

Spot_asymmetry

Following the predictions made for the plasticity experiments, we would expect **variation at extreme temperatures are expected to be mainly driven by asymmetric variation, FA especially** as this is where developmental noise caused by temperature stress is expressed.

We start by loading the data, including the estimation of the spot residuals, and the libraries we will need for the analyses:

```
spot.data <- read.table(paste('/Users/ceferino_vg/Documents/Drosophila_suzukii/',
                              'Spot_evolution/data/results_plasticity.txt',
                              sep=''),
                        header=T, sep=',')

spot.data$TEMP <- factor(spot.data$TEMP)

head(spot.data)

##   IND  POP TEMP SIDE   Wing   Spot   Ratio
## 1 L04 PARIS  16    D 1995044 101003.5 0.05068861
## 2 L04 PARIS  16    G 1977244  83436.5 0.04219839
## 3 L06 PARIS  16    D 1959810  86874.5 0.04432802
## 4 L06 PARIS  16    G 1932712  82319.5 0.04259274
## 5 L07 PARIS  16    G 2026222  78718.5 0.03884989
## 6 L09 PARIS  16    D 1892918  75860.0 0.04007569

library(ggplot2)
library(ggsignif)
library(car)
library(wesanderson)
library(cvequality)

cohens.d <- function(pop1, pop2) {
  d <- (mean(pop1)-mean(pop2))/
    sqrt(((length(pop1)-1)*var(pop1)+(length(pop2)-1)*var(pop2))/(length(pop1)+length(pop2)-2))

  return(d)
}
```

We first create a matrix with the just the complete individuals of the dataset and then we add the second measure of the whole dataset:

```
non.sym <- c(0)

for (i in 1:length(spot.data$IND)) {

  if (length(intersect(intersect(
    which(as.character(spot.data$IND[i]) == as.character(spot.data$IND[-i])),
    which(spot.data$TEMP[i] == spot.data$TEMP[-i])
  ), which(spot.data$POP[i] == spot.data$POP[-i])))) == 0) {

    non.sym <- c(non.sym,i)
  }

}
```

```

spot.sym <- spot.data[-non.sym,]

spot.ind <- aov(Spot ~ Wing, data = spot.sym)

spot.sym$Res <- spot.ind$residuals

error <- read.table(paste("/Users/ceferino_vg/Documents/Drosophila_suzukii/",
                          "Spot_evolution/data/errors.txt",
                          sep = ""
), header = T, sep = ",")

error$Res <- aov(Spot ~ Wing, data = error)$residuals

spot.sym.error <- rbind(spot.sym, error)

```

We create the same categories to run the analyses:

```

Paris_idx <- which(spot.sym.error$POP=='PARIS')
Sappo_idx <- which(spot.sym.error$POP=='SAPPORO')
Sokol_idx <- which(spot.sym.error$POP=='SOKOL')
temp16_idx <- which(spot.sym.error$TEMP==16)
temp22_idx <- which(spot.sym.error$TEMP==22)
temp28_idx <- which(spot.sym.error$TEMP==28)

Paris16 <- intersect(Paris_idx, temp16_idx)
Paris22 <- intersect(Paris_idx, temp22_idx)
Paris28 <- intersect(Paris_idx, temp28_idx)
Sokol16 <- intersect(Sokol_idx, temp16_idx)
Sokol22 <- intersect(Sokol_idx, temp22_idx)
Sokol28 <- intersect(Sokol_idx, temp28_idx)
Sapporo16 <- intersect(Sappo_idx, temp16_idx)
Sapporo22 <- intersect(Sappo_idx, temp22_idx)
Sapporo28 <- intersect(Sappo_idx, temp28_idx)

Pops <- list(Paris16, Paris22, Paris28, Sapporo16, Sapporo22, Sapporo28,
             Sokol16, Sokol22, Sokol28)

```

And here we go! First we test for FA in all nine different populations, storing the mean squares to manually estimate the significance of DA and individual variation in future analyses. We report the ratio between the Mean Sq of the IND:SIDE interaction and the Mean Sq of the Residuals and the p-value and effect size of the DA estimation. We also include which of the two wings has the largest spot size:

```

combinations <- matrix(c(rep(5:8,9), rep(1:9, each=4)),ncol=2)

for (i in 1:36) {

Pop <- spot.sym.error[Pops[[combinations[i,2]]],]

FA <- summary(aov(Pop[,combinations[i,1]] ~ IND*SIDE, data = Pop))

DA <- 1 - pf((FA[[1]][ 'Mean Sq' ][2,]/FA[[1]][ 'Mean Sq' ][3,]),1,FA[[1]][ 'Df' ][3,])

cat(as.character(Pop[1,2]),' ', as.character(Pop[1,3]) , ' ', 'FA results for',
    colnames(Pop)[combinations[i,1]], "\n")

```

```

cat('Error (ratio) = ', FA[[1]]['Mean Sq'][3,]/FA[[1]]['Mean Sq'][4,], "\n")

cat(as.character(Pop[1,2]), ' ', as.character(Pop[1,3]), ' ', 'DA results for',
    colnames(Pop)[combinations[i,1]], "\n")
cat('F value = ', FA[[1]]['Mean Sq'][2,]/FA[[1]]['Mean Sq'][3,], '; df2 = ',
    FA[[1]]['Df'][3,], '; p-val = ', DA, "\n")

if (DA < 0.05) {
  meanDA <- aggregate(Spot ~ SIDE, data=Pop, FUN = mean)
  side_DA <- as.character(meanDA$SIDE[which(meanDA$Spot==max(meanDA$Spot))])
  cat('The larger spot size is in the ',side_DA, ' wing.', "\n")
}

}

