$$\begin{array}{ccc} S & \longrightarrow & \mathbf{Fil}(S) & \longrightarrow & \mathbf{Proj} * \mathbf{Fil}(S) \\ & & & & \downarrow \mathbf{Smd} \\ & \widetilde{S} & \longrightarrow & \mathbf{Fil}(\widetilde{S}) & \xrightarrow{\mathbf{Smd}} & ^{\perp}(S^{\perp}) \end{array}$$