Bitcoin: A Peer-to-Peer Electronic Cash System

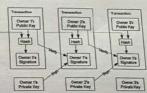
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Abstract. A purely psec-to-psec version of electronic eash would allow enlice payments to be aged directly from one party to another without going through a financial institution. Digital signatures provide part of the nothino, but the main benefits are less if a warset dired party is still required to prevent double-spending poleme using a peer-to-pse metwork. The network timestemps transactions by hashing them into an ongoing chain of hash-based proof-of-work. The longest chain not only serves as proof of the sequence of events wireness, but proof that it came from the largest pool of CPU power, a long as a majority of CPU power is controlled by nodes that are not cooperating to attack the network, they'll generate the longest chain and outpose-attackers. The network itself requires primitimal structure. Memages are broadcast on a best effort basis, and nodes can leave and rejoin the network at well, according to longest proof-of-work chain as proof of work chain as proof of what happened while they were gone.

1. Introduction

Commerce on the Internet has come to rely almost exclusively on financial institutions serving as trusted third parties to process electronic payments. While the system works well enough for most transactions, it still suffers from the inherent weaknesses of the trust based model. Completely non-reverable transactions are not really possible, since financial institutions cannot avoid mediating disputes. The cost of mediation increases transaction costs, limiting the minimum practical transaction size and cutting off the possibility for small casual transactions, and there is a broader cost in the less of ability to make non-reversible payments for some reversible services. With the possibility of reversal, the need for trust spreads. Merchanis mediates can be avoided in person by using them for more information than they would otherwise need. A certain percentage of fraud is accepted as unavoidable. These costs and payment uncertainties can be avoided in person by using physical currency, but no nechanism exists to did with the control of t

2. Transactions



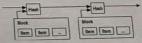
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The problem of course is the payee carl verify that one of the owners did not of the coin. A common solution is to introduce a stusted central suthority, or mist, that transaction for double spending. After each transaction, the cois must be returned to issue a new coin, and only cons issued directly from the mist are trusted not to be The problem with this solution is that the fate of the entire money system deconpany training the mint, with every transaction having to go Inrough tem, but I we need a way for the payee to know that the previous owners did not significantly after the property of the payee to know that the previous owners did not significantly after the property of the payee to know that the previous owners did not significantly of the payee of all transactions. The not but counts, so about later attempts to double-spend. The only way se confirm the absence of a to be saver of all transactions. In the mint based model, the mint was saves of all the decided which arrived first. To accomplish this without a trusted party, transaphicly, amounced [1], and we need a system for participants to agree on a single order in which they were received. The payee needs proof that at the time of each majority of sodes agreed it was the first received.

3. Timestamp Server

The solution we propose begins with a timestamp server. A timestamp server works by taking a hash of a block of items to be timestamped and widely publishing the hash, such as in a newspaper or Useset post [2-5]. The timestamp proves that the data must have existed at be time, obviously, in order to get into the bask. Each innestamp includes the previous timestamp in its hash, forming a chain, with each additional timestamp reinforcing the ones before it.



4. Proof-of-Work - ADALR

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To implement a distributed timestamp server on a peer-to-peer basis, we will need to use a proofof-work smaller to Adum Back's Hashcash [6], rather than mewapaper or Usenet posts,
the proof-of-work involves scanning for a value that when hashed, anch as with SIA-256, the
hash begins with a number of zero bits. The average work need it exponential in the number
of zero bits required and can be verified by executing a single hash.

For our timestamp actwork, we implement the proof-of-work by incrementing a nonce in the
block until a value is found that gives the block's bash required zero bits. Once the CPUdiffert, lass been expended to make it statisfy the proof-of-work, the block cannot be changed
without redoing the work. As later blocks are chained after it, the work to change the block
would include redoing all the blocks after it.

The proof-of-work also solves the problem of determining representation in majority decision making. If the majority were based on one-IP-eddress-one-vote, it could be subverted by anyone able to allocate many IPs. Proof-of-work is essentially one-CPU-one-vote. The majority decision is represented by the longest claim, which has the greatest proof-of-fer first invested in it. If a majority of CPU power is controlled by honest nodes, the honest claim will grow the fastest and outpace any competing chains. To modify a past block, an attacker would have to redo the proof-of-work of the block and all blocks after it and then eated up-with and unpass the work of the honest nodes. We will show later that the probability of a slower attacker citching up diminishe exponentially as subsequent blocks are adole. To compensate for increasing hardware speed and varying interest in running nodes over time, the proof-of-work difficulty is determined by a moving average targeting an average number of blocks per hour. If they're generated too fast, the difficulty increases.

The steps to run the network are as follows:

- New transactions are broadcast to all nodes.
 Each node collects new transactions into a block.
 Each node works on finding a difficult proof-of-work for its block.
 When a node finds a proof-of-work, it breadcasts the block to all nodes.
 Nodes accept the block only if all transactions in it are valid and not already speat.
 Nodes express their acceptance of the block by working on creating the next block in the chain, using the hash of the accepted block as the previous hash.