```

```

## PARIS 16 FA results for Wing
## Error (ratio) = 27.15904
## PARIS 16 DA results for Wing
## F value = 0.8044544 ; df2 = 6 ; p-val = 0.404314
## PARIS 16 FA results for Spot
## Error (ratio) = 5.984192
## PARIS 16 DA results for Spot
## F value = 1.947844 ; df2 = 6 ; p-val = 0.2122823
## PARIS 16 FA results for Ratio
## Error (ratio) = 6.205058
## PARIS 16 DA results for Ratio
## F value = 1.971083 ; df2 = 6 ; p-val = 0.2099192
## PARIS 16 FA results for Res
## Error (ratio) = 6.582908
## PARIS 16 DA results for Res
## F value = 2.160808 ; df2 = 6 ; p-val = 0.1919674
## PARIS 22 FA results for Wing
## Error (ratio) = 65.06422
## PARIS 22 DA results for Wing
## F value = 1.442039 ; df2 = 11 ; p-val = 0.2550298
## PARIS 22 FA results for Spot
## Error (ratio) = 12.67938
## PARIS 22 DA results for Spot
## F value = 17.84582 ; df2 = 11 ; p-val = 0.001425709
## The larger spot size is in the D wing.
## PARIS 22 FA results for Ratio
## Error (ratio) = 13.51184
## PARIS 22 DA results for Ratio
## F value = 12.29544 ; df2 = 11 ; p-val = 0.004913887
## The larger spot size is in the D wing.
## PARIS 22 FA results for Res
## Error (ratio) = 14.71576
## PARIS 22 DA results for Res
## F value = 11.84046 ; df2 = 11 ; p-val = 0.005514956
## The larger spot size is in the D wing.
## PARIS 28 FA results for Wing
## Error (ratio) = 25.72928
## PARIS 28 DA results for Wing
## F value = 1.667539 ; df2 = 12 ; p-val = 0.2209091

```

```

## PARIS 28 FA results for Spot
## Error (ratio) = 198.9337
## PARIS 28 DA results for Spot
## F value = 6.155342 ; df2 = 12 ; p-val = 0.02890526
## The larger spot size is in the D wing.
## PARIS 28 FA results for Ratio
## Error (ratio) = 192.8433
## PARIS 28 DA results for Ratio
## F value = 6.004318 ; df2 = 12 ; p-val = 0.03057244
## The larger spot size is in the D wing.
## PARIS 28 FA results for Res
## Error (ratio) = 178.7393
## PARIS 28 DA results for Res
## F value = 5.733005 ; df2 = 12 ; p-val = 0.03386451
## The larger spot size is in the D wing.
## SAPPORO 16 FA results for Wing
## Error (ratio) = 10.4987
## SAPPORO 16 DA results for Wing
## F value = 1.631945 ; df2 = 11 ; p-val = 0.2277376
## SAPPORO 16 FA results for Spot
## Error (ratio) = 7.27965
## SAPPORO 16 DA results for Spot
## F value = 25.44203 ; df2 = 11 ; p-val = 0.0003755921
## The larger spot size is in the D wing.
## SAPPORO 16 FA results for Ratio
## Error (ratio) = 8.579777
## SAPPORO 16 DA results for Ratio
## F value = 19.74721 ; df2 = 11 ; p-val = 0.0009888071
## The larger spot size is in the D wing.
## SAPPORO 16 FA results for Res
## Error (ratio) = 7.842425
## SAPPORO 16 DA results for Res
## F value = 20.13967 ; df2 = 11 ; p-val = 0.0009196161
## The larger spot size is in the D wing.
## SAPPORO 22 FA results for Wing
## Error (ratio) = 15.60197
## SAPPORO 22 DA results for Wing
## F value = 0.4732123 ; df2 = 11 ; p-val = 0.5057601
## SAPPORO 22 FA results for Spot
## Error (ratio) = 110.5867
## SAPPORO 22 DA results for Spot
## F value = 0.1132701 ; df2 = 11 ; p-val = 0.7427846
## SAPPORO 22 FA results for Ratio
## Error (ratio) = 108.5214
## SAPPORO 22 DA results for Ratio
## F value = 0.04079544 ; df2 = 11 ; p-val = 0.8436202
## SAPPORO 22 FA results for Res
## Error (ratio) = 122.995
## SAPPORO 22 DA results for Res
## F value = 0.0777248 ; df2 = 11 ; p-val = 0.7855762
## SAPPORO 28 FA results for Wing
## Error (ratio) = 18.01684
## SAPPORO 28 DA results for Wing
## F value = 0.4517414 ; df2 = 14 ; p-val = 0.5124493

