

# Investigating and Modeling Motorized and Non-Motorized Interaction Behavior in Shared Spaces of Intersections

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Motivation  
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Methodology  
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Result  
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Discussion  
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Conclusion  
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# Outline

1 Motivation

2 Methodology

3 Result

4 Discussion

5 Conclusion

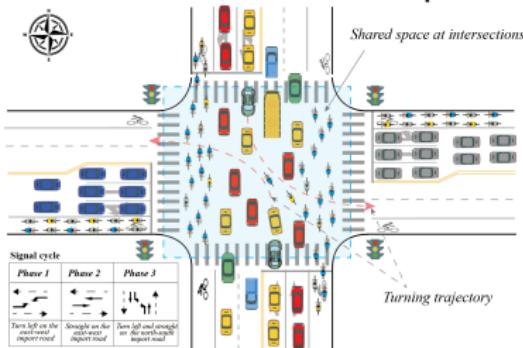
## Motivation

# Motivation

- Backgrounds
- Research Gaps

# Backgrounds

- What is the shared space?



- Why study intersection shared spaces?

- High rate of motorized and non-motorized collisions.
- There are significant challenges for self-driving vehicles in complex interaction environments.
- Lack of elaborate management strategies for proactive safety control.

- What is an intersection shared space?

# Existing studies

## Econometric and statistical models

An analysis of factors influencing conflict risk based on an econometric statistical model. Both the time of risk exposure and the level of risk are selected as dependent variables. The analysis methods are linear regression model, Logit (liu et al.,2015) , random effects, Poisson model, extreme value model (Fu et al.,2022), etc.

## Machine learning models

"Black-box" prediction, which do not require clear relationships between variables, have a strong learning ability and can accurately predict the risk state.

## Research gaps

- It is difficult to reflect the dynamic process of risk transition, and the accuracy of risk prediction is low.
- It is hard to identify the key causal factors and lack of causal link analysis.

To establish a conflict risk evolution model for the interaction process between motorized and non-motorized vehicles, to clarify the conflict causal chain, and to identify the core causes of conflict.

Motivation  
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Methodology  
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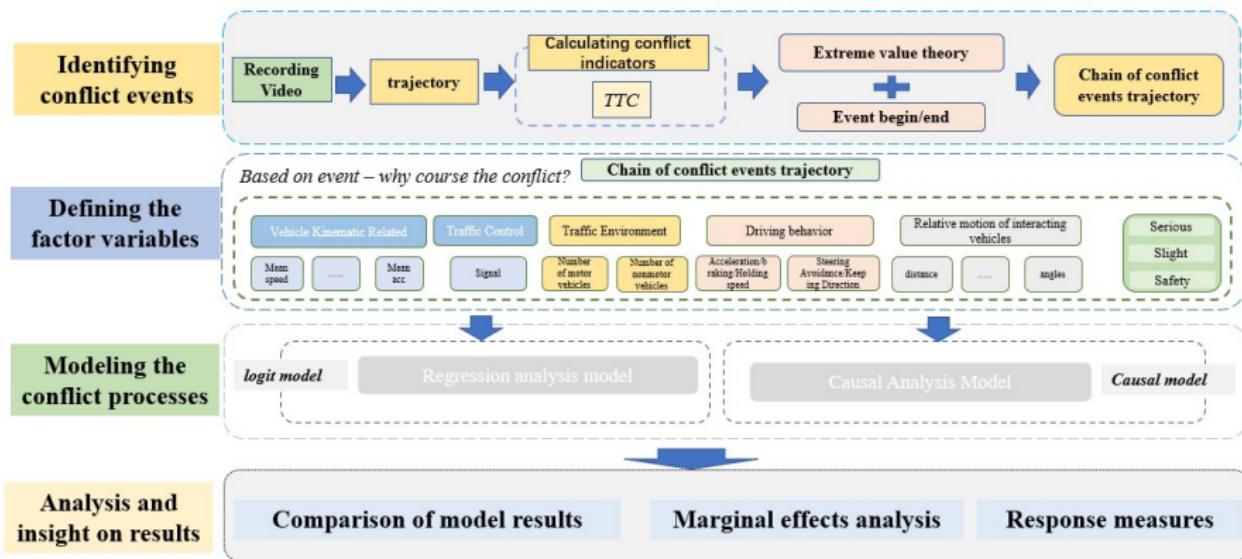
Discussion  
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Conclusion  
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# Methodology

