$$\begin{CD}
\operatorname{Cone}(g \circ f) @>{p(g \circ f)}>> X[1] \\
@V{i(g_*)}VV \star @VV{f[1]}V \\
\operatorname{Cone}(g_*) @>>{p(g)}> Y[1]
\end{CD}$$