```

```

## SAPPORO 28 FA results for Spot
## Error (ratio) = 26.39958
## SAPPORO 28 DA results for Spot
## F value = 2.996871 ; df2 = 14 ; p-val = 0.1053932
## SAPPORO 28 FA results for Ratio
## Error (ratio) = 32.21979
## SAPPORO 28 DA results for Ratio
## F value = 2.388111 ; df2 = 14 ; p-val = 0.1445616
## SAPPORO 28 FA results for Res
## Error (ratio) = 35.23728
## SAPPORO 28 DA results for Res
## F value = 2.46008 ; df2 = 14 ; p-val = 0.1390923
## SOKOL 16 FA results for Wing
## Error (ratio) = 71.06317
## SOKOL 16 DA results for Wing
## F value = 0.9397218 ; df2 = 9 ; p-val = 0.3576777
## SOKOL 16 FA results for Spot
## Error (ratio) = 8.596647
## SOKOL 16 DA results for Spot
## F value = 4.441974 ; df2 = 9 ; p-val = 0.06432001
## SOKOL 16 FA results for Ratio
## Error (ratio) = 8.592499
## SOKOL 16 DA results for Ratio
## F value = 3.980105 ; df2 = 9 ; p-val = 0.07716983
## SOKOL 16 FA results for Res
## Error (ratio) = 9.037187
## SOKOL 16 DA results for Res
## F value = 3.713459 ; df2 = 9 ; p-val = 0.08608085
## SOKOL 22 FA results for Wing
## Error (ratio) = 31.02616
## SOKOL 22 DA results for Wing
## F value = 0.8261475 ; df2 = 10 ; p-val = 0.3847715
## SOKOL 22 FA results for Spot
## Error (ratio) = 21.51362
## SOKOL 22 DA results for Spot
## F value = 8.298962 ; df2 = 10 ; p-val = 0.0163633
## The larger spot size is in the D wing.
## SOKOL 22 FA results for Ratio
## Error (ratio) = 24.55957
## SOKOL 22 DA results for Ratio
## F value = 9.559751 ; df2 = 10 ; p-val = 0.01140728
## The larger spot size is in the D wing.
## SOKOL 22 FA results for Res
## Error (ratio) = 23.99074
## SOKOL 22 DA results for Res
## F value = 9.111226 ; df2 = 10 ; p-val = 0.01292897
## The larger spot size is in the D wing.
## SOKOL 28 FA results for Wing
## Error (ratio) = 1.816481
## SOKOL 28 DA results for Wing
## F value = 3.339042 ; df2 = 13 ; p-val = 0.09069199
## SOKOL 28 FA results for Spot
## Error (ratio) = 70.02448
## SOKOL 28 DA results for Spot

```

```
## F value = 9.68205 ; df2 = 13 ; p-val = 0.008260259
## The larger spot size is in the D wing.
## SOKOL 28 FA results for Ratio
## Error (ratio) = 64.45344
## SOKOL 28 DA results for Ratio
## F value = 10.26345 ; df2 = 13 ; p-val = 0.006918648
## The larger spot size is in the D wing.
## SOKOL 28 FA results for Res
## Error (ratio) = 62.54225
## SOKOL 28 DA results for Res
## F value = 9.999089 ; df2 = 13 ; p-val = 0.007494505
## The larger spot size is in the D wing.
```

We then decompose our data into a symmetric component (the individual average between wings) and the asymmetric component (the individual differences between wings). Computationally, it is easier to estimate the latter if we first build the matrix for the symmetric component, so we do that:

```
Sym.comp <- aggregate(Ratio ~ IND + TEMP + POP,
  data = spot.sym, FUN = mean
)

Sym.comp$Spot <- aggregate(Spot ~ IND + TEMP + POP,
  data = spot.sym, FUN = mean
)[, 4]

Sym.comp$Wing <- aggregate(Wing ~ IND + TEMP + POP,
  data = spot.sym, FUN = mean
)[, 4]

Sym.comp$Res <- aggregate(Res ~ IND + TEMP + POP,
  data = spot.sym, FUN = mean
)[, 4]
```

As we have build a matrix where each row is an individual, we use it as a ‘model’ matrix for the asymmetric component matrix. Then, for each individual (for each name within the first column) we find the position of its two wings in the raw data, we identify right and left wings and then we estimate the asymmetric component as the difference of the right wing minus the left wing. Finally, we discard the NAs (those individuals that have just one wing within the raw dataset):

```
Asym.comp <- Sym.comp

for (i in 1:nrow(Sym.comp)) {
  indexes <- intersect(intersect(
    which(spot.sym$IND == Sym.comp[i, 1]),
    which(spot.sym$TEMP == Sym.comp[i, 2])
  ), which(spot.sym$POP == Sym.comp[i, 3]))

  if (spot.sym$SIDE[indexes[1]] == "D") {
    ind_droite <- indexes[1]
    ind_gauche <- indexes[2]
  } else {
    ind_gauche <- indexes[1]
    ind_droite <- indexes[2]
  }

  Asym.comp[i, 4] <- spot.sym$Ratio[ind_droite] - spot.sym$Ratio[ind_gauche]
```

```

Asym.comp[i, 5] <- spot.sym$Spot[ind_droite] - spot.sym$Spot[ind_gauche]
Asym.comp[i, 6] <- spot.sym$Wing[ind_droite] - spot.sym$Wing[ind_gauche]
Asym.comp[i, 7] <- spot.sym$Res[ind_droite] - spot.sym$Res[ind_gauche]
}

```

```

ParisAsym_idx <- which(Asym.comp$POP=='PARIS')
SappoAsym_idx <- which(Asym.comp$POP=='SAPPORO')
SokolAsym_idx <- which(Asym.comp$POP=='SOKOL')
temp16Asym_idx <- which(Asym.comp$TEMP==16)
temp22Asym_idx <- which(Asym.comp$TEMP==22)
temp28Asym_idx <- which(Asym.comp$TEMP==28)