Nodes always consider the loagest chain to be the correct one and will keep werking on extending it. If two nodes broadcast different versions of the next block simultaneoutly, some nodes may receive one or the other first. In that case, they work on the first one they received, but save the other branch in case it becomes longer. The tie will be broken when the next proof-of-work is found and one branch becomes longer the nodes that were working on the other branch will then switch to the longer one.

New transaction broadcasts do not necessarily need to reach all nodes. As long as they reach many nodes; they will get into a Slock before long. Block broadcasts are also tolerant of dropped measures. If a node does not receive a block, it will request it when it receives the next block and realizes it missed one.

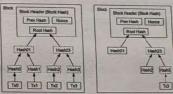
6. Incentive - Computed for Upar computer

By convention, the first transaction in all slock is appeal transaction that starts a new coin owned by the creator of the block. This in all slock is appeal transaction that starts a new coin owned by the creator of the block. This starts and starts in control to a special transaction that starts a provides a way to initially distribute coins into circulation, since there has been always to see that the start of the starts of the starts of amount of new coins is analogued and the special miner expending recourse to add gold to circulation. In our case, it is CPU time send all the miner expending recourse to add gold to circulation. In our case, it is CPU time send all the mineral country when the removal is the mine input value, the difference is a transaction feet that is added to the increasive value of the shock committing the transaction. Once a predetermined runner of coins have suntesed clocks in incremitive con transaction entirely to transaction feet and be completely inflation from the control of the control of the start of the control of the co

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7. Reclaiming Disk Space - Mark 10 TREE

Once the latest transaction in a coin is buried under enough blocks, the spent transactions before it can be discurded to save disk space. To facilitate his without breaking the block's bank, transactions are hashed in a Medic Tere [17][21], with early the not included in the block's bank. Old blocks can then be compacted by stubbing off branches of the tree. The interior bashes do not need to be stored.

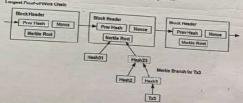


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A block header with no transactions would be about 80 bytes. If we suppose blocks are generated every 10 minutes, 80 bytes 16 * 24* 365 * 42.MB per year. With computer systems typically selling with 220° E 64.MB so of 2008, and Moore's Law predicting current growth of 1.2GB per year, storage should not be a problem even if the block headers must be kept in

s. Simplified Payment Verification

It is possible to verify payments without aunning a full network node. A user only needs to keep a copy of the block headers of the longest proof-of-work chain, which he can get by querying linking the transaction to the block it's timestamped in. He can't check the transaction for an about the chain, he can see that a network node has accepted it, and blocks added after it further confirm the network has accepted it.



As such, the verification is reliable as long as honest notes control the network, but is more vulnerable if the network is overpowered by an attacker. White network nodes can verify transactions for themselves, the simplified method can be fooled by an attacker's fibricated transactions for as long as the attacker can continue to overpower the network. One strategy to protect against this would be to accept alerts from network nodes when they detect an invalid took, prompting the user's software to download the full block and alerted transactions to confirm the inconsistency. Businesses that receive frequent payments will probably still want to run their own nodes for more independent security and quicker verification.

9. Combining and Splitting Value

Although it would be possible to handle coins individually, it would be unwieley to make a separate transaction for every cent in a transfer. To allow value to be split and combined, remsactions contain multiple inputs and outputs. Normally there will be either a single input from a larger previous transaction or multiple inputs combining smaller amounts, and at most two outputs: one for the payment, and one returning the change, if any, back to the sender.

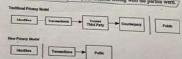


It should be noted that fan-out, where a transaction depends on several transactions, and those transactions depend on many more, is not a problem here. There is never the need to extract a complete standalone copy of a transaction's history.

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10. Privacy

The traditional binking model achieves a level of privacy by limiting access to information to the parties involved and the trusted third party. The necessity to amounce all transactions publicly precludes this method, but privacy can still be maintained by breaking the flow of information in mother place. By keeping public leavs amongmous. The public can see that someone is sending an amount to sounceme tele, but without information linking the transaction to arrow. This is amiliar to the level of information released by stock exchanges, where the time and size of individual trades the "taps", is made public, but without telling who the parties were:



As an additional firewall, a new key asir should be used for each transaction to keep them from being linked to a common owner.] Some linking is still enavoidable with multi-input transactions, which necessarily reveal that their inputs were covered by the same owner. The risk is that if the owner of a key is revealed, linking ould reveal other transactions that belonges to the same owner.