# Methodology

# Flowchart



# Extracting and reconstructing trajectories



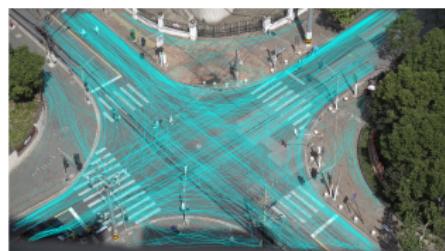
Longchang-Changyang intersection



Longchang-Changyang intersection



Trajectory of Longchang-Changyang



Trajectory of Ningwu-Hejian

Yolov7+Deepsort is used to extract each type of vehicle trajectory data, and the SFPF Algorithm that is proposed in the previous research is applied to reconstruct the missing and noisy trajectories.

# Extract the Conflict Chain

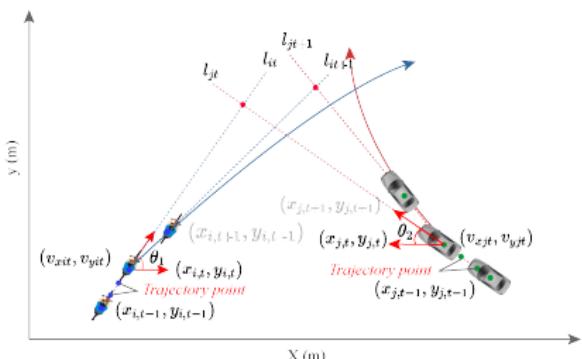
- Calculate conflict points

$$x_{it} = \frac{(y_2 - y_1) - (x_2 \cdot \tan \theta_2 - x_1 \cdot \tan \theta_1)}{\tan \theta_1 - \tan \theta_2} \quad (1)$$

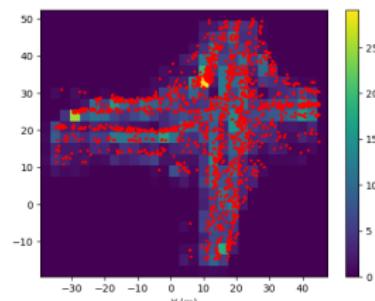
$$y_{it} = \frac{(x_2 - x_1) - (y_2 \cdot \cot \theta_2 - y_1 \cdot \cot \theta_1)}{\cot \theta_1 - \cot \theta_2} \quad (2)$$

- Calculation of conflict time

$$|TX_1 - TX_2| < \sigma \quad (3)$$



Process diagram of conflict between MV and NMV



Heat Map of Conflict Point Distribution( $ttc < 5s$ )

## • Define the Variable

Variable type	variable name	variable encoding	Variable Definition	amount	Percentage
Conflict level	ttc(s)	ttc1 ttc2 ttc3 ttc4 ttc5	[5,∞) [3,5) [2,3) [1,2) [0,1)	241 374 475 592 31	14.07 21.83 27.73 34.56 1.81
	fdir	fdir1	Left turning	107	12.75
		fdir2	straight	364	43.38
		fdir3	Left turning	368	43.86
Driving Purpose	sdir	sdir1	Left turning	397	47.32
		sdir2	straight	422	50.30
		sdir3	Left turning	20	2.38
	fs (m/s)	fs1	[0,4]	392	46.72
		fs2	(4,8]	408	48.63
		fs3	(8,12]	39	4.65
Vehicle Movement Status	faa (m/s <sup>2</sup> )	faa1	(-∞,-5]	1	0.12
		faa2	(-5,0]	375	44.70
		faa3	(0,5]	463	55.18
	ftc(m)	ftc1	[0,5]	347	41.36
		ftc2	(5,15]	338	40.29
		ftc3	(15,30]	111	13.23
ss (m/s)	ftc4	ftc4	(30,+∞)	43	5.13
		ss1	[0,4]	422	50.30
		ss2	(4,8]	405	48.27
	saa(m/s <sup>2</sup> )	ss3	(8,12]	12	1.43
		saa1	(-∞,0]	402	47.91
		saa2	(0,5]	437	52.09
Traffic environment	stc(m)	stc1	[0,5]	356	42.43
		stc2	(5,15]	341	40.64
		stc3	(15,30]	99	11.80
	fnn	stc4	(30,+∞)	43	5.13
		fnn1	(0,1)	377	44.93
		fnn2	[1,3]	433	51.61
Traffic environment	fmn	fnn3	(3,+∞)	29	3.46
		fnn1	(0,1)	377	44.93
		fmn2	[1,3]	433	51.61
	snn	fmn3	(3,+∞)	29	3.46
		snn1	(0,1)	620	73.9
		snn2	[1,3]	219	26.1
smn	smn	smn1	(0,1)	625	73.3
		smn2	[1,3]	224	26.7

