

# BDC-Adapter: Brownian Distance Covariance for Better Vision-Language Reasoning

Yi Zhang<sup>\*1,2</sup>, Ce Zhang<sup>\*3</sup>, Zihan Liao<sup>2</sup>, Yushun Tang<sup>2</sup>, Zhihai He<sup>2,4</sup>

<sup>1</sup>Harbin Institute of Technology <sup>2</sup>Southern University of Science and Technology

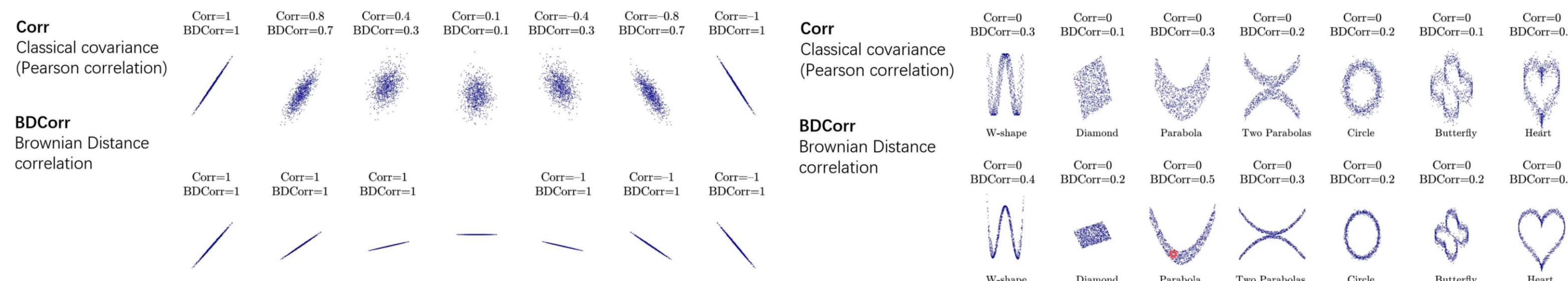
<sup>3</sup>Carnegie Mellon University <sup>4</sup>Pengcheng Laboratory

## I. Abstract

Large-scale pre-trained Vision-Language Models (VLMs), such as CLIP and ALIGN, have introduced a new paradigm for learning transferable visual representations. Recently, there has been a surge of interest among researchers in developing lightweight fine-tuning techniques to adapt these models to downstream visual tasks. We recognize that current state-of-the-art fine-tuning methods, such as Tip-Adapter, simply consider the covariance between the query image feature and features of support few-shot training samples, which only captures linear relations and potentially instigates a deceptive perception of independence. To address this issue, in this work, we innovatively introduce Brownian Distance Covariance (BDC) to the field of vision-language reasoning. The BDC metric can model all possible relations, providing a robust metric for measuring feature dependence. Based on this, we present a novel method called BDC-Adapter, which integrates BDC prototype similarity reasoning and multi-modal reasoning network prediction to perform classification tasks. Our extensive experimental results show that the proposed BDC-Adapter can freely handle non-linear relations and fully characterize independence, outperforming the current state-of-the-art methods by large margins.

