whole circuit that is enclosed within box with dashed lines.
- iii) For what value of  $R_L$  is the power transferred from the rest of the circuit to  $R_L$  a maximum? Calculate the power dissipated in  $R_L$ .

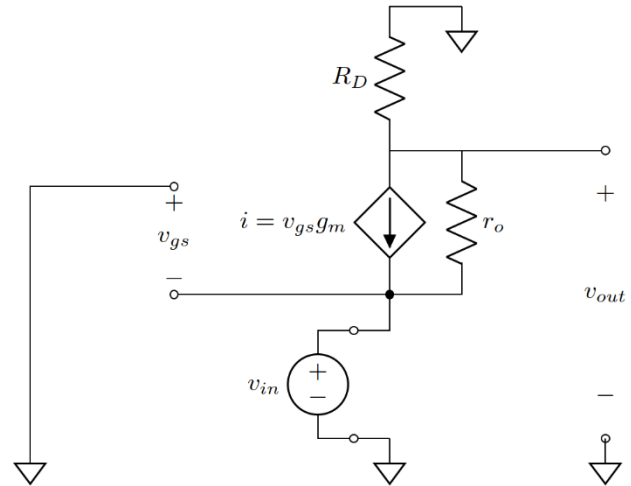


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**Q5. 20 Points.**

Consider the circuit in the diagram.

- (i) Calculate the gain of the circuit,  $v_{out}/v_{in}$ , when the output is open circuited as shown in the figure.
- (ii) Find the Thevenin equivalent circuit that represents the circuit's behavior at the  $v_{out}$  port.
- (iii) What does the Thevenin resistance in (ii) become if  $g_m \rightarrow \infty$ ?
- (iv) What is the Thevenin equivalent circuit that represents the circuit's behavior at the *input* port? (i.e., everything except the  $v_{in}$  voltage source, with the output open circuited)
- (v) What does the Thevenin resistance in (iv) become if  $g_m \rightarrow \infty$ ?



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