## • Define the Variable

Variable type	variable name	variable encoding	Variable Definition	amount	Percentage
fba	fba1		continue direction	648	77.23
	fba2		evasive behavior	191	22.77
	fbeh1		Constant acceleration	678	80.81
fbeh	fbeh2		breaking	49	5.84
	fbeh3		accelerate	112	13.35
	sba1		continue direction	679	80.93
sba	sba2		evasive behavior	160	19.07
	sbeh1		Constant acceleration	650	77.47
	sbeh2		breaking	96	11.44
Interaction Behavior	sbeh3		accelerate	93	11.08
	fts1	[0,5]		145	17.28
	fts2	(5,15]		562	66.98
	fts3	(15,30]		127	15.14
	fts4	(30,+∞)		5	0.60
vfs(m/s)	vfs1	[0,4]		485	57.81
	vfs2	(4,8]		255	30.39
	vfs3	(8,12]		98	11.68
	vfs4	(12,+16]		1	0.12
fas(m)	fas1	[0,5]		717	85.46
	fas2	(5,10]		95	11.32
	fas3	(10,30]		27	3.22
	afs1	[0,10]		410	48.87
afs(m/s)	afs2	(10,30]		332	39.57
	afs3	(30,60]		86	10.25
	afs4	(60,90]		11	1.31
signal control	sig1	[0,10]		82	9.77
	sig2	(10,L-10]		698	83.19
	sig3	(L-10,L]		59	7.03
other factor	s-type1		bicycle	234	27.89
	s-type2		electric bicycle	605	72.11

## • Orginal Logit

$$y_i = j \quad \text{if } \gamma_{j-1} < \gamma_i^* \leq \gamma_j \quad (4)$$

Where,  $\tau = (\gamma_0, \gamma_1, \dots, \gamma_j, \dots, \gamma_J)$ , A grading point indicating the severity of a conflict event. Here  $(\lambda_0 < \lambda_1 < \dots < \lambda_j < \dots < \lambda_J, \lambda_0 = -\infty, \lambda_J = +\infty)$

$$y_i^* = BX_i^T + \varepsilon \quad (5)$$

Where,  $X_i^T = (x_{i1}, x_{i2}, \dots, x_{ik}, \dots, x_{iK}; i = 1, \dots, N; k = 1, \dots, K)$  is a vector of observations of factors influencing the severity of conflict events.  $B = (\beta_0, \beta_1, \dots, \beta_k, \dots, \beta_K)$  is the parameters corresponding to influencing factor variables. The  $x_{ik}$  in  $X_i^T$  is the observed value of the  $k - th$  influencing factor in the  $i - th$  conflict event.  $N$  is the total number of accidents in the sample;  $K$  is the number of factors affecting each accident;  $\varepsilon_i$  is the random error term, which is the sum of other factors that are difficult to observe but impact the severity of the accident.

- The probability that the severity of the  $i - th$  accident is  $y_j$ .

$$\begin{aligned} Pr(y_i = j | X_i, B, \Gamma) &= Pr(\gamma_{j-1} - X_i^T B < \varepsilon_i \leq \gamma_j - X_i^T B) \\ &= F(\gamma_j - X_i^T B) - F(\gamma_{j-1} - X_i^T B) \end{aligned} \quad (6)$$