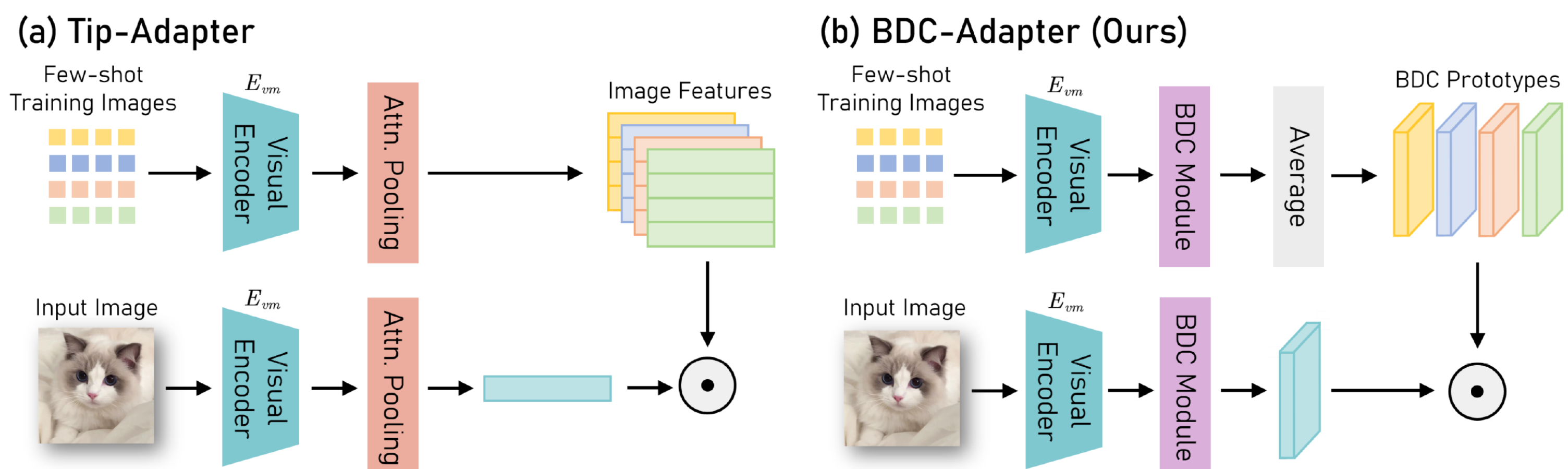
## II. Motivation

- The current state-of-the-art Tip-Adapter method, establishes a key-value cache model and evaluates the similarities of the query image feature and features of support few-shot training samples to perform classification.
- However, we recognize that Tip-Adapter simply considers the covariance between each image feature pair, which only measures marginal distributions and captures linear relations.
- In this paper, we introduce Brownian Distance Covariance (BDC) to the field of vision-language reasoning to provide a robust metric for measuring feature dependence. While classical covariance can only capture linear relations, Brownian covariance can model all possible relations.



## III. Method

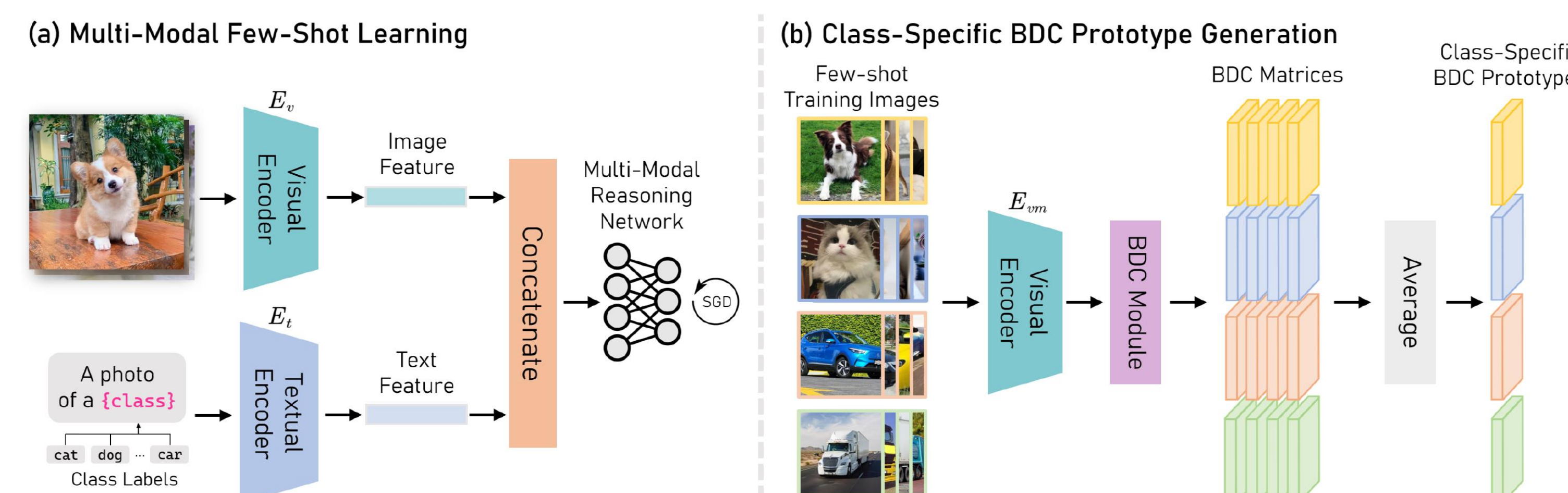
- Differences with Tip-Adapter. Tip-Adapter can only capture linear relations. Our BDC-Adapter represents each image by a BDC matrix, which considers the joint distributions and measures non-linear dependence during inference.



