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HW#: 4

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I. INTRODUCTION

A. Equipment

There is a minimal amount of equipment to be used in this lab. The few requirements are listed below:

- Python 3.7.0 (Anaconda)
- Win10

B. function profiling

In this section how to realize the functions in **BayesianNetworks.py** will be introduced.

```
1. joinFactors(factor1, factor2)
```

The function returns a factor table that is the join of factor1 and factor2. The *pd.merge* is used to merge two factortables into one which is the join of tow tables. A new column named 'bridge' is established to combine factor1 and factor2 to avoid there is no same coloum in two tables. For the new table, the probability coloum in factor1 and factor2 will be represented as 'probs_x' and 'probs_y'. The joint distribution probability can be computed as probs x multiply probs y. Then the needless 'probs' and 'bridge' can be deleted.

```
def joinFactors(factor1, factor2):
      # your code
      if ( factor1.empty) or ( factor2.empty):
          return ( factor1 if factor2.empty else factor2)
      intersection =list((factor1.columns).intersection((factor2.columns)))
      intersection.remove('probs')
      # print(intersection)
      copy_factor1 =pd.DataFrame.copy(factor1)
      copy_factor2 =pd.DataFrame.copy(factor2)
copy_factor1['bridge']=1
      copy_factor2['bridge']=1
11
      intersection.append('bridge')
      Factor =pd.merge(copy_factor1, copy_factor2, how='outer', on=intersection)
13
      # print(Factor)
      Factor['probs_x'] *=Factor['probs_y']
15
      # print(Factor)
      Factor =Factor.rename(columns={'probs_x':'probs'}).drop(columns=['probs_y','bridge'])
17
```

2. marginalizeFactor(factorTable, hiddenVar)

The function returns a factor table that marginalizes marginal variable 'hiddenVar' out of the 'factorTable'. If the hidden variable is not in the columns of factorTable, return the factorTable directly. Else, delete the hidden variable column. If current table only has the column of probability, return the factorTable directly. Else, the *pd.groupby* is used to group the table after deleting the column of hidden variable and the probability.

```
def marginalizeFactor(factorTable, hiddenVar):
    # your code
    copy_factorTable =pd.DataFrame.copy(factorTable)

if hiddenVar not in list(copy_factorTable.columns):
    # print('return raw')

# print(list(copy_factorTable.columns), hiddenVar)
```

```
return factorTable

if hiddenVar in list(copy_factorTable.columns):
    # print(list(copy_factorTable.columns),hiddenVar)

copy_factorTable =copy_factorTable.drop(columns=hiddenVar) # delete
    val_list =list(copy_factorTable.columns)

val_list.remove('probs')
    if not val_list:
        return factorTable

copy_factorTable =copy_factorTable.columns].groupby(val_list, as_index=False).mean()

return copy_factorTable
```

3. marginalizeNetworkVariables(bayesNet, hiddenVar)

The function returns a Bayesian network containing a list of factor tables that results when the list of variables in hiddenVar is marginalized out of bayesnet. As the function can marginalize more than one hidden variable in a bayesNet, two loops are used as one loop for the factortables of the net and another loop for the variables which need to be marginalized. The function marginalizeFactor(factorTable, hiddenVar) is used here.

```
def marginalizeNetworkVariables(bayesNet, hiddenVar):
    # your code
    marginalized_bayesNet =[]

for factorTable in bayesNet:
    # print(factorTable)
    copy_factorTable =pd.DataFrame.copy(factorTable)
    for hiddenVar_x in hiddenVar:
        result =marginalizeFactor(copy_factorTable, hiddenVar_x)
    # print(factorTable)
    copy_factorTable =pd.DataFrame.copy(result)

marginalized_bayesNet.append(result)
return marginalized_bayesNet
```

4. evidenceUpdateNet(bayesNet, evidenceVars, evidenceVals)

The function sets the values of the evidence variables. Other values for the variables should be removed from the tables. And the normalization of factors is not required. For each evidence variable variable and the corresponding variable value value, if the variable is included in the column of factorTable, the row whose value of the variable is equal to the value will be saved in the result.

```
else:
current_net.append(factorTable)
return current_net
```

5. inference(bayesNet, hiddenVar, evidenceVars, evidenceVals)

This function takes in a Bayesian network and returns a single joint probability table resulting from the given set of evidence variables and marginalizing a set of hidden variables. The table will be normalized to give valid probabilities. The final table will be a proper probability table (entries sum to 1). The hidden variables shown in hiddenVar will not be in the returned table.

