

# 561 hw4

Jiawei Zhang

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## 1 Q1

let  $Dup = \pi_A(\sigma_{A_1=A_2 \wedge B_1 \neq B_2}(W_1 \times W_2))$   
 $Dup \cup (\pi_A(W) - \pi_A(\sigma_{Dup.A \neq W.A}(Dup \times W)))$

## 2 Q2

**2.1 (a) (10 points) Find the sid and sname of each student who bought a book that cites another book.**

$\pi_{Sid, Sname}(\sigma_{Student.Sid=Buys.Sid \wedge Buys.BookNo=Cites.BookNo}(Student \times Buys \times Cites))$   
or

$\pi_{Sid, Sname}(Student \bowtie Buys \bowtie Cites)$

**2.2 (b) (10 points) Find the sid and sname of each student who has at least two majors.**

$\pi_{SMaj.Sid, SMaj.Sname}(\sigma_{SMaj.Sid=Major2.Sid \wedge SMaj.Major \neq SMaj.Major}((Major1 \bowtie Student) \bowtie SMaj \times Major2))$

**2.3 (c) (10 points) Find the sid of each student who bought exactly one book.**

$\pi_{Sid}(Buys) - \pi_{Sid}(\sigma_{Buys1.Sid=Buys2.Sid \wedge Buys1.BookNo \neq Buys2.BookNo}(Buys1 \times Buys2))$

**2.4 (d) (10 points) Find the bookno and title of each book with the second to lowest price.**

let  $CheapestBookPrice = \pi_{Price}(Book) - \pi_{Book2.Price}(\sigma_{Book1.Price < Book2.Price}(Book1 \times Book2))$

$\pi_{BookNo}(\sigma_{Book.Price > CheapestBookPrice} Book) -$

$\pi_{Book2.BookNo}(\sigma_{Book1.Price < Book2.Price \wedge Book1.price \neq CheapestBookPrice}(Book1 \times Book2))$

- 2.5 (e) (10 points)** Find the bookno and title of each book that was only bought by the student with sid = 1001.

$$\pi_{BookNo,title}(Book) - \pi_{BookNo,title}(\sigma_{Sid \neq 1001}(Buys \bowtie Books))$$

- 2.6 (f) (10 points)** Find the sid and sname of each student who bought at least two books that cost less than \$50.

$$\begin{aligned} \text{let } BoughtPrice &= \sigma_{Sid,BookNo,Price}(Buys \bowtie Book) \\ \pi_{Sid,Sname} &(\sigma_{B1.Sid=B2.Sid \wedge B1.BookNo \neq B2.BookNo \wedge B1.price < 50 \wedge B2.price < 50 \wedge B1.Sid=Sid} \\ &(BoughtPrice \text{ as } B1 \times BoughtPrice \text{ as } B2 \times Student)) \end{aligned}$$

- 2.7 (g) (10 points)** Find the bookno of each book that was not bought by all students who major in CS.

$$\text{let } CSMajorStudent = \pi_{Sid}(\sigma_{Major.Major='CS'}(Major))$$

$$\pi_{BookNo}(CSMajorStudent \times Book - Buys)$$

- 2.8 (h) (10 points)** Find the bookno of each book that is not cited by a book that cost more than \$50.

$$\pi_{BookNo}(Book) - \pi_{CitedBookNo}(Cites \bowtie \sigma_{Book.Price > 50}(Book))$$

- 2.9 (i) (10 points)** Find the sid of each student who not only bought books that cost less than \$30.

$$BookCostLessThan30 = \pi_{BookNo}(\sigma_{Price < 30} Book)$$

$$\pi_{Sid}(Buys - \pi_{Sid,BookNo}(BookCostLessThan30 \times Student))$$

- 2.10 (j) (10 point)** Find each pair (s; b) such that s is the sid of a student who bought a book that does not cite the book with bookno b.

$$\begin{aligned} \pi_{Sid,c} &(\pi_{Sid,Buys.BookNo,(Book.BookNo \text{ as } c)}(Buys \times Book) - \\ &\pi_{Sid,Buys.BookNo,(Cite.CitedBookNo \text{ as } c)}(Buys \bowtie \sigma_{Buys.BookNo=Cite.Cite} Cites)) \end{aligned}$$

- 2.11 (k) (10 points)** Find the pair of different booknos (b1; b2) that were bought by the same CS students.

$$\begin{aligned} \pi_{B1.BookNo,B2.BookNo}(Book \times Book) - \\ ( \\ \pi_{b.sid,B1.BookNo \text{ as } bno1,B2.BookNo \text{ as } bno2}(\sigma_{Buys.Sid=Major.Sid \wedge Major.Major='CS'} \end{aligned}$$

$$\begin{aligned}
& \wedge B.BookNo=B1.BookNo(Buys \times Major \times Book \text{ as } B1 \times Book \text{ as } B2))) \\
& - (\pi_{b.sid,B1.BookNo \text{ as } bno1,B2.BookNo \text{ as } bno2}(\sigma_{Buys.Sid=Major.Sid \wedge Major.Major='CS'} \\
& \wedge B.BookNo=B2.BookNo(Buys \times Major \times Book \text{ as } B1 \times Book \text{ as } B2))) \\
& ) \\
& \cup \\
& \pi_{B1.BookNo,B2.BookNo}(Book \times Book) - \\
& ( \\
& (\pi_{b.sid,B1.BookNo \text{ as } bno1,B2.BookNo \text{ as } bno2}(\sigma_{Buys.Sid=Major.Sid \wedge Major.Major='CS'} \\
& \wedge B.BookNo=B2.BookNo(Buys \times Major \times Book \text{ as } B1 \times Book \text{ as } B2))) \\
& - (\pi_{b.sid,B1.BookNo \text{ as } bno1,B2.BookNo \text{ as } bno2}(\sigma_{Buys.Sid=Major.Sid \wedge Major.Major='CS'} \\
& \wedge B.BookNo=B1.BookNo(Buys \times Major \times Book \text{ as } B1 \times Book \text{ as } B2))) \\
& )
\end{aligned}$$