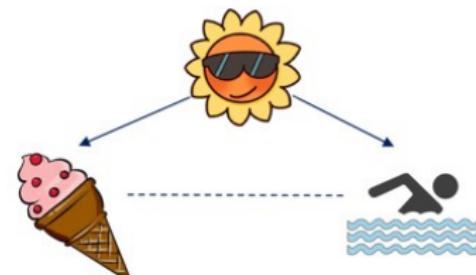
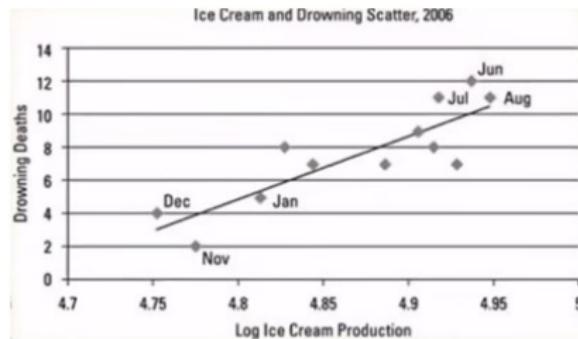
- Rate Ratio

$$\Omega_j = \frac{Pr(y_i \leq j | X_i, B, \Gamma)}{1 - Pr(y_i \leq j | X_i, B, \Gamma)} = \frac{Pr(y_i \leq j | X_i, B, \Gamma)}{Pr(y_i > j | X_i, B, \Gamma)} = \exp(\gamma_j - X_i^T B) \quad (7)$$

# Causal Inference

- Define of Causal inference

- classic example



- The basic three V-structures :

- chain
- fork
- collide

# Causal Inference

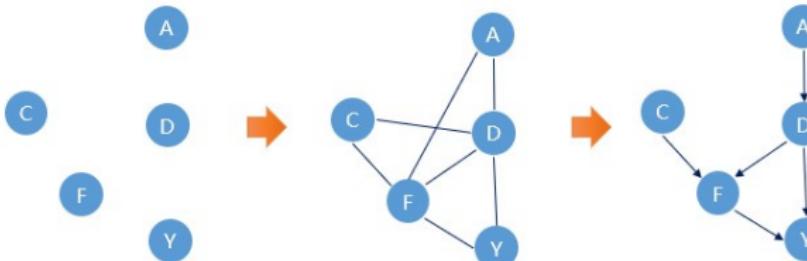
- Network learning methodology

- network learning
  - Structural learning
  - Parameter learning

- **Methodology based on conditional independence testing**

- **Basic Processes**

① Based on the independence test  
Constructing a network skeleton



**Feature Analysis:**

- ✓ Strict following of causal inference theory and fully faithful to the dataset
- ✓ Requires a sufficient amount of rich data with a little noise
- ✓ Suitable for networks with a small number of nodes

② Combining V-structures  
Make directional inferences

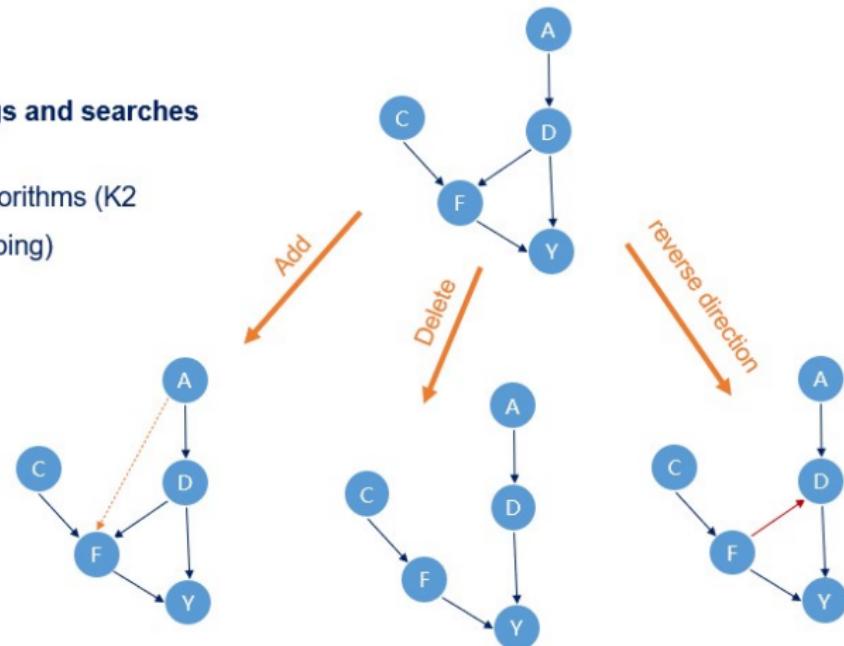
③ Adjustments based on expert experience