To realize the function, firstly the bayesNet will be updated with the provided hiddenVar and evidenceVars via the function evidenceUpdateNet(bayesNet, evidenceVars, evidenceVals). After filtering out all the variables in the columns, for each variable variable, a loop is used to dispose variable in the factorTable factorTable of the net. If variable is in the column of the factorTable, the joinFactors(factor, factorTable) will be used to join two factors. After the loop for the net, if the variable is one of the hidden variable, the marginalizeFactor(factor, variable) will be used to marginalize it.

To realize the normalization, the $norm_scale$ is computed to normalize the probability whose entries sum to 1.

```
def inference(bayesNet, hiddenVar, evidenceVars, evidenceVals):
      # your code
      # update net with evidenceUpdateNet
      updated_net =evidenceUpdateNet(bayesNet,evidenceVars,evidenceVals)
      # filter all the variables
      all_variables =set()
      for factorTable in bayesNet:
         all variables.update(factorTable.columns)
10
      all_variables.remove('probs')
12
      # for each variable in the net
14
      for variable in all_variables:
         copy_net =updated_net.copy()
         updated_net =[]
16
         factor =pd.DataFrame(columns=['probs'])
18
         # for each table in the net
         for factorTable in copy_net:
20
             if variable in factorTable.columns:
                factor =joinFactors(factor, factorTable)
22
                updated_net.append(factorTable)
24
          if variable in hiddenVar:
             # if variable is in hiddenVar, whitch means it should be marginalized
26
             factor =marginalizeFactor(factor, variable)
28
         updated_net.append(factor)
      # normalization
30
      norm_scale =sum(list(factor['probs']))
      factor['probs'] /=norm scale
32
      return factor
```

II. USE BAYESIANNETWORKS TO BEHAVIORAL RISK FACTOR SURVEILLANCE SYSTEM SURVEY

Q1 Answer:

The size of networks can be computed by:

$$8 + 8 \times 2 + 8 \times 2 + 8 \times 2 \times 4 + 8 \times 2 \times 2 \times 4 + 8 \times 2 \times 2 \times 2 + 4 \times 4 + 4 \times 4 \times 2 \times 2 + 4 \times 4 \times 2 \times 2 + 4 \times 4 \times 2 \times 2 = 504$$

The total number of probabilities needed to store the full joint distribution is

$$8 \times 2 \times 2 \times 4 \times 4 \times 2 \times 2 \times 2 \times 2 \times 4 = 2^{15} = 32768$$

Q2 Answer:

The probability of the outcome if I have bad habits or good habits and the probability of the outcome if I have poor health or good health are shown in Table I. The output of the code for question 2 are shown in Figure 1.

health outcomes		bad habits	good habits	pool health	good health
	1	15.05%	12.71%	11.54%	5.771%
diabetes	2	0.8965%	0.8865%	0.7662%	9.543%
	3	82.24%	84.77%	86.09%	92.22%
	4	1.810%	1.632%	1.604%	1.055%
stroke	1	4.926%	3.611%	8.269%	1.446%
	2	95.07%	96.39%	91.73%	98.55%
heart attack	1	7.433%	5.280%	14.08%	1.616%
neart attack	2	92.57%	94.72%	85.92%	98.38%
angina	1	8.045%	5.476%	16.16%	1.333%
angilla	2	91.96%	94.52%	83.84%	98.67%