```

Now, we can start the analyses on the asymmetric component. We start by looking at whether there is a systematic effect on DA:

```
summary(aov(Spot ~ TEMP*POP, data = Asym.comp))
```

```

##              Df      Sum Sq   Mean Sq F value Pr(>F)
## TEMP          2 2.383e+08 119173849   1.476  0.234
## POP           2 6.494e+08 324701194   4.022  0.021 *
## TEMP:POP      4 2.017e+08  50425074   0.625  0.646
## Residuals    97 7.830e+09  80724332
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```
cohens.d(Asym.comp$Spot[ParisAsym_idx],Asym.comp$Spot[SappoAsym_idx])
```

```
## [1] 0.6321301
```

```
cohens.d(Asym.comp$Spot[ParisAsym_idx],Asym.comp$Spot[SokolAsym_idx])
```

```
## [1] 0.2406642
```

```
cohens.d(Asym.comp$Spot[SokolAsym_idx],Asym.comp$Spot[SappoAsym_idx])
```

```
## [1] 0.4667466
```

```
summary(aov(Wing ~ TEMP*POP, data = Asym.comp))
```

```

##              Df      Sum Sq   Mean Sq F value Pr(>F)
## TEMP          2 5.356e+08 267797599   0.563  0.571
## POP           2 6.894e+08 344688498   0.725  0.487
## TEMP:POP      4 3.776e+09 943919656   1.985  0.103
## Residuals    97 4.612e+10 475459629

```

```
summary(aov(Ratio ~ TEMP*POP, data = Asym.comp))
```

```

##              Df      Sum Sq   Mean Sq F value Pr(>F)
## TEMP          2 0.000313 1.564e-04   3.323 0.0402 *
## POP           2 0.000345 1.723e-04   3.661 0.0293 *
## TEMP:POP      4 0.000131 3.281e-05   0.697 0.5957
## Residuals    97 0.004565 4.706e-05
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```
summary(lm(Ratio ~ TEMP, data = Asym.comp))$r.squared
```

```
## [1] 0.05842831
```

```
cohens.d(Asym.comp$Ratio[ParisAsym_idx],Asym.comp$Ratio[SappoAsym_idx])
```

```
## [1] 0.597357
```

```
cohens.d(Asym.comp$Ratio[ParisAsym_idx],Asym.comp$Ratio[SokolAsym_idx])
```

```
## [1] 0.2145836
```

```
cohens.d(Asym.comp$Ratio[SokolAsym_idx],Asym.comp$Ratio[SappoAsym_idx])
```

```
## [1] 0.4936126
```

```
summary(aov(Ratio ~ TEMP:POP, data = Asym.comp))
```

```
##           Df    Sum Sq   Mean Sq F value Pr(>F)
## TEMP:POP      8 0.000789 9.858e-05    2.095 0.0434 *
## Residuals    97 0.004565 4.706e-05
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
summary(lm(Ratio ~ TEMP:POP, data = Asym.comp))$r.squared
```

```
## [1] 0.1473159
```

```
summary(aov(Res ~ TEMP*POP, data = Asym.comp))
```

```
##           Df      Sum Sq   Mean Sq F value Pr(>F)
## TEMP         2 2.280e+08 114021818    1.369 0.2592
## POP          2 6.364e+08 318177144    3.821 0.0253 *
## TEMP:POP     4 1.730e+08 43252736    0.519 0.7217
## Residuals    97 8.078e+09 83275158
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
summary(lm(Res ~ TEMP:POP, data = Asym.comp))$r.squared
```

```
## [1] 0.1138121
```

```
cohens.d(Asym.comp$Res[ParisAsym_idx],Asym.comp$Res[SappoAsym_idx])
```

```
## [1] 0.6139757
```

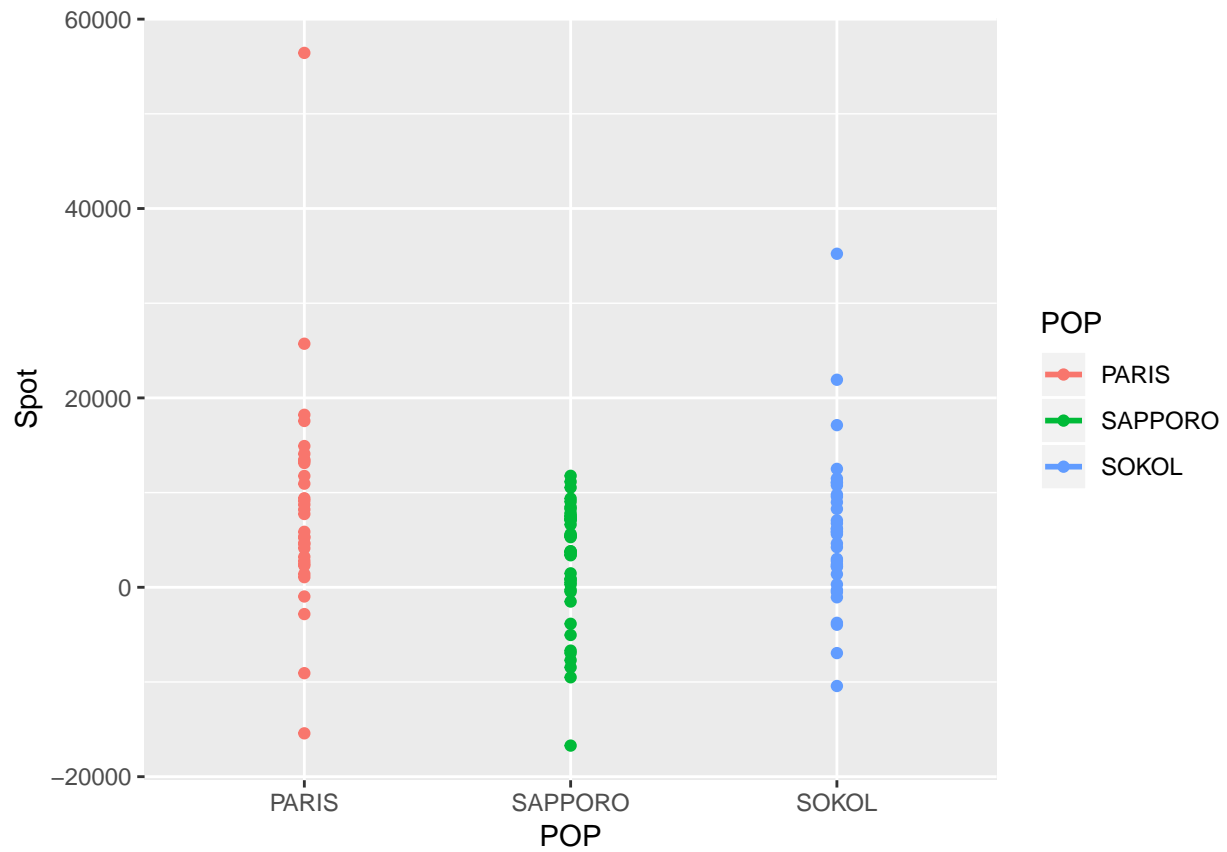
```
cohens.d(Asym.comp$Res[ParisAsym_idx],Asym.comp$Res[SokolAsym_idx])
```

```
## [1] 0.2079479
```