# Causal Inference

- Network learning methodology

- Methods based on ratings and searches

- Greedy search algorithms (K2 algorithm, hill-climbing)



Motivation  
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Methodology  
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Conclusion  
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# Result

# Result

# Ordered Logit

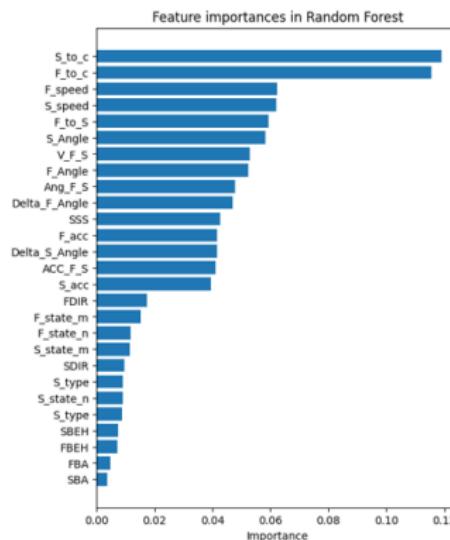
- Conflict Risk Ordered Logit Model ( $p-values < 0.05$ )

ttc-level	Coefficient	Std.err.	$P >  z $	ttc-level	Coefficient	Std.err.	$P_i - z -$
fdir1	0.729	0.371	0.049	fbeh1	-0.164	0.223	0.462
fdir3	0.574	0.271	0.034	fbeh2	-0.581	0.340	0.088
sdir1	0.873	0.265	0.001	ss2	1.195	0.164	0.000
sdir3	1.184	0.534	0.027	ss3	0.454	0.636	0.475
fs2	0.606	0.159	0.000	smn1	0.267	0.168	0.112
fs3	0.733	0.368	0.046	stc1	5.178	0.710	0.000
fba1	-0.495	0.188	0.009	stc2	3.703	0.700	0.000
ftc2	-1.308	0.163	0.000	stc3	1.863	0.684	0.006
ftc3	-2.735	0.250	0.000	sig2	-0.042	0.240	0.863
ftc4	-2.123	0.609	0.000	sig3	1.297	0.373	0.001
sba1	-0.642	0.172	0.000	s-type2	0.609	0.167	0.000

# Causal Inference

Selecting Key Variables

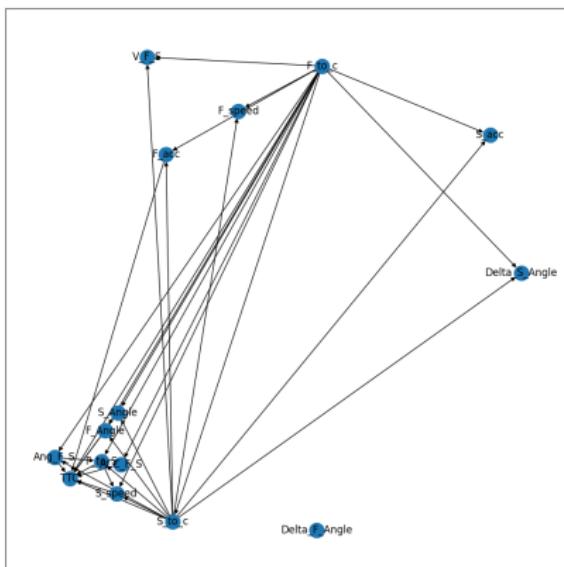
$$\text{Normalized}(x) = \text{sign}(x) \times \left( \frac{|x| - \min(|x|)}{\max(|x|) - \min(|x|)} \right) \quad (8)$$



