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import numpy as np
import pdb

"""
This code was based off of code from cs231n at Stanford University,
and modified for ECE C147/C247 at UCLA.
"""

class KNN(object):

    def __init__(self):
        pass

    def train(self, X, y):
        """
        Inputs:
        - X is a numpy array of size (num_examples, D)
        - y is a numpy array of size (num_examples, )
        """
        self.X_train = X
        self.y_train = y

    def compute_distances(self, X, norm=None):
        """
        Compute the distance between each test point in X and each
        training point
        in self.X_train.

        Inputs:
        - X: A numpy array of shape (num_test, D) containing test data.
        - norm: the function with which the norm is taken.

        Returns:
        - dists: A numpy array of shape (num_test, num_train) where
        dists[i, j]
        is the Euclidean distance between the ith test point and the jth
        training
        point.
        """
        if norm is None:
            norm = lambda x: np.sqrt(np.sum(x**2))
            #norm = 2

        num_test = X.shape[0]
        num_train = self.X_train.shape[0]
        dists = np.zeros((num_test, num_train))
        for i in np.arange(num_test):

            for j in np.arange(num_train):
                #

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===== #
    # YOUR CODE HERE:
        # Compute the distance between the ith test point and the
jth
        # training point using norm(), and store the result in
dists[i, j].
    # =====
#
    dists[i, j] = norm(X[i] - self.X_train[j])
    #
===== #
    # END YOUR CODE HERE
    #
===== #

    return dists

def compute_L2_distances_vectorized(self, X):
    """
    Compute the distance between each test point in X and each
training point
    in self.X_train WITHOUT using any for loops.

    Inputs:
    - X: A numpy array of shape (num_test, D) containing test data.

    Returns:
    - dists: A numpy array of shape (num_test, num_train) where
dists[i, j]
        is the Euclidean distance between the ith test point and the jth
training
        point.
    """
    num_test = X.shape[0]
    num_train = self.X_train.shape[0]
    dists = np.zeros((num_test, num_train))

    # =====
#
    # YOUR CODE HERE:
    # Compute the L2 distance between the ith test point and the jth
    # training point and store the result in dists[i, j]. You may
    # NOT use a for loop (or list comprehension). You may only use
    # numpy operations.
    #
    # HINT: use broadcasting. If you have a shape (N,1) array and
    # a shape (M,) array, adding them together produces a shape (N,
M)
    # array.
    # =====

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#
    #  $\sqrt{x^2 - y^2} = \sqrt{x^2 + y^2 - 2xy}$ 
    dists = np.sqrt(np.sum(X**2, axis=1)[..., np.newaxis] +
np.sum(self.X_train**2, axis=1) - 2 * np.dot(X, self.X_train.T))

    # =====
#
    # END YOUR CODE HERE
    # =====
#

    return dists

def predict_labels(self, dists, k=1):
    """
    Given a matrix of distances between test points and training
    points,
    predict a label for each test point.

    Inputs:
    - dists: A numpy array of shape (num_test, num_train) where
    dists[i, j]
        gives the distance between the ith test point and the jth
    training point.

    Returns:
    - y: A numpy array of shape (num_test,) containing predicted
    labels for the
        test data, where y[i] is the predicted label for the test point
    X[i].
    """
    num_test = dists.shape[0]
    y_pred = np.zeros(num_test)
    for i in np.arange(num_test):
        # A list of length k storing the labels of the k nearest
    neighbors to
        # the ith test point.
        closest_y = []
        #
    ===== #
        # YOUR CODE HERE:
        # Use the distances to calculate and then store the labels of
        # the k-nearest neighbors to the ith test point. The function
        # numpy.argsort may be useful.
        #
        # After doing this, find the most common label of the k-
    nearest
        # neighbors. Store the predicted label of the ith training

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example
    # as y_pred[i]. Break ties by choosing the smaller label.
    #
    ===== #
    sorted_pts = np.argsort(dists[i])
    closest_y = self.y_train[sorted_pts[:k]]
    y_pred[i] = np.argmax(np.bincount(closest_y))

    #
    ===== #
    # END YOUR CODE HERE
    #
    ===== #

    return y_pred

```