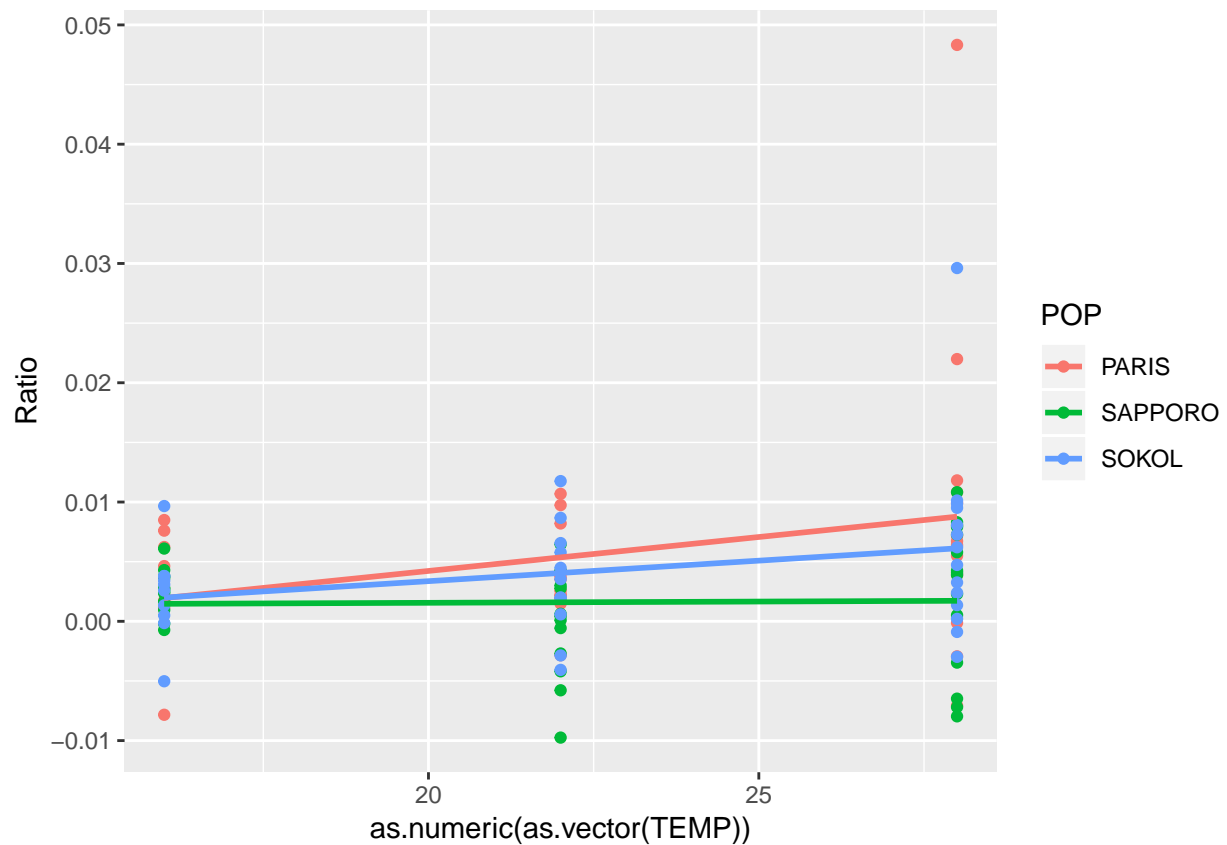
```
cohens.d(Asym.comp$Res[SokolAsym_idx],Asym.comp$Res[SappoAsym_idx])
```

```
## [1] 0.4935809
```

