$$\mathrm{KER}(\delta) := \{\ker f \mid \qquad \begin{array}{c} M \longrightarrow Y \longrightarrow C & \delta \\ & \downarrow f & \downarrow \\ M \longrightarrow X \longrightarrow C' & \mathrm{preenvelift} \end{array}$$