- Multi-Modal Few-Shot Learning. After feature extraction, we concatenate the image and text features and use this joint features  $f_i$  to train a one-layer multi-modal reasoning network  $\psi$  by cross-entropy loss:

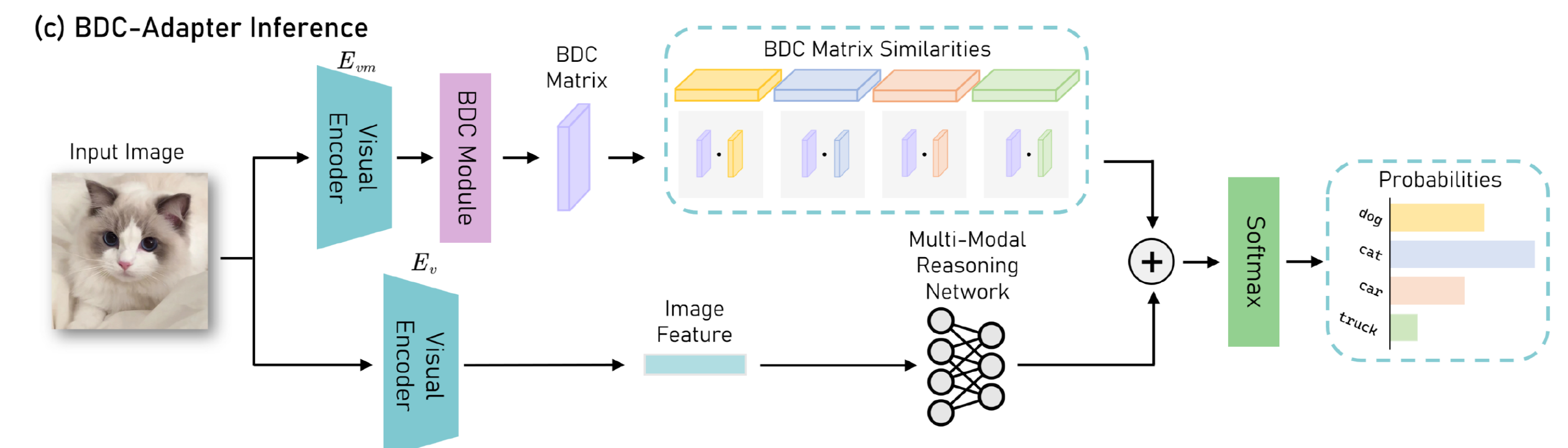
$$\mathcal{L}_{CE} = \sum_{i=1}^n H(y_i, \psi(f_i)) = - \sum_{i=1}^n \log \left( \frac{e^{w_{y_i} \cdot f_i}}{\sum_{y'} e^{w_{y'} \cdot f_i}} \right).$$

- Class-Specific BDC Prototype Generation. Given all the BDC matrices of M images within class y, we define the prototype of class y to be the average of the BDC matrices, denoted as  $P_y = \frac{1}{M} \sum_{m=1}^M B_y(x_m)$ .