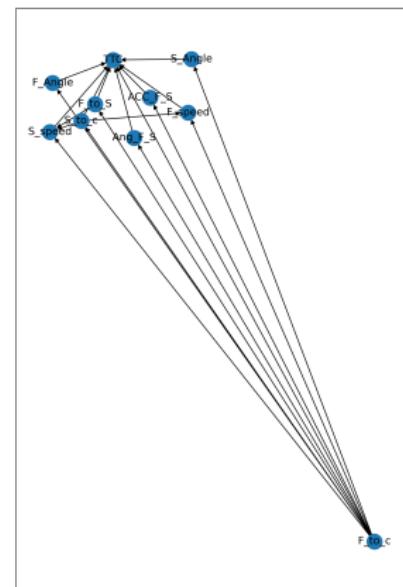
The importance of the variables is ranked based on the Random Forest

# Causal Inference

- Network learning methodology



initial diagram



Adjustment based on experience

# Causal Inference

- chain of cause and effect

causal chain	Node1	→	Node2	→	Node3	→	Node4	→	Node5
1	F_to_c	→	F_to_S	→	TTC				
2	F_to_c	→	S_speed	→	TTC				
3	F_to_c	→	F_angle	→	TTC				
4	F_to_c	→	S_to_c	→	TTC				
5	F_to_c	→	Ang_F_S	→	TTC				
6	F_to_c	→	ACC_F_S	→	TTC				
7	F_to_c	→	S_Angle	→	TTC				
8	F_to_c	→	F_angle	→	S_speed	→	TTC		
9	F_to_c	→	F_to_S	→	S_speed	→	TTC		
10	F_to_c	→	S_to_c	→	F_angle	→	TTC		
11	F_to_c	→	S_to_c	→	F_angle	→	S_speed	→	TTC

Motivation  
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Methodology  
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Result  
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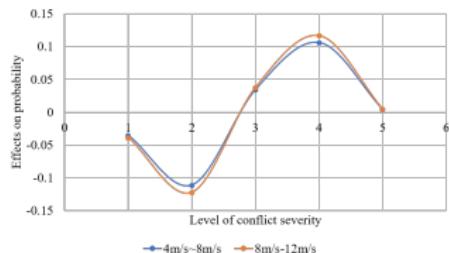
Discussion  
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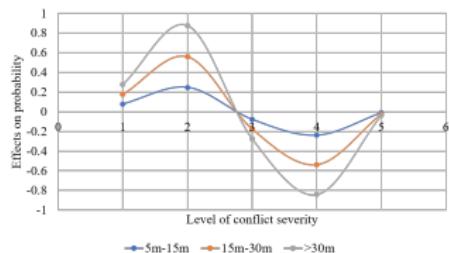
## Discussion

# Discussion

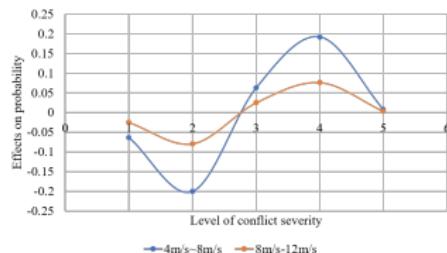
## Marginal Effects of Significant Variables.



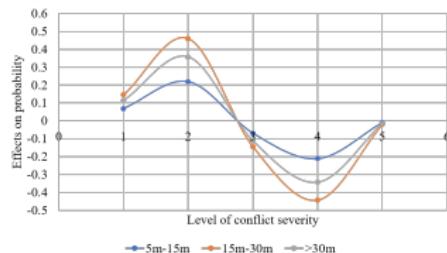
Marginal effects of the Speed with Non-motor vehicle



Marginal effects of the distances from non-motor vehicles to points of conflict



Marginal effects of Motor vehicle driving behavior



Marginal effects of the distances from motor vehicles to points of conflict

Motivation  
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## Conclusion

# Conclusion

- The main variables affecting the severity of conflict between motorized and NMV are: Direction of vehicle travel, speed of vehicle, avoidance behavior of vehicle, distance from conflict point, environment of NMV, and signal time and type of NMV, with significance values below 0.05.
- The direction of travel of interacting vehicles at the intersection has a significant effect on the severity of collisions during the interaction, increasing the likelihood of serious conflict by more than 15% between a left-turn-right-turn interaction and a right-turn-right-turn interaction compared to a straight-right-turn interaction.
- The probability of serious conflict for interaction events that occurred within 10 seconds of the end of the green light phase was 20% higher than in the 10 seconds before the green light was activated.

Complete parameter learning and compare model conclusions.

Thanks for your listening!  
Any Questions?



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