$$0 \longrightarrow \varinjlim Q_{\bullet} \longrightarrow \varinjlim (P_{\bullet} \oplus Q_{\bullet}) \longrightarrow \varinjlim P_{\bullet} \longrightarrow 0$$

$$\downarrow \qquad \qquad \downarrow \qquad$$