11. Calculations

All Calculations

We consider the scenario of an attacker trying to generate an alternace chain faster than the houset chain. Even if this is accomplished, it does not throw the system open to abitrary changes, such as creating value out of thin air or taking money fast new belonged to the snacker. Notes are not going to accept an invalid transaction as payment, and honest nodes will never accept a block containing them. An attacker can only try to change one of his som transactions to lake lack concept accepts spear.

The true between the honest chain and an attacker chain can be characterized as a Binomial Random Valki. The success event is the honest chain being extended by one block, increasing its lead by +1, and the failure event is the attacker's chain being extended by one block, reducing the grap by -1.

The probability of an attacker catching up from a given deficit is analogous te a Gumbler's Rain problem. Suppose a guantible with ustimated credit attria at a deficit and plays postability an infinite number of trials to try to reach breakeven. We can calculate the probability he ever reaches breakever, or that an attacker ever catches up with the honest chain, as follows [8]:

p = probability an honest node finds the next block q = probability the attacker finds the next block q_z = probability the attacker will ever catch up from z blocks behind

$$q_i = \begin{bmatrix} 1 & \text{if } p \leq q \\ (q \mid p)^t & \text{if } p > q \end{bmatrix}$$

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Given our assumption that p > q, the probability drops exponentially as the number of blocks the attacker has to catch up with increases. With the odds against him, if he doesn't make a lucky lunge forward early on, his chances become vanishingly small as he falls further behind. We now consider how long the recipient of a new transaction needs to wait before being sufficiently certain the sender can't change the transaction. We assume the sender is an attacker who wants to make the recipient before he paid him for a while, then switch it to pay back to sender hopes it will be too late. The receiver will be alerted when that happens, but the Sender hopes it will be too late. The receiver generates a new key pair and gives the public key to the sender shortly before signing. This prevents the sender from preparing a chain of blocks about of time by working on that momenty until he is lucky enough to get far enough shead, then executing the transaction is sent, the dishonent sender starts working in secret on a parallel chain containing an alternate version of his transaction.

The receiptent waits uatflit the transaction has been added to a block and x blocks have been linked after it. He doesn't know the exact amount of progress the attacker his made, but assuming the honest blocks took the average expected time per block, the attacker's potential progress will be a Poisson distribution with expected value:

$$\lambda = z \frac{q}{p}$$

To get the probability the attacker could still catch up now, we multiply the Poissen density for each amount of progress he could have made by the probability he could catch up from that point:

$$\sum_{k=0}^{m} \frac{\lambda^k e^{-\lambda}}{k!} \cdot \begin{bmatrix} (q/p)^{(s-k)} & \text{if } k \leq z \\ 1 & \text{if } k > z \end{bmatrix}$$

Rearranging to avoid summing the infinite tail of the distribution.

$$1 - \sum_{k=0}^{s} \frac{\lambda^{k} e^{-\lambda}}{k!} \left(1 - (q/p)^{(s-k)} \right)$$

Converting to C code...

```
#include <math.h>
double AttackerSuccessProbability(double q, int z)
       double p = 1.0 - qt
double lambda = t * (q / p) t
double sum = 1.0t
int i, kt
for (k = 0) k <= xt k+t
               double poisson = exp(-lambda);
for (i = 1; i <= k; i++)
poisson *= lambda / i;
sum -= poisson * (i - pow(q / p, z - k));
     return sum;
```

ning some results, we can see the probability drop off exponentially with z.

```
q=0.1
z=0
z=1
z=2
z=3
z=4
z=5
z=6
z=7
z=8
z=9
z=10
                                                       P=1.0000600
P=0.2045873
P=0.0509779
P=0.0131722
P=0.0009137
P=0.0009137
P=0.00002428
P=0.0000647
P=0.00000137
P=0.0000013
  q=0.3
z=0
z=5
z=10
z=15
z=20
z=25
z=36
z=36
z=41
z=50
```

Solving for Pless than 0.1%.

```
P < 0.001

q=0.10 x=5

q=0.15 z=8

q=0.20 z=11

q=0.25 z=15

q=0.30 z=24

q=0.35 z=41

q=0.40 z=89

q=0.45 z=340
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                                 hord a length in
12. Conclusion
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We have proposed a system for electronic transactions without relying on trust. We started with
the usual framework of coins made from digital signatures, which provides strong control of
ownership, but is incomplete without a way to prevent deathe-spending. To solve tals, we
proposed a per-to-per network using proof-of-work to record a public history of ransactions
that quickly becomes computationally impractical for an attacker to change if bonest notes
control a majority of CPU power. The network is robust in its unstructured simplicity. Notes
work all at once with little coordination. They do not need to be identified, since necessages are
not routed to any particular pace and only need to be delivered on a best effert basis. Nodes can
leave and rejoin the network at will, accepting the proof-of-work chain as proof of what
happened while they were gone. They vote with their CPU power, expressing their acceptance of
valid blocks by working on extending them and rejecting invasid blocks by refusing to work on
them. Any needed rules and incentives can be enforced with this consensus recchanism.