TABLE I: Results for Question 2.

```
with bad habits:
                                                    with good habits:
    diabetes:
                                                    diabetes:
        smoke
               exercise
                          diabetes
                                         probs
                                                       smoke
                                                               exercise
                                                                          diabetes
                                                                                         probs
    0
            1
                       2
                                  1
                                     0.150516
                                                           2
                                                    0
                                                                      1
                                                                                  1
                                                                                     0.127119
    1
                       2
                                  2
                                     0.008965
            1
                                                    1
                                                            2
                                                                       1
                                                                                     0.008865
    2
            1
                       2
                                     0.822423
                                                    2
                                                            2
                                                                       1
                                                                                     0.847693
                       2
            1
                                     0.018096
                                                            2
                                                                       1
                                                                                  4
                                                                                     0.016323
    stroke:
                                                    stroke:
        smoke
               exercise
                          stroke
                                       probs
                                                               exercise
                                                                          stroke
                                                       smoke
                                                                                     probs
    0
                                   0.049264
                       2
                                1
            1
                                                    0
                                                           2
                                                                       1
                                                                                1
                                                                                   0.03611
                       2
    1
            1
                                2
                                   0.950736
                                                            2
                                                    1
                                                                       1
                                                                                2
                                                                                   0.96389
    attack:
                                                    attack:
        smoke
               exercise
                          attack
                                      probs
                                                       smoke
                                                               exercise
                                                                          attack
                                                                                      probs
    0
                       2
                                   0.07433
                                                    0
                                                           2
                                                                       1
                                                                                   0.052798
            1
            1
                       2
                                2
                                   0.92567
                                                                       1
                                                    1
                                                            2
                                                                                   0.947202
    angina:
                                                    angina:
        smoke
               exercise
                          angina
                                       probs
                                                       smoke
                                                               exercise
                                                                          angina
                                                                                      probs
    0
                                   0.080448
                                                                                   0.054755
            1
                       2
                                1
                                                    0
                                                           2
                                                                       1
                                                                                1
    1
            1
                       2
                                2
                                   0.919552
                                                           2
                                                                       1
                                                                                2
                                                                                   0.945245
with pool health:
                                                    with good health:
diabetes:
                                                    diabetes:
   bmi
        diabetes
                       probs
                                                        bmi
                                                            diabetes
                                                                           probs
0
                   0.115423
                                                    0
                                                          2
                                                                        0.057710
     3
                1
                                                                     1
                                                    1
                                                          2
                                                                        0.009543
1
                2
                   0.007662
                                                                     2
2
                   0.860873
                                                                        0.922194
                                                          2
                                                                        0.010553
                   0.016043
                                                                     4
                4
                                                    stroke:
stroke:
   cholesterol
                 bmi
                       bp
                           stroke
                                        probs
                                                        cholesterol
                                                                      bmi
                                                                           bp
                                                                                stroke
                                                                                           probs
0
                                                    0
                                                                   2
                                                                        2
                                                                            3
                                                                                         0.01446
              1
                    3
                        1
                                 1
                                    0.082686
              1
                    3
                                    0.917314
                                                    1
                                                                   2
                                                                        2
                                                                            3
                                                                                     2
                                                                                         0.98554
                                                    attack:
attack:
                                                                                            probs
   cholesterol
                 bmi
                       bp
                           attack
                                        probs
                                                        cholesterol
                                                                      bmi
                                                                           bp
                                                                                attack
                                                                                         0.016161
                                                    0
0
              1
                    3
                                 1
                                    0.140784
                                                                        2
                                                                                     1
                                                                                     2
                                                                                         0.983839
                        1
                                 2
                                                    1
                                                                   2
                                                                             3
1
              1
                                    0.859216
                                                                        2
                                                    angina:
angina:
                                                        cholesterol
                                                                                angina
   cholesterol
                       bp
                           angina
                                                                      bmi
                                                                           bp
                                                                                            probs
                 hmi
                                        probs
                                                    0
                                                                                         0.013326
0
                                    0.161608
                                                                   2
                                                                        2
                                                                                     1
                    3
                        1
                                                    1
1
                                                                   2
                                                                        2
                                                                                     2
                                                                                         0.986674
              1
                                 2
                                    0.838392
```

FIG. 1: Results for Question 2.

Q3 Answer:

The effect that a person's income has on their probability of having one of the four health outcomes are evaluated and the comparations are shown in Figure 2. We can conclude that the higher a person's income status is ,the less probabilities to have diseases problem. But the people who earn 10000-15000\$ seem to be more likely to have diseases problem compared to the people who earn less than 10000\$.