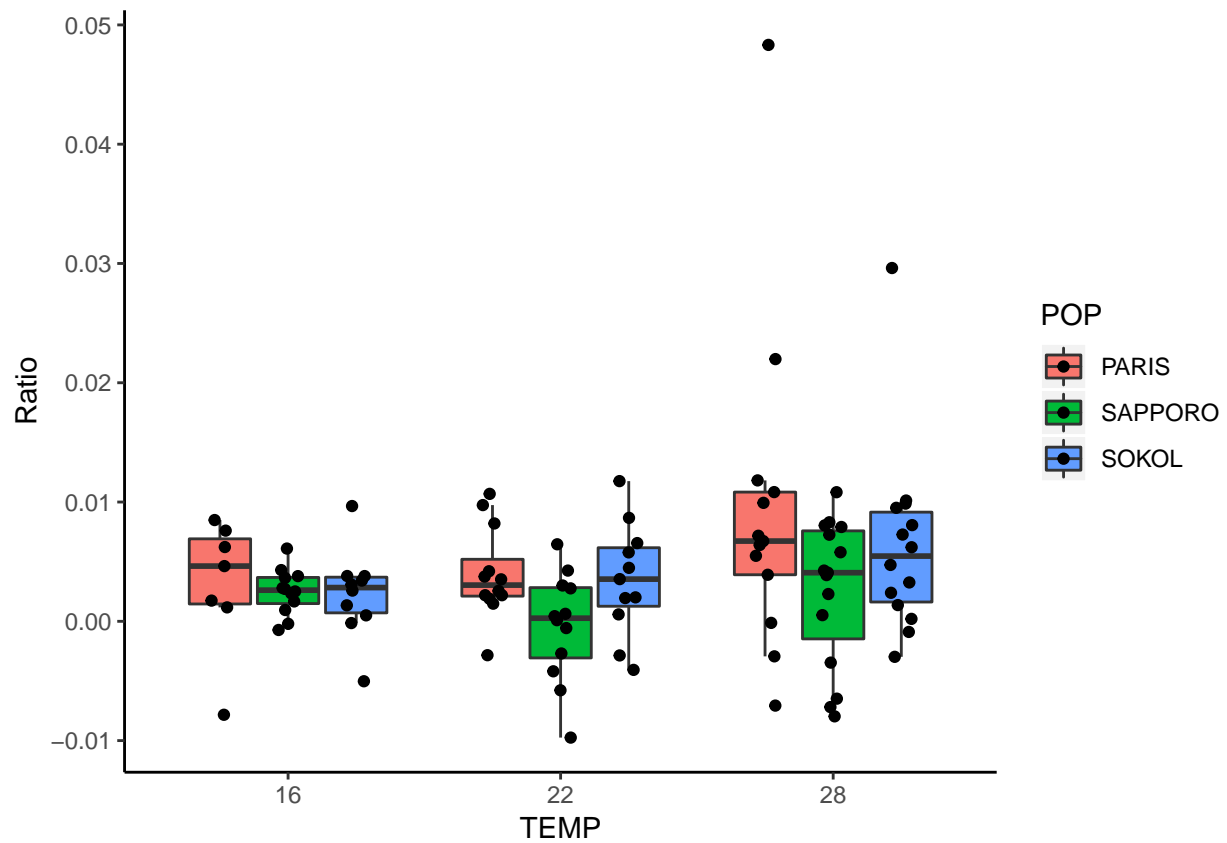
```
ggplot(data=Asym.comp,
       aes(x = POP, y = Spot, color = POP)) +
  geom_point() +
  geom_smooth(method = 'lm', se = FALSE)
```

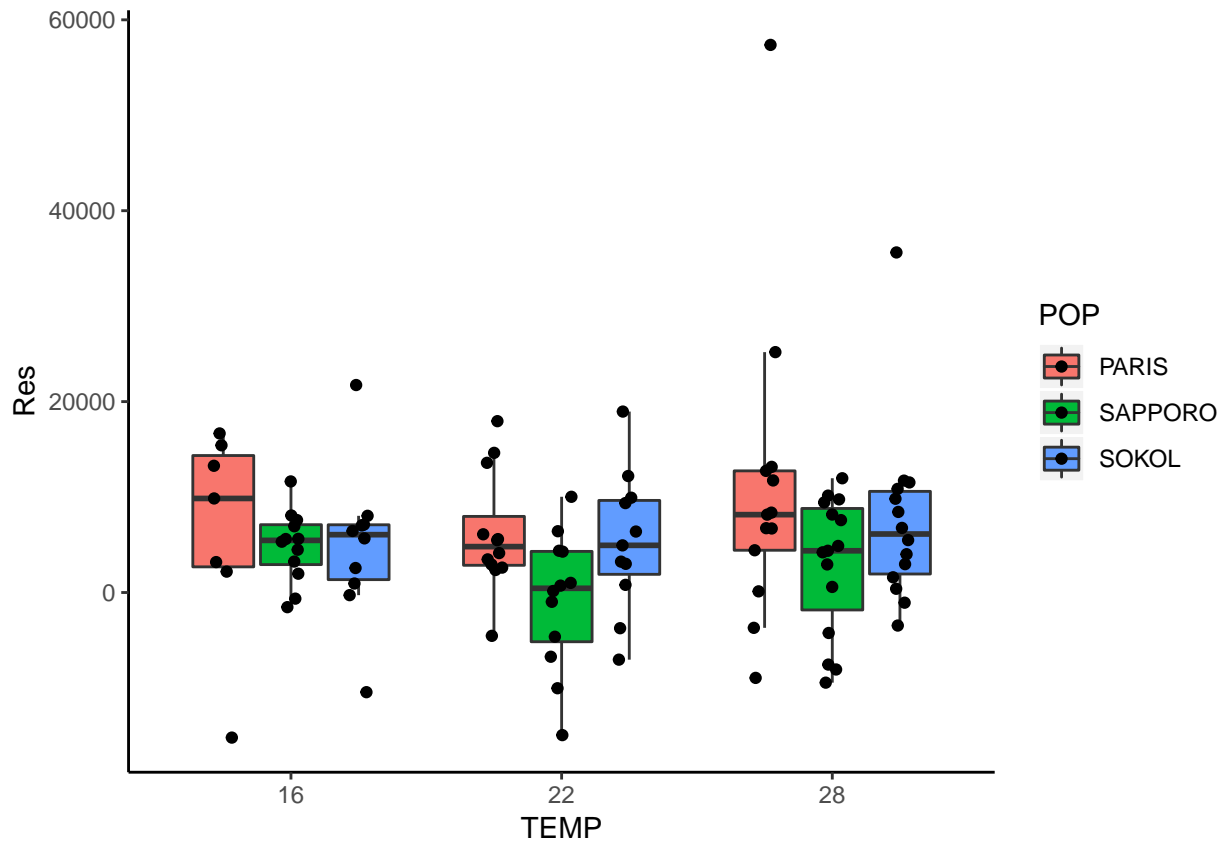
```
ggplot(data=Asym.comp,
  aes(x = as.numeric(as.vector(TEMP)), y = Ratio, color = POP)) +
  geom_point() +
  geom_smooth(method = 'lm', se = FALSE)
```



```
ggplot(data = Asym.comp,
  aes(x = TEMP, y = Ratio, fill = POP)) +
  geom_boxplot(outlier.shape = NA) +
  geom_jitter(position = position_jitterdodge(jitter.width = 0.2)) +
  theme(panel.grid.major = element_blank(), panel.grid.minor = element_blank(),
    panel.background = element_blank(), axis.line = element_line(colour = "black"))
```



```
ggplot(data = Asym.comp,
       aes(x = TEMP, y = Res, fill = POP)) +
  geom_boxplot(outlier.shape = NA) +
  geom_jitter(position = position_jitterdodge(jitter.width = 0.2)) +
  theme(panel.grid.major = element_blank(), panel.grid.minor = element_blank(),
        panel.background = element_blank(), axis.line = element_line(colour = "black"))
```



