$$\ker p \cap \operatorname{im}(\alpha) \stackrel{}{\longleftrightarrow} \operatorname{im}(\alpha) \stackrel{p|_{\operatorname{im}(\alpha)}}{\longrightarrow} M$$

$$\downarrow \qquad \qquad \downarrow \qquad \qquad \downarrow \qquad \qquad \parallel$$

$$\longrightarrow \ker p \stackrel{}{\longleftrightarrow} P \stackrel{p}{\longrightarrow} M \longrightarrow 0$$