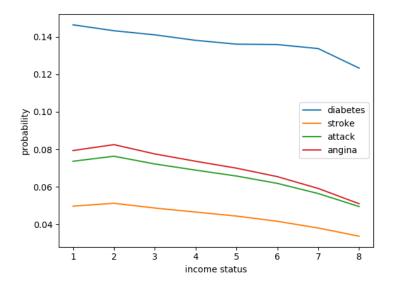


FIG. 2: Results for Question 3.

Q4 Answer:

As there are no links in the graph between the habits (smoking and exercise) and the outcomes, it can be infered that the effects of smoking and exercise on health problems are ignored, in other words, an assumption that smoking and exercise have no effects on health problems is made. Test for the validity of these assumptions is made by adding edges from smoking to each of the four outcomes and edges from exercise to each of the four outcomes.

The probability of the outcome if I have bad habits or good habits and the probability of the outcome if I have poor health or good health are shown in Table II. The output of the code for question 2 are shown in Figure 3.

health outcomes		bad habits	good habits	pool health	good health
diabetes	1	21.09%	9.855%	12.35%	5.417%
	2	6.915%	0.9884%	0.7460%	0.9731%
	3	76.07%	87.76%	85.24%	92.60%
	4	2.145%	1.399%	1.664%	1.014%
stroke	1	7.804%	2.421%	8.426%	1.400%
	2	92.20%	97.57%	91.57%	98.60%
heart attack	1	12.12%	3.102%	14.22%	1.547%
	2	87.88%	96.90%	85.78%	98.45%
angina	1	11.90%	3.68%	16.30%	1.294%
	2	88.10%	96.32%	83.70%	98.71%

TABLE II: Results for Question 4.