Now we compare the effect of temperature for invasive and native populations:

```
Sappotemp <- summary(lm(Ratio ~ TEMP, data = Asym.comp[SappoAsym_idx,]))$coefficients
Sokoltemp <- summary(lm(Ratio ~ TEMP, data = Asym.comp[SokolAsym_idx,]))$coefficients
Paristemp <- summary(lm(Ratio ~ TEMP, data = Asym.comp[ParisAsym_idx,]))$coefficients
```

```
db <- (Sokoltemp[2,1]-Sappotemp[2,1])
sd <- sqrt(Sokoltemp[2,2]^2+Sappotemp[2,2]^2)
df <- (lm(Ratio ~ TEMP, data = Asym.comp[SappoAsym_idx,])$df.residual+lm(Ratio ~ TEMP,
data = Asym.comp[SokolAsym_idx,])$df.residual)
td <- db/sd
td
```

```
## [1] 1.267522
```

```
df
```

```
## [1] 68
```

```
2*pt(-abs(td), df)
```

```
## [1] 0.209292
```

```
db <- (Paristemp[2,1]-Sappotemp[2,1])
sd <- sqrt(Paristemp[2,2]^2+Sappotemp[2,2]^2)
df <- (lm(Ratio ~ TEMP, data = Asym.comp[SappoAsym_idx,])$df.residual+lm(Ratio ~ TEMP,
data = Asym.comp[ParisAsym_idx,])$df.residual)
td <- db/sd
td
```

```
## [1] 0.7651761
```

```
df

## [1] 65
2*pt(-abs(td), df)

## [1] 0.4469361
db <- (Paristemp[2,1]-Sokoltemp[2,1])
sd <- sqrt(Paristemp[2,2]^2+Sokoltemp[2,2]^2)
df <- (lm(Ratio ~ TEMP, data = Asym.comp[SokolAsym_idx,])$df.residual+lm(Ratio ~ TEMP,
                                                                    data = Asym.comp[ParisAsym_idx,])$df.residual)

td <- db/sd
td
```

```
## [1] -0.07134414
```

```
df
```

```
## [1] 61
```

```
2*pt(-abs(td), df)
```

```
## [1] 0.9433573
```

To study the effect of temperature and population on fluctuating asymmetry we use Levene tests. We follow the same procedure than for the variation tests than for the symmetric component of variation:

```
leveneTest(Asym.comp$Wing, group = Asym.comp$TEMP)
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group  2  2.4491 0.09138 .
##      103
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
leveneTest(Asym.comp$Spot, group = Asym.comp$TEMP)
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group  2   1.166 0.3157
##      103
```

```
leveneTest(Asym.comp$Ratio, group = Asym.comp$TEMP)
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group  2  4.5289 0.01303 *
##      103
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
leveneTest(Asym.comp$Res, group = Asym.comp$TEMP)
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group  2  0.9736 0.3812
##      103
```

We can then look at what temperature is different in the wing FA:

```
leveneTest(Asym.comp$Wing[-temp16Asym_idx], group = Asym.comp$TEMP[-temp16Asym_idx])
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 1  3.9876 0.04947 *
##      75
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
leveneTest(Asym.comp$Wing[-temp22Asym_idx], group = Asym.comp$TEMP[-temp22Asym_idx])
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 1  5.8114 0.01859 *
##      69
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
leveneTest(Asym.comp$Wing[-temp28Asym_idx], group = Asym.comp$TEMP[-temp28Asym_idx])
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 1  0.0165 0.8983
##      62
```

```
sd(Asym.comp$Wing[temp16Asym_idx])
```

```
## [1] 23468.35
```

```
sd(Asym.comp$Wing[temp22Asym_idx])
```

```
## [1] 29213.05
```

```
sd(Asym.comp$Wing[temp28Asym_idx])
```

```
## [1] 12245.05
```

Overall, FA is reduced for the wing at 28?.

