

## Key steps of PCA algorithm

1. Compute the mean  $\mu$  of the data matrix  $\mathbf{X} = [\mathbf{x}_1 | \dots | \mathbf{x}_N]^\top \in \mathbb{R}^{N \times D}$
2. Mean subtraction: Replace all data points  $\mathbf{x}_i$  with  $\tilde{\mathbf{x}}_i = \mathbf{x}_i - \mu$ .
3. Divide the data by its standard deviation in each dimension:  
 $\bar{\mathbf{X}}^{(d)} = \tilde{\mathbf{X}} / \sigma(\mathbf{X}^{(d)})$  for  $d = 1, \dots, D$ .
4. Compute the eigenvectors (orthonormal) and eigenvalues of the data covariance matrix  $\mathbf{S} = \frac{1}{N} \bar{\mathbf{X}}^\top \bar{\mathbf{X}}$
5. Choose the eigenvectors associated with the  $M$  largest eigenvalues to be the basis of the principal subspace.
6. Collect these eigenvectors in a matrix  $\mathbf{B} = [\mathbf{b}_1, \dots, \mathbf{b}_M]$
7. Orthogonal projection of the data onto the principal axis using the projection matrix  $\mathbf{B}\mathbf{B}^\top$