smoke	exercise	diabetes probs	smoke exercise diabetes probs
0 1	2	1 0.210939	0 2 1 1 0.098552
1 1	2		1 2 1 2 0.009884
2 1	2		2 2 1 3 0.877576
3 1	2	4 0.021447	3 2 1 4 0.013988
stroke:			stroke:
smoke		stroke probs	smoke exercise stroke probs
0 1		1 0.078035	0 2 1 1 0.024311
1 1	2	2 0.921965	1 2 1 2 0.975689
attack:			attack:
smoke	exercise	attack probs	smoke exercise attack probs
0 1			0 2 1 1 0.031015
1 1	2	2 0.878834	0 2 1 1 0.031015 1 2 1 2 0.968985
angina:			angina:
		angina probs	smoke exercise angina probs
0 1	2	1 0.119007	0 2 1 1 0.0368
1 1	2	2 0.880993	1 2 1 2 0.9632
with pool heal	lth:		
diabetes:			with good health:
	l bo bmi	diabetes probs	diabetes:
0			choiester of by bill diabetes probs
	L 1 3	2 0.007460	0 2 3 2 1 0.054173 1 2 3 2 2 0.009731
	L 1 3	3 0.852416	1 2 3 2 2 0.009/31
			2 2 2 2 2 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
3	L 1 3	4 0.016643	2 2 3 2 3 0.925952
3 : stroke:	l 1 3	4 0.016643	3 2 3 2 4 0.010144
stroke:		4 0.016643	3 2 3 2 4 0.010144 stroke:
stroke:	l bmi bp	4 0.016643 stroke probs 1 0.084257	3 2 3 2 4 0.010144 stroke: cholesterol bmi bp stroke probs
stroke: cholestero 0	l bmi bp l 3 1	4 0.016643 stroke probs 1 0.084257	3 2 3 2 4 0.010144 stroke: cholesterol bmi bp stroke probs 0 2 2 3 1 0.013997
stroke: cholestero 0	l bmi bp l 3 1	4 0.016643 stroke probs	3 2 3 2 4 0.010144 stroke: cholesterol bmi bp stroke probs 0 2 2 3 1 0.013997 1 2 2 3 2 0.986003
stroke: cholestero 0 1	l bmi bp l 3 1 l 3 1	4 0.016643 stroke probs 1 0.084257 2 0.915743	3 2 3 2 4 0.010144 stroke: cholesterol bmi bp stroke probs 0 2 2 3 1 0.013997 1 2 2 3 2 0.986003 attack:
stroke: cholestero 0 1 attack:	l bmi bp l 3 1 l 3 1	4 0.016643 stroke probs 1 0.084257 2 0.915743 attack probs	3 2 3 2 4 0.010144 stroke: cholesterol bmi bp stroke probs 0 2 2 3 1 0.013997 1 2 2 3 2 0.986003 attack: cholesterol bmi bp attack probs
stroke: cholestero 1 attack: cholestero	l bmi bp l 3 1 l 3 1 l bmi bp l 3 1	4 0.016643 stroke probs 1 0.084257 2 0.915743 attack probs	3 2 3 2 4 0.010144 stroke: cholesterol bmi bp stroke probs 0 2 2 3 1 0.013997 1 2 2 3 2 0.986003 attack: cholesterol bmi bp attack probs 0 2 2 3 1 0.015469
stroke: cholestero 1 attack: cholestero	l bmi bp l 3 1 l 3 1 l bmi bp l 3 1	4 0.016643 stroke probs 1 0.084257 2 0.915743 attack probs 1 0.142199	3 2 3 2 4 0.010144 stroke: cholesterol bmi bp stroke probs 0 2 2 3 1 0.013997 1 2 2 3 2 0.986003 attack: cholesterol bmi bp attack probs 0 2 2 3 1 0.015469 1 2 2 3 2 0.984531
stroke: cholestero attack: cholestero angina:	l bmi bp l 3 1 l 3 1 l bmi bp l 3 1 l 3 1	4 0.016643 stroke probs 1 0.084257 2 0.915743 attack probs 1 0.142199	3 2 3 2 4 0.010144 stroke: cholesterol bmi bp stroke probs 0 2 2 3 1 0.013997 1 2 2 3 2 0.986003 attack: cholesterol bmi bp attack probs 0 2 2 3 1 0.015469 1 2 2 3 2 0.984531 angina:
stroke: cholestero attack: cholestero angina: cholestero	l bmi bp l 3 1 l 3 1 l bmi bp l 3 1 l 3 1	4 0.016643 stroke probs 1 0.084257 2 0.915743 attack probs 1 0.142199 2 0.857801	3 2 3 2 4 0.010144 stroke: cholesterol bmi bp stroke probs 0 2 2 3 1 0.013997 1 2 2 3 2 0.986003 attack: cholesterol bmi bp attack probs 0 2 2 3 1 0.015469 1 2 2 3 2 0.984531

with good habits:

diabetes:

FIG. 3: Results for Question 4.

2

0.987056

2 0.837028

Compare Table II and Table I, we can find that habits have significant impacts on the health outcome, while health status do not. For habits and outcomes, we can find that with good habits the morbidity will decrease and with bad habits it will increase, which means that there are some dependences between habits and outcomes and the assumption of habits is not valid. But for the health status and outcomes, the assumption that health status and outcomes are independent is valid.

Q5 Answer:

with bad habits:

diabetes:

As there are no edges between the four outcomes, it can be infered that the effects between four outcomes are ignored, in other words, an assumption that one outcome have no effects on others is made.

The output of the code for question 5 are shown in Figure 4.

```
P(stroke = 1|diabetes = 1)
  stroke diabetes
                    0.044164
                 1 0.955836
P(stroke = 1|diabetes = 3)
   stroke diabetes
                       probs
0
                    0.040478
1
                    0.959522
Add an edge from diabetes to stroke
P(stroke = 1|diabetes = 1)
  diabetes stroke
                       probs
                 1 0.076198
                 2 0.923802
P(stroke = 1|diabetes = 3)
  diabetes stroke
                       probs
                 1 0.035015
          3
                  2 0.964985
```

FIG. 4: Results for Question 5.

From the results we can find that a person with diabetes problem is much more likely to face stroke problem, which means that the diabetes and stroke are correlative and the assumption that diabetes and stroke are independent is invalid.