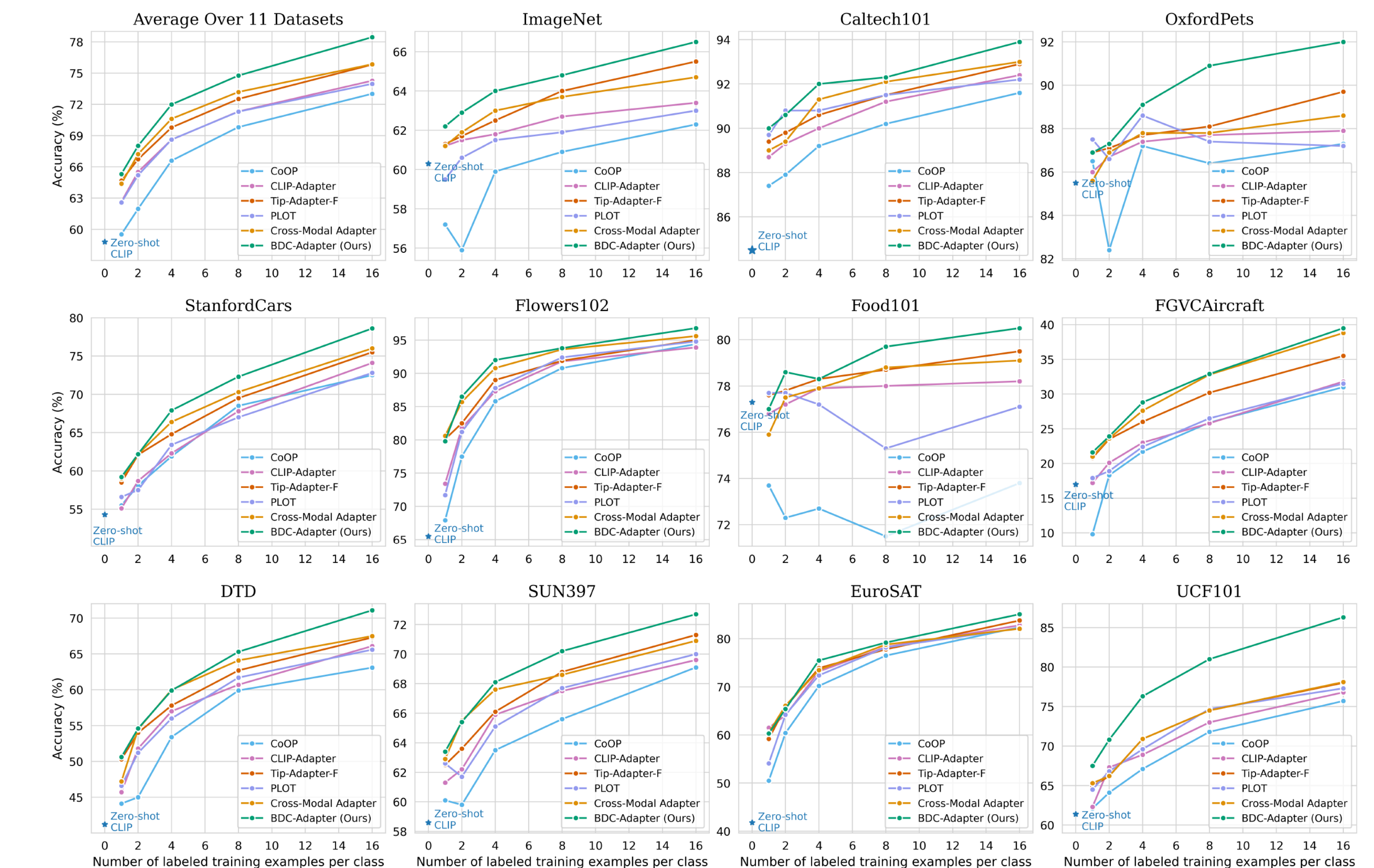
- BDC-Adapter Inference. During inference, BDC-Adapter integrates BDC prototype similarity reasoning and multi-modal reasoning network prediction to perform classification tasks, denoted as

$$p(y = y_n | x_{test}) = \alpha p_b(y = y_n | x_{test}) + p_m(y = y_n | x_{test}) \\ = \alpha \exp(-\delta (1 - \text{vec}(B(x_{test})) \cdot \text{vec}(P_{y_n}))) + w_{y_n} \cdot f_{test}.$$



## IV. Experimental Results

- Performance comparisons on few-shot learning on 11 datasets.