We can then look at what temperature is different in the ratio FA:

```
leveneTest(Asym.comp$Ratio[-temp16Asym_idx], group = Asym.comp$TEMP[-temp16Asym_idx])
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 1  3.5426 0.06369 .
##      75
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
leveneTest(Asym.comp$Ratio[-temp22Asym_idx], group = Asym.comp$TEMP[-temp22Asym_idx])
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 1  6.0699 0.01625 *
##      69
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
leveneTest(Asym.comp$Ratio[-temp28Asym_idx], group = Asym.comp$TEMP[-temp28Asym_idx])
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 1  2.0689 0.1554
##      62
```

```
sd(Asym.comp$Ratio[temp16Asym_idx])
```

```
## [1] 0.003557128
```

```
sd(Asym.comp$Ratio[temp22Asym_idx])
```

```
## [1] 0.004699225
```

```
sd(Asym.comp$Ratio[temp28Asym_idx])
```

```
## [1] 0.009797143
```

Overall, FA is increased for the ratio at 28?, probably as a consequence of the decreased variation in wing size.

Table 1: Populations significantly different and the sense of their difference

	16?	22?	28?
Spot	ND	ND	ND
Wing	+	+	-
Ratio	-	-	+
Residual	ND	ND	ND

Populations within and among temperatures

Overall we did not find significant differences in FA among geographic populations:

```
leveneTest(Asym.comp$Wing, group = Asym.comp$POP)
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 2  0.9981 0.3721
##     103
```

```
leveneTest(Asym.comp$Spot, group = Asym.comp$POP)
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 2  1.1761 0.3126
##     103
```

```
leveneTest(Asym.comp$Ratio, group = Asym.comp$POP)
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 2  1.1568 0.3185
##     103
```

```
leveneTest(Asym.comp$Res, group = Asym.comp$POP)
```

```
## Levene's Test for Homogeneity of Variance (center = median)
```

```
##           Df F value Pr(>F)
## group    2  1.2464 0.2918
##           103
```

Within temperatures, just the Wing size at 28? presents differences among geographic populations, where the Sokol populations showed a decreased FA:

```
leveneTest(Asym.comp$Wing[temp28Asym_idx], group = Asym.comp$POP[temp28Asym_idx])
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##           Df F value Pr(>F)
## group    2  4.0177 0.02591 *
##           39
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
leveneTest(Asym.comp$Wing[c(intersect(temp28Asym_idx,ParisAsym_idx),
                             intersect(temp28Asym_idx,SappoAsym_idx))],
           group = Asym.comp$POP[c(intersect(temp28Asym_idx,ParisAsym_idx),
                                       intersect(temp28Asym_idx,SappoAsym_idx))])
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##           Df F value Pr(>F)
## group    1  0.1816 0.6735
##           26
```

```
sd(Asym.comp$Wing[intersect(temp28Asym_idx,SokolAsym_idx)])
```

```
## [1] 6192.193
```

```
sd(Asym.comp$Wing[intersect(temp28Asym_idx,ParisAsym_idx)])
```

```
## [1] 15073.22
```

```
sd(Asym.comp$Wing[intersect(temp28Asym_idx,SappoAsym_idx)])
```

```
## [1] 12949.33
```

Table 2: 28? temperature

	Sapporo	Paris	Sokol
Spot	ND	ND	ND
Wing	+	+	-
Ratio	ND	ND	ND
Residual	ND	ND	ND

Within populations, just Sapporo shows differences in FA: for the relative spot size FA is reduced for the 16?.

```
leveneTest(Asym.comp$Ratio[SappoAsym_idx], group = Asym.comp$TEMP[SappoAsym_idx])
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##           Df F value Pr(>F)
## group    2  3.8545 0.03042 *
##           36
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```



```

leveneTest(Asym.comp$Ratio[c(intersect(temp28Asym_idx, SappoAsym_idx),
                                intersect(temp22Asym_idx, SappoAsym_idx))],
            group = Asym.comp$TEMP[c(intersect(temp28Asym_idx, SappoAsym_idx),
                                         intersect(temp22Asym_idx, SappoAsym_idx))])

## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 1  0.9307 0.3439
##      25

leveneTest(Asym.comp$Ratio[c(intersect(temp22Asym_idx, SappoAsym_idx),
                                intersect(temp16Asym_idx, SappoAsym_idx))],
            group = Asym.comp$TEMP[c(intersect(temp22Asym_idx, SappoAsym_idx),
                                         intersect(temp16Asym_idx, SappoAsym_idx))])

## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 1  4.4545 0.04641 *
##      22
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

leveneTest(Asym.comp$Ratio[c(intersect(temp28Asym_idx, SappoAsym_idx),
                                intersect(temp16Asym_idx, SappoAsym_idx))],
            group = Asym.comp$TEMP[c(intersect(temp28Asym_idx, SappoAsym_idx),
                                         intersect(temp16Asym_idx, SappoAsym_idx))])

## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 1  7.4777 0.01131 *
##      25
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

sd(Asym.comp$Ratio[intersect(temp16Asym_idx, SappoAsym_idx)])

## [1] 0.00190968

sd(Asym.comp$Ratio[intersect(temp22Asym_idx, SappoAsym_idx)])

## [1] 0.004555277

sd(Asym.comp$Ratio[intersect(temp28Asym_idx, SappoAsym_idx)])

## [1] 0.006138387

```

Table 3: Sapporo population

	16?	22?	28?
Spot	ND	ND	ND
Wing	ND	ND	ND
Ratio	-	+	+
Residual	ND	ND	ND