**2.12 (l) (10 points) Find the pairs of different sid (s1,s2) of students such that all books bought by student s1 were also bought by student s2.**

$$\begin{aligned}
& \pi_{Sid1,Sid2}(\pi_{S1.Sid \text{ as } Sid1,s2.Sid \text{ as } Sid2}(Student \text{ as } S1, Student \text{ as } S2) \\
& - \\
& \pi_{Sid1,Sid2}( \\
& \pi_{S1.Sid \text{ as } Sid1,s2.Sid \text{ as } Sid2}(\sigma_{B.Sid=S1.Sid}(Buys \text{ as } B, Student \text{ as } S1, Student \text{ as } S2) \\
& - \\
& \pi_{S1.Sid \text{ as } Sid1,s2.Sid \text{ as } Sid2}(\sigma_{B.Sid=S2.Sid}(Buys \text{ as } B, Student \text{ as } S1, Student \text{ as } S2)) \\
& )
\end{aligned}$$

**2.13 (m) (10 points) Find the bookno of each book that is cited by all but one book.**

$$\text{let notCite} = \pi_{c1.BookNo,c2.BookNo \text{ as } notCited}(Cites \times Cites) - Cited$$

$$\begin{aligned}
& \pi_{bookno}(notCite) \\
& - \\
& \pi_{notCited}(\sigma_{(nc1.bookno \neq nc2.bookno \wedge nc1.notCited = nc2.notCited)}(notCite \times notCite))
\end{aligned}$$

### 3 Q3

**3.1 (a) Find the sid and major of each student who bought a book that cost less than \$20.**

$$\pi_{Sid,Major}(\sigma_{t.bookno=b.bookno \wedge b.price < 20 \wedge m.sid=t.sid}(major \text{ as } m, buys \text{ as } t, book \text{ as } b))$$

- 3.2 (b)** Find each (s; b) pair where s is the sid of a student and where b is the bookno of a book whose price is the cheapest among the books bought by that student.

$$\pi_{Sid, Bookno}(\sigma_{t.bookno=b.bookno}(buys \text{ as } t, book \text{ as } b)) -$$

$$\pi_{Sid, Bookno}(\sigma_{t.bookno=b.bookno \wedge t1.bookno=b1.bookno \wedge t.Sid=t1.Sid \wedge not b.price > b1.price}$$

$$(buys \text{ as } t, book \text{ as } b, buys \text{ as } t1, book \text{ as } b1))$$

- 3.3 (c)** Find the bookno and title of each book that cost between \$20 and \$40 and that is cited by another book.

$$\pi_{sid, sname}(\sigma_{20 \leq b.price \wedge b.price \leq 40 \wedge c.citedbookno=b.bookno}(book \text{ as } b, cites \text{ as } c))$$

- 3.4 (d)** Find the sid and name of each student who majors in 'CS' and who bought a book that is cited by a lower priced book.

$$\pi_{sid, sname}(\sigma_{s.sid=m.sid \wedge m.major='CS' \wedge s.sid=t.sid \wedge t.bookno=c.citedbookno \wedge c.citedbookno=b1.bookno}$$

$$\wedge c.bookno=b2.bookno \wedge b1.price > b2.price)$$

$$(student \text{ as } s, major \text{ as } m, buys \text{ as } t, cites \text{ as } c, book \text{ as } b1, book \text{ as } b2))$$

- 3.5 (e)** Find the bookno and title of each book that is not bought by all students who major in 'CS'.

$$\pi_{bookno, title}(\sigma_{m.major='CS'}(major \text{ as } m, Book \times \text{ as } b) -$$

$$\sigma_{m.major='CS' \wedge m.sid=t.sid \wedge t.bookno=b.bookno}(major \text{ as } m \times Book \text{ as } b \times Buys \text{ as } t))$$

- 3.6 (f)** Find the bookno and title of each book that is bought by all students who major in both 'CS' and in 'Math'.

$$\pi_{bookno, title}(\pi_{bookno, title}(book))$$

$$-$$

$$\pi_{bookno, title}(\pi_{s.sid, b.Bookno, b.title}(\sigma_{s.sid=m.sid \wedge m.major='CS' \wedge s.sid=m2.sid \wedge m2.major='Math'}$$

$$(student \text{ as } s \times major \text{ as } m \times major \text{ as } m2 \times book \text{ as } b)))$$

$$-$$

$$(\pi_{s.sid, b.Bookno, b.title}(\sigma_{s.sid=m.sid \wedge m.major='CS' \wedge s.sid=m2.sid \wedge m2.major='Math' \wedge s.sid=t.sid \wedge t.bookno=b.bookno}$$

$$(student \text{ as } s \times major \text{ as } m \times major \text{ as } m2 \times book \text{ as } b \times buys \text{ as } t))))$$

$$)$$