- Performance comparisons on robustness to natural distribution shifts.
- A few-shot learning instance from the Bongard-HOI.

Method	Source		Target			
	ImageNet	-V2	-Sketch	-A	-R	Avg.
Zero-Shot CLIP [39]	60.33	53.27	35.44	21.65	56.00	41.59
Linear Probe CLIP [39]	56.13	45.61	19.13	12.74	34.86	28.09
CoOp [68]	63.33	55.40	34.67	23.06	56.60	42.43
CoCoOp [67]	62.81	55.72	34.48	23.32	57.74	42.82
ProGrad [70]	62.17	54.70	34.40	23.05	56.77	42.23
PLOT [6]	63.01	55.11	33.00	21.86	55.61	41.40
DeFo [50]	64.00	<b>58.41</b>	33.18	21.68	55.84	42.28
TPT [42]	60.74	54.70	35.09	26.67	<b>59.11</b>	43.89
TPT + CoOp [42]	<b>64.73</b>	57.83	<b>35.86</b>	<b>30.32</b>	58.99	<b>45.75</b>
<b>BDC-Adapter (Ours)</b>	<b>66.46</b>	<b>58.05</b>	<b>36.92</b>	<b>30.77</b>	<b>59.52</b>	<b>46.31</b>

- Visual reasoning performance comparisons on the Bongard-HOI dataset.

Method	Seen act.		Unseen act.		Avg.
	Seen obj.	Unseen obj.	Seen act.	Unseen act.	
CNN-Baseline [35]	50.03	49.89	49.77	50.01	49.92
Meta-Baseline [8]	58.82	58.75	58.56	57.04	58.30
ProtoNet [44]	58.90	58.77	57.11	58.34	58.28
HOITrans [72]	59.50	64.38	63.10	62.87	62.46
TPT (RN50) [42]	<b>66.39</b>	<b>68.50</b>	<b>65.98</b>	<b>65.48</b>	<b>66.59</b>
<b>BDC-Adapter (RN50)</b>	<b>68.36</b>	<b>69.15</b>	<b>67.67</b>	<b>67.82</b>	<b>68.25</b>

- Ablation study on 16-shot ImageNet.
- Efficiency comparison.

Few-shot Setup	1	2	4	8	16
MRN (w/o init.)	60.55	61.07	61.89	63.04	63.57
MRN (w/ init.)	61.12	61.77	62.73	63.78	64.68
<b>MRN + BDC (Ours)</b>	<b>62.19</b>	<b>62.91</b>	<b>63.95</b>	<b>64.83</b>	<b>66.46</b>

Method	Epochs	Training	GFLOPs	Param.	Acc.
CoOp [68]	200	15 h	>10	<b>0.01M</b>	62.95
CLIP-Adapter [18]	200	50 min	0.004	0.52M	63.59
Tip-Adapter-F [63]	<b>20</b>	5 min	0.030	16.3M	65.51
<b>BDC-Adapter (Ours)</b>	<b>20</b>	<b>2 min</b>	<b>0.001</b>	1.02M	<b>66.46</b>

## V. Contributions

- We introduce Brownian Distance Covariance to the field of vision-language reasoning to provide a robust metric for measuring feature dependence.
- Based on this, we propose a novel approach called BDC-Adapter that leverages BDC to enhance vision-language reasoning ability, which integrates BDC prototype similarity reasoning and multi-modal reasoning network prediction to perform classification tasks.
- Our extensive experimental results show that BDC-Adapter outperforms the current state-of-the-art methods by large margins.